

Design-by-Contract Approach

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Basics

- ▶ To specify the constraints that govern the design and correct use of a **class**
- ▶ Contract:
 - ▶ **Class invariant**: assertions about the state of an object that hold before and after each method call
 - ▶ **Preconditions**: assertions about the state of the object and the argument values that must hold prior to invoking the method
 - ▶ **Postconditions**: assertions about the state of the object after the execution of a method

¹Bertrand Meyer. Applying Design by Contract. In Computer IEEE, vol. 25, no. 10, October 1992

Example

Bank Account

- ▶ Property: `balance`
- ▶ Operations: `deposit(int amt)`, `withdraw(int amt)`
- ▶ Invariant: `balance > 0`
- ▶ `deposit(int n)`:
 - ▶ **pre:** $n > 0$
 - ▶ **post:** $\text{balance}' = \text{balance} + n$
- ▶ `withdraw(int n)`:
 - ▶ **pre:** $n < \text{balance}$
 - ▶ **post:** $\text{balance}' = \text{balance} - n$

Interpretation

- ▶ **Precondition:** an **obligation for the client** and a **guarantee for the supplier**
- ▶ **Postcondition:** an **obligation for the supplier** and a **guarantee for the client**
- ▶ **Invariant:** a property that is **assumed on entry** and **guaranteed on completion**

Implementation

- ▶ The code is enriched with a specification of the contract
- ▶ A **run-time mechanism** monitors the satisfaction of the contract
 1. When a client invokes an method, the precondition is checked and an **exception is raised** if the precondition is violated
 - ▶ the client is blamed
 2. The provider executes the invoked code
 3. After completion, the postcondition is evaluated and an **exception is raised** if the postcondition is violated
 - ▶ the provider is blamed

Contracts and Higher-order functions

```
filter ((int → bool) pred) : ([int] → [int])
```

- ▶ it receives a predicate to check whether an integer is an even number, and
- ▶ it returns a function that allows to filter the elements of a list that are even

Its contract could be:

- ▶ **pre:** $\forall x : \text{int}. (x \bmod 2 = 0) \iff \text{pred } x$
- ▶ **post:** $\forall x : \text{int}. x \in (\text{filter } \text{pred}) \text{ } ls \iff (x \in ls \ \& \ x \bmod 2 = 0)$

Issues

- ▶ Checking of pre- and postconditions
 - ▶ we cannot check whether `pred` satisfies `pre` when `filter` is invoked
 - ▶ we cannot check if `(filter pred)` satisfies `post` on return
- ▶ Blame assignment:
 - ▶ if `(filter pred)` violates the postcondition, it may be because of `pred`
 - ▶ `filter` may use `pred` as a parameter when invoking auxiliary functions (and violates the contracts of auxiliary functions)

- ▶ An extension of Programming Computable Functions (PCF) with contracts for higher-order functions
- ▶ Expressions can be decorated with contracts that link a client and a provider
- ▶ Contracts are evaluated only over values of basic types (not over functions)
- ▶ When a contract is violated, blame is assigned to either the client or the provider

²Robert Bruce Findler, Matthias Felleisen: ICFP 2002: Contracts for higher-order functions.

³Christos Dimoulas, Robert Bruce Findler, Cormac Flanagan, Matthias Felleisen: Correct blame for contracts: no more scapegoating. POPL 2011.

Programming Computable Functions (PCF)

Syntax

Types	t	$::=$	$b \mid t \rightarrow t$
	b	$::=$	$\text{int} \mid \text{bool} \mid \text{unit}$
Expression	e	$::=$	$v \mid x \mid e_1 e_2 \mid \text{if } e \text{ then } e_1 \text{ else } e_2 \mid \dots (\text{number expr})$
Value	v, w	$::=$	$() \mid \text{true} \mid \text{false} \mid \dots$ $\mid \lambda x. e$

Programming Computable Functions (PCF)

Typing $\Gamma \vdash e : t$

[t-unit]

$$\frac{}{\Gamma \vdash () : \text{unit}}$$

[t-true]

$$\frac{}{\Gamma \vdash \text{true} : \text{bool}}$$

[t-false]

$$\frac{}{\Gamma \vdash \text{false} : \text{bool}}$$

[t-var]

$$\frac{}{\Gamma, x : t \vdash x : t}$$

[t-if]

$$\frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash e_1 : t \quad \Gamma \vdash e_2 : t}{\Gamma \vdash \text{if } e \text{ then } e_1 \text{ else } e_2 : t}$$

[t-fun]

$$\frac{\Gamma, x : t \vdash e : s}{\Gamma \vdash \lambda x. e : t \rightarrow s}$$

[t-app]

$$\frac{\Gamma \vdash e : t \rightarrow s \quad \Gamma \vdash e_2 : t}{\Gamma \vdash e_1 e_2 : s}$$

Programming Computable Functions (PCF)

Semantics $e \rightarrow e$

[if-true]

$$\frac{}{\text{if true then } e_1 \text{ else } e_2 \rightarrow e_1}$$

[if-false]

$$\frac{}{\text{if false then } e_1 \text{ else } e_2 \rightarrow e_2}$$

[beta]

$$\frac{}{(\lambda x. e)v \rightarrow e\{v/x\}}$$

[context]

$$\frac{e_1 \rightarrow e_2}{\mathcal{C}[e_1] \rightarrow \mathcal{C}[e_2]}$$
$$\mathcal{C} ::= [] \mid \mathcal{C}e \mid v\mathcal{C} \mid \text{if } \mathcal{C} \text{ then } e_1 \text{ else } e_2$$

Programming Computable Functions (PCF) + Contracts

$\text{mon}^{k,l}(\kappa, e)$

- ▶ Contract κ mediates the interaction between e (provider) and its context (client)
- ▶ any value that flows between e and its context is monitored for conformance with κ
- ▶ k and l are the blame labels for the two parties to the contract

error^l

- ▶ blame is assigned to l

Programming Computable Functions (PCF) + Contracts

$\text{flat}(e)$

- ▶ A contract for an expression of a basic type `unit`, `bool`, `unit`, ...
- ▶ e is a predicate (for values of a basic type)

$\text{flat}(\lambda x. x \geq 0)$

$\kappa_1 \mapsto \kappa_2$

- ▶ A contract for a function
- ▶ κ_1 is the contract for the domain (the precondition)
- ▶ κ_2 is the contract for the codomain (the postcondition)

$\text{flat}(\lambda x. x \geq 0) \mapsto \text{flat}(\lambda x. x \leq 0)$

Programming Computable Functions (PCF) + Contracts

Syntax

Types $t ::= b \mid t \rightarrow t \mid \text{con}(t)$

$b ::= \text{int} \mid \text{bool} \mid \text{unit}$

Contracts $\kappa ::= \text{flat}(e) \mid \kappa \mapsto \kappa$

Expression $e ::= v \mid x \mid e_1 e_2 \mid \text{if } e \text{ then } e_1 \text{ else } e_2 \mid \dots (\text{number expr})$
 $\mid \text{mon}^{I,I}(\kappa, e) \mid \text{error}^I$

Value $v, w ::= () \mid \text{true} \mid \text{false} \mid \dots$
 $\mid \lambda x. e$

Programming Computable Functions (PCF) + Contracts

Example

```
ge =  $\lambda x. x \geq 0$   
le =  $\lambda x. x \leq 0$   
op =  $\lambda x. x * (-1)$   
opmon = monk,l(flat(ge)  $\mapsto$  flat(le), op)
```

Programming Computable Functions (PCF)+ Contracts

Typing $\Gamma \vdash e : t$

[t-unit]

$$\frac{}{\Gamma \vdash () : \text{unit}}$$

[t-true]

$$\frac{}{\Gamma \vdash \text{true} : \text{bool}}$$

[t-false]

$$\frac{}{\Gamma \vdash \text{false} : \text{bool}}$$

[t-var]

$$\frac{}{\Gamma, x : t \vdash x : t}$$

[t-if]

$$\frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash e_1 : t \quad \Gamma \vdash e_2 : t}{\Gamma \vdash \text{if } e \text{ then } e_1 \text{ else } e_2 : t}$$

[t-fun]

$$\frac{\Gamma, x : t \vdash e : s}{\Gamma \vdash \lambda x. e : t \rightarrow s}$$

[t-app]

$$\frac{\Gamma \vdash e : t \rightarrow s \quad \Gamma \vdash e_2 : t}{\Gamma \vdash e_1 e_2 : s}$$

Typing for contracts $\Gamma \vdash e : t$

[t-flat]

$$\frac{\Gamma \vdash e : o \rightarrow \text{bool}}{\Gamma \vdash \text{flat}(e) : \text{con}(o)}$$

[t-contract]

$$\frac{\Gamma \vdash \kappa_1 : \text{con}(t_1) \quad \Gamma \vdash \kappa_2 : \text{con}(t_2)}{\Gamma \vdash \kappa_1 \mapsto \kappa_2 : \text{con}(t_1 \rightarrow t_2)}$$

[t-mon]

$$\frac{\Gamma \vdash \kappa : \text{con}(t) \quad \Gamma \vdash e : t}{\Gamma \vdash \text{mon}^{k,l}(\kappa, e) : t}$$

[t-error]

$$\frac{}{\Gamma \vdash \text{error}^l : t}$$

Programming Computable Functions (PCF) + Contracts

Semantics $e \rightarrow e$

$$\begin{array}{c}
 \text{[if-true]} \\
 \hline
 \text{if true then } e_1 \text{ else } e_2 \rightarrow e_1 \\
 \text{[if-false]} \\
 \hline
 \text{if false then } e_1 \text{ else } e_2 \rightarrow e_1 \\
 \text{[beta]} \\
 \hline
 (\lambda x. e)v \rightarrow e\{v/x\} \\
 \text{[context]} \\
 \hline
 e_1 \rightarrow e_2 \\
 \hline
 \mathcal{E}[e_1] \rightarrow \mathcal{E}[e_2] \\
 \text{[flat]} \\
 \hline
 \text{mon}^{k,l}(\text{flat}(e), v) \rightarrow \text{if } ev \text{ then } v \text{ else error}^k \\
 \text{[func]} \\
 \hline
 \text{mon}^{k,l}(\kappa_1 \mapsto \kappa_2, v) \rightarrow \lambda x. \text{mon}^{k,l}(\kappa_2, v \text{ mon}^{l,k}(\kappa_1, x))
 \end{array}$$

$$\mathcal{E} ::= [] \mid \mathcal{E}e \mid v\mathcal{E} \mid \text{if } \mathcal{E} \text{ then } e_1 \text{ else } e_2 \mid \text{mon}^{l,l}(\kappa, \mathcal{E})$$

Programming Computable Functions (PCF) + Contracts

Example

```
ge =  $\lambda x. x \geq 0$   
le =  $\lambda x. x \leq 0$   
op =  $\lambda x. x * (-1)$   
 $\text{op}_{\text{mon}} = \text{mon}^{k,l}(\text{flat}(\text{ge}) \mapsto \text{flat}(\text{le}), \text{op})$   
 $\text{op}_{\text{mon}} \rightarrow \lambda x. \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{mon}^{l,k}(\text{flat}(\text{ge}), x))$ 
```

$\text{op}_{\text{mon}} 1$

```
 $\text{op}_{\text{mon}} 1 \rightarrow (\lambda x. \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{mon}^{l,k}(\text{flat}(\text{ge}), x))) 1$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{mon}^{l,k}(\text{flat}(\text{ge}), 1))$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{if } \text{ge } 1 \text{ then } 1 \text{ else error}^l)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{if } 1 \geq 0 \text{ then } 1 \text{ else error}^l)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{if true then } 1 \text{ else error}^l)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } 1)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), 1 * (-1))$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), (-1))$   
 $\rightarrow \text{if } \text{le } (-1) \text{ then } (-1) \text{ else error}^k$   
 $\rightarrow \text{if } (-1) \leq 0 \text{ then } (-1) \text{ else error}^k$   
 $\rightarrow \text{if true then } (-1) \text{ else error}^k$   
 $\rightarrow (-1)$ 
```

Programming Computable Functions (PCF) + Contracts

Example

```
ge =  $\lambda x. x \geq 0$   
le =  $\lambda x. x \leq 0$   
op =  $\lambda x. x * (-1)$   
opmon = monk,l(flat(ge)  $\mapsto$  flat(le), op)  
opmon  $\rightarrow \lambda x. \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op mon}^{l,k}(\text{flat}(\text{ge}), x))$ 
```

op_{mon}(-1)

```
opmon(-1)  $\rightarrow (\lambda x. \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op mon}^{l,k}(\text{flat}(\text{ge}), x))) (-1)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op mon}^{l,k}(\text{flat}(\text{ge}), (-1)))$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{if } \text{ge } (-1) \text{ then } (-1) \text{ else error}^l)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{if } (-1) \geq 0 \text{ then } 1 \text{ else error}^l)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{if false then } 1 \text{ else error}^l)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), \text{error}^l)$   
 $\rightarrow \text{error}^l$ 
```

The blame is assigned to the **client**

Programming Computable Functions (PCF) + Contracts

Example

```
ge =  $\lambda x. x \geq 0$   
le =  $\lambda x. x \leq 0$   
op =  $\lambda x. x$   
opmon = monk,l(flat(ge)  $\mapsto$  flat(le), op)  
opmon  $\rightarrow \lambda x. \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{mon}^{l,k}(\text{flat}(\text{ge}), x))$ 
```

op_{mon} 1

```
opmon 1  $\rightarrow (\lambda x. \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } \text{mon}^{l,k}(\text{flat}(\text{ge}), x))) 1$   
 $\rightarrow^* \text{mon}^{k,l}(\text{flat}(\text{le}), \text{op } 1)$   
 $\rightarrow \text{mon}^{k,l}(\text{flat}(\text{le}), 1)$   
 $\rightarrow \text{if } \text{le } 1 \text{ then } 1 \text{ else error}^k$   
 $\rightarrow \text{if } 1 \leq 0 \text{ then } 1 \text{ else error}^k$   
 $\rightarrow \text{if false then } 1 \text{ else error}^k$   
 $\rightarrow \text{error}^k$ 
```

The blame is assigned to the **provider**

Dependent contracts

$$\kappa := \dots \mid \kappa \stackrel{d}{\mapsto} (\lambda x. \kappa)$$

Example

```
succ = λx. x + 1  
κ = flat(λx. true)  $\stackrel{d}{\mapsto}$  (λx. flat(λy. y > x))  
succmon = monk,l(κ, succ)
```

Dependent contracts

Typing for contracts $\Gamma \vdash e : t$

$$\frac{\text{[t-contract]} \quad \Gamma \vdash \kappa_1 : \text{con}(t_1) \quad \Gamma \vdash \kappa_2 : t_1 \rightarrow \text{con}(t_2)}{\Gamma \vdash \kappa_1 \stackrel{d}{\mapsto} \kappa_2 : \text{con}(t_1 \rightarrow t_2)}$$

Semantics $e \rightarrow e$

$$\frac{\text{[d-func]}}{\text{mon}^{k,l}(\kappa_1 \stackrel{d}{\mapsto} (\lambda x. \kappa_2), v) \rightarrow \lambda x. \text{mon}^{k,l}(\kappa_2, v \text{ mon}^{l,k}(\kappa_1, x))}$$

Dependent Contract

Example

$$\begin{aligned}\text{succ} &= \lambda x. x + 1 \\ \kappa &= \text{flat}(\lambda x. \text{true}) \mapsto^d (\lambda x. \text{flat}(\lambda y. y > x)) \\ \text{succ}_{\text{mon}} &= \text{mon}^{k,l}(\kappa, \text{succ})\end{aligned}$$
$$\text{succ}_{\text{mon}} \rightarrow \lambda x. \text{mon}^{k,l}(\text{flat}(\lambda y. y > x), \text{succ mon}^{l,k}(\text{flat}(\lambda x. \text{true}), x))$$

$\text{succ}_{\text{mon}} \ 2$

$$\begin{aligned}\text{succ}_{\text{mon}} &\rightarrow (\lambda x. \text{mon}^{k,l}(\text{flat}(\lambda y. y > x), \text{succ mon}^{l,k}(\text{flat}(\lambda x. \text{true}), x))) \ 2 \\ &\rightarrow \text{mon}^{k,l}(\text{flat}(\lambda y. y > 2), \text{succ mon}^{l,k}(\text{flat}(\lambda x. \text{true}), 2)) \\ &\rightarrow^* \text{mon}^{k,l}(\text{flat}(\lambda y. y > 2), \text{succ } 2) \\ &\rightarrow^* \text{mon}^{k,l}(\text{flat}(\lambda y. y > 2), 3) \\ &\rightarrow^* 3\end{aligned}$$