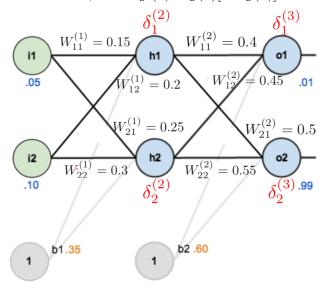
Practice Problem

Perform one iteration of forward propagation and backpropagation in the following neural network, assuming learning rate $\alpha = 0.5$. We also assume a sigmoid activation function g(x) for the hidden nodes, where g'(x) = g(x)[1 - g(x)].



Backpropagation Implementation

- For each (hidden) node i in layer $l = L 1, L 2, \dots, 2$: $\delta_i^{(l)} = \left(\sum_{j=1}^{s_{l+1}} W_{ji}^{(l)} \delta_j^{(l+1)}\right) f'(z_i^{(l)})$
- Compute the desired partial derivatives as: $\frac{\vartheta J(\mathbf{W}, \mathbf{b})}{\vartheta W_{ij}^{(l)}} = \alpha_j^{(l)} \delta_i^{(l+1)}, \ \frac{\vartheta J(\mathbf{W}, \mathbf{b})}{\vartheta b_i^{(l)}} = \delta_i^{(l+1)}$
- $\bullet \ \text{Update the weights as:} \ W_{ij}^{(l)} := W_{ij}^{(l)} \alpha \frac{\vartheta J(\mathbf{W}, \mathbf{b})}{\vartheta W_{ij}^{(l)}}, \ b_i^{(l)} := b_i^{(l)} \alpha \frac{\vartheta J(\mathbf{W}, \mathbf{b})}{\vartheta b_i^{(l)}}$