

Introduction To Data Science

NAME: MUHAMMAD HUZAFIA JAWAD

Roll No: SP20-BCS-144

Group: 4 (IV)

Submitted to: SIR Muhammad Sharjeel

ASSIGNMENT # 05

Question 01:

S1: "sunshine state enjoy sunshine"

S2: "brown fox jump high, brown fox run"

S3: "sunshine state fox run fast"

BoW Model

	sunshine	state	enjoy	brown	fox	jump	high	run	fast	Total length
S1	2	1	1	0	0	0	0	0	0	4
S2	0	0	0	2	2	1	1	1	0	7
S3	1	1	0	0	1	0	0	1	1	5

TF Model

	sunshine	state	enjoy	brown	fox	jump	high	run	fast	Total length
S1	$\frac{2}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	0	0	0	0	0	0	4
S2	0	0	0	$\frac{2}{7}$	$\frac{2}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	0	7
S3	$\frac{1}{5}$	$\frac{1}{5}$	0	0	$\frac{1}{5}$	0	0	$\frac{1}{5}$	$\frac{1}{5}$	5

IDF Model

formula :

$$\text{IDF}(\text{'word'}) = \log \left(\frac{\text{total no. of Documents}}{\text{no. of Documents containing 'word'}} \right)$$

$$\text{IDF}(\text{sunshine}) = \log(3/2) = 0.1761$$

$$\text{IDF}(\text{state}) = \log(3/2) = 0.1761$$

$$\text{IDF}(\text{enjoy}) = \log(3/1) = 0.4771$$

$$\text{IDF}(\text{brown}) = \log(3/1) = 0.4771$$

$$\text{IDF}(\text{fox}) = \log(3/2) = 0.1761$$

$$\text{IDF}(\text{jump}) = \log(3/1) = 0.4771$$

$$\text{IDF}(\text{high}) = \log(3/1) = 0.4771$$

$$\text{IDF}(\text{run}) = \log(3/2) = 0.1761$$

$$\text{IDF}(\text{fast}) = \log(3/1) = 0.4771$$

	sunshine	state	enjoy	brown	fox	jump	high	run	fast
IDF	0.1761	0.1761	0.4771	0.4771	0.1761	0.4771	0.4771	0.1761	0.4771

TF-IDF values

for S_1 :

$$\begin{aligned} \text{tf.idf}(\text{sunshine}) &= \frac{2}{4} * 0.1761 = 0.0880 \\ \text{tf.idf}(\text{state}) &= \frac{1}{4} * 0.1761 = 0.0440 \\ \text{tf.idf}(\text{enjoy}) &= \frac{1}{4} * 0.4771 = 0.1192 \end{aligned}$$

for S_2 :

$$\begin{aligned} \text{tf.idf}(\text{brown}) &= \left(\frac{2}{7}\right) (0.4771) = 0.1363 \\ \text{tf.idf}(\text{fox}) &= \left(\frac{2}{7}\right) (0.1761) = 0.0503 \\ \text{tf.idf}(\text{jump}) &= \left(\frac{1}{7}\right) (0.4771) = 0.0681 \\ \text{tf.idf}(\text{high}) &= \left(\frac{1}{7}\right) (0.4771) = 0.0681 \\ \text{tf.idf}(\text{run}) &= \left(\frac{1}{7}\right) (0.1761) = 0.0251 \end{aligned}$$

for S_3 :

$$\begin{aligned} \text{tf.idf}(\text{sunshine}) &= \left(\frac{1}{5}\right) (0.1761) = 0.0352 \\ \text{tf.idf}(\text{state}) &= \left(\frac{1}{5}\right) (0.1761) = 0.0352 \\ \text{tf.idf}(\text{fox}) &= \left(\frac{1}{5}\right) (0.1761) = 0.0352 \\ \text{tf.idf}(\text{run}) &= \left(\frac{1}{5}\right) (0.1761) = 0.0352 \\ \text{tf.idf}(\text{fast}) &= \left(\frac{1}{5}\right) (0.4771) = 0.0954 \end{aligned}$$

	S_1	S_2	S_3
sunshine	0.0880	0	0.0352
state	0.0440	0	0.0352
enjoy	0.1192	0	0
brown	0	0.1363	0
fox	0	0.0503	0.0352
jump	0	0.0681	0
high	0	0.0681	0
run	0	0.0251	0.0352
fast	0	0	0.0954

QUESTION # 02:

cosine Similarity b/w s_1 & s_3 .

using Bow model to generate vectors

$$s_1 = \langle 2 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \rangle$$

$$s_3 = \langle 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1 \rangle$$

formula :

$$\cos(\theta) = \frac{s_1 \cdot s_3}{|s_1| |s_3|}$$

$$s_1 \cdot s_3 = (2)(1) + (1)(1) + (1)(0) + (0)(0) + (0)(1) + (0)(0) + (0)(0) + (0)(1) + (0)(1)$$

$$= 2 + 1$$

$$= 3$$

$$|s_1| = \sqrt{2^2 + 1^2 + 1^2 + 0^2 + 0^2 + 0^2 + 0^2 + 0^2 + 0^2}$$
$$= \sqrt{4 + 1 + 1} = \sqrt{6}$$

$$|s_1| = 2.4494$$

$$|s_3| = \sqrt{1^2 + 1^2 + 0^2 + 0^2 + 1^2 + 0^2 + 0^2 + 1^2 + 1^2}$$
$$= \sqrt{5}$$

$$|s_3| = 2.2360$$

$$\cos(s_1, s_3) = \frac{3}{(2.4494)(2.2360)}$$

$$\cos(s_1, s_3) = 0.5477$$

$$s_1, s_3 = \cos^{-1}(0.5477)$$

$$s_1, s_3 = 56.78$$