

Lecture 12: January 29, 2016

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12.1 Arc Length Example

Example 12.1 Determine the length of the of $x = \frac{2}{3}(y^2 + 1)^{\frac{3}{2}}$ from $y = -2$ to $y = 1$

$$\begin{aligned} L &= \int_{-2}^1 \sqrt{1 + (2y(y^2 + 1)^{\frac{1}{2}})^2} dy = \int_{-2}^1 \sqrt{1 + 4y^2(y^2 + 1)} dy \\ &= \int_{-2}^1 \sqrt{1 + 4y^4 + 4y^2} dy \\ &= \int_{-2}^1 \sqrt{(2y^2 + 1)^2} dy \\ &= \int_{-2}^1 (2y^2 + 1) dy \\ &= \left[\frac{2}{3}y^3 + y \right]_{-2}^1 \\ &= 9 \end{aligned}$$

12.2 Area of Surface of Revolution

Formula :

about x - axis : $SA = \int 2\pi y ds$ where $ds = \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx$ if $y = f(x), a \leq y \leq b$

about y - axis : $SA = \int 2\pi x ds$ where $ds = \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy$ if $x = g(y), c \leq y \leq d$

End of Lecture Notes
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