IML Project Report

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Read data

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
from sklearn import linear_model

npf_test = pd.read_csv("initial_data/npf_test_hidden.csv")
npf_train = pd.read_csv("initial_data/npf_train.csv")
```

Preprocess data & Feature selection

```
npf_train_test = npf_train.set_index("date")
npf_train_test = npf_train_test.drop(['id', 'partlybad'], axis=1)

class2 = np.array(["nonevent", "event"])
class2 = class2[(npf_train_test["class4"]!="nonevent").astype(int)]
#class2 = class2.apply(lambda x: 1 if "event" else 0)
npf_train_test.insert(loc=0, column="class2", value=class2)

npf_train_test["class2"].replace(["event", "nonevent"],[1,0], inplace=True)
npf_train_test["class4"].replace(["nonevent", "Ia", "Ib", "II"],[0, 1, 2, 3], inplace=True)
#DROPS STANDARD DEVIATIONS (STD)
npf_train_test = npf_train_test.filter(regex='mean|class4|class2')
```

As standard deviations didn't affect the accuracy, we decided to exclude them when training the models.

The following table shows the first five columns and rows of our data.

```
knitr::kable(head(py$npf_train_test[,1:5]), row.names = TRUE, digits = 2)
```

	class2	class4	CO2168.mean	CO2336.mean	CO242.mean
2000-01-17	1	2	368.77	368.67	369.37
2000-02-28	0	0	378.20	378.08	378.67
2000-03-24	1	2	373.04	372.93	373.57
2000-03-30	1	3	375.64	375.55	376.05
2000-04-04	0	0	377.66	377.61	378.12
2000-04-07	1	1	373.87	373.79	374.36

Only the means were chosen as features, and the data was not normalized.

Imports

We compared some of the models we encountered during the course.

```
from sklearn.dummy import DummyRegressor
from sklearn.linear_model import LogisticRegression
from sklearn.model_selection import train_test_split, cross_val_score
from sklearn.metrics import mean_squared_error, accuracy_score

from sklearn.naive_bayes import GaussianNB
from sklearn.discriminant_analysis import QuadraticDiscriminantAnalysis
from sklearn.ensemble import RandomForestClassifier

from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import StandardScaler
from sklearn.svm import SVC

from sklearn.neighbors import KNeighborsClassifier
```

Functions for model loss & accuracy

```
def loss(X_tr, y_tr, X_te, y_te, m):
    return mean_squared_error(y_te, m.fit(X_tr, y_tr).predict(X_te), squared=False)

def accuracy(X_tr, y_tr, X_te, y_te, m):
    return accuracy_score(y_te, m.fit(X_tr, y_tr).predict(X_te))
```

Train, fit, evaluate

We use the common 80:20 train-test split, although it might not be the optimal ratio for classification, as a recent study shows it is not optimal for regression. We also set the random_state to make the results reproducible.

	train_loss	cv_loss	test_loss	test_accuracy	test_perplexity
Dummy	0.71	0.72	0.71	0.49	2.00
Logistic1	0.37	0.39	0.34	0.88	1.36
Logistic2	0.39	0.39	0.33	0.88	1.37
Logistic3	0.38	0.39	0.34	0.88	1.37
Logistic4	0.38	0.39	0.33	0.89	1.35
Logistic5	0.39	0.39	0.34	0.88	1.37
GausNB	0.41	0.42	0.41	0.83	3.42
QDA	0.19	0.40	0.40	0.84	16.08
RF	0.00	0.30	0.27	0.94	1.30
KN	0.36	0.43	0.44	0.81	Inf
SVM	0.30	0.36	0.27	0.92	NaN

```
-cross_val_score(
    m, X_train, y_train, cv=10, scoring="neg_root_mean_squared_error"
).mean()
    for m in models
]
# Los on test data, for model trained on training data:
res["test_loss"] = [loss(X_train, y_train, X_test, y_test, m) for m in models]
res["test_accuracy"] = [accuracy(X_train, y_train, X_test, y_test, m) for m in models]

perplexity = lambda p: np.exp(-np.mean(np.log(y_test*p + (1 - y_test) * (1 - p))))
#temporary solution since sum is weird with perplexity, KEEP SVM LAST!!
list = [perplexity(m.predict_proba(X_test)[:,1]) for m in models[0:-1]]
res["test_perplexity"] = np.append(list, np.nan)
```

Define and compare models

We began the experimentation with logistic regression and different parameters.

```
results_class2 <- py$results_class2
rownames(results_class2) <- c('Dummy', 'Logistic1', 'Logistic2', 'Logistic3', 'Logistic4', 'Logistic5', 'Gaustresults_class4 <- py$results_class4
rownames(results_class4) <- c('Dummy', 'Logistic1', 'Logistic2', 'Logistic3', 'Logistic4', 'Logistic5', 'Gaustlibrary(kableExtra)
library(tidyverse)</pre>
```

Binary classification (class2)

```
knitr::kable(results_class2, row.names = TRUE, digits = 2)%>%kable_styling()%>%row_spec(9,bold=T,hline_
```

	train_loss	cv_loss	test_loss	test_accuracy	test_perplexity
Dummy	1.73	1.73	1.74	0.49	1.51
Logistic1	1.08	1.12	1.17	0.63	1.40
Logistic2	1.20	1.23	1.12	0.63	1.53
Logistic3	1.20	1.23	1.12	0.63	1.52
Logistic4	1.08	1.12	1.17	0.63	1.40
Logistic5	1.20	1.23	1.12	0.63	1.54
GausNB	1.31	1.37	1.30	0.54	3.12
QDA	0.54	1.36	1.25	0.63	Inf
\mathbf{RF}	0.00	1.03	1.09	0.72	1.38
KN	0.94	1.17	1.41	0.57	Inf
SVM	0.91	1.02	1.17	0.68	NaN

	train_loss	cv_loss	test_loss	test_accuracy	test_perplexity
gini	0	1.03	1.11	0.73	1.43
log_loss	0	1.04	1.09	0.74	1.43
entropy	0	1.01	1.04	0.72	1.39
gini n=50	0	0.97	1.15	0.72	1.45
gini n=250	0	1.01	1.00	0.72	1.40
useless	0	0.98	1.01	0.70	NaN

Multiclass classification (class4)

```
knitr::kable(results_class4, row.names = TRUE, digits = 2)%>%kable_styling()%>%row_spec(9,bold=T,hline_
```

As we can see, many models produce good results, but random forest had the highest accuracy by a small margin.

Classification with random forest (James et al.)

Random forest is an ensemble method consisting of bagging (bootstrap + aggregation) multiple decision trees and decorrelating them to explore the model space more thoroughly. The RandomForestClassifier implemented in Sklearn inherently supports multiclass classification, so therefore, we could straightforwardly use it for both of the classification problems.

Decision tree is a binary tree that splits the training data, minimizing the impurity at each split as measured by some criterion, and ends up in leaf nodes, where only a single class is present. Bootstrap creates $n_{estimators}$ new trees from randomly sampled rows of the training data set. At each split, decorrelation is achieved by sampling m predictors for the splits to use. Finally, the predictions made by the trees are aggregated through majority vote to output the predicted class.

With a sufficient number of trees, the bagging prevents overfitting, but may still get stuck in local optima. The addition of decorrelating avoids this downside, reducing test and OOB (out-of-bag) errors.

RandomForestClassifier with different parameters

```
results_class4 <- py$results_class4
rownames(results_class4) <- c('gini', 'log_loss', 'entropy', 'gini n=50', 'gini n=250', 'useless')
knitr::kable(results_class4, row.names = TRUE, digits = 2)%>%kable_styling()%>%row_spec(1,bold=T,hline_
```

For our parameters, we chose the Gini index as the impurity measure (criterion) and set the number of trees (n_estimators) at 100, as these produced the best accuracy. These just so happen to be the default parameters for the Sklearn implementation of RandomForest.

Final models

For both binary and multiclass classification, we use all the available data, including what was previously reserved for testing.

Binary classification (class2)

We first train the model and classify events and nonevents (class2)

```
npf_test_clean = npf_test.drop(['id', 'partlybad', 'date'], axis=1)
#DROPS STDS
npf_test_clean = npf_test_clean.filter(regex='mean|class4|class2')
X = npf_train_test.drop(columns=['class2', 'class4'])
y = npf_train_test['class2']
rfc = RandomForestClassifier(criterion='gini')
model = rfc.fit(X, y)
predict_x = npf_test_clean.drop(columns='class4')
probas = pd.DataFrame(predict_x.copy())
def get_predict_proba(row, model):
  probas = model.predict_proba(row.values.reshape(1,-1))
  nonevent_p = probas[0][0]
  event_p = 1-nonevent_p
  return event_p
probas['proba'] = probas.apply(lambda row: get_predict_proba(row, model), axis=1)
predicts = pd.DataFrame(model.predict(predict_x))
final = predicts.merge(probas['proba'].to_frame(), left_index=True, right_index=True)
final[0].replace([0, 1],["nonevent", "event"], inplace=True)
```

Multiclass classification (class4)

Our multiclass classifier utilizes the above binary classification, relying on the predictions it has made. It is trained using only the rows that were classified as events while ignoring the nonevents. This means that only the results which have already been classified as events are reclassified as different types of events.

```
npf_test_clean = npf_test.drop(['id', 'partlybad', 'date'], axis=1)
```

```
# DROPS STDS
npf_test_clean = npf_test_clean.filter(regex='mean|class4|class2')
# SELECT ROWS WHERE BINARY CLASSIFIER PREDICTED EVENTS AS TRAINING DATA
npf_train_events = npf_train_test[npf_train_test['class2']==1]
X = npf_train_events.drop(columns=['class2', 'class4'])
y = npf train events['class4']
rfc = RandomForestClassifier(criterion='gini')
model = rfc.fit(X, y)
predict_x = npf_test_clean.loc[final[final[0]=='event'].index].drop(columns='class4')
predicts = pd.DataFrame(model.predict(predict_x))
predicts[0].replace([1, 2, 3],["Ia", "Ib", "II"], inplace=True)
for index, row in final.iterrows():
  if row[0] == 'event':
   final.at[index, 0] = predicts.iloc[i,0]
    i += 1
# Save answers.csv
row0 = pd.DataFrame({0: 0.9, 'proba':''}, index =[0])
row1 = pd.DataFrame({0: 'class4', 'proba':'p'}, index =[0])
merged = pd.concat([row1, final])
merged = pd.concat([row0, merged])
merged.to_csv('answers.csv', index=False, header=False)
```

Conclusion

Why the good accuracy?

(For the challenge set: binary accuracy $\approx 88\%$ and multiclass accuracy $\approx 71\%$)

Although linear regression did perform well, decision trees may perform better, when the relationship between the features and the response is non-linear and complex (James et al.). Random forest substantially mitigates the downsides of decision trees as well. Therefore, it seems that the relationship between the features and the response was non-linear and complex enough to slightly favor random forest over "classical approaches".

Random forest includes randomization in the sampling of both the observations and the features, which makes us think we got lucky with the random state.

Why infinite perplexity?

Some points in the test set probably got assigned 0% probability (either outliers or then the model is not general enough?)

What could we have done differently?

- More EDA (e.g., seaborn pairwise) to further inform feature and model selection
- We would have pursued PCA further if we had more time on our hands, as some tests suggested that it could have improved test accuracy
- Set random_state for the RF model as well to make the results reproducible
- Use a systematic process to try out different random states for both the data split and the models themselves to see the resulting variance in results
- After the model was chosen, we only compared parameters for class4, while we could have also done it for class2

References

James, Witten, Hastie, and Tibshirani, 2021. An Introduction to Statistical Learning with applications in R, 2nd edition. Springer.

https://scikit-learn.org/stable/modules/generated/sklearn.ensemble. Random Forest Classifier. html

 $https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LogisticRegression.html\\$

https://scikit-learn.org/stable/modules/multiclass.html

https://www3.nd.edu/~dchiang/teaching/nlp/2016/notes/chapter5v5.pdf (inf perplexity)