

Lecture 3: January 10, 2018

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3.1 Consumer Choice Continued

- Given a preference relation \succeq on \mathbb{R}_*^2 ,
 - The strict preference relation \succ on \mathbb{R}_*^2 is defined such that $x \succ y$ if and only if $x \succeq y$ but not $y \succeq x$
 - The indifference relation \sim on \mathbb{R}_*^2 is defined such that $x \sim y$ iff $x \succeq y$ and $y \succeq x$
 - Having as primitives the weak preference relation is equivalent to having as primitives the strict preference and indifference relations
- An arbitrary preference relation need not correspond to preferences we find interesting or reasonable

Example 3.1 Fix pref. rel. \succeq on \mathbb{R}_*^2

1. Say \succeq such that not $x \succeq y$ for all $x, y \in \mathbb{R}_*^2$
 - Consumer is **not** indifferent between all bundles, but incapable of stating preferences
2. Say \succeq is such that there exists $x, y, z \in \mathbb{R}_*^2$ with $x \succ y \succ z$ and $z \succ x$
 - Ranking of bundles x and z are inconsistent when,
 - * compared through y , x is best
 - * compared directly, z is best

Definition 3.2 The preference relation \succeq on \mathbb{R}_*^2 is

1. Complete if, for all $x, y \in \mathbb{R}_*^2$, either $x \succeq y$ or $y \succ x$ (or both)
2. Transitive if, for all $x, y, z \in \mathbb{R}_*^2$ such that $x \succeq y \succeq z$, we have $x \succeq z$

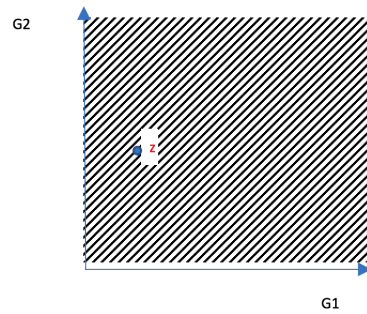
- These are rationality assumptions
- Completeness assumes that DM has capacity to reflect on his preferences
- Transitivity
 - is critical theoretically (without it, optimal choices need not exist)
 - is problematic empirically
 - * Say good 1 is beer, good 2 is cigarettes

$$x = (2, 0) \quad y = (0, 0), \quad z = (2, 1)$$

Definition 3.3 Given a preference relation \succeq on \mathbb{R}_*^2 and a bundle z , the indifference curve of z is the set of $\{x \in \mathbb{R}_*^2; x \sim z\}$

- Indifference curves need not be line segments

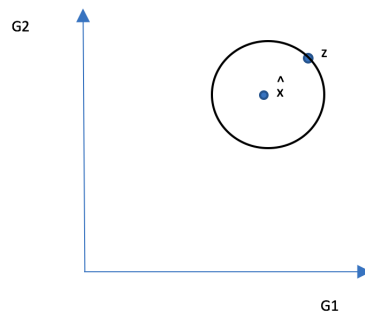
Example 3.4 Say \succeq on \mathbb{R}_*^2 such that $x \succeq y$ for all $x, y \in \mathbb{R}_*^2$



- Indifference curves need not be downward sloping.

Example 3.5 Say \succeq on \mathbb{R}_*^2 such that there exists bundle \hat{x} such that $x \succeq y$ iff x is lower to \hat{x} than y is

– \hat{x} is the "bliss point"



- Indifference curves need not be smooth or differentiable

Example 3.6 Perfect complements, i.e. \succeq on \mathbb{R}_*^2 such that $x \succeq y$ iff $\min\{x_1, x_2\} \geq \min\{y_1, y_2\}$

