Solutions to Exercises 2

- **2.2.2** Represent sums of money in cents, as follows:
 - (a) C or C++: use type int or long (whichever is 32 bits).
 - (b) JAVA: use type int.
 - (c) ADA:

```
type Money is range 0 .. 10000000;
```

- **2.2.3** There are about 200 countries in the world. Represent them as follows:
 - (a) C or C++: use a suitable enumeration type.
 - (b) JAVA: use type **char** (unsigned 16 bits).
 - (c) ADA: use a suitable enumeration type.
- 2.3.1
- (a) C++ types:

```
 \begin{array}{ll} \text{Suit} = \{\textit{club}, \textit{diamond}, \textit{heart}, \textit{spade}\} & \text{\#Suit} = 4 \\ \text{Card} = \text{Suit} \times \text{Byte} & \text{\#Card} = 4 \times 256 = 1024 \\ \text{Hand} = \{0, 1, \ldots\} \rightarrow \text{Card} & \text{\#Hand} = 1024^{2\text{M}} \\ \text{Turn} = \text{Boolean} \times \text{Card} & \text{\#Turn} = 2 \times 1024 = 2048 \\ \end{array}
```

(b) ADA types:

```
Suit = {club, diamond, heart, spade} #Suit = 4
Rank = {2, ..., 14} #Rank = 13
Card = Suit × Rank #Card = 4 \times 13 = 52
Hand = {1, ..., 7} \rightarrow Card #Hand = 52^7
Turn = false Card + true Unit #Turn = 52 + 1 = 53
```

- 2.3.2 C arrays are static; JAVA arrays are flexible (and are classified as objects); ADA arrays are dynamic. C and JAVA arrays have integer index ranges with lower bound 0; ADA arrays have index range of any discrete primitive type or subtype.
 - (a) Accessing al[i] when i is out of range causes a C program to behave unpredictably; a JAVA or ADA program throws a suitable exception.
 - (b) Assigning a2 to a1 in C is illegal; in JAVA it makes a1 contain a reference to the same array as a2; in ADA it assigns to a1 a copy of the a2 array.
- 2.3.3 Since a JAVA array is an object, it can be used wherever an object is allowed. For instance, the components of a List or Set may be arrays as well as other objects.

Also, reference semantics is adopted for arrays as for all other objects.

- 2.3.5 Arrays and function procedures both implement mappings. The fundamental difference is that an array implements the mapping by means of a data structure (whose index must be finite), whilst a function procedure does so by means of an algorithm (whose argument need not be finite).
 - (a) In ADA:

```
not: constant array (Boolean) of Boolean
:= (false => true, true => false);
```

```
function not (b: Boolean) return Boolean is
             begin
                  if b then
                     return false;
                  else
                     return true;
                  end if;
             end;
          (b) In ADA:
             type Small is Natural range 0 .. 10;
             fac: constant array (Small) of Positive
                     := (0 \Rightarrow 1, 1 \Rightarrow 1, 2 \Rightarrow 2, 3 \Rightarrow 6,
                         4 \Rightarrow 24, 5 \Rightarrow 120, 6 \Rightarrow 720,
                          7 \Rightarrow 5040, 8 \Rightarrow 40320,
                          9 => 362880, 10 => 3628800);
             function fac (n: Small) return Positive is
             begin
                  if n \le 1 then
                     return 1;
                  else
                    return n * fac(n-1);
                  end if;
             end;
* 2.6.2
          Possible extension to ADA:
               Expression ::= ...
                           | if Expression
                              then Expression
                              else Expression end if;
** 2.6.4
          Possible extension to JAVA (array constructions):
               Expression ::= ...
                           | { Expression ( , Expression )* }
```

2.7.1 Representation of ADA types of Exercise 2.3.1:

The enumeration type Suit would be represented by a single cell containing one of $\{club, diamond, heart, spade\}$ (where the enumerands are represented by 0, 1, 2, and 3, respectively).

The integer type Rank would be represented by a single cell containing one of $\{2, ..., 14\}$.

The record type Card would be represented by a pair of fields, where the first field contains a Suit value and the second field contains a Rank value. (See illustration below.)

The array type Hand would be represented by a row of 7 pairs of fields, where each pair of fields represents a Card record. (See illustration below.)

The discriminated record type Turn would be represented by a tag field containing a boolean value, together with *either* a pair of fields representing a Card record (if the tag is *false*) *either* nothing (if the tag is *true*). (See illustration below.)

Card	Hand		Turn	
spade	spade		either	or
2	2		false	true
	club		spade	
	14		2	
	heart	'		
	10			
	spade			
	5			
	spade			
	11			
	heart			
	14			
	club			
	12.			