

---

# Open Domain Question Answering System

---



**Hoang Nghia Tuyen**

Supervisor: **Asst. Prof. Pun Chi Seng**

Co-supervisor: **Assoc. Prof. Joty Shafiq Rayhan**

School of Physical & Mathematical Sciences

A thesis submitted to the Nanyang Technological University  
submitted as part of the honours requirements for the degree of  
Bachelor of Science in Mathematical Sciences

**2022**

# Acknowledgements

I wish to express my greatest gratitude to my advisor.

# Abstract

My abstracts

# Contents

Acknowledgements	i
Abstract	ii
List of Figures	iv
List of Tables	v
Symbols and Acronyms	vi
<b>1 Introduction</b>	<b>1</b>
1.1 Some useful hints . . . . .	1
1.2 Major Contributions . . . . .	1
1.3 Outline of the Thesis . . . . .	2
<b>2 Literature Review</b>	<b>3</b>
2.1 Part 1 . . . . .	3
2.2 Part 2 . . . . .	3
<b>3 Chapter3 Name</b>	<b>5</b>
3.1 Section1 . . . . .	5
<b>4 Chapter4 Name</b>	<b>6</b>
4.1 Section 1 . . . . .	6
4.2 Section 2 . . . . .	7
<b>5 Chapter5 Name</b>	<b>8</b>
5.1 Section 1 . . . . .	8
5.2 Section 2 . . . . .	9
<b>A Proofs for Part I or Chapter 3</b>	<b>10</b>
A.1 Proof of Lemma . . . . .	10
A.2 Proof of another Lemma . . . . .	10

# List of Figures

1.1	An illustration. . . . .	2
3.1	Another illustration. . . . .	5

# List of Tables

3.1	My Table. . . . .	5
-----	-------------------	---

# Symbols and Acronyms

## Symbols

$\mathcal{R}^n$	the $n$ -dimensional Euclidean space
$\mathcal{H}$	the Euclidean space
$\ \cdot\ $	the 2-norm of a vector or matrix in Euclidean space
$\ \cdot\ _G$	the induced norm of a vector in G-space
$\ \cdot\ _E$	the induced norm of a vector or matrix in probabilistic space
$\odot$	the Hadamard (component-wise) product
$\otimes$	the Kronecker product
$\langle \cdot, \cdot \rangle$	the inner product of two vectors
$\circ$	the composition of functions
$\nabla f$	the gradient vector
$\mathcal{C}^k$	the function with continuous partial derivatives up to $k$ orders
$x_{i,k}$	the $i$ -th component of a vector $x$ at time $k$
$\bar{x}$	the vector with the average of all components of $x$ as each element
$\mathbf{1}$	all-ones column vector with proper dimension
$\mathcal{C}$	the average space, i.e., $\text{span}\{\mathbf{1}\}$
$\mathcal{C}^\perp$	the disagreement space, i.e., $\text{span}^\perp\{\mathbf{1}\}$
$\Pi_\parallel$	the projection matrix to the average space $\mathcal{C}$
$\Pi_\perp$	the projection matrix to the disagreement space $\mathcal{C}^\perp$
$O(\cdot)$	order of magnitude or ergodic convergence rate (running average)
$o(\cdot)$	non-ergodic convergence rate
$\mathcal{N}_i$	the index set of the neighbors of agent $i$

## Acronyms

DOP	Distributed Optimization Problem
EDOP	Equivalent Distributed Optimization Problem
SDOP	Stochastic Distributed Optimization Problem
OEP	Optimal Exchange Problem
OCF	Optimal Consensus Problem
DOCP	Dynamic Optimal Consensus Problem
AugDGM	Augmented Distributed Gradient Methods
AsynDGM	Asynchronous Distributed Gradient Methods
D-ESC	Distributed Extremum Seeking Control
D-SPA	Distributed Simultaneous Perturbation Approach
D-FBBS	Distributed Forward-Backward Bregman Splitting
ADMM	Alternating Direction Method of Multipliers
DSM	Distributed (Sub)gradient Method
GAS	Globally Asymptotically Stable
UGAS	Uniformly Globally Asymptotically Stable
SPAS	Semi-globally Practically Asymptotically Stable
USPAS	Uniformly Semi-globally Practically Asymptotically Stable
HoS	Heterogeneity of Stepsize
FPR	Fixed Point Residual
OBE	Objective Error
i.i.d.	independent and identically distributed
<i>a.s.</i>	almost sure convergence of a random sequence



# Chapter 1

## Introduction

### 1.1 Some useful hints

My figure citation: Figure [1.1](#). (command: `fref`)

My section citation: Section [1.2](#). (command: `sref`)

My Chapter citation: Chapter [1](#). (command: `cref`)

My Paper citation: [\[1\]](#). (notice back reference to page from bibliography)

My equation citation: [\(1.1\)](#). (command: `eqref`), or cite equation by tag: [\(DOP\)](#).

$$F(\theta) = \sum_{i=1}^m f_i(\theta) \tag{DOP}$$

$$F(\theta) = \sum_{i=1}^m f_i(\theta) \tag{1.1}$$

### 1.2 Major Contributions

Our main contributions can be stated as follows:

- *First part*: My first contributions, several lines



FIGURE 1.1: An illustration.

- *Second*: Second contributions, several lines
- *Third name*: Third contributions, several lines

## 1.3 Outline of the Thesis

Chapter 1 introduces ...

Chapter 2 reviews ...

More chapters ....

....

# Chapter 2

## Literature Review

### 2.1 Part 1

When you cite a paper [1], the back reference from bibgraph will apper as page number.

You can also cite paper with author name using the command ‘citet’: such as: Bauschke and Combettes [1].

### 2.2 Part 2

cite another paper [2].

**Lemma 2.1** (My lemma). *A great lemma.*

$$c^2 = a^2 + b^2 \tag{2.1}$$

**Theorem 2.2** (My theorem). *A great theorem.*

$$c^2 = a^2 + b^2 \tag{2.2}$$

*Proof.* The proof is intuitive. □

**Corollary 2.3** (My corollary). *A great corollary.*

$$c^2 = a^2 + b^2 \tag{2.3}$$

**Proposition 2.1** (My proposition). *A great proposition.*

$$c^2 = a^2 + b^2 \tag{2.4}$$

**Example 2.1** (My example). A great example.

$$c^2 = a^2 + b^2 \tag{2.5}$$

**Definition 2.1** (My definition). A great definition.

$$c^2 = a^2 + b^2 \tag{2.6}$$

**Assumption 2.1** (My assumption). A great assumption.

$$c^2 = a^2 + b^2 \tag{2.7}$$

*Remark 2.1* (My remark). A great remark.

$$c^2 = a^2 + b^2 \tag{2.8}$$

# Chapter 3

## Chapter3 Name

### 3.1 Section1

See Figure [3.1](#)



FIGURE 3.1: Another illustration.

Let’s cite out first table: Table [3.1](#).

Table	Group 1		Group 2	
	Col 1	Col 2	Col 1	Col 2
Row 1	14.37	<b>5.76</b>	2.65	<b>2.84</b>
Row 2	5.43	<b>7.36</b>	2.22	<b>2.49</b>
Row 3	5.54	<b>5.68</b>	<b>4.42</b>	2.92

TABLE 3.1: My Table.

# Chapter 4

## Chapter4 Name

Quisque facilisis auctor sapien. Pellentesque gravida hendrerit lectus. Mauris rutrum sodales sapien. Fusce hendrerit sem vel lorem. Integer pellentesque massa vel augue. Integer elit tortor, feugiat quis, sagittis et, ornare non, lacus. Vestibulum posuere pellentesque eros. Quisque venenatis ipsum dictum nulla. Aliquam quis quam non metus eleifend interdum. Nam eget sapien ac mauris malesuada adipiscing. Etiam eleifend neque sed quam. Nulla facilisi. Proin a ligula. Sed id dui eu nibh egestas tincidunt. Suspendisse arcu.

### 4.1 Section 1

Quisque facilisis auctor sapien. Pellentesque gravida hendrerit lectus. Mauris rutrum sodales sapien. Fusce hendrerit sem vel lorem. Integer pellentesque massa vel augue. Integer elit tortor, feugiat quis, sagittis et, ornare non, lacus. Vestibulum posuere pellentesque eros. Quisque venenatis ipsum dictum nulla. Aliquam quis quam non metus eleifend interdum. Nam eget sapien ac mauris malesuada adipiscing. Etiam eleifend neque sed quam. Nulla facilisi. Proin a ligula. Sed id dui eu nibh egestas tincidunt. Suspendisse arcu.

## 4.2 Section 2

Quisque facilisis auctor sapien. Pellentesque gravida hendrerit lectus. Mauris rutrum sodales sapien. Fusce hendrerit sem vel lorem. Integer pellentesque massa vel augue. Integer elit tortor, feugiat quis, sagittis et, ornare non, lacus. Vestibulum posuere pellentesque eros. Quisque venenatis ipsum dictum nulla. Aliquam quis quam non metus eleifend interdum. Nam eget sapien ac mauris malesuada adipiscing. Etiam eleifend neque sed quam. Nulla facilisi. Proin a ligula. Sed id dui eu nibh egestas tincidunt. Suspendisse arcu.

# Chapter 5

## Chapter5 Name

Quisque facilisis auctor sapien. Pellentesque gravida hendrerit lectus. Mauris rutrum sodales sapien. Fusce hendrerit sem vel lorem. Integer pellentesque massa vel augue. Integer elit tortor, feugiat quis, sagittis et, ornare non, lacus. Vestibulum posuere pellentesque eros. Quisque venenatis ipsum dictum nulla. Aliquam quis quam non metus eleifend interdum. Nam eget sapien ac mauris malesuada adipiscing. Etiam eleifend neque sed quam. Nulla facilisi. Proin a ligula. Sed id dui eu nibh egestas tincidunt. Suspendisse arcu.

### 5.1 Section 1

Quisque facilisis auctor sapien. Pellentesque gravida hendrerit lectus. Mauris rutrum sodales sapien. Fusce hendrerit sem vel lorem. Integer pellentesque massa vel augue. Integer elit tortor, feugiat quis, sagittis et, ornare non, lacus. Vestibulum posuere pellentesque eros. Quisque venenatis ipsum dictum nulla. Aliquam quis quam non metus eleifend interdum. Nam eget sapien ac mauris malesuada adipiscing. Etiam eleifend neque sed quam. Nulla facilisi. Proin a ligula. Sed id dui eu nibh egestas tincidunt. Suspendisse arcu.



## 5.2 Section 2

Quisque facilisis auctor sapien. Pellentesque gravida hendrerit lectus. Mauris rutrum sodales sapien. Fusce hendrerit sem vel lorem. Integer pellentesque massa vel augue. Integer elit tortor, feugiat quis, sagittis et, ornare non, lacus. Vestibulum posuere pellentesque eros. Quisque venenatis ipsum dictum nulla. Aliquam quis quam non metus eleifend interdum. Nam eget sapien ac mauris malesuada adipiscing. Etiam eleifend neque sed quam. Nulla facilisi. Proin a ligula. Sed id dui eu nibh egestas tincidunt. Suspendisse arcu.

# Appendix A

## Proofs for Part I or Chapter 3

### A.1 Proof of Lemma

$$\psi^{av}(\theta) = \frac{1}{T} \int_0^T [\psi(\theta + \mu(\tau)) + C] \otimes \frac{\mu(\tau)}{a} d\tau$$

### A.2 Proof of another Lemma

$$\begin{aligned} \gamma_1(\|x\|) &\leq W(t, x) \leq \gamma_2(\|x\|) \\ \frac{\partial W}{\partial t} + \frac{\partial W}{\partial x} \phi(t, x, 0) &\leq -\gamma_3(\|x\|) \end{aligned} \tag{A.1}$$

# Bibliography

- [1] Heinz H Bauschke and Patrick L Combettes. *Convex analysis and monotone operator theory in Hilbert spaces*. Springer Science & Business Media, 2011. [1](#), [3](#)
- [2] J. B. Rawlings and B. T. Stewart. Coordinating multiple optimization-based controllers: New opportunities and challenges. *Journal of Process Control*, 18:839–845, 2008. [3](#)