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Report for Knapsack solutions

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1 Experiment Set-up

1.1 Data extraction

In the process of experiment setup, the data.zip file was acquired from the provided repository located at https://github.com/likr/kplib, and subsequently underwent extraction. Due to the substantial magnitude of the dataset, consisting of 20,800.kp files, executing all samples was deemed unfeasible. Consequently, a random sampling methodology was devised to ensure the selection of a representative subset. This sampling method was performed on the files:

- change_folder_name.py: I compiled all folder names into a single array named folder_name. Subsequently, for each folder within this array, I systematically renamed its subfolders with numerical labels ranging from 1 to 8, mirroring their sequential order within the original directory structure.
- random_data.py: After that, I iterated through each subfolder from 1 to 8. And with each subfolder, I randomly selected 5 files from the subsubfolders R01000 and R10000, respectively. Then, I wrote the paths to the selected files into the testcases_path.txt file.

1.2 Using Google OR-Tools

Google OR-Tools is an open-source optimization toolkit that offers efficient optimization algorithms. When applied to the knapsack problem, OR-Tools provides effective solving methods to find ways to pack items into a limited-capacity bag, aiming to maximize value.

When using this tool for the Knapsack problem, I will utilize the function set_time_limit(180) to restrict the solution time to 180 seconds, equivalent to 3 minutes. According to my research at https://developers.google.com/optimization/reference/python/algorithms/pywrapknapsack_solver#set_time_limit, when a finite time limit is set, the solution obtained might not be optimal if the limit is reached.

Therefore, if the problem finds a solution before the time limit, we refer to it as an optimal or best solution. However, if the problem-solving time is 180 seconds, corresponding to the set time limit, then the solution obtained is not optimal.

2 Statistics and Evaluation of Knapsack Problem Results

2.1 Statistics

The **output** folder contains all the solutions of the randomly selected test cases as described in the above **Experiment Set-up**. For this report, we only sampled a subset of test cases from 13 folders: 00Uncorrelated, 01WeaklyCorrelated, 02StronglyCorrelated, 03InverseStronglyCorrelated, 04AlmostStronglyCorrelated, 05SubsetSum, 06UncorrelatedWithSimilarWeights, 07SpannerUncorrelated, 08SpannerWeaklyCorrelated, 09SpannerStronglyCorrelated, 10MultipleStronglyCorrelated, 11ProfitCeiling, 12Circle. In each folder, we selected one test case for each N_items value ranging from n00500 to n20000.

- **Test case:** This represents the path to the test case file.
- Time: The time taken to find the solution and measured in seconds. This time is limited to a maximum of 180 seconds.
- Value: The total value of the optimally packed items.
- Weight: The total weight of the optimally packed items.
- Optimal: True if it is an optimal solution. If the time taken to find the solution is less than 180 seconds, it will be marked as True. However, if the time taken equals 180 seconds, which is equivalent to the set_time_limit(), it will be marked as False.

| Testcase | N_items | Execution Time | Capacity | Total Value | Total Weight | Optimal |
|--|----------------|-------------------|--|---------------------|--|--------------|
| /00Uncorrelated/1/R10000/s030 | 50 | 0.000 | 127555 | 201461 | 127530 | True |
| /00Uncorrelated/2/R01000/s051 | 100 | 0.000 | 26220 | 45629 | 26204 | True |
| /00Uncorrelated/3/R10000/s030 | 200 | 0.001 | 474730 | 809165 | 474569 | True |
| /00Uncorrelated/4/R01000/s049 | 500 | 0.000 | 122191 | 196691 | 122178 | True |
| /00Uncorrelated/5/R01000/s022 /00Uncorrelated/6/R10000/s010 | $1000 \\ 2000$ | $0.000 \\ 0.001$ | $\begin{array}{c} 247104 \\ 4924266 \end{array}$ | $400290 \\ 8166357$ | $\begin{array}{c} 247103 \\ 4924263 \end{array}$ | True True |

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| Testcase | N_items | Execution Time | Capacity | Total Value | Total Weight | Optimal |
|---|-------------|-------------------|-----------------------|--------------------|-----------------------|----------------|
| /00Uncorrelated/7/R01000/s024 | 5000 | 0.000 | 1192393 | 2067317 | 1192392 | True |
| /00Uncorrelated/8/R10000/s017 | 10000 | 0.000 | 24670351 | 40300050 | 24670348 | True |
| /01WeaklyCorrelated/1/R01000/s094 | 50 | 0.000 | 11888 | 13175 | 11885 | True |
| /01WeaklyCorrelated/2/R01000/s025 | 100 | 0.000 | 23220 | 25875 | 23220 | True |
| /01WeaklyCorrelated/3/R10000/s024 | 200 | 0.000 | 502927 | 561884 | 502915 | True |
| /01WeaklyCorrelated/4/R10000/s079 | 500 | 0.000 | 1201558 | 1336791 | 1201556 | True |
| /01WeaklyCorrelated/5/R01000/s066 | 1000 | 0.000 | 248350 | 273740 | 248350 | True |
| /01WeaklyCorrelated/6/R01000/s064 | 2000 | 0.000 | 494251 | 548275 | 494251 | True |
| /01WeaklyCorrelated/7/R01000/s047 | 5000 | 0.032 | 1243366 | 1375240 | 1243366 | True |
| /01WeaklyCorrelated/8/R01000/s047 | 10000 | 0.016 | 2484197 | 2742854 | 2484197 | True |
| /02StronglyCorrelated/1/R10000/s083 | 50 | 0.386 | 122235 | 156235 | 122235 | True |
| /02StronglyCorrelated/2/R10000/s091 | 100 | 1.758 | 270311 | 338311 | 270311 | True |
| /02StronglyCorrelated/3/R01000/s050 | 200 | 20.606 | 47460 | 61760 | 47460 | True |
| /02StronglyCorrelated/4/R01000/s075 | 500 | 180.046 | 122676 | 157500 | 122400 | False |
| /02StronglyCorrelated/5/R01000/s073 | 1000 | 180.029 | 241402 | 311690 | 241090 | False |
| /02StronglyCorrelated/6/R10000/s018 | 2000 | 180.001 | 4963941 | 6359261 | 4959261 | False |
| /02StronglyCorrelated/7/R10000/s036 | 5000 | 179.968 | 12330501 | 15846553 | 12325553 | True |
| /02StronglyCorrelated/8/R10000/s015 | 10000 | 179.709 | 24775197 | 31808958 | 24769958 | True |
| /03InverseStronglyCorrelated/1/R01000/s092 | 50 | 1.083 | 16307 | 14524 | 16224 | True |
| /03InverseStronglyCorrelated/2/R10000/s026 | 100 | 0.000 | 289321 | 259320 | 289320 | True |
| /03InverseStronglyCorrelated/3/R01000/s016 | 200 | 180.043 | 56460 | 50260 | 56460 | False |
| /03InverseStronglyCorrelated/4/R01000/s020 | 500 | 180.043 | 143201 | 128001 | 143201 | False |
| /03InverseStronglyCorrelated/5/R01000/s020 | 1000 | 180.038 | 306206 | 273966 | 306166 | False |
| /03InverseStronglyCorrelated/5/R01000/s034 /03InverseStronglyCorrelated/6/R10000/s017 | 2000 | 180.012 | 5959872 | 5326865 | 5955865 | False False |
| | 5000 | | | | | |
| /03InverseStronglyCorrelated/7/R10000/s030 /03InverseStronglyCorrelated/8/R01000/s088 | 10000 | 179.978 179.901 | $14777352 \\ 2964911$ | 13204795 2648835 | $14772795 \\ 2964435$ | True True |
| , , , , , | | | | | | |
| /04AlmostStronglyCorrelated/1/R01000/s036 | 50 100 | 0.000 | 13946 | 17336 | 13946 | True |
| /04AlmostStronglyCorrelated/2/R01000/s055 | | 0.440 | 24611 | 31424 | 24611 | True |
| /04AlmostStronglyCorrelated/3/R10000/s011 | 200 | 180.076 | 497719 | 638830 | 497716 | False |
| /04AlmostStronglyCorrelated/4/R10000/s079 | 500 | 2.579 | 1201558 | 1554738 | 1201557 | True |
| /04AlmostStronglyCorrelated/5/R10000/s011 | 1000 | 180.011 | 2512521 | 3207714 | 2508949 | False |
| /04AlmostStronglyCorrelated/6/R01000/s092 | 2000 | 0.487 | 494716 | 635011 | 494716 | True |
| /04AlmostStronglyCorrelated/7/R10000/s050 | 5000 | 179.945 | 12361648 | 15875198 | 12356757 | True |
| /04AlmostStronglyCorrelated/8/R10000/s092 | 10000 | 179.713 | 24463602 | 31512923 | 24458957 | True |
| /05SubsetSum/1/R10000/s025 | 50 | 0.000 | 113745 | 113745 | 113745 | True |
| /05SubsetSum/2/R10000/s005 | 100 | 0.000 | 246212 | 246212 | 246212 | True |
| /05SubsetSum/3/R10000/s066 | 200 | 0.016 | 498185 | 498185 | 498185 | True |
| /05SubsetSum/4/R01000/s042 | 500 | 0.000 | 124243 | 124243 | 124243 | True |
| /05SubsetSum/5/R01000/s013 | 1000 | 0.000 | 243197 | 243197 | 243197 | True |
| /05SubsetSum/6/R01000/s093 | 2000 | 0.000 | 503252 | 503252 | 503252 | True |
| /05SubsetSum/7/R10000/s007 | 5000 | 0.008 | 12247962 | 12247962 | 12247962 | True |
| /05SubsetSum/8/R10000/s029 | 10000 | 0.016 | 24605208 | 24605208 | 24605208 | True |
| /06 Uncorrelated With Similar Weights/1/R10000/s059 | 50 | 0.078 | 2476461 | 19370 | 2401115 | True |
| /06 Uncorrelated With Similar Weights/2/R01000/s075 | 100 | 0.110 | 4952887 | 37667 | 4902207 | True |
| /06UncorrelatedWithSimilarWeights/3/R10000/s034 | 200 | 0.000 | 9906026 | 77405 | 9904549 | True |
| /06UncorrelatedWithSimilarWeights $/4/R10000/s016$ | 500 | 180.016 | 24764986 | 182355 | 24712578 | False |
| /06UncorrelatedWithSimilarWeights/5/R10000/s014 | 1000 | 0.133 | 49529345 | 369546 | 49525194 | True |
| /06UncorrelatedWithSimilarWeights/6/R01000/s012 | 2000 | 180.015 | 99060009 | 746841 | 99050084 | False |
| /06UncorrelatedWithSimilarWeights/7/R10000/s089 | 5000 | 179.967 | 247648444 | 1865038 | 247624250 | True |
| /06UncorrelatedWithSimilarWeights/8/R10000/s032 | 10000 | 179.815 | 495296685 | 3717155 | 495250511 | True |
| /07SpannerUncorrelated/1/R10000/s004 | 50 | 175.291 | 36554 | 22976 | 36480 | True |
| /07SpannerUncorrelated $/2/R01000/s030$ | 100 | 180.042 | 8221 | 15630 | 8170 | False |
| /07SpannerUncorrelated/3/R10000/s013 | 200 | 180.035 | 350759 | 282842 | 350488 | False |
| /07SpannerUncorrelated/4/R10000/s089 | 500 | 180.046 | 654814 | 830298 | 654266 | False |
| /07SpannerUncorrelated/5/R01000/s025 | 1000 | 171.168 | 130450 | 266204 | 130435 | True |
| /07SpannerUncorrelated/6/R10000/s007 | 2000 | 180.005 | 1754011 | 1440553 | 1753555 | False |
| /07SpannerUncorrelated/7/R01000/s065 | 5000 | 179.983 | 801106 | 481409 | 801084 | True |
| /07SpannerUncorrelated/8/R01000/s030 | 10000 | 179.752 | 806538 | 1700665 | 806512 | True |
| /08SpannerWeaklyCorrelated/1/R10000/s057 | 50 | 179.093 | 43709 | 64137 | 43682 | True |
| /08SpannerWeaklyCorrelated/2/R10000/s068 | 100 | 0.110 | 206737 | 407337 | 206729 | True |
| /08SpannerWeaklyCorrelated/3/R10000/s068 | 200 | 180.054 | 392120 | 771730 | 391590 | False |
| /08SpannerWeaklyCorrelated/4/R10000/s041 | 500 | 180.036 | 378450 | 1647110 | 378334 | False |
| /08SpannerWeaklyCorrelated/5/R10000/s065 | 1000 | 180.040 | 865822 | 2672544 | 865592 | False |
| /08SpannerWeaklyCorrelated/6/R10000/s086 | 2000 | 180.009 | 1996343 | 5485897 | 1996293 | False |
| /08SpannerWeaklyCorrelated/7/R10000/s028 | 5000 | 179.968 | 1505998 | 9384304 | 1505945 | True |
| /08SpannerWeaklyCorrelated/8/R01000/s028 | 10000 | 179.837 | 1451024 | 1372442 | 1451020 | True |
| /08Spanner Weakly Correlated/8/R01000/s098 /09SpannerStrongly Correlated/1/R01000/s053 | 10000 50 | 0.016 | 1451024 8751 | 23937 | 1451020 8737 | True True |
| /09SpannerStronglyCorrelated/2/R01000/s082 | 50 100 | 180.036 | 8237 | 44635 | 8235 | False |
| | | | | | | |
| /09SpannerStronglyCorrelated/3/R01000/s033 | 200 | 180.041 | 29374 | 86673 | 29373 | False |
| /09SpannerStronglyCorrelated/4/R10000/s018 | 500 | 180.043 | 545122 | 2379059 | 545059 | False |
| /09SpannerStronglyCorrelated/5/R01000/s072 | 1000 | 180.031 | 85761 | 481458 | 85758 | False |
| /09SpannerStronglyCorrelated/6/R10000/s011 | 2000 | 177.481 | 2483662 9689660 | 8388603 | 2483603 | True True |
| /09SpannerStronglyCorrelated/7/R10000/s020 | 5000 | 179.969 | | 24883885 | 9688885 | |

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| Testcase | N_items | Execution Time | Capacity | Total Value | Total Weight | Optimal |
|---|---------|-------------------|----------|-------------|-----------------|---------|
| /09SpannerStronglyCorrelated/8/R10000/s041 | 10000 | 179.804 | 7544845 | 40225784 | 7544784 | True |
| /10MultipleStronglyCorrelated/1/R01000/s082 | 50 | 0.000 | 11964 | 19364 | 11964 | True |
| /10MultipleStronglyCorrelated/2/R10000/s011 | 100 | 0.050 | 233898 | 389898 | 233898 | True |
| /10MultipleStronglyCorrelated/3/R01000/s009 | 200 | 17.058 | 46602 | 78302 | 46602 | True |
| /10MultipleStronglyCorrelated/4/R10000/s065 | 500 | 180.021 | 1258980 | 2016980 | 1258980 | False |
| /10MultipleStronglyCorrelated/5/R10000/s056 | 1000 | 180.032 | 2481342 | 4020342 | 2481342 | False |
| /10MultipleStronglyCorrelated/6/R01000/s079 | 2000 | 180.015 | 491946 | 801635 | 491935 | False |
| /10MultipleStronglyCorrelated/7/R01000/s058 | 5000 | 179.958 | 1248000 | 2019962 | 1247862 | True |
| /10MultipleStronglyCorrelated/8/R10000/s031 | 10000 | 179.741 | 25008090 | 40398887 | 25006887 | True |
| /11ProfitCeiling/1/R10000/s076 | 50 | 0.016 | 132392 | 132387 | 132391 | True |
| /11ProfitCeiling/2/R01000/s077 | 100 | 180.042 | 24216 | 24204 | 24214 | False |
| /11ProfitCeiling/3/R10000/s041 | 200 | 17.206 | 511610 | 511584 | 511610 | True |
| /11ProfitCeiling/4/R10000/s082 | 500 | 178.716 | 1271710 | 1271664 | 1271708 | True |
| /11ProfitCeiling/5/R01000/s094 | 1000 | 180.029 | 253114 | 253020 | 253114 | False |
| /11ProfitCeiling/6/R01000/s042 | 2000 | 180.018 | 501242 | 501030 | 501242 | False |
| /11ProfitCeiling/7/R10000/s007 | 5000 | 179.985 | 12247962 | 12247500 | 12247961 | True |
| /11ProfitCeiling/8/R10000/s027 | 10000 | 179.844 | 25002713 | 25001697 | 25002712 | True |
| /12Circle/1/R10000/s033 | 50 | 0.016 | 120976 | 8064659 | 120976 | True |
| /12Circle/2/R10000/s030 | 100 | 180.070 | 258742 | 17248594 | 258742 | False |
| /12Circle/3/R10000/s018 | 200 | 186.202 | 501517 | 33432774 | 501517 | False |
| /12Circle/4/R10000/s007 | 500 | 180.024 | 1188095 | 79202325 | 1188095 | False |
| /12Circle/5/R10000/s072 | 1000 | 180.008 | 2576715 | 171772315 | 2576715 | False |
| /12Circle/6/R10000/s065 | 2000 | 180.029 | 5004504 | 333616736 | 5004504 | False |
| /12Circle/7/R01000/s091 | 5000 | 179.964 | 1244805 | 26229218 | 1244805 | True |
| /12Circle/8/R01000/s095 | 10000 | 179.864 | 2483752 | 52334995 | 2483752 | True |

Table 1: Test Results

2.2 Evaluation

The following table presents statistics for the selected test cases, as described in the **Experiment set-up** section. The difficulty levels are categorized into three categories: Easy, Moderate, and Most Difficult.

- Easy Groups (0 False Cases): Groups 00, 01, 05

 These groups are considered easy as there are no cases where the algorithm failed to find an optimal solution.
- Moderate Difficulty Groups (Low False Cases): Groups 04, 06, 10, 11

These groups exhibit moderate difficulty as the number of cases with non-optimal solutions is relatively low compared to the total number of cases. Specifically, the number of false cases does not exceed 32, equivalent to 40% of the total number of cases.

• Most Difficult Groups (High False Cases): Groups 02, 03, 07, 08, 09, 12

These groups are considered most difficult as the number of cases with failed solutions is relatively high, indicating difficulty in finding optimal solutions.

| Group | True | False | | |
|-------|------|-------|--|--|
| 00 | 80 | 0 | | |
| 01 | 80 | 0 | | |
| 02 | 45 | 35 | | |
| 03 | 44 | 36 | | |
| 04 | 56 | 24 | | |
| 05 | 80 | 0 | | |
| 06 | 61 | 19 | | |
| 07 | 40 | 40 | | |
| 08 | 41 | 39 | | |
| 09 | 34 | 46 | | |
| 10 | 56 | 24 | | |
| 11 | 53 | 27 | | |
| 12 | 47 | 33 | | |

Table 2: Optimal Statistics