

Big Data Algo



Lecture 9

N

A = 2 6 10 15 22 50

a

x = 14

List Looking
↓ ↓
for for

```
def linearSearch(A, x)
    for a in A
        if x <= a
            return a
    return None
```

					l	m	r
0	1	2	3	4	5	6	
1	3	7	10	12	16	18	

l	r	m
0	6	3
4	6	5
4	5	4
5	5	

$x = 14$

```

def bs(A, x, l, r)
    if l == r
        return A[l]
    m = (l + r) // 2
    if x <= A[m]
        return bs(A, x, l, m)
    else
        return bs(A, x, m + 1, r)
  
```

$0 \downarrow$ $\text{len}(A) - 1 \downarrow$

Linear Search $N \rightarrow 2N$

Runtime Double

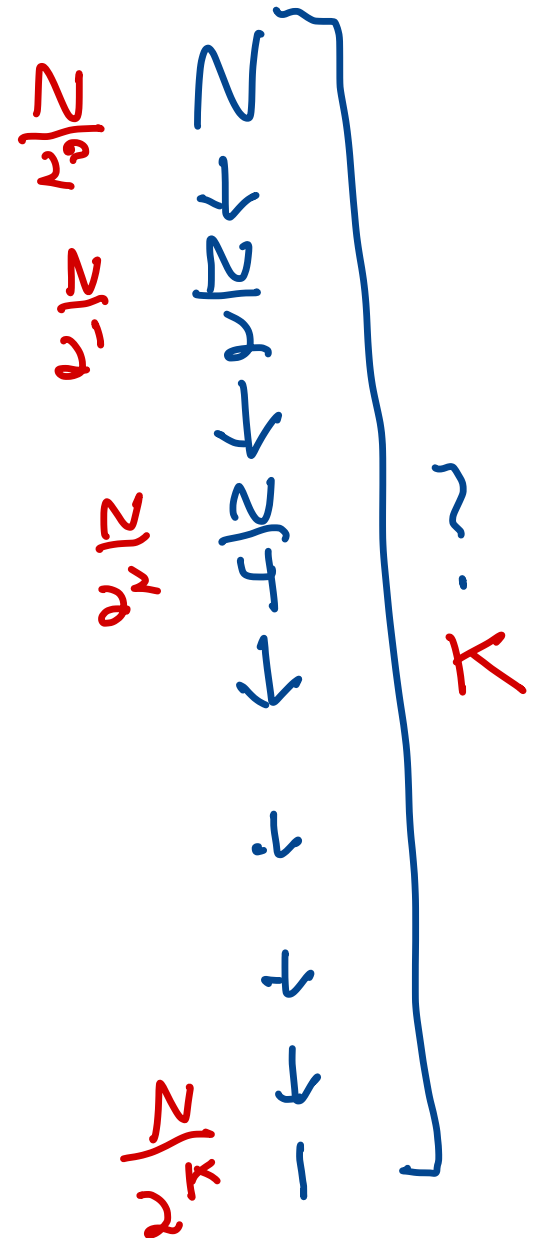
$$O(N)$$

Binary Search $N \rightarrow 2N$

Runtime + same constant

$$O(\log_2 N)$$

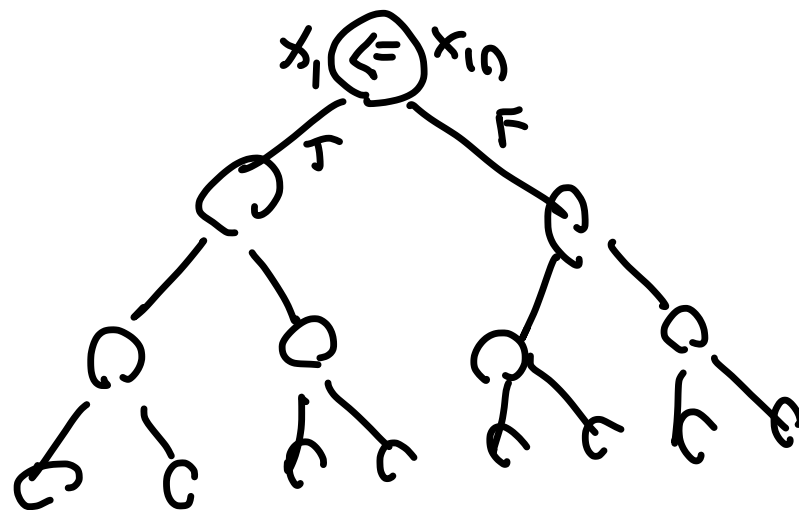
$$\begin{aligned}\frac{N}{2^k} &= 1 \\ N &= 2^k \\ \log_2 N &= k\end{aligned}$$



Can You Do Better?

"Lower Bound" No

To search in N things requires
at least $\log_2 N$ comparisons.



$$2^L \geq N$$
$$L \geq \log_2 N$$

0.4 ns

16-32

CPU

intel x86] Computers
ARM] Portable devices

CACHE

Memory
RAM

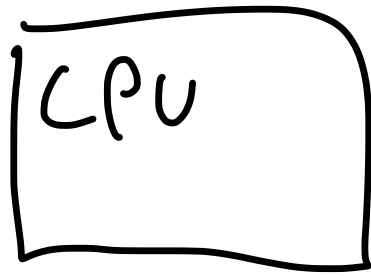
10 ns \approx 8000 TB

CB 8, 16, 32
192

0 1 2 3 4 ...

DISC / 5 TB 100 EWDs 20/TP 10 ms
SSD / 1 TB 173 EWDs 100 μ s
"Secondary Storage"

TP



Speed: 2.4 GHz

$$\frac{1}{2.4 \text{ GHz}} = 0.4 \text{ ns}$$

Has $\approx 16 - 32$ "Registers"

Register: Place to store 1
Value (1 value 64 bits)

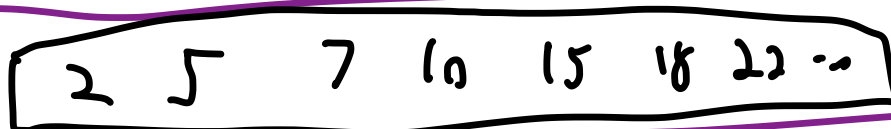
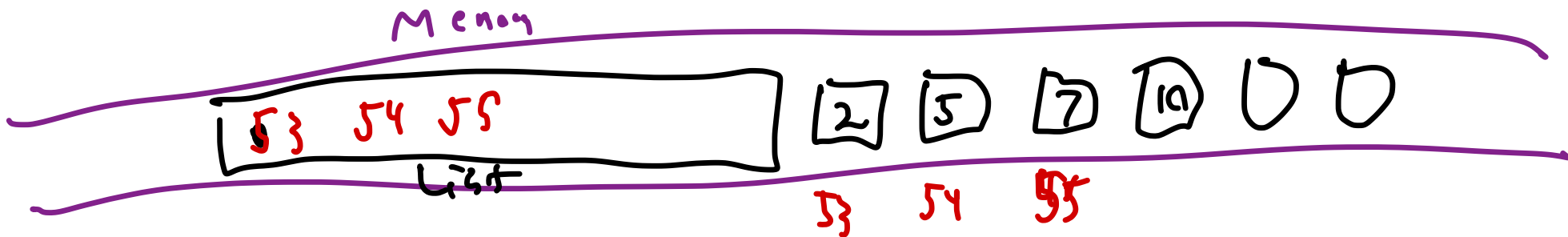
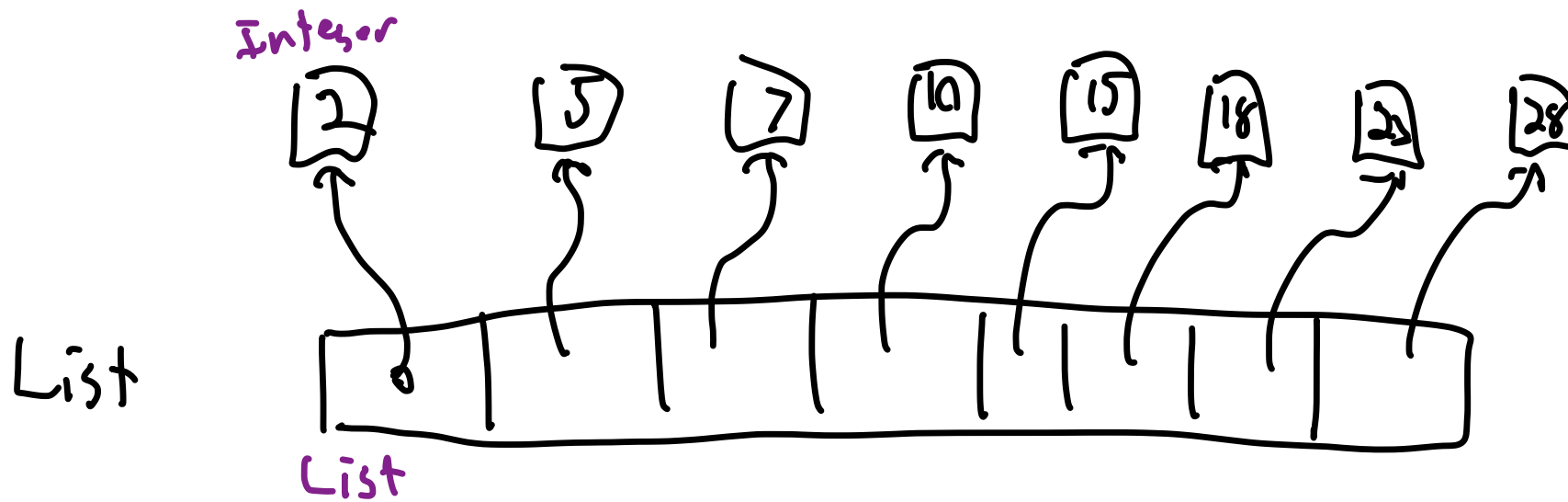
At each time step:

- Do math on the registers
- Read/Write a register from memory

$$\text{ns} = 10^{-9} \text{ s}$$

$$\mu\text{s} = 10^{-6} \text{ s}$$

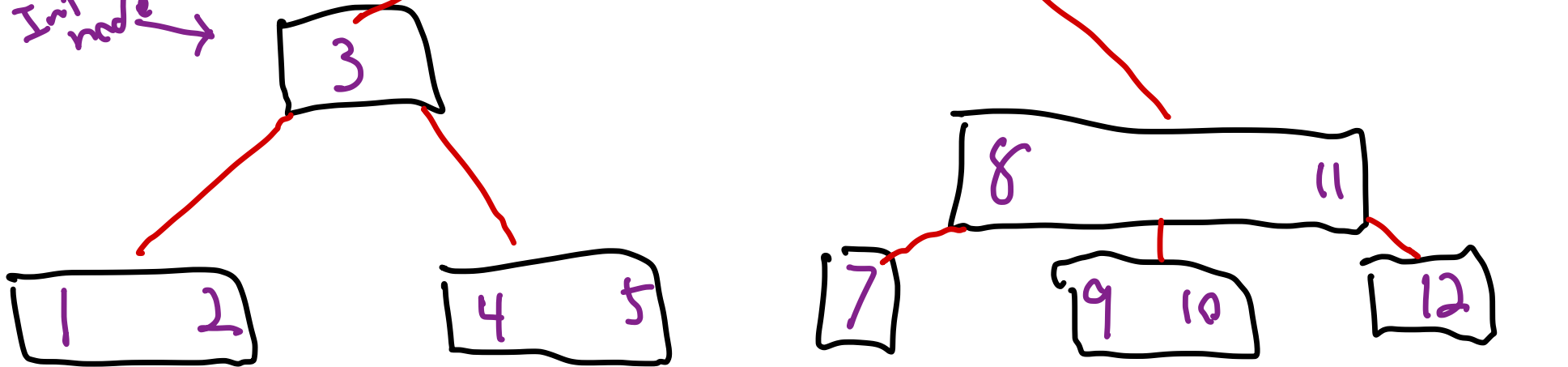
$$\text{ms} = 10^{-3} \text{ s}$$



2-3 Tree

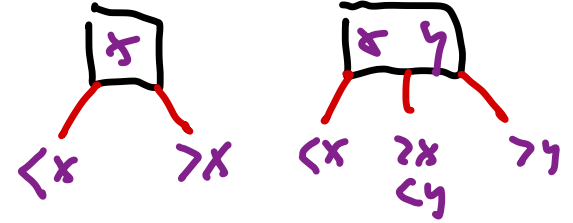
Ins/Del/Search
 $O(\log N)$

Internal
node



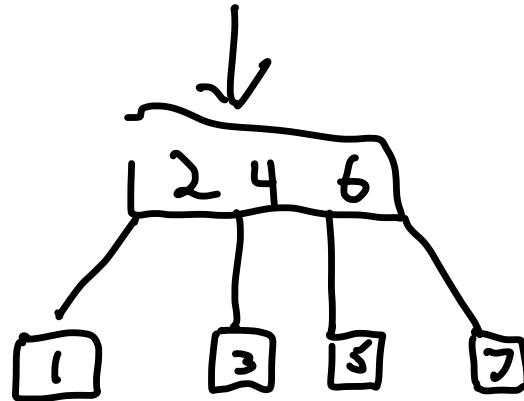
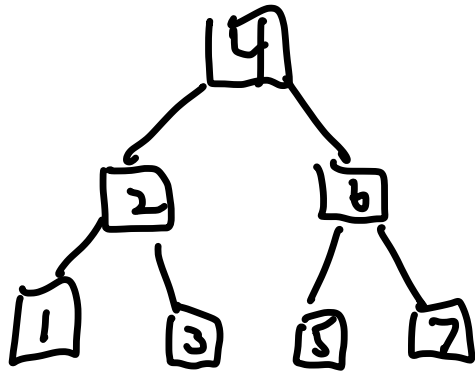
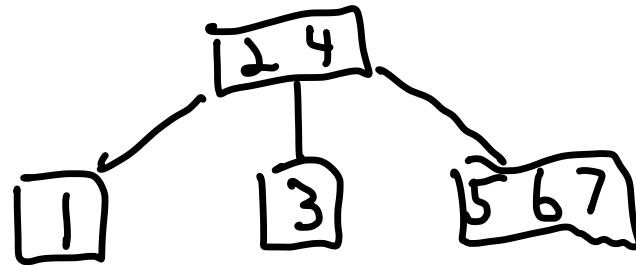
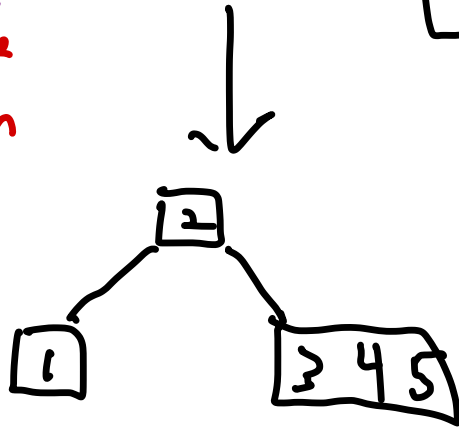
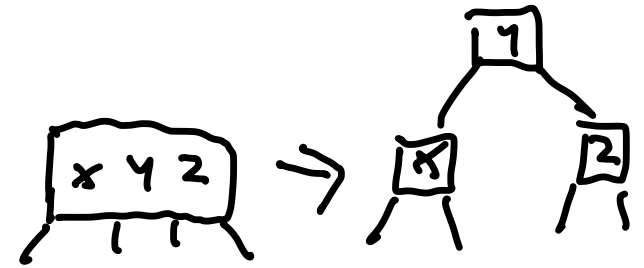
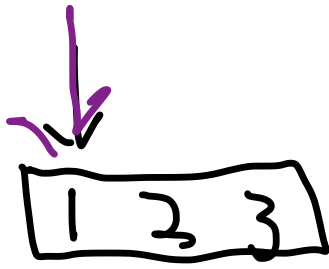
leaves

All leaves are at
the same Depth



1, 2, 3, 4, 5, ...

Class Tree
class Node
└ Data
└ children
root
Insert
Delete
Search



B-Tree

$\approx 2-3$ Tree
Extent $\frac{B}{2} \approx B$

1,000,000

$$\log_2 1,000,000 \approx 10$$

