Algorithm and Hardware Co-Design for Multi-Exit Dropout-based Bayesian Neural Networks

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Abstract—Reliable uncertainty estimation plays a crucial role in various safety-critical applications such as medical diagnosis and autonomous driving. In recent years, Bayesian neural networks (BayesNNs) have gained substantial research and industrial interests due to their capability to make accurate predictions with reliable uncertainty estimation. Nevertheless, the algorithmic complexity and the resulting hardware performance of BayesNNs hinders their adaptation in real-life applications. To bridge this gap, this paper proposes an algorithm and hardware co-design framework that can generate field-programmable gate array (FPGA)-based accelerators for efficient BayesNNs. At the algorithm level, we propose novel multi-exit dropoutbased BayesNNs, which effectively decreases the computational and memory overheads while achieving high accuracy and quality of uncertainty estimation. At the hardware level, this paper introduces a transformation framework that can generate FPGA-based accelerators for the proposed efficient multi-exit BayesNNs. Several optimization techniques such as the mix of spatial and temporal mappings are introduced to reduce resource consumption and improve the overall hardware performance. Comprehensive experiments demonstrate that our approach can achieve higher energy efficiency compared to CPU, GPU, and other state-of-the-art hardware implementations. To support the future development of this research, we have open-sourced our code at: https://github.com/os-hxfan/BayesNN_FPGA_Acc.git

Index Terms—Bayesian Neural Networks, Deep Ensembles, Multi-Exit Optimization, Uncertainty Prediction, Field Programmable Gate Array (FPGA)

I. INTRODUCTION

Deep neural networks (DNNs) have emerged as a cuttingedge frontier of artificial intelligence, with extensive applications in various domains ranging from computer vision [1] to natural language processing [2]. However, conventional DNNs are suffering from critical limitations: they operate akin to black boxes, rendering them incapable of explaining their decisions or unable to estimate their uncertainty reliably when making predictions [3]. The lack of reliable uncertainty estimation undermines the trustworthiness of conventional DNNs, making them unsuitable candidates for safety-critical applications [4], [5], [6] where reliable confidence and uncertainty measures are imperative, in addition to high accuracy.

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Bayesian neural networks (BayesNNs) [7] leverage Bayesian inference to model the epistemic uncertainty, in addition to the default predictive uncertainty, which addresses the limitation of conventional DNNs in estimating uncertainty. By representing the weights as probabilistic distributions, BayesNNs provide a principled approach to quantifying their uncertainty, enhancing the robustness and trustworthiness of their predictions in comparison to standard DNNs. Nevertheless, the benefits of BayesNNs also come with costs: the high dimensionality of modern BayesNNs introduces prohibitively expensive computation and memory overheads, making the exact Bayesian inference intractable [8].

Although various approximation approaches, such as Bayesby-backprop [9] and Monte-Carlo Dropout (MCD) [8], have been introduced to reduce the algorithmic and hardware complexities of BayesNNs, there are still two challenges, while deploying BayesNNs in real-world scenarios. First, BayesNNs generally perform worse than traditional deep ensembles [10] with respect to both accuracy and uncertainty estimation [11]. Second, even with the algorithmic approximations, the computational and memory demands of BayesNNs are still much higher than standard DNNs due to Monte-Carlo (MC) sampling, hindering their deployment in demanding applications, especially those with real-time requirements. While there is extensive research on hardware acceleration for deep learning algorithms, most existing efforts focus on domain-specific hardware [12], [13], [14] or design automation tools [15], [16] for standard DNNs such as convolutional DNNs (CNNs) [17], [18] and long short-term memory (LSTM) recurrent DNNs [19]. Hence there are urgent needs for hardware acceleration and algorithmic performance improvements for BayesNNs.

To reduce the algorithmic and hardware barriers of deploying BayesNNs in real-world applications, this paper proposes an algorithm and hardware co-design framework to improve the algorithm and hardware performance of BayesNNs. At the algorithm level, we propose a novel multi-exit dropout-based BayesNN that attains low computational and memory overheads while achieving better uncertainty estimation than traditional deep ensembles. Furthemore we introduce the hardware support to Masksemble [20]-based DNNs and we extend them to multi-exit architectures proposed in this work. Masksemble is an efficient variant of dropout-based BayesNN without the need for runtime sampling. Both approaches fall under the category of dropout-based BayesNNs, each demonstrating unique trade-offs between algorithmic and hardware performance. At the hardware level, we choose field-programmable gate array (FPGA) as our acceleration platform due to its superior flexibility over application-specific integrated circuit (ASIC) and its potential for achieving higher energy efficiency

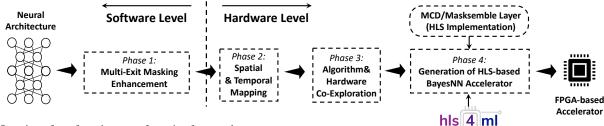


Fig. 1. Overview of our four-phase transformation framework.

over graphical processing units (GPUs) [21]. As shown in Figure 1, we propose a transformation framework to generate high-performance FPGA-based accelerators of multi-exit dropout-based BayesNNs for accurate and efficient uncertainty estimation. With several novel optimizations such as spatial-temporal mapping and algorithm-hardware co-exploration, the generated accelerators achieve higher energy efficiency than previous hardware implementations. To facilitate public access to our implementation, we open-source our code at https://github.com/os-hxfan/MCME_FPGA_Acc.git.

The contributions of this paper can be summarized as follows:

- Novel multi-exit dropout-based Bayesian neural network (BayesNN) approaches that achieve high quality of uncertainty estimation and high accuracy with low compute and memory overheads.
- A design framework for generating FPGA-based accelerators for multi-exit dropout-based BayesNNs with high hardware performance and energy efficiency.
- Various optimization strategies including partial dropout and spatial-temporal mapping and algorithm-hardware coexploration for algorithm and hardware performance improvements.
- A comprehensive evaluation of the proposed approach based on multiple models and datasets, demonstrating the effectiveness of our co-design approach.

This work extends our conference publication [3]. The extended material includes: 1) multi-exit support on Masksembles to improve their algorithmic performance; 2) FPGA-based acceleration of multi-exit Masksemble with optimized implementation to improve hardware performance; 3) a more comprehensive evaluation on the quality of uncertainty estimation across multiple models and datasets.

II. BACKGROUND AND RELATED WORK

A. Bayesian Neural Networks

In comparison to DNNs, BayesNNs demonstrate the capability to effectively mitigate overfitting and enable the estimation of the epistemic uncertainty through the utilization of Bayesian inference [7]. The main difference to non-BayesNNs is that, BayesNNs infer a distribution over their weights through the Bayes rule instead of point-wise weights estimates as encountered in standard DNNs [7]. Despite their advantages, the current BayesNNs [8] have limited utility in real-world settings because of their high dimensionality which renders the analytical calculation of the aggregated weight distribution computationally infeasible.

There are two main approaches aiming to approximate the intractable Bayesian inference required by BayesNNs: Markov chain Monte Carlo (MCMC) and variational inference (VI) [22]. MCMC-based methods directly sample from exact posterior distributions, and representative algorithms include Hamiltonian Monte Carlo (HMC) [23] and stochastic gradient Langevin Dynamic (SGLD) [24] approaches. Instead of sampling from the exact posterior, VI-based approaches [9], [8] use approximate variational distributions with a set of variational parameters. During training, the variational parameters are optimized to ensure the variational parameters are as close as possible to the exact posterior weight distribution.

B. Dropout-based Approximations for BayesNNs

1) MCD-based BayesNNs: Monte-Carlo dropout (MCD) [8] can be categorized as one of the VI-based approaches that adopt dropout [25] masks to perform efficient Bayesian inference [22]. MCD implements a random filterwise binary mask to remove connections between layers of a DNN. The mask values follow a Bernoulli distribution, where the binary random variables take on the value of 0 with a drop rate p. It has been proven that MCD could be interpreted mathematically as approximate Bayesian inference for deep Gaussian processes [8].

A key distinction between dropout traditionally employed in standard DNNs [25] and MCD [8] is that MCD applies dropout during both training and evaluation. During evaluation, MCD-based BayesNNs execute multiple forward passes with dropout on and the results are obtained by averaging the output of the multiple MC samples. Each forward pass uses an independently generated set of masks, allowing for quantification of the model uncertainty, ultimately enhancing the predictive uncertainty and accuracy.

2) Masksemble: By leveraging the predictive power of multiple independent DNNs, deep ensembles [10] can significantly improve accuracy and the quality of uncertainty estimation [10], while achieving higher robustness against dataset shift [11]. However, deep ensembles require the practitioner to train and maintain multiple DNNs in parallel which translates into significantly increasing the computational and memory costs during both training and evaluation.

Inspired by MCD-based BayesNNs, Masksembles [20] train a multi-member deep ensemble inside a single net by using sets of pre-defined dropout masks, effectively reducing the computational and memory overheads in comparison to naive deep ensembles. Besides, there are another two advantages of Masksembles when compared to MCD-based BayesNNs.

First, since the dropout masks are determined before training and inference, Masksembles eliminate the need for runtime sampling, which effectively reduces the hardware cost. Second, the overlap and correlation among different dropout masks in Masksembles can be strictly controlled, making it achieve a similar algorithmic performance as traditional deep ensembles.

C. Multi-Exit DNNs

Conventional deep learning architectures typically employ a single exit per network to generate predictions. However, a single-exit architecture exhibits two drawbacks when processing inputs that necessitate only intermediate features extracted from the middle layers. First, unnecessary computation and memory costs incur as single-exit DNNs always processes all the layers until the output layer even when the intermediate features are informative enough for predictions. Second, certain key features extracted from the intermediate layers might get lost as the network goes deeper, resulting in inaccurate prediction. To avoid these issues, multi-exit [26] DNNs are introduced that make predictions at various depths of a DNN in a single forward pass to improve both the algorithm and hardware performance.

While some architectures are specially designed to around the additional early-exits, like the *Multi-Scale DenseNet* [27], best performance is usually obtained through attaching multiple classifiers to high-performance networks like ResNet [27]. Common choices for where to attach the early exits is after specific number of floating-point operations (FLOPs) or groupings of convolutional layers [28], [29]. In this paper, we adopt the multi-exit enhancement as an approach to improve the accuracy, uncertainty estimationb quality and compute efficiency of BayesNNs.

D. Related Work

Extensive research has been conducted on DNNs and the use of FPGAs to accelerate them for various applications [1]. Representative work includes energy-efficient CNN acceleration [13] and FPGA-based real-time AI cloud services [12]. Significant research also targets design automation for DNNs, like the open source tool *hls4ml* supporting an automatic design flow involving high-level synthesis to promote low-power machine learning [16].

FPGA-based acceleration of BayesNNs has emerged recently [30]. Early designs include *Bynqnet*, an FPGA-based BayesNNs with quadratic activations for sampling-free uncertainty estimation [31]. Efficient FPGA implementations for 2D and 3D convolutional BayesNNs have been proposed in [32]. For recurrent Bayesian DNNs, [33] proposed an FPGA accelerator as well as an algorithmic co-design framework. Another work is *VIBNN*, an FPGA-based accelerator that supports Gaussian distribution-based BaynesNNs sampled at runtime [34]. Additionally, [35] proposed algorithmic and hardware optimizations for BayesNNs, exploiting their structured sparsity and redundant computations. Lastly, [36] explored quantisation in BayesNNs enabling their efficient execution on FPGAs using integer arithmetic.

In contrast to these approaches, this work extends and differs from the related work in several ways. First, it proposes a novel multi-exit dropout-based Bayesian DNN, which effectively decreases the computational and memory overhead while achieving high-quality uncertainty estimation and accuracy. Second, it introduces an automatic pipeline which translates a software description of the multi-exit BayesNN into a hardware design, executable on an FPGA. Third, it introduces several optimization techniques to reduce overall resource consumption and improve the hardware performance of multi-exit BayesNNs without harming their algorithmic performance. These contributions are generalisable to different datasets and DNN architectures, as shown in the experiments, and extensible to previous work mainly through the addition of sampling-based early exits and their hardware consideration.

III. MULTI-EXIT DROPOUT-BASED BAYESNNS

A. Multi-Exit Enhancement

As mentioned in Section II-B, while both MCD-based BayesNNs and Masksembles demonstrate the potential for efficient predictions and uncertainty estimation, they still suffer from limitations. On one hand, MCD-based approximation methods have been criticised due to their inferior performance in uncertainty estimation and confidence calibration when compared to deep ensembles [11], [10]. It has been empirically shown that the introduction of MCD layers after activations in vanilla MCD-based BayesNNs can hamper their predictive power, worsening both their accuracy and uncertainty quantification capabilities [37]. On the other hand, dropout-based BayesNNs impose a heavy computational burden since obtaining each a prediction necessitates running the entire network multiple times with respect to different dropout masks. This compute inefficiency hinders their widespread adoption for efficient uncertainty estimation. To address these drawbacks, this paper proposes a novel multi-exit enhancement for both dropout-based BayesNNs spanning MCD and Masksemble generated masks. By adopting this approach, we aim to achieve effective and efficient uncertainty estimation, mitigating the limitations of both methods.

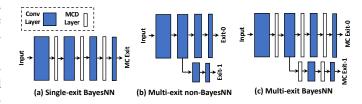


Fig. 2. Difference between a single-exit BayesNN, a multi-exit NN and a multi-ext BayesNN.

1) Multi-Exit MCD-based BayesNNs: Figure 2 presents the network architectures of three distinct approaches: a vanilla MCD-based BayesNN, a multi-exit non-BayesNN, and a multi-exit MCD-based BayesNN proposed in this work. By adding multiple exits to vanilla MCD-based BayesNNs, we propose multi-exit MCD-based BayesNNs, as decipted in Figure 2(c). In contrast to the traditional single-exit MCD-based BayesNNs, our multi-exit MCD-based approach makes

predictions from exits at different depths of the network, which effectively improves the quality of uncertainty estimation as well as hardware efficiency, as demonstrated in Section V-C. Furthermore, when compared to multi-exit non-BayesNNs, our proposed approach has the advantage of generating arbitrary prediction MC samples with the use of MCD layers, improving the flexibility for uncertainty estimation. An intriguing aspect of multi-exit MCD-based BayesNNs lies in the capability of capturing the uncertainty across different network depths. This stems from the utilization of diverse intermediate features extracted from different stages of the network to which enable the network to make diverse predictions.

2) Multi-Exit Masksembles: Although the use of MCD layers enables flexibility in making arbitrarrily many predictions, it also introduces hardware overhead due to the frequent Bernoulli samplingto generate the masks. To provide a hardware-efficient alternative, we propose multi-exit Masksembles that replace MCD layers with Masksemble layers. To avoid the highly correlated predictive results across multiple exits, we adopt the mask scale parameter [20] to control the overlap among different pre-defined masks. There are two distinct computational differences when comparing MCD- and Masksemble-based approaches. First, by adopting pre-defined binary masks, multi-exit Masksembles eliminate the need for sampling during runtime. As the locations of zeros are fixed, it provides us with the opportunity for designing efficient hardware accelerators to intelligently skip redundant computation associated with zero values, as discussed in Section IV-E. Second, MCD-based method applies dropout in the channel granularity, while Masksemble layer adopts point-wise masks with more fine-grained dropout granularity. These two difference lead to distinct hardware design requirements while accelerating multi-exit MCD-based BayesNNs and multi-exit Masksembles.

In this paper, we treat both MCD and Maskensemble layers as two distinct dropout layers, each exhibiting specific tradeoffs among accuracy, uncertainty and hardware performance. To fulfil the diverse needs of different users, we propose a codesign framework dedicated to optimizing the dropout layers, as elaborated in Section IV. This optimization enables users to tailor the final network for their target applications, ultimately leading to efficient prrediction and uncertainty estimation for various scenarios.

B. Partial Dropout

Applying dropout after every convolution incurs large computational overhead since it requires running the whole network multiple times to get the predictions. Inspired by [38], [39], [3], we propose partial dropout for both multi-exit Masksembles and multi-exit MCD-based BayesNNs. Rather than applying dropout to every learnable layer [8], we insert dropout layers starting from exits towards the input part of the network. We refer to the layers without dropout applied as the non-Bayesian component of the network. By placing dropout layers closer to each exit, fewer computations are required since the non-Bayesian results can be cached and reused for different prediction samples.

With partial dropout applied, both multi-exit MCD-based BayesNN and multi-exit Masksemble can be interpreted as ensembles of approximated BayesNNs built upon the non-Bayesian component feature extractor. Given an M-exit architecture with inputs \mathbf{X} , our approach first maps the data from input space into feature space by using $f_i(X)$, where $f_i(.)$ denotes the feature extractor of each exit with $1 \leq i \leq M$. Build upon the features extracted by $f_i(X)$, each exit then adopts the dropout-based Bayesian approach through either MCD or Masksemble layer to make predictions. The final result ensembles predictions from different approximated BayesNNs with multiple exits.

C. Compute Efficiency

We demonstrate that our proposed multi-exit dropout-based BayesNNs have higher compute efficiency over single-exit BayesNNs in making predictions. Given that the FLOPs of the non-Bayesian feature extractor and all the exits are $FLOP_{main}$ and $FLOP_{exit}$ respectively. To get a single MC sample, it is necessary to run the entire BayesNN end-to-end and the computational cost of running N_{sample} MC samples can be formulated as:

$$N_{sample} \times (FLOP_{main} + FLOP_{exit}).$$
 (1)

In contrast, the required FLOPs of an N_{exit} multi-exit dropout-based BayesNN to get the same number of predictions is:

$$FLOP_{main} + \frac{N_{sample}}{N_{exit}} \times FLOP_{exit}.$$
 (2)

The reduction rate is given by dividing Equation 1 by Equation 2,

$$\frac{1+\alpha}{\frac{1}{N_{sample}} + \frac{\alpha}{N_{exit}}},\tag{3}$$

where $\alpha = \frac{FLOP_{exit}}{FLOP_{main}}$. The reduction rate varies by different multi-exit architectures, depending on N_{sample} , N_{exit} and α .

Section II-C discusses the wide variety of possible methods in which multi-exit networks can be created and trained. In this work, the exit branches are placed according to the approach used in [28]. Semantic groupings are formed for each network, splitting the network architecture into "blocks" separated by pooling layers. An exit branch is then placed after each of these blocks. In order to allow for more direct validation of the work performed in this paper, the bidirectional distillation training method in [28] is used.

IV. TRANSFORMATION FRAMEWORK

A. Framework Overview

This section describes the proposed transformational framework presented in Figure 1. It comprises multiple steps: (1) adaptation of the architecture and evaluation protocol for multi-exit dropout, (2) spatial and temporal mapping optimization, (3) algorithm and hardware co-exploration and (4) generation of FPGA-based accelerators for BayesNNs using High-Level Synthesis (HLS).

Given the neural architecture description as an input, the first phase applies early-exits enhanced either with MCD [8]

or Masksemble [20] approaches, and decides the number of MC samples according to the user-specified requirements. The second phase exploits spatial and temporal processing in BayesNNs and implements optimisations to improve the runtime hardware performance. The third phase involves algorithm and hardware co-exploration to optimize design parameters such as bitwidth and execution strategies depending both on the network architecture as well as the available hardware resources in terms of DSPs or memory budget. Given the network architecture as well as the obtained hardware parameters, the last phase produces the final HLS-based hardware implementation executable on an FPGA. We adopt the design flow and HLS template of common NN layers from hls4ml [16] and we develop an HLS-based implementation of MCD/Masksemble layers and Keras-to-HLS conversion into the design flow in order to generate the executable hardware implementation.

B. Multi-Exit Dropout: Phase 1

Multi-exit dropout phase optimizes the design parameters for multi-exit dropout-based BayesNNs, including: the number of exits N_{exit} , the number of forward passes N_{pass} , the type of dropout layers and the associated dropout parameters, and the total number of MC samples N_{sample} . The parameters tradeoff software and hardware performance, namely accuracy, calibration and latency. For instance, the total MC samples N_{sample} from a multi-exit dropout BayesNN with N_{exit} exits and N_{pass} passes is calculated as $N_{sample} = N_{pass} \times N_{exit}$. Higher values of N_{exit} and N_{pass} can improve accuracy and calibration but also increase the total N_{sample} count. This leads to worse hardware performance because more forward passes through the network or the exits are needed, increasing computational and memory demands. To optimize these hyperparameters for different applications and architectures, balancing both algorithm and hardware metrics, we propose a multi-exit dropout optimization flow as shown in Figure 3.

The multi-exit dropout optimization starts by constructing different dropout-based BayesNNs based on the default input architecture provided by the user. By inserting N_{exit} exits with either MCD or Masksemble layers, different BayesNNs candidates are constructed and trained on the target dataset. After training, we evaluate each model with respect to software and hardware metrics like accuracy, calibration, and FLOPs. Models that do not meet specified constraints on these metrics, given by the users, are filtered out. Then, according to the optimization metric priority, design space exploration is performed to find the optimal design configuration via grid search. The priority can be set with respect to a single or multiple metrics, specified by the user e.g. accuracy, calibration and the number of FLOPs. The final optimized design is fed into the next stage for hardware design generation.

C. Spatial and Temporal Mappings: Phase 2

Bayesian components with either MCD or Masksemble layers require multiple forward passes to generate MC samples from the predictive distribution. Compared with conventional

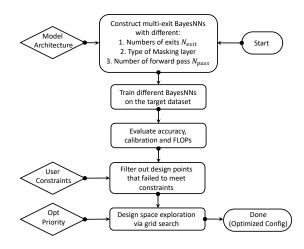


Fig. 3. Optimization flow.

non-Bayesian NNs, the Bayesian components exhibit concurrency along the MC sampling dimension. This creates new opportunities for parallelism compared to non-Bayesian networks. Therefore, we propose two mapping hardware optimisation strategies, spatial and temporal, to accelerate Bayesian NNs, which are illustrated in Figure 4.

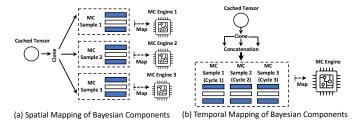


Fig. 4. Spatial and temporal mappings for Bayesian components.

In both mapping strategies, the data generated from the last non-Bayesian layer is cached and cloned. As shown in Figure 4(a), spatial mapping uses separate MC engines for each sample. Although spatial mapping effectively reduces latency by enabling parallel sampling, it also significantly increases computational resource usage when the number of MC samples becomes high. To alleviate this issue, we propose temporal mapping that shares one MC Engine among multiple MC samples. As shown in Figure 4(b), the cloned copies of the cached data are concatenated before feeding it into the shared engine. The engine then maps the computation of different MC samples one by one onto a single MC Engine. Our approach optimizes the mix of spatial and temporal mappings to meet different latency and resource constraints.

D. Algorithm and Hardware Co-Exploration: Phase 3

Our hardware accelerator has various design parameters, such as the implementation strategy used in *hls4ml*, layer reuse factors and Bayesian mapping approaches. On the algorithm side, given an input model architecture, we can optimize hyperparameters like the number of channels for different layers and bitwidths for activations/weights. We co-explore both algorithm and hardware parameters using grid search to optimize the design with similar algorithm accuracy to

defaults. To reduce search costs, we experiment with heuristics such that the bitwidth for activations or weights is chosen from $\{4,6,8,16\}$ bits and the channels selected from $\{C,\frac{C}{2},\frac{C}{4},\frac{C}{8}\}$ with C being the original number of channels. Users can also define other dimensions for the search space. This joint optimization allows customizing algorithmic and hardware configurations for different constraints.

E. Generation of FPGA-based Accelerator: Phase 4

We generate HLS-based accelerators using hls4ml design and our custom templates for MCD/Masksemble layers. The accelerators are synthesized and implemented in Vivado HLS to produce FPGA bitstreams for deployment. The pseudocodes of HLS-based implementation of MCD and Masksemble layers are presented in Algorithm 1 and 2, respectively. We apply optimizations like pipelining and caching, as described in the previous Section, to improve performance. In both implementations, the HLS directive *HLS PIPELINE* is used to improve the overall performance through pipelining. We cache the temporary result in the variable temp, before generating the final outputs. The hardware receives layer inputs and streams outputs to the next layer. For MCD, the dropout rate $P_{dropout}$ is a specified parameter by the user at the beginning of running each model. A multiplexer selects between zero or the input scaled by the rate based on comparing to a random number. The control signal of the multiplexer is generated by comparing $P_{dropout}$ with uniform_random. To support the MCD layer with arbitrary $P_{dropout}$, a random number generator is used in our design to generate uniform_random. For Masksemble, the masks are provided as inputs, avoiding sampling in hardware. The inputs with mask values being one are passed through to the outputs.

Algorithm 1 Pseudocode of MCD layer

```
1: Input: input[dropout_size], keep_rate
2: Output: output[dropout_size]
3: for (i from 0 to dropout_size) do ▷ #pragma PIPELINE
4: temp = input[i]
5: uniform_random = random_number_generator()
6: if (uniform_random > keep_rate) then temp = 0
7: output[i] = temp * keep_rate
```

Algorithm 2 Pseudocode of Masksemble layer

```
1: Input: input[mask_size], mask_index,
2: generated_masks[mask_num][mask_size]
3: Output: output[mask_size]
4: for (i from 0 to mask_size) do ▷ #pragma PIPELINE
5: mask_value = generated_masks[mask_index][i]
6: if (mask_value == 0) then
7: output[i] = 0
8: else
9: output[i] = input[i]
```

V. EXPERIMENTS AND EVALUATION

Our optimization framework is implemented in Python 3.8.12, PyTorch 1.11.0, and Keras 2.9.0. We use Vivado-HLS

2020.1 for hardware implementation. QKeras 0.9.0 is used for quantization. The latency and resource consumption are obtained from C-synthesis reports provided by Vivado-HLS. Vivado 2020.1 is used to run place and route for the final designs. We set Xilinx Kintex XCKU115 as our target FPGA board. All the designs are optimized by our spatial-temporal mapping and algorithm-hardware co-exploration to ensure they can be fitted into the target platform.

A. Resource Cost of Being Bayesian

Inserting dropout layers transforms conventional DNNs into BayesNNs, enabling reliable uncertainty estimation required by various safety-critical applications. To quantitatively investigate the hardware overhead imposed by the transformation, we evaluate the resource consumption of Bayesian accelerators against their non-Bayesian counterparts. Three BayesNNs and datasets are used in our experiments, i.e., LetNet5 on MNIST, ResNet-18 on CIFAR-10, and VGG-11 on SVHN. As we aim to evaluate the resource cost of being Bayesian, all the models use single-exit to eliminate the hardware overhead introduced by the multi-exit optimization. We generate different Bayesian accelerators with distinct numbers of dropout layers using our proposed design flow from Section IV. For non-Bayesian accelerators, we set the number of dropout layers as zero. In order to fit BayesNNs onto FPGA, we apply quantization and custom channel numbers to ease the memory requirements. To further reduce compute resource consumption, we adopt temporal mapping on all the hardware designs.

Figure 6 shows the resource consumption of Block RAM (BRAM), DSP, Flip-Flop (FF) and Look-up Tables (LUTs) We implement two different dropout types, MCD and Masksemble with varied numbers of dropout layers for each model. As can be observed in all three models, the BRAM and DSP usage stays almost the same across different numbers of dropout layers and dropout types. The reason is that dropout layers do not contain compute and memory-intensive operations. The designs of both MCD and Masksemble layers can be implemented by mainly just using logic resources. In contrast, an increasing trend can be observed in both FF and LUT consumption when more dropout layers are inserted. The most significant increase is found on MCD-based Bayes-VGG, where nearly 13% more FF resources are utilized for the insertion of 8 dropout layers. However, this overhead is caused by inserting MCD layers after every convolution. With our proposed partial dropout Section III-B, the LUT and FF resource overheads of one MCD layer are just around $1\% \sim 2\%$, demonstrating the resource-efficiency of our codesign approach.

B. Latency Reduction of Masksemble and Spatial Mapping

By adopting a set of pre-defined dropout masks, Masksembles eliminate the need for runtime Bernoulli sampling, exhibiting higher hardware efficiency than MCD-based BayesNNs. To quantitatively evaluate the hardware performance improvement of Masksembles compared with MCD-based BayesNNs, we generate different accelerators for both approaches with distinct numbers of dropout layers. We set

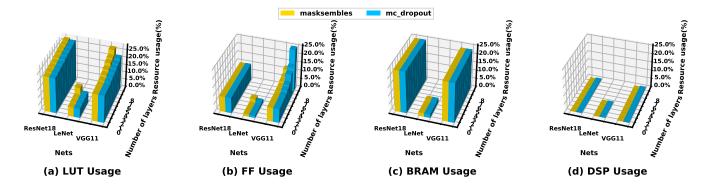


Fig. 5. Resource consumption of mask-based BayesNNs with LeNet, ResNet18 and VGG11 as network backbones. The quantization and custom number of channels are applied to fit models onto FPGAs.

TABLE I
PERFORMANCE COMPARISON AMONG SE CNNS, MCD BAYESNNS, ME AND MCD-ME BAYESNNS WITH 32-BIT FLOATING POINT (FP32).

	ResNet18				VGG19				
	Acc-Opt		ECE-Opt		Acc-Opt		ECE-Opt		
	Accuracy	FLOPs	ECE	FLOPs	Accuracy	FLOPs	ECE	FLOPs	
SE	0.752 ± 0.002	1.00	0.0840 ± 0.0008	1.00	0.693 ± 0.002	1.00	0.165 ± 0.006	1.00	
MCD	0.758 ± 0.002	N	0.069 ± 0.001	N	0.696 ± 0.004	N	0.131 ± 0.006	N	
Mask	0.759 ± 0.004	N	0.065 ± 0.02	N	0.709 ± 0.004	N	0.156 ± 0.003	N	
ME	0.7719 ± 0.0006	1.026 ± 0.003	0.017 ± 0.002	1.026 ± 0.003	0.747 ± 0.002	0.977	0.025 ± 0.001	0.46 ± 0.05	
MCD+ME (Ours)	0.776 ± 0.001	1.019 ± 0.004	0.014 ± 0.001	0.672 ± 0.003	0.747 ± 0.001	0.982	0.017 ± 0.001	0.45 ± 0.02	
Mask+ME (Ours)	0.764 ± 0.004	1.032 ± 0.006	0.016 ± 0.001	0.605 ± 0.001	0.741 ± 0.001	0.982	0.019 ± 0.003	0.49 ± 0.05	

TABLE II
PERFORMANCE COMPARISON AMONG SE CNNS, MCD BAYESNNS, ME AND MCD-ME BAYESNNS WITH 32-BIT FLOATING POINT (FP32).

			ResN	Vet18			
	Acc-Opt		ECE	-Opt	aPE-Opt		
	Accuracy	FLOPs	ECE	FLOPs	aPE	FLOPs	
SE	0.752 ± 0.002	1.00	0.0840 ± 0.0008	1.00	0.693 ± 0.002	1.00	
MCD	0.758 ± 0.002	N	0.069 ± 0.001	N	0.696 ± 0.004	N	
Mask	0.759 ± 0.004	N	0.065 ± 0.02	N	0.709 ± 0.004	N	
ME	0.7719 ± 0.0006	1.026 ± 0.003	0.017 ± 0.002	1.026 ± 0.003	0.747 ± 0.002	0.977	
MCD+ME (Ours)	0.776 ± 0.001	1.019 ± 0.004	0.014 ± 0.001	0.672 ± 0.003	0.747 ± 0.001	0.982	
Mask+ME (Ours)	0.764 ± 0.004	1.032 ± 0.006	0.016 ± 0.001	0.605 ± 0.001	0.741 ± 0.001	0.982	

the *hls4ml* optimization strategy as "*Resource*" to ensure the generated accelerators can be fitted onto the target FPGA board. Figure 6(a)~(c) show the normilzed latency of Bayes-LetNet5, Bayes-ResNet and Bayes-VGG-11, respectively. As it can be observed, the use of Masksemble layers can effectively reduce the latency of the generated accelerators. This latency reduction is more significant on Bayes-LetNet and Bayes-VGG with a larger number of dropout layers.

Spatial mapping is another optimization that we propose to reduce latency when more hardware resources are available on the FPGA. To demonstrate the effectiveness of spatial mapping in reducing latency, we evaluate accelerators with and without spatial mapping optimization. As the type of dropout layer will not affect this demonstration, we take MCD-based BayesNNs as examples and apply partial masking by only inserting MCD

after the last convolutional layer. The *hls4ml* optimization strategy is set as "*Latency*" to ensure best latency performance. Figure 6(d)~(e) show the latency results of both optimized and un-optimized accelerators with different numbers of MC samples on three network backbones. As can be seen, the latency of an unoptimized accelerator increases linearly with the increase of MC samples. In contrast, the latency of spatial-optimized accelerators stays almost the same when the number of MC samples increases, demonstrating the effectiveness of spatial mapping. The improvement of spatial mapping stems from its mechanism of deploying multiple physical cores to compute MC samples in parallel.

	CPU	GPU	ASPLOS'18 [34]	DATE'20 [31]	DAC'21 [3]	TPDS'22 [35]	Our Work
Platform	Intel Core i9-9900K	NVIDIA RTX 2080	Altera Cyclone V	Zynq XC7Z020	Arria 10 GX1150	Arria 10 GX1150	XCKU 115
Frequency (MHz)	3600	1545	213	200	225	220	181
Technology	14 nm	12 nm	28 nm	28 nm	20 nm	20 nm	20 nm
Power (W)	205	236	6.11	2.76	45.00	43.6	4.6
Latency (ms)	1.26	0.57	5.5	4.5	0.42	0.32	0.89
Energy Efficiency (J/Image)	0.258	0.134	0.033	0.012	0.019	0.014	0.004

TABLE III
PERFORMANCE COMPARISON OF OUR FINAL FPGA DESIGNS WITH CPU, GPU, AND OTHER FPGA-BASED IMPLEMENTATIONS.

C. Effect of Multi-Exit Enhencement

To demonstrate the advantage of multi-exit BayesNNs over the baseline approaches, we evaluate two commonly-used multi-exit models, VGG19 and ResNet18 for image classification. Cifar100 dataset, a curated subset of a larger dataset scraped from the web containing photo-realistic tiny 32×32 images with a single main object, is used in this experiment.

We compare six different implementations: *i)* Single-exit model with only one exit at the end of the network (SE). There is no MCD or Multi-Exit applied, which is the original implementation of both the *ResNet-18* and *VGG-19*. *ii)* MCD-based BayesNN without multi-exit (MCD). The MCD is only applied to the single exit of the network. *iii)* Masksemble-based BayesNN without multi-exit (Mask). The Masksemble layer is only applied to the single exit of the network. *iv)* Multi-exit model without dropout layers (ME). We add one exit after each ResNet and VGG block to make multiple exits. *v)* MCD-based BayesNN with multi-exit (MCD + ME). The MCD is applied

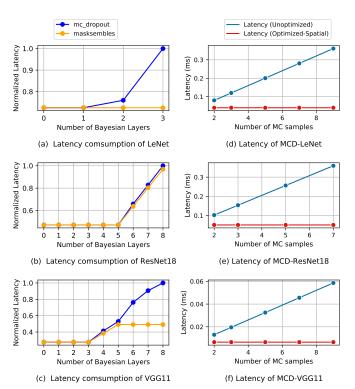


Fig. 6. Latency reduction of different hardware optimization techniques.

to every exit of the network. vi) Maskemble-based BayesNN with multi-exit (Mask + ME). The Masksemble layer is applied to every exit of the network. Stochastic gradient descent (SGD) is used with a weight decay of 5×10^{-4} , an initial learning rate of 0.1 and a momentum of 0.9, along with a batch size of 64.

As discussed previously, the usage of too many dropout layers in a BayesNN can overregularize the network and adversely affect performance. However, there is no standard method to find the best balance between the level of dropout and calibration. Therefore, a small grid search is performed over different dropout configurations. For MCD layers, we optimize the dropout rates from 0.125, 0.25, 0.375 and 0.5. The scale parameter of the Masksemble layer is selected from 3, 4, 5 and 6. Similarly, the confidence threshold which optimally balances the computational cost and the network performance is found through testing the same thresholds as in [29]: 0.1, 0.15, 0.25, 0.5, 0.6, 0.7, 0.8, 0.9, 0.95, 0.99, 0.999. It is noted that two sets of results from performing confidencebased exiting are calculated, using the predictions at each exit or the largest possible ensemble at each exit respectively. Each ensemble is an equally weighted average of the predictions from each exit, as in [40].

The grid search covers all combinations of the above dropout configurations, which is applied to the= networks. The predictions from each of the exits and the ensembles formed by averaging the results from each exit are calculated, alongside the predictions from confidence exiting. The best results are presented in Table II with the confidence calibration captured by expected calibration error (ECE) [41]: a low value of ECE denotes a higher quality. As the dropout rate of MCD and the confidence threshold of multi-exit may affect both accuracy and calibration, two configurations for each implementation and model are reported: those that achieve the highest accuracy (*Acc-Opt*) and those with the lowest ECE (*ECE-Opt*). For each configuration, we also calculate the FLOPs as a fraction of the SE implementation.

On ResNet18, our approach, MCD + ME, improves the accuracy by $2.4\% \pm 0.002\%$ with only 0.019 times more FLOPs compared with the SE implementation. Our method also shows higher accuracy than both MCD and ME implementations. In Acc-ECE, we achieve the lowest ECE and FLOPs among four implementations. A similar trend can also be observed in VGG-19. Moreover, our approach can match or outperform both of the methods individually, while costing a

 $\label{thm:continuous} TABLE\ IV$ Power breakdown of our FPGA-based accelerator.

		Dyn	gt				
	Clocking	Logic& Signal	BRAM	Ю	DSP	Static	Total
Used	0.374	1.359	0.422	0.998	0.191	1.299	4.6
Percentage	8%	30%	9%	21%	4%	28%	100%

similar amount of FLOPs. The best model is able to massively reduce the ECE of the SE implementation by 0.148 ± 0.006 , an improvement of almost 90%, while costing less than half the amount of FLOPs. These results show that multi-exit BayesNNs can lead to better calibrated and more powerful networks, while costing similar or fewer FLOPs.

D. Comparison with CPU, GPU, and FPGA implementations

To demonstrate the energy efficiency of our approach, we also compare it against CPU, GPU, and other FPGA-based implementations. The comparison uses MNIST dataset since it is the most common dataset across different work [34], [31], [3], [35]. As both [34] and [31] do not support *Bayes-LeNet5*, we use their reported throughput (GOP/s) to estimate their performance on *Bayes-LeNet5*. The performance is obtained by using three MC samples. Both CPU and GPU performance are quoted from the vanilla implementations of MCD-based BayesNNs in [35]. Although there are some other BayesNN accelerators [42], [30], they do not report any end-to-end latency and energy consumption.

As shown in Table III, our design achieves 65 and 33 times higher energy efficiency than CPU and GPU implementations, despite the FPGA adopting 20nm technology while the CPU adopting 14nm technology and the GPU adopting 12nm technology. Our accelerator also shows lower latency and better energy efficiency than both [34] and [31]. Although both [3] and [35] are faster than our design, they consume much higher energy due to the high resource utilization and frequent data transfer between on-chip and off-chip memory, leading to nearly 5 and 4 times lower energy efficiency than our design. Also, compared with their Verilog-based implementations, our HLS-based accelerator has advantages in development time [43], which can improve designer productivity and can facilitate extending our approach to cover other NNs such as LSTM [19]. Table IV provides the power consumption breakdown obtained from the Xilinx Power Estimator (XPE) tool after place and route. The dynamic power occupies 72% of the total power. The logic&signal and IO consume most of the dynamic power, accounting for 30% and 21%, respectively. The high IO power consumption results from our spatial mapping strategy with multiple MC engines running in parallel.

VI. CONCLUSION

This paper proposes an algorithm and hardware co-design approach for accelerating dropout-based multi-exit Bayesian Neural Networks (BayesNNs). On the algorithm side, we propose novel multi-exit dropout-based BaeysNNs that achieve

high algorithmic performance with low computational and memory overhead. At the hardware level, we introduce a transformation framework to generate FPGA-based accelerators for multi-exit dropout-based BayesNNs. Multiple optimizations including the mix of spatial and temporal mappings are proposed to further improve the overall performance of dropout-based BaeysNNs. Comprehensive experiments demonstrate that our approach achieves higher algorithmic and energy efficiency than state-of-the-art designs. To facilitate public access to BayesNNs hardware accelerators, we have made our code accessible as an open-source resource at: https://github.com/os-hxfan/BayesNN_FPGA_Acc.git In the future, we aim to automate the transformation framework, extend support for attention-based BayesNNs, and incorporate capabilities such as run-time reconfiguration.

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