

Basic Trigonometric Identities and Equations

Trigonometric Identities

Quotient Identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \quad \cot \theta = \frac{\cos \theta}{\sin \theta}$$

Reciprocal Identities

$$\sin \theta = \frac{1}{\csc \theta} \quad \cos \theta = \frac{1}{\sec \theta} \quad \tan \theta = \frac{1}{\cot \theta}$$

Pythagorean Identities

$$\sin^2 \theta + \cos^2 \theta = 1 \quad \tan^2 \theta + 1 = \sec^2 \theta \quad \cot^2 \theta + 1 = \csc^2 \theta$$

$$\sin^2 \theta = 1 - \cos^2 \theta \quad \tan^2 \theta = \sec^2 \theta - 1 \quad \cot^2 \theta = \csc^2 \theta - 1$$

Using the identities you now know, find the trig value.

1.) If $\cos \theta = 3/4$, find $\sec \theta$

$$\sec \theta = \frac{1}{\cos \theta} = \frac{1}{\frac{3}{4}} = \frac{4}{3}$$

2.) If $\cos \theta = 3/5$, find $\csc \theta$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta + \left(\frac{3}{5}\right)^2 = 1$$

Simplify each expression

1.) If
 $\cos \theta = 3/4$,
find $\sec \theta$

$$\sec \theta = \frac{1}{\cos \theta}$$

2.) If $\cos \theta = 3/5$, find
 $\csc \theta$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta + \left(\frac{3}{5}\right)^2 = 1$$

2.) If $\cos \theta = 3/5$, find
 $\csc \theta$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta + \left(\frac{3}{5}\right)^2 = 1$$

Example

Simplify:

a) \csc

Practice

| | | | |
|--------------|--------------|--------------|--------------|
| $\sec\theta$ | $\sec\theta$ | $\sec\theta$ | $\sec\theta$ |
| $\sec\theta$ | $\sec\theta$ | $\sec\theta$ | $\sec\theta$ |

