W18x50

$$h \coloneqq 18 \ \textit{in} = 457.2 \ \textit{mm}$$

 $b_f \coloneqq 7.5 \ \textit{in} = 190.5 \ \textit{mm}$
 $t_f \coloneqq 0.57 \ \textit{in} = 14.478 \ \textit{mm}$
 $t_w \coloneqq 0.355 \ \textit{in} = 9.017 \ \textit{mm}$

$$A_g := 2 \cdot t_f \cdot b_f + (h - 2 \cdot t_f) \cdot t_w = (9.378 \cdot 10^3) \ mm^2$$

$$I_{x} \coloneqq \left(2 \cdot \left(b_{f} \cdot \frac{t_{f}^{\ 3}}{12} + b_{f} \cdot t_{f} \cdot \left(\frac{\left(h - 2 \cdot t_{f}\right)}{2} + \frac{t_{f}}{2}\right)^{2}\right) + t_{w} \cdot \frac{\left(h - 2 \cdot t_{f}\right)^{3}}{12}\right) = \left(3.294 \cdot 10^{8}\right) \ \textit{mm}^{4}$$

$$S_x \coloneqq \frac{I_x}{\left(\frac{h}{2}\right)} = \left(1.441 \cdot 10^6\right) \, \mathbf{mm}^3$$

$$Z_x \coloneqq b_f \cdot t_f \cdot \left(h - t_f \right) + \frac{1}{4} \cdot \left(h - 2 \ t_f \right)^2 \cdot t_w = \left(1.634 \cdot 10^6 \right) \ \textit{mm}^3$$

$$r_x := \sqrt{\frac{I_x}{A_g}} = 187.421 \ \textit{mm}$$

$$I_y := 2 \cdot \left(t_f \cdot \frac{b_f^{\ 3}}{12}\right) + \left(h - 2 \cdot t_f\right) \cdot \frac{t_w^{\ 3}}{12} = \left(1.671 \cdot 10^7\right) \ mm^4$$

$$S_y \coloneqq \frac{I_y}{b_f} = \left(1.754 \cdot 10^5\right) \, \boldsymbol{mm}^3$$

$$Z_y := \frac{1}{2} \cdot b_f^2 \cdot t_f + \frac{1}{4} \cdot (h - 2 \cdot t_f) \cdot t_w^2 = (2.714 \cdot 10^5) \ mm^3$$

$$r_y \coloneqq \sqrt{rac{I_y}{A_g}} = 42.21$$
 mm

$$c_w \coloneqq \frac{\left(h - t_f\right)^2 \cdot b_f^{-3} \cdot t_f}{24} = \left(8.174 \cdot 10^{11}\right) \ m{mm}^6$$

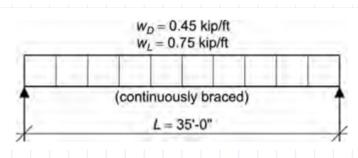
$$J := \frac{2 \cdot b_f \cdot t_f^{\ 3} + (h - t_f) \cdot t_w^{\ 3}}{3} = (4.936 \cdot 10^5) \ \boldsymbol{mm}^4$$

$$r_{ts} \coloneqq \sqrt{\frac{\sqrt{I_y \cdot c_w}}{S_x}} = 50.643 \; \emph{mm}$$
 (1) For doubly symmetric I-shapes

$$c = 1 (F2-8a)$$

$$h_0 \coloneqq h - t_f = 442.722 \ \textit{mm}$$
 (2) For channels

$$c := 1$$
 $c = \frac{h_o}{2} \sqrt{\frac{I_y}{C_w}}$ (F2-8b)



$$l = 35 \ ft = (1.067 \cdot 10^4) \ mm$$

$$w \coloneqq 1.2 \cdot 0.45 \frac{\mathbf{kip}}{\mathbf{ft}} + 1.6 \cdot 0.75 \frac{\mathbf{kip}}{\mathbf{ft}} = 1.74 \frac{\mathbf{kip}}{\mathbf{ft}}$$

$$w := 1.2 \cdot 6.567 \frac{kN}{m} + 1.6 \cdot 10.945 \frac{kN}{m} = 25.392 \frac{kN}{m}$$

$$M \coloneqq \frac{w \cdot l^2}{8} = 266.427 \ \textit{kip} \cdot \textit{ft}$$

$$M \coloneqq \frac{w \cdot l^2}{8} = 361.227 \ \mathbf{kN} \cdot \mathbf{m}$$

$$F_y = 50 \ ksi = 344.738 \ MPa$$

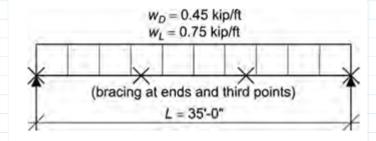
$$E = 29000 \ ksi = (1.999 \cdot 10^5) \ MPa$$

$$\phi M_{n1} = 0.9 \cdot F_u \cdot Z_x = 374.03 \ kip \cdot ft$$

$$\phi M_{n1} = 0.9 \cdot F_y \cdot Z_x = 507.116 \ kN \cdot m$$

$$M\coloneqq \frac{w \cdot l^2}{8} = 266.427 \; extbf{kip} \cdot extbf{ft}$$

$$M \coloneqq \frac{w \cdot l^2}{8} = 361.227 \ \mathbf{kN} \cdot \mathbf{m}$$



$$L_b = \frac{35 \ ft}{3} = 3.556 \ m$$

$$L_p \coloneqq 1.76 \cdot r_y \cdot \sqrt{\frac{E}{F_y}} = 1.789 \ \boldsymbol{m}$$

$$L_r \coloneqq 1.95 \cdot r_{ts} \cdot \frac{E}{0.7 \cdot F_y} \cdot \sqrt{\frac{J \cdot c}{S_x \cdot h_0} + \sqrt{\left(\frac{J \cdot c}{S_x \cdot h_0}\right)^2 + 6.76 \cdot \left(\frac{0.7 \cdot F_y}{E}\right)^2}} = 5.179 \ \textit{m}$$

$$\phi M_{n2} \coloneqq 0.9 \cdot \left(F_y \cdot Z_x - \left(F_y \cdot Z_x - 0.7 \cdot F_y \cdot S_z \right) \cdot \frac{L_b - L_p}{L_r - L_p} \right) = 405.905 \text{ kN} \cdot m$$

$$\parallel > \parallel M \coloneqq \frac{w \cdot t^2}{8} = 361.227 \text{ kN} \cdot m$$

$$w_0 = 0.45 \text{ kipft}$$

$$w_t = 0.75 \text{ kipft}$$

$$w_t = 0.75 \text{ kipft}$$

$$(\text{bracing at ends and midpoint})$$

$$L = 35 \cdot 0^{\circ}$$

$$L_b \coloneqq \frac{35 \text{ } ft}{2} = 5.334 \text{ } m$$

$$C_b \coloneqq 1.3$$

$$F_{cr} \coloneqq C_b \cdot \frac{\pi^2 \cdot E}{\left(\frac{L_b}{r_{ts}}\right)^2} \cdot \sqrt{1 + 0.078 \cdot \frac{J \cdot c}{S_x \cdot h_0} \cdot \left(\frac{L_b}{r_{ts}}\right)^2} = 298.801 \text{ } MPa$$

$$\phi M_{n3} \coloneqq 0.9 \cdot F_{cr} \cdot S_x = 387.505 \text{ kN} \cdot m$$

$$\parallel > \parallel M \coloneqq \frac{w \cdot t^2}{8} = 361.227 \text{ kN} \cdot m$$

$$\phi M_{n3} \coloneqq 0.9 \cdot F_{cr} \cdot S_x = 298.081 \text{ kN} \cdot m$$

$$\parallel < \parallel M \coloneqq \frac{w \cdot t^2}{8} = 361.227 \text{ kN} \cdot m$$