

Lecture 2

Part 2:

Unordered Data

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Set ADT

$S.\text{Add}(x)$

$S.\text{Remove}(x)$

$x \in S?$

Unordered Data

Set AOT

S.Add(x)

S.Remove(x)

x in S?

Key / Value Store

HashMap

Associative Array

S.Add(k,v) S.Replace(k,v)

S.Remove(k)

x in S

value stored with key k

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Python

Dictionary
S={}

S[k]=v

del S[k]

k in S

S[k]

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Allow: Big keys, values

Don't Allow: Any other queries, eg proximity, range

Today's Plan

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- Hash Tables

General-purpose way to store
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Compact way to store an array
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Compact way to store an array
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- Bloom Filters

Compact way of storing
general-purpose data at
the cost of allowing errors

Hash Tables

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(expected)

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- Use Hash Functions
- The best structure to use in many situations

Hash Tables : Basic idea

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- Build a table with b buckets

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 $\text{hash}(\text{"cat"}) = 123$ $\text{hash}(\text{"maose"}) = 313$
 $\text{hash}(\text{"dog"}) = 456$

$H[\text{"cat"}] = \text{"shadow"}$
 $H[\text{"dog"}] = \text{"bilou"}$
 $H[\text{"maose"}] = \text{"melvin"}$

Hash Tables : Basic idea

Data structure:
Table : list
Bucket : list
K,V pair : list



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__contains__ $K \text{ in } H$

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bucket A helper method to determine which bucket a key belongs to

Code : ..contains..

k in H

H.~.contains~.(k)

def __contains__(self, key)

for k,v in self.A [self._bucket(key)]

if k == key

return True

return False

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- Python will rebuild the table to keep $\frac{n}{b} = O(1)$ and thus keep the runtime $O(1)$
- Python supports more operations
e.g. for x in H : (iterator)

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- Motivates what will come next