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VNU-HUS MAT1206E/3508: Introduction to AI

Logic Programming with PROLOG In-class Discussion

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Learn Prolog Now!

- <https://www.let.rug.nl/bos/lpn/index.php>
- by **Patrick Blackburn, Joost Bos, and Kristina Striegnitz.**



Basic of PROLOG

- PROLOG = Programming in Logic
- PROLOG is used in many projects, primarily in AI and computational linguistics.
- We will now give a short introduction to this language, present the most important concepts, show its strengths, and compare it with other programming languages and theorem provers.
- Those looking for a complete programming course are directed to textbooks such as [Bratko 2011]; [Clocksin and Mellish 2013] and the documentations at
<https://www.swi-PROLOG.org/> and
<http://www.gPROLOG.org/>.
- PROLOG systems interpret *Warren Abstract Machine code (WAM)*.
- PROLOG source code is compiled into so-called WAM code, which is then interpreted by the WAM.
- **Performance:** up to 10 million logical inferences per second (LIPS) on a 1 Gigahertz PC

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Basic of PROLOG

- PROLOG is a *declarative programming language*, i.e., the programmer declares *what* the program should accomplish without specifying *how* to achieve the result.
- PROLOG is based on *Horn clauses*.
- A PROLOG program consists of a *knowledge base* (*database*), which is simply a set of *facts* and *rules* about some problem domain.
 - A *knowledge base KB* of family relationships is coded as a PROLOG program

```
1 child(oscar, karen, frank).  
2 child(mary, karen, frank).  
3 child(eve, anne, oscar).  
4 child(henry, anne, oscar).  
5 child(isolde, anne, oscar).  
6 child(clyde, mary, oscar).
```

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Basic of PROLOG

- The execution of a PROLOG program is initiated by a *query*, which is answered by proving that the query logically follows from the facts and rules in the program.

- Example query

```
?- child(eve, anne, oscar).
```

- The query asks whether eve is a child of anne and oscar.
 - The expected answer is true (because it is a fact in the knowledge base *KB*).
 - How does PROLOG find the answer?
 - PROLOG tries to unify the query with the facts in the knowledge base *KB*.
 - There are six facts in the knowledge base.
 - Unification is attempted between the query and each of the complementary literals in the input data in order of occurrence. (In this example, the query unifies with the third fact.)
 - If one of the alternatives fails, this results in backtracking to the last branching point, and the next alternative is tested.

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Variables

- **Variables** begin with a Capital letter, or “_”
 - For example, X, Tom, _result
- “_” is a nameless (anonymous) variable. We use it when we need to use a variable, but we’re not interested in what PROLOG instantiates the variable to
 - A variable can have a value



Basic of PROLOG

Atoms

- An *atom* is a constant in terms; it just stands for itself.
- Atoms do not begin with a capital letter
 - For example, x, tom
- Atomic formulas are called *structures in PROLOG*.
- You can make an atom containing any characters at all by enclosing it in *single quotes*:
 - For example, 'C:\\My Documents\\examples.pl'
 - If you use double quotes, you will get a list of ASCII values, which is probably not what you want
 - ?- X = "Hello". results
X = [72, 101, 108, 108, 111].
- In a quoted atom, a single quote must be doubled or backslashed
 - For example, 'Can''t, or won't?'
- Backslashes in file names must also be doubled
 - For example, 'C:\\My Documents\\examples.pl'
 - Better yet, use forward slashes in paths; every OS, including Windows, understands this

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Basic of PROLOG

Predicates

- A ***predicate*** is a definition of a ***functor*** (predicate symbol), which is *collection of clauses with the same functor and arity (number of arguments)*.
 - `loves(john, mary).`
 - `loves(mary, bill).`
 - `loves(chuck, X) :- female(X), rich(X).`
- These clauses should stay together.
- The scope of a variable (such as X) is the single clause in which it occurs.
- A PROLOG program is just a collection of predicates.

Common Problems

- Capitalization is ***meaningful!***
- No space is allowed between a functor and its argument list:
 - `man(tom), not man (tom).`
- Double quotes indicate a list of ASCII character values, ***not*** a string
- Don't forget the period! (But if you do, you can put it on the next line.)

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Basic of PROLOG

Central Ideas of PROLOG

■ SUCCESS (true) / FAILURE (false)

- any computation can “succeed” or “fail”, and this is used as a ‘test’ mechanism.

■ UNIFICATION (2-WAY MATCHING)

- any two data items can be compared for similarity, and values can be bound to variables in order to allow a match to succeed.

■ SEARCHING

- the whole activity of the PROLOG system is to search through various options to find a combination that succeeds.

■ BACKTRACKING

- when the system fails during its search, it returns to previous choices to see if making a different choice would allow success.

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Let's try some examples from "Learn Prolog Now!"
(<https://www.let.rug.nl/bos/lpn/index.php>).



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Exercise 1

Given the following KB

```
1  woman(mia).  
2  woman(jody).  
3  woman(yolanda).  
4  playsAirGuitar(jody).  
5  party.
```

What is the expected answer to the following queries? Why?

```
?- woman(mia).
```

```
?- playsAirGuitar(mia).
```

```
?- playsAirGuitar(vincent).
```

```
?- tatooed(jody).
```

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Exercise 2

Given the following KB

```
1 happy(yolanda).  
2 listens2Music(mia).  
3 listens2Music(yolanda):- happy(yolanda).  
4 playsAirGuitar(mia):- listens2Music(mia).  
5 playsAirGuitar(yolanda):- listens2Music(yolanda).
```

What is the expected answer to the following queries? Why?

```
?- playsAirGuitar(mia).
```

```
?- playsAirGuitar(yolanda).
```

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Exercise 3

Given the following *KB*

```
1 happy(vincent).  
2 listens2Music(butch).  
3 playsAirGuitar(vincent) :- listens2Music(vincent),  
4     happy(vincent).  
5 playsAirGuitar(butch) :- happy(butch).  
6 playsAirGuitar(butch) :- listens2Music(butch).
```

What is the expected answer to the following queries? Why?

```
?- playsAirGuitar(vincent).
```

```
?- playsAirGuitar(butch).
```

Explain why we can replace the two rules in lines 6–7 by the single rule. (Note: Look up the meaning of the semicolon ; in PROLOG.)

```
playsAirGuitar(butch) :- happy(butch);  
listens2Music(butch).
```

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Exercise 4

Given the following KB

```
1  woman(mia).  
2  woman(jody).  
3  woman(yolanda).  
  
4  
5  loves(vincent,mia).  
6  loves(marsellus,mia).  
7  loves(pumpkin,honey_bunny).  
8  loves(honey_bunny,pumpkin).
```

What is the expected answer to the following queries? Why?

```
?- woman(X).
```

```
?- loves(marsellus,X), woman(X).
```

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Exercise 5

Given the following KB

```
1   loves(vincent,mia).  
2   loves(marsellus,mia).  
3   loves(pumpkin,honey_bunny).  
4   loves(honey_bunny,pumpkin).  
5  
6   jealous(X,Y) :-  loves(X,Z),  loves(Y,Z).
```

What is the expected answer to each of the following queries?

Why?

```
?-  jealous(marsellus,W).
```

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References

- In PROLOG, we can define predicates recursively.
- A recursive definition requires:
 - At least one *base case* (non-recursive)
 - At least one *recursive case*
- Let's look at a classic example from "Learn PROLOG Now!": Eating and Digestion



Recursive Definitions

Example: Eating

Consider the following knowledge base:

```
1  is_digesting(X,Y)  :-  just_ate(X,Y) .  
2  is_digesting(X,Y)  :-  
3      just_ate(X,Z) ,  
4      is_digesting(Z,Y) .  
  
5  
6  just_ate(mosquito,blood(john)) .  
7  just_ate(frog,mosquito) .  
8  just_ate(stork,frog) .
```

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- The definition of `is_digesting/2` is recursive
- It appears in both head and body of the second rule
- The first rule (base case) provides an “escape” from circularity



Recursive Definitions

Declarative Meaning

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- ***Declarative meaning:*** The logical meaning of the PROLOG knowledge base
- Base clause (non-recursive):
 - “If X has just eaten Y , then X is now digesting Y ”
- Recursive clause:
 - “If X has just eaten Z and Z is digesting Y , then X is digesting Y too”
- This captures the intuition of indirect digestion through food chains

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Recursive Definitions

Procedural Meaning

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- *Procedural meaning*: How PROLOG actually executes the queries
- For a query `is_digesting(X,Y)`, PROLOG:
 - First tries the base rule: “Has x just eaten y ? ”
 - If that fails, tries the recursive rule by finding some z where:
 - x has just eaten z , AND
 - z is digesting y (recursive subgoal)



Recursive Definitions

Example Execution

For the query:

```
?- is_digesting(stork,mosquito).
```

PROLOG's execution:

1. Try base rule with X=stork, Y=mosquito:
`just_ate(stork,mosquito)` \Rightarrow fails
2. Try recursive rule:
 - Find Z where `just_ate(stork,Z)` \Rightarrow Z = frog
 - New subgoal: `is_digesting(frog,mosquito)`
 - Try base rule: `just_ate(frog,mosquito)` \Rightarrow succeeds!
3. Query succeeds: Yes, stork is digesting mosquito

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Recursive Definitions

The Importance of Base Cases

Warning

Always include a base case in recursive definitions!

Consider this dangerous rule:

```
p :- p.
```

- Declaratively: “If property p holds, then property p holds” (logical)
- Procedurally: Creates an *infinite loop*
 - To prove p , I need to prove p
 - To prove p , I need to prove p
 - ...and so on, forever
- Without a base case, PROLOG won’t terminate

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Recursive Definitions

Another Example: Family Relationships

Consider the following knowledge base:

```
1  child(oscar, karen, frank).  
2  child(mary, karen, frank).  
3  child(eve, anne, oscar).  
4  child(henry, anne, oscar).  
5  child(isolde, anne, oscar).  
6  child(clyde, mary, oscarb).  
7  
8  child(X,Z,Y) :- child(X,Y,Z).  
9  
10 descendant(X,Y) :- child(X,Y,Z).  
11 descendant(X,Y) :- child(X,U,V), descendant(U,Y).
```

The following query is not answered:

```
?- descendant(clyde,karen).
```

- The clause in line 8, which specifies symmetry of the child predicate, calls itself recursively without the possibility of termination.

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Recursive Definitions

Another Example: Family Relationships

This problem can be solved with the following new program.

rel01.pl

```
1 child(oscar, karen, frank).
2 child(mary, karen, frank).
3 child(eve, anne, oscar).
4 child(henry, anne, oscar).
5 child(isolde, anne, oscar).
6 child(clyde, mary, oscarb).
7
8 descendant(X,Y) :- child(X,Y,Z).
9 descendant(X,Y) :- child(X,Z,Y).
10 descendant(X,Y) :- child(X,U,V), descendant(U,Y).
```

```
?- descendant(clyde, karen).
true .

?- child(eve,oscar,anne).
false .
```

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But now **the query**

```
?- child(eve,oscar,anne).
```

is no longer correctly answered because the symmetry of
child in the last two variables is no longer given.



Recursive Definitions

Another Example: Family Relationships

A solution to both problems is found in the program.

rel02.pl

```
1 child_fact(oscar, karen, frank).
2 child_fact(mary, karen, frank).
3 child_fact(eve, anne, oscar).
4 child_fact(henry, anne, oscar).
5 child_fact(isolde, anne, oscar).
6 child_fact(clyde, mary, oscarb).
7
8 child(X,Z,Y) :- child_fact(X,Y,Z).
9 child(X,Z,Y) :- child_fact(X,Z,Y).
10
11 descendant(X,Y) :- child(X,Y,Z).
12 descendant(X,Y) :- child(X,U,V), descendant(U,Y).
```

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A solution to both problems is found in the program.

rel02.pl

```
1 child_fact(oscar, karen, frank).  
2 child_fact(mary, karen, frank).  
3 child_fact(eve, anne, oscar).  
4 child_fact(henry, anne, oscar).  
5 child_fact(isolde, anne, oscar).  
6 child_fact(clyde, mary, oscarb).  
7  
8 child(X,Z,Y) :- child_fact(X,Y,Z).  
9 child(X,Z,Y) :- child_fact(X,Z,Y).  
10  
11 descendant(X,Y) :- child(X,Y,Z).  
12 descendant(X,Y) :- child(X,U,V), descendant(U,Y).
```

The PROLOG programmer must *pay attention to processing* and *avoid infinite loops*

The program is no longer as elegant and simple as the—logically correct—first variant



Execution Control and Procedural Elements

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Note

As we have seen in the previous examples, *it is important to control the execution of PROLOG.*

- *Avoiding unnecessary backtracking* especially can lead to large increases in efficiency. One means to this end is the *cut* operator. *By inserting an exclamation mark into a clause, we can prevent backtracking over this point.*
- Another possibility for execution control is the built-in predicate *fail*, which is never true.



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Example 1 (Cut operator in PROLOG)

max(X, Y, Max) means “the maximum of two numbers *X* and *Y* is *Max*”

max.pl

```
1 max(X,Y,X) :- X >= Y.  
2 max(X,Y,Y) :- X < Y.
```

maxwCut.pl

```
1 max(X,Y,X) :- X >= Y, !.  
2 max(X,Y,Y).
```

- Without cut.
- In query `?- max(2,3,Z), Z > 10.`, backtracking is employed because `Z = 3` and the second clause is tested for `max`, which is doomed to failure

- With cut.
- The second clause is only called if it is really necessary, that is, if the first clause fails.
- However, this optimization makes the program harder to understand.



Execution Control and Procedural Elements

Example 2 (Predicate fail in PROLOG)

- In the family relationship example we can quite simply print out all children and their parents with the query

```
?- child_fact(X,Y,Z), write(X),  
    write(' is a child of '), write(Y),  
    write(' and '), write(Z), write('.').  
nl, fail.
```

- The corresponding output is

```
oscar is a child of karen and frank.  
mary is a child of karen and frank.  
eve is a child of anne and oscar.  
henry is a child of anne and oscar.  
isolde is a child of anne and oscar.  
clyde is a child of mary and oscarb.  
false.
```

where the predicate `nl` causes a line break in the output. What would be the output in the end without use of the `fail` predicate?

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Example 3 (Negation as Failure)

- In the family relationship example, the query

```
?- child_fact(ulla,X,Y).
```

would result `false`. because there are no facts about `ulla`.

- This answer is *not logically correct*. Specifically, *it is not possible to prove that there is no object with the name `ulla`*. Here the prover E would correctly answer “No proof found.”
- Thus if *PROLOG answers false.*, this only means that *the query Q cannot be proved*. For this, however, $\neg Q$ must not necessarily be proved.



Lists

- A collection of *ordered data*.
- Has zero or more elements enclosed by **square brackets** and **separated by commas (',')**.

Example	Description
[A]	A list with one element
[]	An empty list
[34, tom, [2,3]]	A list with three elements where the third element is a list of two elements
[mia, love(honey), mia]	A list with three elements where the first and last elements are identical

- Like any object, a list can be unified with a variable

```
?- X = [Any, list, 'of elements'].  
X = [Any, list, 'of elements'].
```

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Lists

- A list can be decomposed into its *head* (first element) and *tail* (remaining elements) using the vertical bar operator ('|').
- For example, the list [A, B, C] can be decomposed as follows:

```
?- [Head|Tail] = [A, B, C].  
Head = A,  
Tail = [B, C].
```

- What are the head and the tail of the list `[dead(z)]`?
- **Note:** The empty list has neither a head nor a tail. That is, the empty list has no internal structure; for PROLOG, [] is a special, particularly simple, list.
 - What is the output of the following query?

```
?- [H|T] = [].
```

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Exercise 6

Explain the purpose of each query and give PROLOG's expected answer. For each query below, state (1) what the query asks, (2) the expected result (true/false or variable bindings), and (3) a brief justification.

```
?- [X|Y] = [[] , dead(z) , [2, [b, c]] , [] , Z].
```

```
?- [X,Y | W] =  
      [[] , dead(z) , [2, [b, c]] , [] , Z].
```

```
?- [X1,X2,X3,X4 | Tail] =  
      [[] , dead(z) , [2, [b, c]] , [] , Z].
```

```
?- [_,X,_,Y|_] =  
      [[] , dead(z) , [2, [b, c]] , [] , Z].
```

```
?- [_,_,[_|X]|_] =  
      [[] , dead(z) , [2, [b, c]] , [] , Z].
```

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Lists

First recursive list program

It's time to look at an example (from "Learn Prolog Now!") of a recursive PROLOG program for lists: the predicate `member/2`.

- Goal: given an object `X` and a list `L`, decide whether `X` belongs to `L`.
- The standard definition (one fact and one recursive rule):

```
1  member(X, [X|T]) .  
2  member(X, [H|T]) :- member(X, T) .
```

- First clause (fact): "`X` is a member of a list if `X` is the head of that list." (uses the `|` operator)
- Second clause (recursive rule): "`X` is a member of a list if `x` is a member of the tail of the list."
- Declaratively this is straightforward: the two clauses capture membership directly from the structure of lists.

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Procedural behaviour — examples

Consider how PROLOG answers queries.

- Immediate success:

```
?- member(yolanda, [yolanda, trudy, vincent, jules])
```

PROLOG succeeds immediately by unifying with the first clause.

- Requires recursion/backtracking:

```
?- member(vincent, [yolanda, trudy, vincent, jules])
```

PROLOG tries the first clause (fails), uses the recursive clause repeatedly until the subgoal

```
member(vincent, [vincent, jules])
```

unifies with the first clause and succeeds.

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Failure and termination

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- If the queried element is not in the list, recursion eventually reaches the empty list and cannot proceed:

```
?- member(zed, [yolanda, trudy, vincent, jules]).
```

- PROLOG will derive successive goals

```
member(zed, [trudy, vincent, jules])
member(zed, [vincent, jules])
member(zed, [jules])
member(zed, [])
```

and at `member(zed, [])`, neither clause applies (empty list cannot be split), so search stops and the answer is no.



Lists

Enumerating members & a small improvement

- `member/2` can be used with variables to enumerate elements:

```
?- member(X,[yolanda,trudy,vincent,jules]).  
X = yolanda ;  
X = trudy ;  
X = vincent ;  
X = jules ;  
no
```

- Small stylistic improvement: use anonymous variables for irrelevant parts

```
1  member(X,[X|_]).  
2  member(X,[_|T]) :- member(X,T).
```

Semantically identical, but clearer because each clause names only what matters.

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Self-modifying Programs

- PROLOG programs are not fully compiled, rather, they are interpreted by the WAM. Therefore *it is possible to modify programs at runtime*. A program can even modify itself.
- With commands such as `assert` and `retract`, facts and rules can be added to the knowledge base or taken out of it.
- Assert predicates
 - `assert(X)`: Adds a new fact or clause to the database.
Term is asserted as the last fact or clause with the same key predicate.
 - `asserta(X)`: Same as assert, but adds a clause at the beginning of the database.
 - `assertz(X)`: Exactly same as `assert(X)`.
- Retract predicates
 - `retract(X)`: Removes fact or clause X from the database.
 - `retractall(X)`: Removes all facts or clauses from the database for which the head unifies with x.

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Self-modifying Programs

A simple application of `asserta` is the addition of derived facts to the beginning of the knowledge base with the goal of avoiding a repeated, potentially time-expensive derivation.

Example 4 (Family Relationship)

dynamic_rel.pl

```
1 child_fact(oscar, karen, frank).
2 child_fact(mary, karen, frank).
3 child_fact(eve, anne, oscar).
4 child_fact(henry, anne, oscar).
5 child_fact(isolde, anne, oscar).
6 child_fact(clyde, mary, oscarb).
7
8 child(X,Z,Y) :- child_fact(X,Y,Z).
9 child(X,Z,Y) :- child_fact(X,Z,Y).
10
11 :- dynamic descendant/2.
12 descendant(X,Y) :- child(X,Y,Z), asserta(descendant(X,Y)).
13 descendant(X,Y) :- child(X,U,V), descendant(U,Y),
14                               asserta(descendant(X,Y)).
```

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Self-modifying Programs

```
?- [dynamic_rel].  
true.  
  
?- descendant(clyde, karen).  
true .  
  
?- listing(descendant).  
:- dynamic descendant/2.  
  
descendant(clyde, karen).  
descendant(mary, karen).  
descendant(X, Y) :-  
child(X, Y, Z),  
asserta(descendant(X, Y)).  
descendant(X, Y) :-  
child(X, U, V),  
descendant(U, Y),  
asserta(descendant(X, Y)).  
  
true.
```

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Self-modifying Programs

- By manipulating rules with assert and retract, even programs that change themselves completely can be written. This idea became known under the term *genetic programming*. It allows the construction of arbitrarily flexible learning programs.
- In practice, however, it turns out that, due to the *huge number of senseless possible changes, changing the code by trial and error rarely leads to a performance increase*.
- *Systematic changing of rules*, on the other hand, *makes programming so much more complex* that, so far, such programs that extensively modify their own code have not been successful.
- *Machine learning* has been quite successful. However, only *very limited modifications* of the program code are being conducted here.

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A Planning Example

Exercise 7

Understand how to solve this problem using PROLOG.

A farmer wants to bring a cabbage, a goat, and a wolf across a river, but his boat is so small that he can only take them across one at a time. The farmer thought it over and then said to himself: "If I first bring the wolf to the other side, then the goat will eat the cabbage. If I transport the cabbage first, then the goat will be eaten by the wolf. What should I do?"



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Constraint Logic Programming

- The *programming of scheduling systems*, in which many (sometimes complex) logical and numerical conditions must be fulfilled, *can be very expensive and difficult with conventional programming languages.*
- This is precisely where *logic could be useful.*
- An approach is to simply *write all logical conditions in PL1 and then enter a query. Usually this approach fails miserably.* The reason is *the penguin problem* discussed in “Limitations of Logic”. The fact `penguin(tweety)` does ensure that `penguin(tweety)` is true but does not rule out that `raven(tweety)` is also true. To rule this out with additional axioms is very inconvenient.
- *Constraint Logic Programming (CLP)* [Jaffar and Lassez 1987], which allows the *explicit formulation of constraints for variables*, offers an elegant and very efficient mechanism for solving this problem.
 - The *interpreter constantly monitors the execution of the program for adherence to all of its constraints.*
 - The programmer is fully relieved of the task of controlling the constraints, which in many cases can greatly simplify programming.

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Constraint Logic Programming

Example 5 (Applying the CLP mechanism of GNU-PROLOG (The finite domain (FD) constraint solver))

The secretary of Albert Einstein High School has to come up with a plan for allocating rooms for final exams. He has the following information: the four teachers Mayer, Hoover, Miller and Smith give tests for the subjects German, English, Math, and Physics in the ascendingly numbered rooms 1, 2, 3 and 4. Every teacher gives a test for exactly one subject in exactly one room. Besides that, he knows the following about the teachers and their subjects.

- (1) Mr. Mayer never tests in room 4.
- (2) Mr. Miller always tests German.
- (3) Mr. Smith and Mr. Miller do not give tests in neighboring rooms.
- (4) Mrs. Hoover tests Mathematics.
- (5) Physics is always tested in room number 4.
- (6) German and English are not tested in room 1.

Who gives a test in which room?

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Constraint Logic Programming

raumplan.pl

```
1   %%% Run in GNU-PROLOG
2   start :-  
3     fd_domain([Mayer, Hoover, Miller, Smith],1,4),  
4     fd_all_different([Mayer, Miller, Hoover, Smith]),  
5  
6     fd_domain([German, English, Math, Physics],1,4),  
7     fd_all_different([German, English, Math, Physics]),  
8  
9     fd_labeling([Mayer, Hoover, Miller, Smith]),  
10  
11    Mayer #\=4,                                          % Mayer not in room 4  
12    Miller #= German,                                  % Miller tests German  
13    dist(Miller, Smith) #>= 2,                        % Distance Miller/Smith >= 2  
14    Hoover #= Math,                                      % Hoover tests mathematics  
15    Physics #= 4,                                        % Physics in room 4  
16    German #\= 1,                                        % German not in room 1  
17    English #\= 1,                                        % English not in room 1  
18    nl,  
19    write([Mayer, Hoover, Miller, Smith]), nl,  
20    write([German, English, Math, Physics]), nl.
```

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Constraint Logic Programming

■ GNU-PROLOG built-in predicates:

- `fd_domain(Vars, Lower, Upper)` constrains each element X of Vars to take a value in Lower..Upper.
- `fd_all_different(List)` constrains all variables in List to take distinct values.
- `fd_labeling(Vars, Options)` assigns a value to each variable X of the list Vars according to the list of labeling options given by Options. This predicate is re-executable on backtracking. `fd_labeling(Vars)` is equivalent to `fd_labeling(Vars, [])`.
- The variables Mayer, Hoover, Miller, Smith as well as German, English, Math, Physics can each take on an integer value from 1 to 4 as the room number. (Lines 3–6.)
- A binding Mayer = 1 and German = 1 means that Mr. Mayer gives the German test in room 1.
- Lines 4 and 7 ensure that the four particular variables take on different values.
- Line 9 ensures that all variables are assigned a concrete value in the case of a solution. This line is not absolutely necessary here. If there were multiple solutions, however, only intervals would be output.
- In lines 11–17 the constraints are given, and the remaining lines output the room numbers for all teachers and all subjects in a simple format.

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Constraint Logic Programming

The program is loaded into GNU-PROLOG with
['raumplan.pl']., and with start. we obtain the output

```
[3,1,2,4]  
[2,3,1,4]
```

```
true ?
```

```
yes
```

This output corresponds to the plan

Room num.	1	2	3	4
Teacher	Hoover	Miller	Mayer	Smith
Subject	Math	German	English	Physics

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