

Semester Project - P2P insurance supported by
the blockchain

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Introduction

Insurance companies greatly suffer from fraud. It seems to be explained by the fact that they have conflicting interests with their customers. It's no rocket science that insurance companies need to be profitable and therefore have a natural tendency to try to reduce the bill when it comes to reimbursing a customer. On the other hand, customers might have the feeling that they already contribute enough through their regular insurance fees to be covered when they need to. Therefore, it appears that as they feel a bit cheated by the company and their natural reaction is to try to cheat the company as well.

In order to go against that problem, the principal intuition would be to align insurance's goals with users'. By creating a company held and governed by the users, such a compromise can be found.

Two problems remain:

- What kind of insurance is suitable for such a framework?
- How to create such a community with a fair repartition of trust and power?

First of all, we considered car deductibles to be the most suited value to insure. A deductible may be used to describe one of the several types of clauses that are used by insurance companies as a threshold for policy payments. In the case of car insurance, they are frequently used for a responsible crash in the case of an "all-risks" insured car. The driver always has to pay from his/her own pocket the deductible part: if an insurance policy has a deductible of \$100 then all crashes requiring repairs costing less than \$100 will not benefit from any insurance help while a \$400 repair cost will receive a \$300 help from the insurance. This was considered as a great framework since it allows to ensure that the value insured per user remains bounded and relatively low. Also, it would allow having a consistent value to insure among users: most car insurances have the same value magnitude when it comes to deductibles.

Then, in order to create such community we need to have a common fund managed by all users. This is quite complicated to implement: how to coordinate multiple users without the help of a central referee? This justifies the use of the blockchain. As it will be explained in later discussions, the blockchain technology provides a useful framework to create such a community.

Using such system, users could be insured by the community. All of them would contribute to a common fund and would vote whenever a member needs a reimbursement. Every user is then implicitly encouraged to be careful on how

he evaluates the legitimacy of each claim, including its own. This is due to the fact that once the common pot goes dry no user is insured anymore. Therefore, it is in their own interest to make the pot last as long as possible. Also, the statistics of the users may be used to show how often do they approve claims from other users so that when they claim a crash, voters can decide whether or not they play by the rule of the community, how generous they are with their votes and how often do they happen to ask for a reimbursement.

We will first explain the model that was iteratively created for this system. Then different technology alternatives to implement the system will be described along with the reasons why one was chosen over the other. In a third time, some implementation details and difficulties will be exposed to raise awareness about some limitations and possible attacks. Finally, we will present the improvements that we have thought about should the project be continued.

Why the blockchain

Chapter 1

The System Model

In this section we will discuss the model of the system . That is, the theoretical design of the community and the maths supporting it. It will be as decoupled as possible from the underlying implementation.

1.1 Claims

The project is about insuring members of the community. In order for a user to pretend to a reimbursement from the community, he/she needs to submit a **claim**. Each claim only concerns members of the community at the time it is posted, i.e., a member votes and pays only for claims published at a time they belonged to the community. At the creation of the community we will choose the **Debating period**, an amount of time voters have to decide to approve or reject a claim. Each claim is submitted along with:

- **Amount of the claim:** the amount of money requested by the claimer.
- **Description:** a short explanation about the claim.
- **Documents information** (*not yet implemented*): URLs and hashes of official documents used to support the claim. The need for such information will be made clear later on.

Since each user is insured for only one car, they can only make one claim at a time.

1.2 Funding

This paragraph tries to explain how the system is funded. The basic idea is to have each user deposit at the launch of the community a fixed amount of money which will be used to refund claims until the community cannot support claims anymore (this condition will be further described in the following paragraph). The money funded by each user is kept in his/her virtual **balance**.

Once the community cannot support a new claim anymore, a refunding is initiated. Users have the choice to either leave or stay in the community. If

they decide to stay, using the statistics from the end of the last funding to the current date, called the **inter-funding period**, an estimated amount of claim per user in a year¹ is computed. Using the latter and the average price of a claim a new funding amount per user is computed. Mathematically it expresses as follows:

A **funding** is a period during which users of the community must contribute to common funds used to reimburse potential claims. This period has a given duration `FUNDING_DURATION` (denoted d_f in math equations). A user is insured only once he has contributed to the current funding. The funding will last enough time to ensure that users can fund the community.

The funding k happens for $t \in [t_k; t_k + d_f]$. We denote by T_k (**the top-off value**) the amount that will be in every member's balance at the end of the funding², that is, at $t = t_k + d_f$.

Let $x_{i,t}$ represent the balance for user i for $i \in \{1, \dots, n_t\}$ at time t , where n_t represents the number of users in the community at time t

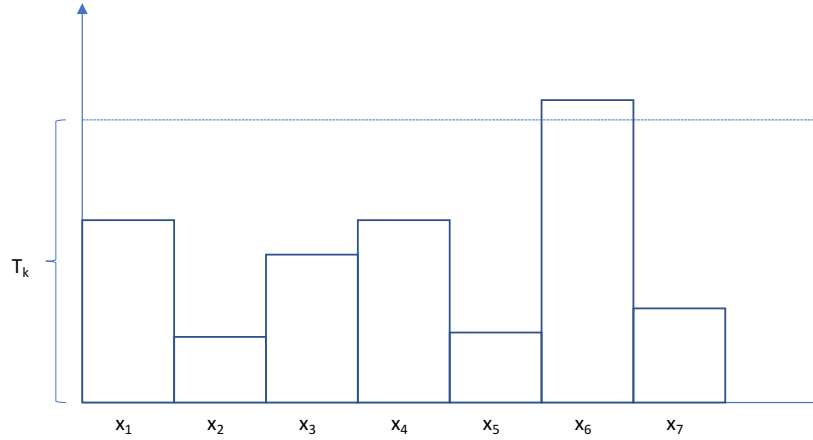


Figure 1.1: Balances at time t_k

In Figures 1.1, 1.2 and 1.3, we characterise what is T_k . Note that the time at which the balances are considered is made clear in the caption so that we do not overload the graphic with the extra subscript. Fig. 1.1 shows the situation at the time where the funding is required. While Fig. 1.2 explains how each user top-offs its balance in order to stay in the community in the case where no user arrives between t_k and $t_k + d_f$ (which is explained in Fig. 1.3). An extra rule that can be observed is that user 6 already has a balance over T_k , therefore he/she does not need to top off.

¹The period for which the estimate is computed can be tuned in order to be realistic and depending on further implementation choices.

²The scenario where a user did not fund by the end of the period is explained in 1.2.5.

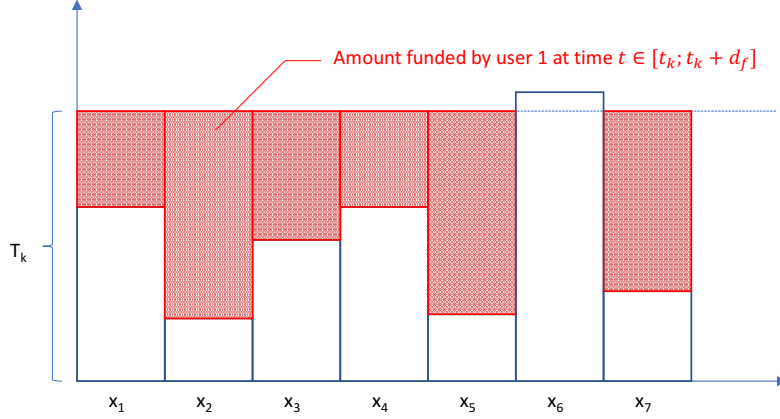


Figure 1.2: Balances at time $t_k + d_f$ when no user has joined during funding period

1.2.1 Initial Balance Value : $x_{i,t}$

- Genesis of the system: let P_{hist} be the average price of a claim and C_{hist} be the average number of claim per user in a year³ based on historical data. Then :

$$\forall i \in \{1, \dots, n_0\} \quad x_{i,0} = C_{hist} \times P_{hist} = T_0 \quad (1.1)$$

- Upon arrival of a new user: Suppose a new participant arrives at time t_a . Then he will pay the same amount than the top-off value that had to be reached by other users upon last funding. To avoid mathematical difficulties denote by k the index of the funding that was initiated at t_k and suppose that there was no other funding initiated between t_k and t_a . Then if we denote by j the index of the new user:

$$x_{j,t_a} = T_k \quad (1.2)$$

1.2.2 Condition Upon Which a New Funding is Required

While we first did not consider that having a user with a negative balance would be a problem, it turns out that this makes it difficult to handle what to do when such user decides to leave the community. It seems clear that we cannot reach a point at which one user's balance would become negative after reimbursing a claim.

Suppose t_{new} is the current time and corresponds to a new claim being added. We need to ensure that at this time the balance of every user can reimburse all

³This number will have to be a bit exaggerated in order to cope with the possible differences between historical rate and observed rate.

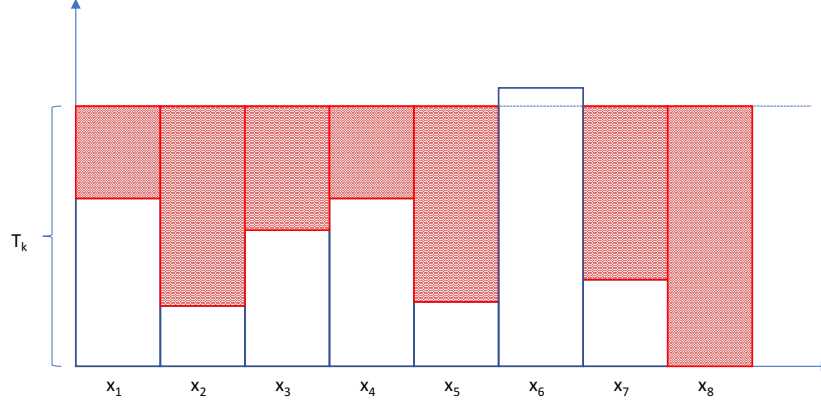


Figure 1.3: Balances at time $t_k + d_f$: user 8 has joined during the funding period

claims that are pending as well as this new claim that is submitted. In Fig.1.4, one can observe that the amount that has to be paid per user depends on the number of user at the time of the claim, and on the price of the claim. In the simple example offered by Fig. 1.4, the condition that is checked at time t_{new} is :

$$\forall i \in \{1, \dots, n_{t_{\text{new}}}\} \quad x_{i,t_{\text{new}}} - \frac{p_1}{n_{t_1}} - \frac{p_2}{n_{t_2}} > \frac{p_{\text{new}}}{n_{t_{\text{new}}}} \quad (1.3)$$

where p_i denotes the price of the i^{th} pending claim and t_i the time at which it was submitted.

In this example, we see that we need to check that once each user has potentially reimbursed his/her share of the first two claims he/she will still be able to reimburse his/her share of the last claim.

It's important to note that by using the previous condition we are actually checking something stronger than we actually need: e.g. a user that arrives after t_1 is not involved in the reimbursement of the first claim but we still check that he/she has enough to reimburse it on top of other claims. But if all balances of users that are involved in claim 1 pass the condition then this latter user will also verify it. This is due to the fact that his/her balance is greater or equal to the balance of one of the member with the least amount of ether in his/her balance (due to the computation of the top-off value). The reason we do not only check for users concerned by claims is to have a more systematic check that will turn out to be less computationally expensive.

If the previous condition check fails, then a new funding will be launched should the condition that is later discussed in 1.2.6 also be verified.

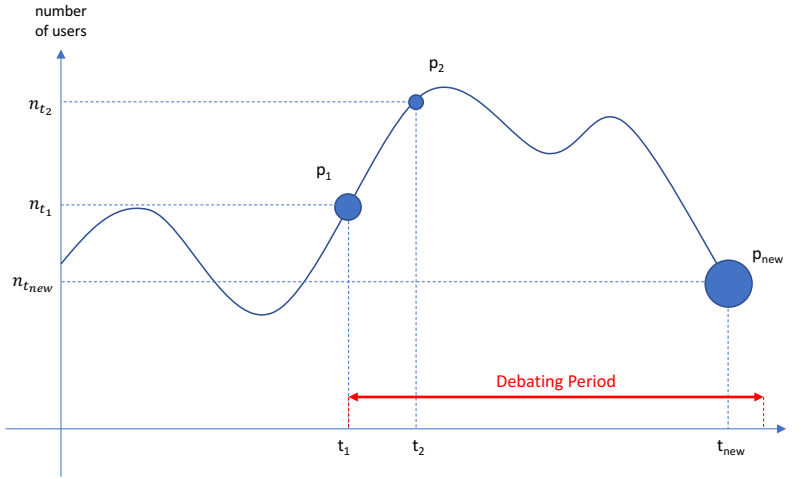


Figure 1.4: Illustration of the funding condition

1.2.3 System Behavior During a Funding Period

There are multiple ways to treat the claims which triggered the funding:

- The claim is still accepted and its deadline is extended by the funding duration. This is the best solution for the claimer's point of view. But, we would have to pause any action related to this claim until the end of the funding because we want to restrict voting to people that have funded the community. Moreover, this would imply that if users choose to not fund the community, the amount needed for the claim might not be reached, whereas the claim would be active, which can lead the community in an inconsistent state.
- The claim is buffered until the end of the funding period. This solves the previous point since the claim is only instantiated when funding is finished. However, we cannot provide the claimer with any information about the creation date of its claim. Indeed, even if the funding period has a defined deadline, the action of finishing the funding will not be taken until users show some activity on the community after this deadline (c.f. 3.2 and 4.3.4). Then the creation date of the claim is unknown to the claimer and can lead to confusion.
- The best alternative we thought of is the simplest: reject the claim. The claimer would be informed that the community is currently unable to support his/her claim and that he/she should try again after the funding period.

Naturally, it should not be possible for users to deposit a claim during a funding period, since the size and funds of the community are in a transient state.

However, we decided that it should still be possible to vote and execute pending claims, which had been instantiated before the current funding period. Indeed, these claims can be supported by the community, and we are guaranteed that users have the necessary amount in their balance. Therefore we only pause submission of new claims.

1.2.4 Computation of Top-off Value at Each Funding: T_k

One must keep in mind that the system must adapt to the long term and short term community. To do so, we will keep track of a **virtual user**. This user will save the amount paid by a user during each inter-funding period. Therefore we will have three state variables:

1. **PaidSinceLastFunding** (denoted **PSLF** in equations) which keeps track of what is paid by the virtual user since previous funding.
2. **PaidYearlyAcc** which accumulates the sum of all yearly payments computed from each inter-funding period.
3. **NumberFundings** which keeps track of the number of finished fundings. (Initialised to one at the very beginning of the community as all members will have funded the first T_0)

As well as one variable that is computed whenever needed :

1. **PaidYearly** which keeps track of what is paid by the virtual user between day 0 and current time on a yearly basis.

The update rule of those three variables is quite intuitive. Every time the community approves a claim and it gets reimbursed, the amount paid by a user is added to **PaidSinceLastFunding**. This variable is reinitialized at the beginning of each inter-funding period. Once a new funding k is initiated:

$$\text{PaidYearlyAcc} += 365 \times \frac{\text{PSLF}}{\text{days}(t_k - t_{k-1})}$$

Then we can obtain the third one simply by :

$$\text{PaidYearly} = \frac{\text{PaidYearlyAcc}}{\text{NumberFundings}}$$

This approach allows for **PaidYearly** to reflect what a user pays on a yearly basis depending on the historical community as this will average over each inter-funding period. Also, it entirely isolates the variation of the number of users during inter-funding periods since the amount of the claim is divided among the number of members at the time the claim is published.

We compute the top-off value per user:

$$T_k = (\alpha \times \text{PaidYearly} + (1 - \alpha) \times \text{PSLF}_{k-1}) \quad (1.4)$$

where $PSLF_{k-1}$ is the amount paid by the virtual user during the preceding inter-funding period. Such that $PSLF_{-1} = \text{PaidYearly} = C_{Hist} \times P_{hist}$

Since T_k is the amount that a user must reach once they have topped off, users' funding amount is computed using the **Water-filling** solution as explained in Fig. 1.2 and 1.3 s.t.

$$\forall i, j \quad x_{i, t_k + d_f} = x_{j, t_k + d_f} = T_k \quad (1.5)$$

The reason for the weighted average in Equation 1.4 is due to the need for the system to dynamically adjust to the historical behavior since the beginning of the community as well as the possible recent changes in the community composition.

1.2.5 Incentive to Fund

Given the fact that the funding period will be made quite long we decided to exclude all users that have not contributed to the common fund by the end of the period. This will cause the rest of their balance to be kept by the community.

1.2.6 Launching a New Funding

In order to avoid the attack described in Section 3.4, we decided to never launch a new funding if the users all have enough money in their balance. That is if the new top off value is already reached by all users. One can also note that this approach is intuitive for the model, why should the system launch a new funding if the money is already here. The claim that caused the funding to be launched will, therefore, be refused. We refuse it because it either means that we currently have too many pending claims (and we want to artificially limit this number) or that the claimer has posted a claim which amount cannot be supported.

1.3 Voting

1.3.1 Fundamental Behavior

In order to determine whether a claim should be funded by the community or not, a vote is organized. It is not clear at first how to avoid having the user vote for every single claim but this behavior is required in order to be able to scale to a large community. The most appropriate solution resides in **random sampling**. On the same principle than jury duty in the United States, each claim will be voted by a small randomly selected sample of the users. The number of such users has to be defined. Options that are available:

1. Relative: always consider that the jury to be representative of the community should be a given fraction of its members. But this is wrong for a big enough community as only a sample of a given size is necessary in order to achieve a given error margin (see the following paragraph).

2. Absolute: Simply consider that the critical mass (see further explanation of the critical mass) is enough to decide and that the number of voters is fixed for any community size. This turns out to be a good idea. We will require a critical mass that is large enough. This solution was kept anyway because the more users the more the idiosyncratic risk of each member gets diluted over the community. Therefore to have a low community risk we need to have a large enough number of user.

1.3.2 Incentive to Vote

It is important to note that we have not yet defined the incentive for users to vote but this is a very important notion. The whole community relies on voters:

- At first we considered that if a user selected for a given vote does not vote before the end of the debating period then he/she would be excluded from the community. But this seemed as a very unfriendly behavior for users.
- Finally it was decided to have a system of points. A given number of points are issued to each user⁴. Then whenever a voter fails to vote before the deadline, a point is taken away from him/her. Once a user reaches zero points he/she is excluded. Those points will reset after a given number of successful votes⁵. In order to implement such strategy, we introduce the notion of **Minimum Quorum**, which denotes how many voters from the randomly sampled users must vote in order for the voting result to be considered valid.

Once a user is excluded from the community he/she cannot vote nor submit any claim and he/she would have lost all the abilities that were provided to him/her based on his/her fundings.

1.3.3 Error Yielded by Random Sampling of Voters

In the following, we will follow an article by Terence Tao [6]. We will also assume ideal conditions of sampling.

Assumptions: While the article needs to assume a lot of different perfect behaviour, this is not necessary here. In fact, we will explain why the only assumption we need to make is Simple random sampling. Here are the assumptions that were made by the article along with the justification why the assumption is verified in our case.

- **Simple question:** voters are offered only two possible answers (accept or reject claim)
- **Perfect Response Rate:** a vote is considered as valid only if the Minimum Quorum therefore we are ensured that all people we considered to

⁴The number of points is considered as an implementation decision.

⁵Again this number does not really affect the theory.

be our sample will have responded since the sample has size Minimum Quorum. This will introduce a bias since we will

- **Honest Responses:** we are not doing a poll but real vote, therefore, it is safe to assume that voters will vote following their real voting intentions.
- **Fixed Poll Size:** before doing the vote we will always use the same minimum quorum.
- **Honest Reporting:** From the source code of the system one can see that the result of the vote are always reported and used as they are.

Now the only remaining assumption is **Simple Random Sampling without replacement**. This means that each of the n sampled voters has been selected uniformly at random from the entire population independently of others except the fact that we do not allow replacement. That is once a voter has been selected it cannot be selected a second time ⁶.

Let X denote the set of the total population. Let A be the subset of the population that would accept the claim. We wish to compute the margin of error [10] (at the confidence interval 95% [8]). Let p be the proportion of users that accept the claim:

$$p = \frac{|A|}{|X|} \quad (1.6)$$

Now suppose that we sample n users of the community to be representative of the entire community (under the assumptions described above). Then we will have, \bar{p} , the proportion of sampled voters that vote to approve the claim:

$$\bar{p} = \frac{|1 \leq i \leq n : x_i \in A|}{n} \quad (1.7)$$

Finally using Markov's inequality,

$$\forall r > 0 \quad \Pr(|\bar{p} - p| \leq r) \geq 1 - \frac{1}{4nr^2} \quad (1.8)$$

Therefore if we compute a confidence interval of 95% we want :

$$\Pr(|\bar{p} - p| \leq r) \geq 0.95 \quad (1.9)$$

It is sufficient to show :

$$\begin{aligned} 1 - \frac{1}{4nr^2} &\geq 0.95 \\ \Rightarrow r &= \frac{1}{\sqrt{4n(1 - 0.95)}} \\ \Rightarrow \Pr(|\bar{p} - p| \leq r) &\geq 0.95 \end{aligned} \quad (1.10)$$

hence we compute the margin of error r depending on different values of n (the minimum quorum).

⁶It is important to note that by allowing replacement one can obtain joint independence and use Chernoff inequality to further reduce the margin of error.

Minimum Quorum (n)	Margin of error (r)
200	15.811%
500	10.000%
1000	7.071%
5000	3.162%
10'000	2.236%

Table 1.1: Margin of error for different Minimum Quora

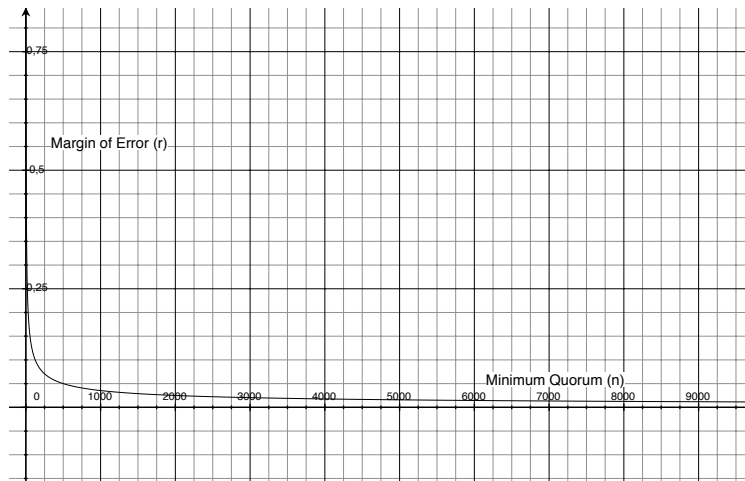


Figure 1.5: Tradeoff between the margin of error and minimum quorum

Choice of Minimum Quorum: it can be observed from Fig. 1.5 that we have a clear tradeoff between how well can we represent the community and how many people do we need to sample. We considered that choosing $n = 1000$ yielded a small enough margin of error.

Sampled size We have seen in 1.3.2 that we need more people than Minimum Quorum in our sample of users to vote.

1.3.4 Critical Mass

Using the previous results on the size of the minimum quorum, we can determine what is the critical mass we wish to have. Since users are allowed to not vote some given number of times, we need to make sure that we are quite confident that among the sampled users, we are quite confident that we will reach the

Minimum Quorum at the issue of the vote. It is quite intuitive using the expectation of a binomial distribution⁷, that if each user does not vote approximately half of the time then the expecting number of selected users that will vote is close to half of them. Then we decided that choosing a Critical Mass of 2000 users would be significant to reach the minimum Quorum with high probability.

1.4 Leaving The Community: Handling Left-over Funds

When members leave the community willingly or not, it is possible that some amount of money remains in their balance. We need to define a policy about how these left-over funds are handled. First of all, they should not be directly considered as *free* funds because a user remains liable for all claims that have been submitted during his/her membership. Therefore we need to keep track of the money that is currently not usable because it will eventually be used to reimburse a claim and the money that is currently usable by the community to reduce the amount paid by each user to reimburse a claim.

We therefore introduced :

- **jackpot** a global variable that will count the amount of usable money. This money will be used to decrease the amount paid by users upon reimbursing a claim. If the **jackpot** is nonzero when a claim must be reimbursed, it is entirely used to subtract from the claim amount before computing what the users must pay from their own balance.
- **leftOvers** a variable stored for each claim. Whenever a user leaves, his/her balance will be split. For each pending claim he/she was supposed to pay for, the amount he/she was supposed to pay will be taken from his/her balance to the claim **leftOvers**. Everything that remains after that will be added to **jackpot** Either the claim gets approved, in which case **leftOvers** are forgotten, or it turns out the claim does not get approved and **leftOvers** goes to the **jackpot**.

This money is only a virtual counter, it does not reveal the real amount of money that is held by the contract. In fact, rounding⁸ will often leave a very small amount of money which is not accounted by the balances, but this amount will be only a very small fraction and is considered to be non-relevant (at least until the possible end of the community as it will be seen later on.). The two counters are used solely for fund tracking purposes (this explains why we simply forget about **leftOvers** once the claim is reimbursed, we do not need to keep track of this amount anymore).

⁷This supposes that the simple random sampling is done without replacement. Even though it is not the case, it will not be too far from the reality given the large community size.

⁸The reason for rounding will be further explained in 3.3

1.5 Anonymity and Verification of Claims' Documents

1.5.1 Anonymity

The very first issue that came to our mind was **anonymity**. The blockchain technology relies on a public ledger, which means that any claim would be visible by anyone even-though they are not members of the community. Therefore, in our use (that is: car deductible), it might be desirable to have some sort of anonymity. But here are the reasons why we rejected the idea of having anonymous users:

- We need to be able to know what car is insured to avoid having a user paying only one registration and insuring multiple vehicles. To identify the vehicle we need a license plate and therefore will void any user anonymity.
- A central part of the vote will be the user profile, to keep statistics about the users (number of claims, age, the percentage of positive votes...), therefore if we do not identify the users, then those statistics can be reset as many time as the user wants.
- End users need to be able to verify that documents linked to the claim are legit. In the standard insurance, it is usually required to have a police report of the crash and/or some witnesses. Those documents are heavily tied with the victim's identity. It would be hard to certify the documents without linking them to a person.

Therefore, judging by the risk at stake we thought that the fact that the system does not ensure anonymity is not such a problem. We could not see many use cases where someone could wish to hide from the public an accident but not from its insurance company. Moreover, where regular insurance companies can decide to have the car inspected for damages in the event of a crash, the community does not have such "experts". Therefore it heavily relies on the documents that prove the crash existence and the profile of the claimer.

1.5.2 Document Integrity Verification

Voters are supposed to base their decision for a claim on the details that are provided by the claimer. The most important are the claim documents (*e.g. police statement, witnesses letters, pictures of the damages,...*). We need to ensure:

- Documents are not changed by the claimer once the claim has been broadcasted to voters.
- Documents from the previous claims are still available in the future (in order to allow the voters to check that the new claim is valid: it does not concern another car, has not been reimbursed yet, ...)

Storing documents on the blockchain is very inefficient (as it will be explained in 3.1.1). Therefore we decided to verify the integrity of the document using the hash of the archive to de-correlate the document sharing policy with the blockchain.

With each claim will be stored a `url` where an archive⁹ of the documents can be downloaded. The voters will be able to check that the archive of documents they obtain is the same than every other voter since its hash can be recomputed and compared to the value stored in the claim.

1.6 Community Suicide

We have seen so far that we need to have a critical mass for the system to be able to work. But then we also always need to check that we will not go below this lower limit once the system is online. Moreover, what should be the policy once we go below such limit? We decided to **suicide the actual community**. In such scenario we would:

1. Take all remaining users and subscribe them to preregistration again (*not implemented yet: so far we simply kill the community forever*).
2. Reimburse the current amount of money contained in each user's virtual balance.
3. As we previously mentioned those balances do not represent the real amount of money held by the system. Therefore a user will be randomly selected¹⁰ to receive all the eventual remaining funds of the system.
4. Delete all the current community to start from scratch if critical mass of preregistration is reached again in the future.

The process by which the user is randomly selected will be further described in Section 2

⁹A compressed folder.

¹⁰To avoid targeted attacks.

Chapter 2

Technical Alternatives Considered

Since many alternatives were considered when designing the system, it was decided to present the "trial and error" protocol that was observed. This will hopefully explain decisions that were undertaken and their deep correlation with our line of thoughts. That is, each topic of the system will be presented depending on when the question showed up during the project development.

2.1 Using Bitcoin with Distributed Wallets

Given the financial aspect of the project, the first technology that presented itself as an evidence was to use Bitcoin.

2.1.1 Principle of Bitcoin

This paragraph presents a very simplified and not comprehensive explanation of the Bitcoin system. Bitcoin is a cryptocurrency where transactions take place between users without the need of a trusted third party. The blockchain represents a public ledger where transactions are recorded after they have been verified by nodes of the network. Transactions are grouped into blocks, forming the well-known Blockchain. This activity of verifying the transactions and adding them to blocks is called **mining**. Bitcoins are created as a reward for a competition into which miners try to constitute blocks with new transactions, and add them to the Blockchain. In order to be the winner and publish a block, a miner must perform a **Proof of Work**. This is what makes mining a hard task. It consists in incrementing a number until the hash of the block verifies some predefined criteria. In order to cheat the blockchain, since all blocks are linked to each other using hashes, one needs to modify all subsequent blocks and recompute all proofs of work. Therefore, as the number of blocks increases, it

becomes harder to modify a past block. This is how transactions do not need to be verified by an intermediary. The network always consider the longest chain to be the valid one [7].

2.1.2 Distributed Wallets

The collaborative funding aspect of the project meant that a common fund **managed by the community** needed to be created. Therefore our reflexion was oriented towards **distributed wallets**. Those wallets, to be opposed to regular Bitcoin wallets, use a multi-signature scheme. This enables to have N-out-of-M participants controlling the wallet. Hence, to be valid, a transaction needs to be signed by at least N out of the M-wallet cosigners. It is important to note that current multi-signature schemes are limited to $M = 15$ [1, p. 127]. These distributed wallets allow having each user's deposit protected by the community (or at least a portion of it). The cosigners would be randomly chosen to protect a deposit. Therefore no deposit can be withdrawn from the community without a consensus among at least N of the cosigners.

2.1.3 Problems With This Alternative

Many problems were discovered about the solution using distributed wallets.

- **Collusion:** if N users out the M cosigners decide to steal the deposit: nothing protects the community from doing so. The assumption that they will not is very weak as the maximum amount of cosigners is 15.
- **Excluding users:** given the fact that the incentive to vote is to avoid exclusion from the community we need to ensure that when excluding someone from the community our protocol is well defined. But if more than $M - N$ cosigners get excluded from the community then access to the wallet is lost and the community suffers from this loss.
- **Need actions from the users to unlock the money:** upon approval of a claim we need to unlock the money from each distributed wallet to reimburse the claimer. But suppose most cosigners on a wallet disapproved the claim. Then, they could decide not to unlock the wallet even though the community approved.
- **The increased price of a claim reimbursement:** By definition of the blockchain, each transaction has to be mined and therefore each transaction has some extra fees to pay the miners. With one distributed wallet per user, that means that each reimbursement involves a transaction from each distributed wallet to the claimer. That means a lot of extra fees (that might even go beyond the reimbursement in itself making the system useless.)

2.1.4 Conclusion

At the sight of the previous problems encountered, it was decided to let go of the idea of distributed wallet. Nevertheless, much of the theoretical approach to the problem is kept and transposed to the next technical alternative.

2.2 Using Ethereum' Smart Contracts to Handle the Common Funds

The previous alternative demonstrated the difficulty of setting up a community fund using Bitcoin. This is where Ethereum came into play.

2.2.1 Principle

In Bitcoin, spending a UTXO requires to sign it with one's private key, to use the multi-signature scheme or finally to write small locking scripts that can only be unlocked by the corresponding unlocking scripts. But the simple stack based Bitcoin scripting language is not Turing complete. Hence it is not possible to write a complex piece of code that executes whatever function is required for a specific use case.

Ethereum would theoretically allow writing complex scripts for our project. The idea is to create, using smart contracts, a Decentralized Autonomous Organization.

Ethereum is a blockchain-based distributed computing platform. It provides a virtual machine (EVM). This virtual machine can execute scripts using an international network of public nodes. Ethereum also provides a value token called "ether", that can be thought of as a bitcoin. Then in order to pay for computational power, the notion of "gas" was introduced. This internal transaction pricing mechanism is used to prevent spam on the network and allocate resources proportionally to the incentive offered by the request. [9]

2.2.2 Ethereum Smart Contracts

Ethereum is composed of two kinds of nodes:

- Smart contract: the guardian of the fund. It will represent the community by gathering the votes, creating the transactions when necessary to reimburse a claimer etc.
- EOA: externally owned accounts. Those are the end users. They will invest in the DAO's wallet, vote whenever they have to, and post claims.

Using this duality we can see that creating a community is simply a matter of creating the correct behaviour for the Smart contract, make an access control policy for interactions between the smart contract and EOA that are part of the community. Once the source code of the contract has been written it can be

coupled with a front-end that will make the whole system transparent for the user.

2.2.3 Conclusion

Therefore Ethereum seemed to be much easier to coordinate users of the community since, as their name suggest, smart contract are meant to be shaped depending on system requirements.

It is easy to see that the Ethereum alternative will not suffer from any of the problems discussed in 2.1.3.

Chapter 3

Implementation

This part will present the implementation details. That is, the different choices that were taken to construct the system.

3.1 Development Set-Up

Solidity was first proposed in 2014 and Ethereum was first released in 2015 [9]. This means that documentation is still quite sparse and that the development tools are not yet very established.

The main problem with Ethereum development is that testing on the live network is quite discouraged by the inherent costs. Both in term of time (one need to wait for miners to execute transactions) and in term of gas (one need to pay the miners for such computing power). Therefore we used widely available tools:

- **testrpc** : a *Node.js* based Ethereum client for testing and development. It uses *ethereumjs* to simulate full client behavior and make developing Ethereum applications much faster. It also includes all popular RPC ¹ functions and features, like events, and can be run deterministically. It can be thought of as a "local blockchain".
- **truffle**: a development environment, testing framework and asset pipeline for Ethereum, aiming to make life as an Ethereum developer easier. In particular, it allows to compile smart contracts, but also to test them using the *Mocha* and *Chai* testing frameworks. It also helped us get started with Solidity as it provides basic contracts along with their migration script², and their testing files.

Then we again quickly encountered some implementation issues.

¹RPC: Remote Procedure Call.

²Code specifying how the contract is posted on the blockchain.

3.1.1 Storing Documents

We need to store documents related to each claim and contract, such as pictures of the car, police crash declaration, and any other documents that can help the community decide whether or not to reimburse the claim. Three alternatives were considered:

- **Storing the documents in the contract's storage:** this turned out to be a very bad idea. To make it simple in February 2016 each GigaByte of data cost 76'000\$ [2]. The only advantage of this would be that each claim document cannot be modified after the claim and would be available in the event of a new claim by the user to check multiple characteristics, such as checking if this is the same car or accident (which can also be achieved using an integrity verification see 1.5.2).
- **Store the documents on a community paid server:** this solution was the simplest for the end user because it would allow offering in the application a "drag and drop" platform to store the documents. But this seemed a bit complex to set up and was not in the scope of our project. (Moreover it might really go against our disintermediation goal)
- **User Managed Storage:** finally, the option that remained was to have each user use its favorite online data storage platform. On the contract, the system would only store a link to the archive containing the document and a hash of the archive (c.f. 1.5.2).

The third solution appeared to be much more scalable to a large community given that each user handles itself this aspect of the system. One of the drawbacks is that not all users will be familiar with any services of this type. This could be documented in the final system. Moreover, given the "community" aspect of the system, it could have a community forum where non-expert users could ask for help.

3.2 Scheduled Calls

Some action have a time limit (e.g. voting has a deadline, funding as well). Once a time limit is reached, we need to execute some code. The problem is that we cannot really call code at a given point in time directly from the contract (*e.g. when the deadline is past*). Therefore we considered multiple techniques:

- **ethereum-alarm-clock** : an externally developed smart contract that allows scheduled contract function calls. This seemed at first like a good idea but some problems remained. It allows to schedule code at a given block number but not at an exact date and time. This could be overcome since blocks are mined at a quite regular interval. But then still, development using this tool would be very complicated given that the contract can only be accessed on the live blockchain.

- Rely entirely on the user: after all, the claimer wants the money, therefore, it's not too much of an assumption to say that he/she can take care of asking for the system to rule the claim once the deadline is past.
- Use the client-side application: we can also consider the option where the client side application (when launched) checks the current pending claim of the user and their deadline and ask the contract to execute the ones that are meant to be finished.

These two last option were considered. Since they do not make any difference in the source code of the contract but only in the UI we have not yet decided which one would result in a more efficient technique.

3.3 Lack of Float Representation in Solidity

Solidity does not yet support floating point representation or operations. Therefore, all the division are rounded integer divisions. This why we avoid as much as possible to have multiple division in a row so that the relative rounding does not propagate. So far, Ethereum uses different unit magnitude to ease development (e.g. ether and wei).

3.4 Attack on statistics

3.4.1 Idea of the attack

While implementing the system we realized we might have a problem. Suppose an attacker wants to affect the value of `PaidYearly` by engaging a new funding before any claim has been executed (reimbursed) for the current inter-funding period. Then we see in equation 1.4 that $PSLF_k$ will be zero. Moreover, when a new funding is launched we update the values of `PaidYearlyAcc` and `PaidYearly`. Here `PaidYearlyAcc` will not be changed and `PaidYearly` will decrease as the number of finished inter-funding periods will increase.

3.4.2 Prerequisites

In order for this attack to take place, we need the following conditions:

- No money was spent so far (that is no claim has been executed yet) in this inter-funding period
- The attacker posts one or more claim such that the system cannot support it/them³.

Since no claim has been executed yet, if we suppose that last funding was the k^{th} one, then each user has T_k in its balance.

³he/she would need to use fake accounts as user are limited to one claim per account.

3.4.3 Avoiding Such Attacks - Effectiveness

In order to avoid the attack, we previously described the fact that no funding is launched if the users already have enough money in their balance. We will try to show how this avoids the mentioned attack. We want to show that in such situation $T_{k+1} \leq T_k$. This will ensure that no funding is launched (according to 1.2.6) and therefore will prevent **PaidYearly** to be updated.

Since $\text{PSLF}_k = 0$:

$$\begin{aligned} T_{k+1} &= [\alpha \times \text{PaidYearly} + (1 - \alpha) \times \text{PSLF}_k] \\ &= \alpha \times \text{PaidYearly} \end{aligned} \quad (3.1)$$

Moreover, suppose that the attack is being performed for the first time. Then $\text{PSLF}_{k-1} \geq 0$

$$\begin{aligned} T_k &= [\alpha \times \text{PaidYearly} + (1 - \alpha) \times \text{PSLF}_{k-1}] \\ &\geq \alpha \times \text{PaidYearly} = T_{k+1} \end{aligned} \quad (3.2)$$

Now we need to show that if the attack happens at the very beginning of the community then the argument holds. At the initialisation of the community, $\text{PSLF}_{-1} = \text{PaidYearly}$ (we do not have any information about the composition of the community and therefore we can only use a "historical estimate" of the yearly price). Then the initial funding top-off value would be:

$$\begin{aligned} T_0 &= [\alpha \times \text{PaidYearly} + (1 - \alpha) \times \text{PSLF}_{-1}] \\ &= [\alpha \times \text{PaidYearly} + (1 - \alpha) \times \text{PaidYearly}] \\ &= \text{PaidYearly} \end{aligned} \quad (3.3)$$

and :

$$\begin{aligned} T_1 &= \alpha \times \text{PaidYearly} \\ &\leq \text{PaidYearly} \end{aligned} \quad (3.4)$$

We have proven that for any $k \geq 0$ denoting the funding before the attack, the condition $T_k \geq T_{k+1}$ holds and therefore no funding is launched. This ensures that **fundingNumber** is not updated and therefore the statistics are not affected by the attack.

3.5 Denial of Service Attack

We also noticed that a potential attacker can make the system unusable by creating a big claim or by creating fake users and posting claims using each account such that the accumulative amount launches a new funding⁴. Therefore we thought of introducing a limit on the amount of a claim.

⁴Recall that a user can only post one claim at a time

3.5.1 Claim Amount Upper Bound

In order to choose this upper bound, we observed that we wanted to avoid the very un-probable case where an attacker has many fake accounts and all voters randomly selected for a claim he/she posted are fake accounts he/she holds. In such case, he/she would be able to decide to get reimbursed for his/her own claim.

Suppose last funding was the k^{th} one. To avoid that situation a simple counter measure is to fix the maximum amount of to be equal to $T_k \times \text{Minimum Quorum}$. This would mean that the attacker cannot be reimbursed more than what he/she paid for in order to create his/her fake accounts and that hopefully protects the community.

3.5.2 Effectiveness

The previous upper bound allows to ensure that no user can post a big claim to launch a funding. Also, since the number of pending claim is auto-regulated (c.f. 1.2.6), then even with a great amount of fake accounts, the attacker cannot either use multiple accounts to launch a new funding. This upper bound will also serve as a good protection against the poor randomness offered by our system (see 3.6.2).

3.6 Random Sampling

A challenge in this application was also the fact that randomness is very hard to obtain in Solidity[4].

3.6.1 Randomness in Ethereum

Nowadays random number generation for Ethereum is still being researched by Solidity enthusiasts. The only way we found to do this properly was to have each user generating a random number and to use a commitment scheme to submit it to the contract. When the number are revealed they are all XORed together to obtain the random number.

The commitment scheme is used because everything that the contract sees an attacker can potentially see. Therefore if the number were sent in clear, a potential attacker could choose his/her number in order to get the number computed by the contract to be any arbitrary value.

That would be the "clean way" of doing things. The problem is that it goes against some principles of our model:

- We need each and every user to submit a random number whenever we do a sampling. But the idea of the sampling was to avoid having every user to vote for every claim.
- Each interaction with the contract cost gas, therefore we want to avoid all those interactions that would cost a lot of money.

Therefore we decided to use a very poor source of randomness and to protect against the possible flaws of an attacker using this weakness.

3.6.2 Using Block Hashes as a Source of Randomness

Before explaining how we use the block hash to generate a pseudo-random number, we want to emphasize the fact that this technique could certainly be greatly improved. This was not the scope of our project and could be the subject of a whole semester project.

Block hashes are unpredictable and contained in the blockchain. This makes them easy to access. However, this is not entirely safe. The problem lies in the fact that miners have (limited) control over them. In fact, they can choose to publish or not a block. By withholding a block they could influence the random function.

This was taken into account already in 3.5.1. In order to obtain a pseudo-random number $r \in \{0, \dots, N\}$:

$$r = H(\text{PreviousBlock}) \bmod N \quad (3.5)$$

where we assume that the Hash of the previous block is an integer.

As we have already said, an attacker can never cheat the community since he/she can only get as much as he/she pays for to be part of the community with his/her fake accounts.

Chapter 4

Further Improvements

This section aims at treating the subjects that we considered in our design but could not implement in the time frame that was allocated for the project. It should serve as a basis to restart the project in the future.

4.1 Preregistration

In 1.3.4 was introduced the notion of **Critical Mass**. This number is defined as the minimum number of users for the community to behave as designed. So far we have considered that this number would be reached whenever the community was created but we did not discuss how that could be achieved.

The idea is to use an external pre-registration platform. This would allow having users register before we launch the platform. There are several possibilities for such platform. It could either be implemented as a smart contract on the blockchain or be completely external.

4.1.1 Idea

Each user that wish to participate in the community will have the possibility to pre-register. In order to do so, he/she will need to provide the initial Top-Off Value T_0 . The preregistration system will hold on to this amount.

Then there are several possibilities that can be imagined.

- The system keeps track of an expiry date for each registration: it refunds the user after that.
- The system can refund users whenever they ask to cancel their pre-registration which they can do only during the pre-registration period, they will not be able to get their money back once the community has been created.

4.1.2 Using Another Smart-contract

The very intuitive idea would be to use the blockchain to implement a system that can manage the funds during the pre-registration. The main justification for this is that we want a decentralised system. Also, this would allow us to automatically go back to preregistration whenever we go below the critical mass without the need for external support. Moreover, by using an external platform, we might need to change the system source code if this platform disappears in the future. Therefore we believe that it would be a good idea to use another smart contract to do pre-registration. It could be created as many times as necessary by the original system. As long as the original system is up and running it means that the Ethereum blockchain is still functional and that we can go back to pre-registration.

4.2 Community Rules

The system that we have described so far is very versatile. In fact, we have talked about car deductible but could have chosen to insure bicycles or any other good. So far we have not talked about what community rules should be.

Those rules are meant to ensure that all the voters base their vote on the same criteria. They were not yet discussed because they would require surveying potential users to discover in what types of situations they wish to be insured and to insure others.

We will simply discuss examples of potential rules that could apply and could be proposed to users:

- In the case of a claim concerning a responsible crash, a proof should be produced that the claimer has not consumed any drugs and/or alcohol.
- The community covers repairs for car body work not exceeding $x\$$.
- We require at least k witnesses that are not affiliated to the claimer.

Those rules can be further developed and their scope has no limit. One could also think about another policy to update those rules based on a community vote. This would allow adapting to changing regulations or community.

4.3 Extra Cost Management

4.3.1 Explanation of Extra Costs

We have not described in many details the effect of gas on the users. We have already explained the use of gas (c.f. 2.2.1), on the other hand the gas limit is used to avoid a user calling buggy code that will run until all its gas reserve is depleted. The product of `gasPrice` and `gas` represents the maximum amount of ether (expressed in Wei¹) that they are willing to pay for executing the transaction. What you specify as `gasPrice` is used by miners to rank transactions

¹Because floats cannot be represented in solidity, they use different units, 1 ether = 10^{18} Wei

for inclusion in the blockchain. It is the price in Wei of one unit of gas, in which operations are priced.

To illustrate that, we could think about how we communicate with our insurances using postal services. To send documents to an insurance it is necessary to pay for a stamp. Different stamp price will yield different services (reliability, tracking, delivery speed etc.). Here the system works as a negotiation. When proposing a transaction to the transaction pool, you specify how much you are willing to pay for each computation power unit. And you also specify what is the limit you do not want to exceed when executing the transaction. Based on this, miners can decide to execute the transaction or not.

4.3.2 Storage - Less of a Concern

Interestingly, storage is also paid by users. Whenever a call to the contract results in an increase or decrease in the contract storage requirements, it will be translated to the transaction gas consumption. But the code does not contain important storage requirements modification that would be launched by a call. Therefore, the storage costs should be evenly split between users. Each user will basically pay for storage added because of his/her activity in the community.

4.3.3 Out-of-gas

Since users will have to pay for each interaction with the system. Should they not have enough ether to pay for the gas expenditure of the transaction execution. The gas spent up to the point where execution stopped will be taken from the caller's ether balance. Then all the state of the smart-contract will be restored to pre-transaction state. This throws an **Out-of-gas** exception.

4.3.4 Consequences For Implementation

The main concern around those extra costs is that we wish to avoid having users unfairly paying more than others. That can happen because of the design decisions that were made for the system. Because of the lack of scheduled calls explained in 3.2 we decided to use contract interaction as triggers.

Whenever a user interacts with the contract, the contract checks that there is nothing to be executed (e.g. executing a claim, finishing a funding, ...). But in the event when something has to be executed, the gas needed to do so will have to be paid by the user who interacted. Some of those actions are very heavy and will need a lot of gas.

Since this is a very early version of the system, implementation did not handle extra cost consideration. But this has to be done. The risk would be that users get discouraged by such high costs and would let the community die.

4.4 Migration Toward the Ethereum Network

`testrpc` has allowed us to develop easily, providing us with a local blockchain, some fake accounts and a total transparency concerning transaction mining. Deploying the contract on the real blockchain will have to happen at some point in time.

It is important to note that once this is done, there is no going back. The system will be live and anyone will be able to interact with it.

However, before migrating to the real Ethereum network, it is possible to take an intermediary step with a public `testnet`². Ethereum `testnets` are real networks, with nodes running across continents, which can be used to simulate a contract at large scale. The advantage over `testrpc` is that delays for block mining and transaction validation are almost identical to the ones experienced on the real network, and multiple users can use the contract, as it is available on a public network. Such networks are `ropsten`, `kovan` or `rinkeby`[3], which differ from the client you can use to access them, and the type of consensus algorithm. Whereas these networks are practical for development purpose, they often lack miners and computing power and are very vulnerable to attackers[5]. Although, it's often not a major problem for users (except for the lack of availability during an outage), since ether used on these networks is fake ether. Users can get it either by mining the network, or using special links.

Once the contract proved its reliability on a public testnet, with a large number of beta users. We can considerate moving it to production on the real public Ethereum network.

This is why it should not be done before the system architecture is finished and bullet proof.

²Note that a `testnet` can also be private, which require setting up hardware and running Ethereum clients to simulate the blockchain activity.

Chapter 5

Conclusion

The blockchain technology seems to be used as a buzzword in the industry. As we experienced it ourselves, its inner-workings are not trivial. Developing blockchain based applications is expensive and time-consuming. It should be made clear to everyone deciding whether or not to use the blockchain to build a system, that if the question comes to their mind it means that they might not need it.

The blockchain should not be used without seriously considering the advantages it provides. For our system, we believe that the choice is justified as we have already explained it.

Because we are convinced of the usability of the blockchain for our use case, we are hoping that the model will be further refined and will hopefully be launched one day. The project was stopped at such point because it will now require more knowledge of car insurances. But it will also require a bit more research on the potential market.

With these pieces of information, the system could be entirely specified (the historical statistics to use, the interface to put in place to interact with the contract, the rules to define for the community). One should also note that before publishing the contract on the blockchain it might be interesting to ask a jurist if the contract is in accordance with the laws of the nation into which the users are insured, but also to ensure that the system designer cannot be held responsible for any problem relative to the model.

More on the personal side, this project was a very rich experience. The LACAL lab let us be very autonomous in our work. Even though this proved to be quite a challenge to handle everything by ourselves, we think it made us grow more mature. We experienced for the first time the design and implementation of a system from beginning to end. We had the possibility also to organise our time and our roles as we wished. It enabled the two of us to really discover our strengths and weaknesses in a team and how to overcome them. g

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