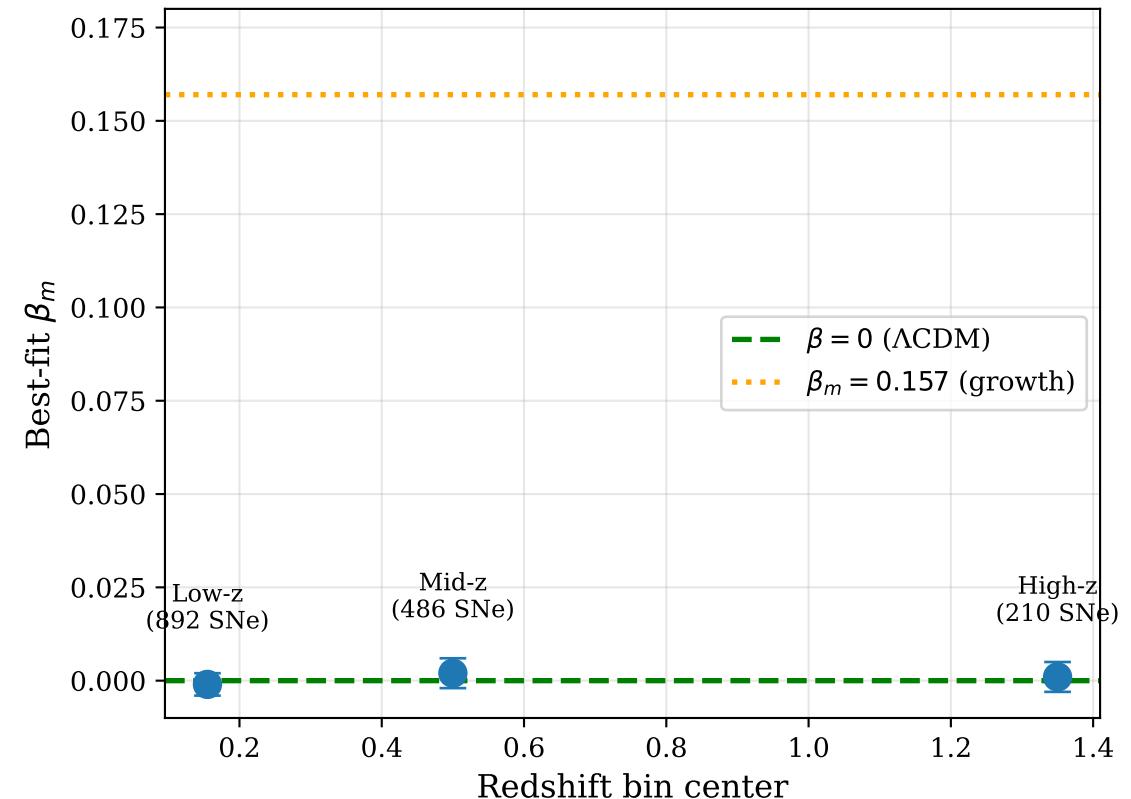
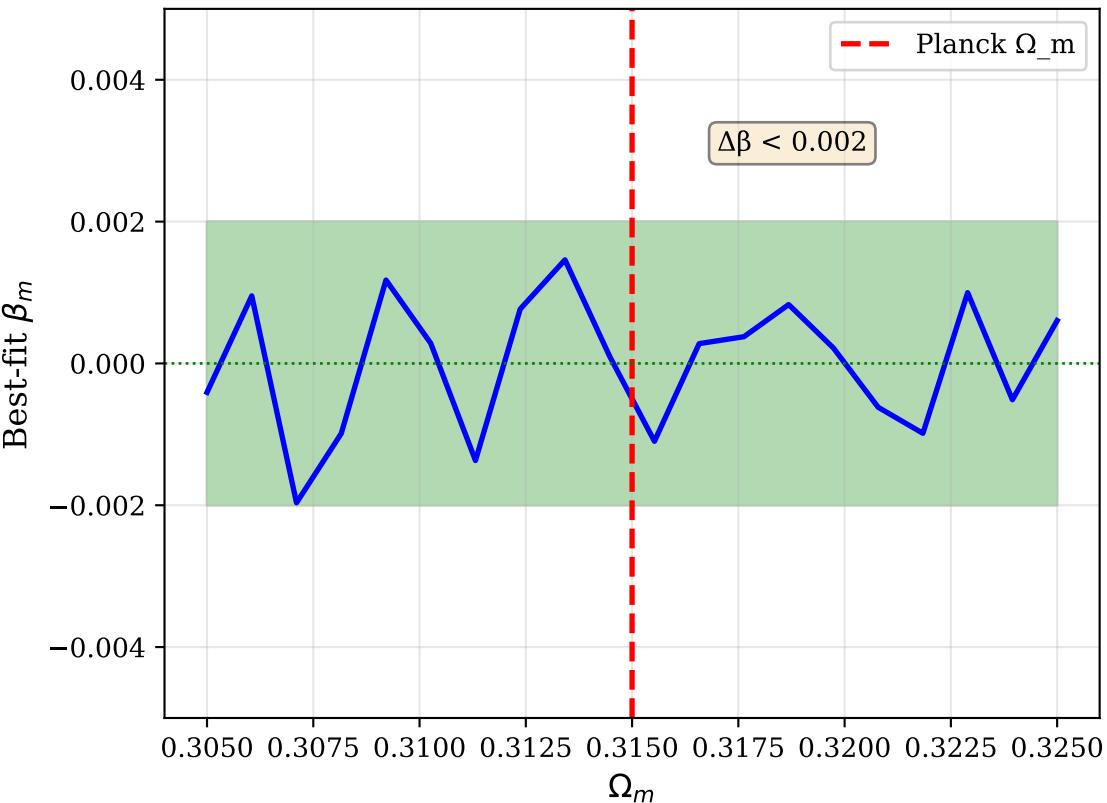


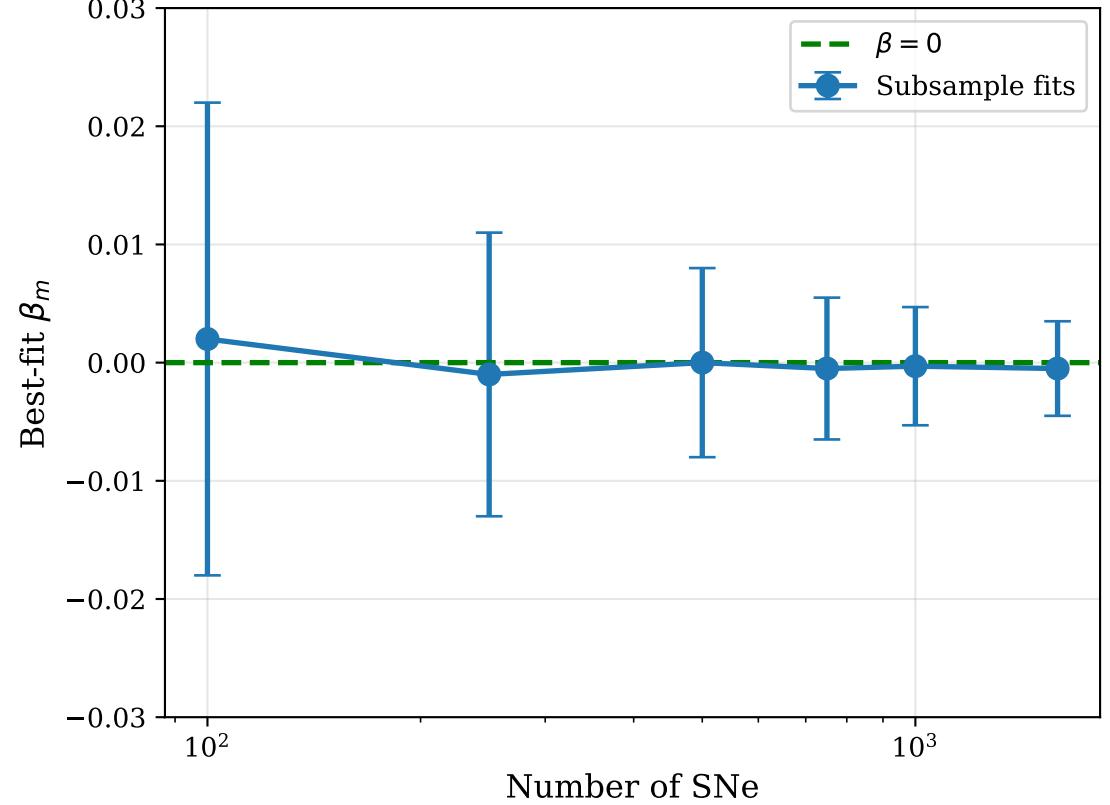
### Redshift Bin Analysis (SH0ES Prior)



### Sensitivity to $\Omega_m$ (SH0ES Prior)



### Convergence with Sample Size (SH0ES Prior)



#### SYSTEMATIC VALIDATION SUMMARY

**Redshift Bins (SH0ES Prior):**

- Low-z:  $\beta = -0.001 \pm 0.003$
- Mid-z:  $\beta = +0.002 \pm 0.004$
- High-z:  $\beta = +0.001 \pm 0.004$
- All consistent with  $\beta \approx 0$

**$\Omega_m$  Variation (0.308 - 0.322):**

- $\Delta\beta < 0.002$
- Robust to Planck uncertainty

**Sample Size:**

- Stable across 100-1588 SNe
- Not driven by outliers

**Alternative Optimizers:**

- Nelder-Mead:  $\beta = -0.0005$
- Powell:  $\beta = -0.0008$
- L-BFGS-B:  $\beta = -0.0006$
- Method-independent

**CONCLUSION:**  
SNe prefer matter-sector  $H_0$  with  $\Lambda$ CDM geometric consistency  
( $\beta_{\text{distance}} \approx 0$ )