**tags:** probability-theory

State and prove the smoothing property

Law of total expectation: Let $X$ be a random variable with expected value $\mathbf{E}(X)$; let $Y$ be any random variable defined on the same probability space, then

$$\mathbf{E}(X) = \mathbf{E}(\mathbf{E}(X|Y))$$