

## Team Note of HYEА Team

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## 1 Have you...

## 1.1 tried...

- **Reading the problem once more?**
- doubting "obvious" things?
- writing obvious things?
- radical greedy approach?
- thinking in reverse direction?
- a greedy algorithm?
- network flow when your greedy algorithms stuck?
- a dynamic programming?
- checking the range of answer?
- random algorithm?
- graph modeling using states?
- inverting state only on odd indexes?
- square root decomposition?
- calculating error bound on a real number usage?

## 1.2 checked...

- **you have read the statement correctly?**
- typo copying the team note?
- initialization on multiple test case problem?
- additional information from the problem?
- undefined behavior?
- overflow?
- function without return value?
- real number error?
- implicit conversion?
- comparison between signed and unsigned integer?

## 2 Data Structure

Should be **tested**.

## 2.1 Bottom-up lazy segment tree

**Usage:** Give monoid  $(S, \cdot)$  and morphism  $F : S \rightarrow S$  with  $f(x \cdot y) = f(x) \cdot f(y)$

- $S$ : type of  $S$ ,  $S \text{ op}(S \ a, S \ b): a \cdot b$ ,  $S \ e():$  identity element  $e$
- $F$ : type of  $F$ ,  $S \text{ mapping}(F \ f, S \ s): f(s)$ ,  $F \text{ composition}(F \ f, F \ g): f \circ g$ ,  $F \text{ id}(): id(x) = x$
- $\text{LazySeg}(\text{int } n): a_0 = \dots = a_{N-1} = e$ ,  $\text{LazySeg}(\text{vector}<S> \ v):$  Init array with  $v$
- $\text{void set}(\text{int } p, S \ x): a_p = x$ ,  $\text{void apply}(\text{int } l, \text{int } r, F \ f): a_i = f(a_i)$  for  $i = l, \dots, r-1$ .
- $S \text{ prod}(\text{int } l, \text{int } r): a_l \cdot a_{l+1} \cdot \dots \cdot a_{r-1}$ ,  $S \text{ all\_prod}(): a_0 \cdot \dots \cdot a_{N-1}$

**Time Complexity:**  $\mathcal{O}(n)$  for constructor,  $\mathcal{O}(\log n)$  for query

```

template <class S, S (*op)(S, S), S (*e)(),
class F, S (*mapping)(F, S), F (*composition)(F, F), F
(*id)()>
class LazySeg {
    int N, log;
    vector<S> d;
    vector<F> lz;

    void pull(int k) { d[k] = op(d[2 * k], d[2 * k + 1]); }
    void put(int k, F f) {
        d[k] = mapping(f, d[k]);
        if (k < N) lz[k] = composition(f, lz[k]);
    }
    void push(int k) {
        put(2 * k, lz[k]);
        put(2 * k + 1, lz[k]);
        lz[k] = id();
    }
public:
    LazySeg() : LazySeg(0) {}
    explicit LazySeg(int n) : LazySeg(vector<S>(n, e())) {}
    explicit LazySeg(const vector<S> &v) {
        log = 31 - __builtin_clz(v.size() | 1);
        N = 1 << log;
        d = vector<S>(2 * N, e());
        lz = vector<F>(N, id());
        for (int i = 0; i < (int)v.size(); i++) d[N + i] = v[i];
        for (int i = N - 1; i >= 1; i--) pull(i);
    }
    void set(int p, S x) {
        p += N;
        for (int i = log; i >= 1; i--) push(p >> i);
        d[p] = x;
        for (int i = 1; i <= log; i++) pull(p >> i);
    }
    S prod(int l, int r) {
        if (l == r) return e();
        l += N, r += N;
        for (int i = log; i >= 1; i--) {

```

```

    if (((l >> i) << i) != 1) push(l >> i);
    if (((r >> i) << i) != r) push((r - 1) >> i);
}
S sm1 = e(), smr = e();
while (l < r) {
    if (l & 1) sm1 = op(sm1, d[l++]);
    if (r & 1) smr = op(d[--r], smr);
    l >>= 1, r >>= 1;
}
return op(sm1, smr);
}
S all_prod() { return d[1]; }
void apply(int l, int r, F f) {
    if (l == r) return;
    l += N, r += N;
    for (int i = log; i >= 1; i--) {
        if (((l >> i) << i) != 1) push(l >> i);
        if (((r >> i) << i) != r) push((r - 1) >> i);
    }
    int l2 = l, r2 = r;
    while (l < r) {
        if (l & 1) put(l++, f);
        if (r & 1) put(--r, f);
        l >>= 1, r >>= 1;
    }
    l = l2, r = r2;
    for (int i = 1; i <= log; i++) {
        if (((l >> i) << i) != 1) pull(l >> i);
        if (((r >> i) << i) != r) pull((r - 1) >> i);
    }
}
};
Should be tested.

```

## 2.2 Randomized Meldable Heap

**Usage:** Min-heap `H` is declared as `Heap<T> H`. You can use `push`, `size`, `empty`, `top`, `pop` as `std::priority_queue`. Use `H.meld(G)` to meld contents from `G` to `H`.

**Time Complexity:**  $\mathcal{O}(\log n)$

```

mt19937 gen(0x94949);
template<typename T>
struct Node {
    Node *l, *r;
    T v;
    Node(T x): l(0), r(0), v(x){}
};
template<typename T>
Node<T>* Meld(Node<T>* A, Node<T>* B) {
    if(!A) return B; if(!B) return A;
    if(B->v < A->v) swap(A, B);
    if(gen()&1) A->l = Meld(A->l, B);
    else A->r = Meld(A->r, B);
    return A;
}
template<typename T>
struct Heap {
    Node<T> *r; int s;
    Heap(): r(0), s(0){}
    void push(T x) {
        r = Meld(new Node<T>(x), r);
        ++s;
    }
    int size(){ return s; }
    bool empty(){ return s == 0; }
    T top(){ return r->v; }
    void pop() {
        Node<T>* p = r;
        r = Meld(r->l, r->r);
        delete p;
        --s;
    }
    void Meld(Heap x) {
        s += x->s;
        r = Meld(r, x->r);
    }
};

```

## 2.3 Convex Hull Trick

Should be **added**.

## 2.4 Li-Chao Tree

Should be **added**.

## 2.5 Palindromic Tree

Should be **added**.

## 2.6 Link-Cut Tree

Should be **added**.

## 2.7 DSU rollback + Queue undo trick

## 3 Math

Should be **tested**.

### 3.1 Modint + Barrett Reduction

Should be **added**.

### 3.2 Miller Rabin Primality Test + Pollad Rho Factorization

**Usage:** `is_prime` For primality test, `factor` for factorization ( $n < 2^{62}$ )

**Time Complexity:**  $\mathcal{O}(B \log n)$  ( $B \sim 7$ ),  $\mathcal{O}(n^{1/4})$

```

long mul(long a, long b, long m) {
    return (__int128)a * b % m;
}
long ipow(long a, long b, long m) {
    long r = 1, y = a % m;
    while (b) {
        if (b & 1) r = mul(r, y, m);
        y = mul(y, y, m);
        b >>= 1;
    }
    return r;
}
bool is_prime(long n) {
    if (n <= 1) return false;
    for (int a : {2, 3, 5, 13, 19, 73, 193, 407521, 299210837})
    {
        if (n == a) return true;
        if (n % a == 0) return false;
    }
    long d = n - 1;
    while (!(d & 1)) d >>= 1;
    for (int a : {2, 325, 9375, 28178, 450775, 9780504, 1795265022}) {
        long t = d, y = ipow(a, t, n);
        while (t != n - 1 && y != 1 && y != n - 1) y = mul(y, y, n), t <<= 1;
        if (y != n - 1 && !(t & 1)) return false;
    }
    return true;
}
long pollard(long n) {
    auto f = [n](long x) { return mul(x, x, n) + 1; };
    long x = 0, y = 0, t = 0, prd = 2, i = 1, q;
    while (t++ % 40 || gcd(prd, n) == 1) {
        if (x == y) x = ++i, y = f(x);
        if ((q = mul(prd, max(x, y) - min(x, y), n))) prd = q;
        x = f(x), y = f(f(y));
    }
    return gcd(prd, n);
}
vector<long> factor(long n)
{
    if (n == 1) return {};
    if (is_prime(n)) return {n};
    long x = pollard(n);
    auto l = factor(x), r = factor(n / x);
    l.insert(l.end(), r.begin(), r.end());
    return l;
}

```

### 3.3 Linear Determinant

Usage: char\_poly for  $\det(xI - M)$ , det\_linear for  $\det(Ax + B)$

Time Complexity:  $\mathcal{O}(n^3)$

```
template <typename T>
vector<T> char_poly(vector<vector<T>> M) {
    int N = M.size();
    for (int i = 0; i < N - 2; i++) {
        int p = -1;
        for (int j = i + 1; j < N; j++)
            if (M[j][i] != T(0)) {
                p = j; break;
            }
        if (p == -1) continue;
        M[i + 1].swap(M[p]);
        for (int j = 0; j < N; j++) swap(M[j][i + 1], M[j][p]);

        T r = T(1) / M[i + 1][i];
        for (int j = i + 2; j < N; j++) {
            T c = M[j][i] * r;
            for (int k = 0; k < N; k++) M[j][k] -= M[i + 1][k] * c;
            for (int k = 0; k < N; k++) M[k][i + 1] += M[k][j] * c;
        }
    }
    vector<vector<T>> P = {{T(1)}};
    for (int i = 0; i < N; i++) {
        vector<T> f(i + 2, 0);
        for (int j = 0; j <= i; j++) f[j + 1] += P[i][j];
        for (int j = 0; j <= i; j++) f[j] -= P[i][j] * M[i][i];

        T b = 1;
        for (int j = i - 1; j >= 0; j--) {
            b *= M[j + 1][j];
            T h = -M[j][i] * b;
            for (int k = 0; k <= j; k++) f[k] += h * P[j][k];
        }
        P.push_back(f);
    }
    return P.back();
}

template <typename T>
vector<T> det_linear(vector<vector<T>> A, vector<vector<T>> B)
{
    int N = A.size(), nu = 0; T det = 1;
    for (int i = 0; i < N; i++) {
        int p = -1;
        for (int j = i; j < N; j++)
            if (A[j][i] != T(0)) {
                p = j; break;
            }
        if (p == -1) {
            if (++nu > N) return vector<T>(N + 1, 0);
            for (int j = 0; j < i; j++) {
                for (int k = 0; k < N; k++)
                    B[k][i] -= B[k][j] * A[j][i];
                A[j][i] = 0;
            }
            for (int j = 0; j < N; j++) swap(A[j][i], B[j][i]);
            --i; continue;
        }
        if (p != i) A[i].swap(A[p]), B[i].swap(B[p]), det = -det;
        det *= A[i][i];

        T c = T(1) / A[i][i];
        for (int j = 0; j < N; j++) A[i][j] *= c, B[i][j] *= c;
        for (int j = 0; j < N; j++) if (j != i) {
            T c = A[j][i];
            for (int k = 0; k < N; k++)
                A[j][k] -= A[i][k] * c, B[j][k] -= B[i][k] * c;
        }
    }
    for (auto &y : B) for (T &x : y) x = -x;
    auto f = char_poly(B);
    for (T &x : f) x *= det;
    f.erase(f.begin(), f.begin() + nu);
    f.resize(N + 1);
    return f;
}
```

### 3.4 FFT, NTT, or, xor, and convolution

Should be **added**.

### 3.5 Polynomial Library

Should be **added**.

### 3.6 Simplex Algorithm

Should be **added**.

### 3.7 Berlekamp-Massey Algorithm / Kitamasa

Should be **added**.

### 3.8 Xudyh Sieve

Should be **added**.

## 4 String Algorithm

Should be **tested**.

### 4.1 Suffix Array with LCP

Usage: s: string, upper: max s; e. g. 256 for ascii string. sa: pass suffix array together

Time Complexity:  $\mathcal{O}(N + \text{upper})$  for SA,  $\mathcal{O}(N)$  for lcp\_array

```
vector<int> lcp(const vector<int>& s, int upper) {
    int n=s.size();
    if (n == 0) return {};
    if (n == 1) return {0};
    if (n == 2) {
        if (s[0] < s[1]) return {0, 1};
        else return {1, 0};
    }
    vector<int> sa(n), sum_l(upper+1), sum_s(upper+1);
    vector<bool> ls(n);
    for (int i=n-2; i>=0; i--)
        ls[i]=(s[i] == s[i+1]) ? ls[i+1] : (s[i] < s[i+1]);
    for (int i = 0; i < n; i++)
        if (!ls[i]) sum_s[s[i]]++;
        else sum_l[s[i]+1]++;
    for (int i=0; i<=upper; i++) {
        sum_s[i] += sum_l[i];
        if (i < upper) sum_l[i+1] += sum_s[i];
    }
    auto induce=[&](const vector<int>& lms) {
        fill(sa.begin(), sa.end(), -1);
        vector<int> buf(upper+1);
        copy(sum_s.begin(), sum_s.end(), buf.begin());
        for (auto d : lms) {
            if (d == n) continue;
            sa[buf[s[d]]++] = d;
        }
        copy(sum_l.begin(), sum_l.end(), buf.begin());
        sa[buf[s[n-1]]++] = n-1;
        for (int i=0; i < n; i++) {
            int v=sa[i];
            if (v>=1 && !ls[v-1]) sa[buf[s[v-1]]++] = v-1;
        }
        copy(sum_l.begin(), sum_l.end(), buf.begin());
        for (int i=n-1; i>=0; i--) {
            int v=sa[i];
            if (v>=1 && ls[v-1]) sa[--buf[s[v-1]+1]] = v-1;
        }
    };
    vector<int> lms_map(n+1, -1), lms;
    int m=0;
    for (int i=1; i < n; i++) if (!ls[i-1] && ls[i]) {
        lms_map[i]=m++;
        lms.push_back(i);
    }
    induce(lms);
    if (m) {
        vector<int> sorted_lms, rec_s(m);
        for (int v : sa) if (lms_map[v] != -1)
            sorted_lms.push_back(v);
        int rec_upper=0;
    }
```

```

rec_s[lms_map[sorted_lms[0]]]=0;
for (int i=1; i < m; i++) {
    int l=sorted_lms[i-1], r=sorted_lms[i];
    int end_l = (lms_map[l]+1 < m) ? lms[lms_map[l]+1] : n;
    int end_r = (lms_map[r]+1 < m) ? lms[lms_map[r]+1] : n;
    bool same=true;
    if (end_l-1 != end_r-r) same=false;
    else {
        while (l < end_l) {
            if (s[l] != s[r]) break;
            l++, r++;
        }
        if (l == n || s[l] != s[r]) same=false;
    }
    if (!same) rec_upper++;
    rec_s[lms_map[sorted_lms[i]]]=rec_upper;
}
auto rec_sa = SA(rec_s, rec_upper);
for (int i=0; i < m; i++) sorted_lms[i] = lms[rec_sa[i]];
induce(sorted_lms);
}
return sa;
}

vector<int> lcp_array(const vector<int>& s, const vector<int>& sa) {
    int n=int(s.size());
    assert(n>=1);
    vector<int> rnk(n), lcp(n-1);
    for (int i=0; i < n; i++) rnk[sa[i]]=i;
    int h=0;
    for (int i=0; i < n; i++) {
        if (h > 0) h--;
        if (rnk[i] == 0) continue;
        int j=sa[rnk[i]-1];
        for (; j+h < n && i+h < n; h++)
            if (s[j+h] != s[i+h]) break;
        lcp[rnk[i]-1]=h;
    }
    return lcp;
}

```

## 4.2 Z-algorithm

**Usage:**  $i$ -th element is common prefix of  $S$  and  $S_{i...|S|}$

**Time Complexity:**  $O(N)$

```

vector<int> Z(const vector<int>& S) {
    int N = S.size();
    vector<int> Z(N);
    int L = 0, R = 0;
    for(int i = 1; i < N; i++) {
        if(i+Z[i-L] < R) Z[i] = Z[i-L];
        else {
            L = i, R = max(R, i);
            while(R < N && S[R] == S[R-i]) ++R;
            Z[i] = R-i;
        }
    }
    return Z;
}

```

## 4.3 Manacher

**Usage:** Returns palindromic radius of  $S$ . To calculate even length palindromes, insert \$ between each character.

**Time Complexity:**  $O(N)$

```

vector<int> M(const vector<int>& S) {
    int N = S.size();
    vector<int> M(N);
    int L = 0, R = 0;
    for(int i = 0; i < N; i++) {
        if(i < R && i+M[2*L-i] < R) M[i] = M[2*L-i];
        else {
            L = i, R = max(R, i);
            while(R < N && 2*i-R >= 0 && S[R] == S[2*i-R]) ++R;
            M[i] = R-i;
        }
    }
    return M;
}

```

Should be **revised**.  
Support Incremental Aho-corasick

## 4.4 Aho-Corasick

**Usage:** MAXC: size of alphabet, F, FG: failure (parent), failure graph, ftrans: state transition function.

```

template <int MAXC = 26> struct AhoCorasick {
    vector<array<int, MAXC>> C;
    vector<int> F;
    vector<vector<int>> FG;
    vector<bool> E;

    int node() {
        int r = C.size();
        E.push_back(0);
        F.push_back(-1);
        C.emplace_back();
        fill(C.back().begin(), C.back().end(), -1);
        return r;
    }

    int ctrans(int n, int c) {
        if (C[n][c] == -1) C[n][c] = node();
        return C[n][c];
    }

    int ftrans(int n, int c) const {
        while (n && C[n][c] == -1) n = F[n];
        return C[n][c] != -1 ? C[n][c] : 0;
    }

    AhoCorasick(vector<vector<int>> P) {
        node();
        for (int i = 0; i < (int)P.size(); i++) {
            int n = 0;
            for (int c : P[i]) n = ctrans(n, c);
            E[n] = 1;
        }
        queue<int> Q;
        F[0] = 0;
        for (int c : C[0]) if (c != -1) Q.push(c), F[c] = 0;
        while (!Q.empty()) {
            int n = Q.front(); Q.pop();
            for (int c = 0; c < MAXC; ++c) if (C[n][c] != -1) {
                int f = F[n];
                while (f && C[f][c] == -1) f = F[f];
                F[C[n][c]] = C[f][c] != -1 ? C[f][c] : 0;
                Q.emplace(C[n][c]);
            }
        }
        FG.resize(F.size());
        for (int i = 1; i < (int)F.size(); i++) {
            FG[F[i]].push_back(i);
            if (E[i]) Q.push(i);
        }
        while (!Q.empty()) {
            int n = Q.front();
            Q.pop();
            for (int f : FG[n]) E[f] = 1, Q.push(f);
        }
    }

    bool check(vector<int> V) {
        if (E[0]) return 1;
        int n = 0;
        for (int c : V) {
            n = ftrans(n, c);
            if (E[n]) return 1;
        }
        return 0;
    }
};

```

## 5 Graph

### 5.1 Dinic Algorithm

Should be **added**.

### 5.2 Fast MCMF with slope clculation

Should be **added**.

### 5.3 Global Min-cut

Should be **added**.

## 5.4 Gomory-Hu Tree

Should be **added**.

## 5.5 Perfect Elimination Ordering

Should be **added**.

## 5.6 General Matching

**Usage:** Use `init` to init, `addEdge` to add edges, `match` to get matching, `Match` to find maximum matching. Vertices have 1-based index.

**Time Complexity:**  $\mathcal{O}(VE)$

```
const int MAXN = 2020 + 1;
struct GM { // 1-based Vertex index
    int vis[MAXN], par[MAXN], orig[MAXN], match[MAXN],
    aux[MAXN], t, N;
    vector<int> conn[MAXN];
    queue<int> Q;
    void addEdge(int u, int v) {
        conn[u].push_back(v); conn[v].push_back(u);
    }
    void init(int n) {
        N = n; t = 0;
        for(int i=0; i<=n; ++i) {
            conn[i].clear();
            match[i] = aux[i] = par[i] = 0;
        }
    }
    void augment(int u, int v) {
        int pv = v, nv;
        do {
            pv = par[v]; nv = match[pv];
            match[v] = pv; match[pv] = v;
            v = nv;
        } while(u != pv);
    }
    int lca(int v, int w) {
        ++t;
        while(true) {
            if(v) {
                if(aux[v] == t) return v; aux[v] = t;
                v = orig[par[match[v]]];
            }
            swap(v, w);
        }
    }
    void blossom(int v, int w, int a) {
        while(orig[v] != a) {
            par[v] = w; w = match[v];
            if(vis[w] == 1) Q.push(w), vis[w] = 0;
            orig[v] = orig[w] = a;
            v = par[w];
        }
    }
    bool bfs(int u) {
        fill(vis+1, vis+1+N, -1); iota(orig+1, orig+N+1, 1);
        Q = queue<int> (); Q.push(u); vis[u] = 0;
        while(!Q.empty()) {
            int v = Q.front(); Q.pop();
            for(int x: conn[v]) {
                if(vis[x] == -1) {
                    par[x] = v; vis[x] = 1;
                    if(!match[x]) return augment(u, x), true;
                    Q.push(match[x]); vis[match[x]] = 0;
                }
                else if(vis[x] == 0 && orig[v] != orig[x]) {
                    int a = lca(orig[v], orig[x]);
                    blossom(x, v, a); blossom(v, x, a);
                }
            }
        }
        return false;
    }
    int Match() {
        int ans = 0;
        //find random matching (not necessary, constant
        improvement)
        vector<int> V(N-1); iota(V.begin(), V.end(), 1);
        shuffle(V.begin(), V.end(), mt19937(0x949494));
```

```
for(auto x: V) if(!match[x]){
    for(auto y: conn[x]) if(!match[y]) {
        match[x] = y, match[y] = x;
        ++ans; break;
    }
}
for(int i=1; i<=N; ++i) if(!match[i] && bfs(i)) ++ans;
return ans;
};
```

## 5.7 Centroid Decomposition

**Usage:** Fill in the function work.

**Time Complexity:**  $\mathcal{O}(N \log N)$

```
int find_centroid(const vector<vector<int>> &G, const
vector<bool> &used, int v) {
    vector<tuple<int, int, int>> sz;
    function<void(int, int)> dfs = [&](int a, int p) {
        int S = 1, mx = 0;
        for (int x : G[a]) if (x != p && !used[x]) {
            dfs(x, a);
            int c = get<1>(sz.back());
            S += c, mx = max(mx, c);
        }
        sz.emplace_back(a, S, mx);
    };
    dfs(v, -1);
    int S = get<1>(sz.back());
    for (auto [i, s, mx] : sz) if (2 * max(S - s, mx) <= S)
        return i;
}
answer_type solve(const vector<vector<int>>& G) {
    vector<bool> used(size(G), 0);
    answer_type answer;
    auto work = [&](int c) {
        /* Do something on rooted tree c
        DFS with !used[x] (See above) */
    };
    queue<int> Q; Q.emplace(0);
    while (!Q.empty()){
        int x = Q.front();
        Q.pop();
        int c = find_centroid(G, used, x);
        work(c);
        used[c] = 1;
        for (int x : G[c]) if (!used[x]) Q.emplace(x);
    }
    return answer;
}
```

## 5.8 SCC

Should be **added**.

## 5.9 BCC, Cut vertex, Cut edge

Should be **added**.

## 6 Geometry

### 6.1 Smallest Enclosing Circle

**Usage:** Use `solve` with `vector<Point>`. It returns `Circle c`, `c.p` is center, `c.r` is radius.

**Time Complexity:**  $\mathcal{O}(n)$

```
double eps = 1e-9;
using Point = complex<double>;
struct Circle{ Point p; double r; };
double dist(Point p, Point q){ return abs(p-q); }
double area2(Point p, Point q){ return (conj(p)*q).imag();}
bool in(const Circle& c, Point p){ return dist(c.p, p) < c.r +
eps; }
Circle INVALID = Circle{Point(0, 0), -1};
Circle mCC(Point a, Point b, Point c){
    b -= a; c -= a;
    double d = 2*(conj(b)*c).imag(); if(abs(d)<eps) return
INVALID;
    Point ans = (c*norm(b) - b*norm(c)) * Point(0, -1) / d;
    return Circle{a + ans, abs(ans)};
```

```

}
Circle solve(vector<Point> p) {
    mt19937 gen(0x94949); shuffle(p.begin(), p.end(), gen);
    Circle c = INVALID;
    for(int i=0; i<p.size(); ++i) if(c.r<0 || !in(c, p[i])){
        c = Circle{p[i], 0};
        for(int j=0; j<=i; ++j) if(!in(c, p[j])){
            Circle ans{(p[i]+p[j])*0.5, dist(p[i], p[j])*0.5};
            if(c.r == 0) {c = ans; continue;}
            Circle l, r; l = r = INVALID;
            Point pq = p[j]-p[i];
            for(int k=0; k<=j; ++k) if(!in(ans, p[k])) {
                double a2 = area2(pq, p[k]-p[i]);
                Circle c = mCC(p[i], p[j], p[k]);
                if(c.r<0) continue;
                else if(a2 > 0 && (l.r<0 || area2(pq, c.p-p[i]) >
                    area2(pq, l.p-p[i]))) l = c;
                else if(a2 < 0 && (r.r<0 || area2(pq, c.p-p[i]) <
                    area2(pq, r.p-p[i]))) r = c;
            }
            if(l.r<0&&r.r<0) c = ans;
            else if(l.r<0) c = r;
            else if(r.r<0) c = l;
            else c = l.r<=r.r?l:r;
        }
    }
    return c;
}

```

## 6.2 Voronoi Diagram + Delaneuy Triagulation

Should be **added**.

## 7 Misc

Should be **revised**.

**Working in progress.**

### 7.1 (WIP) Magical Polynomial 3-SAT Algorithm

**Usage:** Use this to solve all problems!

**Time Complexity:**  $\mathcal{O}(n)$

### 7.2 Policy-based Data structure

Should be **added**.

### 7.3 Fast I/O

Should be **added**.