

PHAN TICH THIET KE THUAT TOAN – CS112.L11.KHCL

Phan tich thuat toan perfectly balanced tree va quick select

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Cau 1:

Thoi gian chay thuat toan tao cay nhi phan bang thuc nghiem

| n | t(n) |
|------|-------|
| 100 | 0.003 |
| 450 | 0.032 |
| 800 | 0.062 |
| 1150 | 0.08 |
| 1500 | 0.081 |
| 1850 | 0.103 |
| 2200 | 0.144 |
| 2550 | 0.175 |
| 2900 | 0.17 |
| 3250 | 0.161 |
| 3600 | 0.186 |
| 3950 | 0.241 |
| 4300 | 0.327 |
| 4650 | 0.253 |
| 5000 | 0.23 |
| 5350 | 0.207 |
| 5700 | 0.22 |
| 6050 | 0.259 |
| 6400 | 0.282 |
| 6750 | 0.402 |
| 7100 | 0.464 |
| 7450 | 0.316 |

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| | |
|------|-------|
| 7800 | 0.353 |
| 8150 | 0.36 |
| 8500 | 0.347 |
| 8850 | 0.391 |
| 9200 | 0.365 |
| 9550 | 0.368 |
| 9900 | 0.352 |

Do phuc tap cua thuat toan tao cay nhi phan bang thuc nghiem tu ket qua

| TB lgn - n | TB sqrt(n) - c | TB n - c | TB nlgn - c | TB n^2 - c | TB n^3 - c |
|-------------|----------------|-------------|-------------|-------------|-------------|
| 11.58011301 | 66.24017412 | 4999.760897 | 62881.79503 | 33574999.76 | 2.53625E+11 |

Ta thay trung binh chenh lech cua log n la nho nhat nen chon log n

Cau 2:

Phuong trinh de quy do phuc tap thuat toan tao cay nhi phan can bang hoan hao

$$T(n) = \begin{cases} C1 \\ T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + C2 \end{cases}$$

$$\begin{aligned} T(n) &= 2T\left(\frac{n}{2}\right) + C2 \\ &= 2[2T\left(\frac{n}{4}\right) + C2] + C2 \\ &= 4T\left(\frac{n}{4}\right) + 3C2 \\ &= 4[2T\left(\frac{n}{8}\right) + C2] + 3C2 \\ &= 8T\left(\frac{n}{8}\right) + 7C2 \\ &= 8[2T\left(\frac{n}{16}\right) + C2] + 7C2 \\ &= 16T\left(\frac{n}{16}\right) + 15C2 \end{aligned}$$

$$\Rightarrow T(n) = 2^i T\left(\frac{n}{2^i}\right) + (2^i - 1)C2$$

$$\text{Khi } i = \log_2 n \Rightarrow nC' + (n-1) * C2$$

$$\Rightarrow \text{Do phuc tap la } \log_2 n$$

Cau 3:

Thoi gian chay thuat toan quick select bang thuc nghiem

| | |
|---|---|
| k | t |
|---|---|

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| | |
|------|---------|
| 100 | 3.213 |
| 500 | 18.894 |
| 900 | 33.773 |
| 1300 | 50.718 |
| 1700 | 61.472 |
| 2100 | 76.53 |
| 2500 | 117.976 |
| 2900 | 61.802 |
| 3300 | 88.477 |
| 3700 | 182.524 |
| 4100 | 228.378 |
| 4500 | 315.38 |
| 4900 | 342.713 |
| 5300 | 393.447 |
| 5700 | 194.629 |
| 6100 | 379.642 |
| 6500 | 399.27 |
| 6900 | 565.222 |
| 7300 | 391.981 |
| 7700 | 393.284 |

Vay thoi gian phu thuoc vao gia tri cua k

Cau 4:

Do phuc tap quick select bang thuc nghiem tu ket qua cau 3

| TB lgn - n | TB sqrt(n) - c | TB n - c | TB nlgn - c | TB n ² - c | TB n ³ - c |
|-------------|----------------|------------|-------------|-----------------------|-----------------------|
| 203.8669332 | 157.3920367 | 3685.03375 | 47462.31288 | 20529785.03 | 1.21563E+11 |

Ta thay trung binh chenh lech ca sqrt n là nhỏ nhất nên chn sqrt n

Cau 5:

Phuong trinh de quy do phuc tap thuat toan quick select

$$T(n) = \begin{cases} c1vin = 1 \\ cn + T\left(\frac{n}{2}\right) \end{cases}$$

$$\begin{aligned} T(n) &= T\left(\frac{n}{2}\right) + cn \\ &= T\left(\frac{n}{4}\right) + c\frac{n}{2} + cn \\ &= T\left(\frac{n}{8}\right) + c\frac{n}{4} + c\frac{n}{2} + cn \\ &= T\left(\frac{n}{16}\right) + c\frac{n}{8} + c\frac{n}{4} + c\frac{n}{2} + cn \\ &= T\left(\frac{n}{16}\right) + c\left(\frac{n}{8} + \frac{n}{4} + \frac{n}{2} + n\right) \end{aligned}$$

$$\Rightarrow T(n) = c\left(n + \frac{n}{2^i} + \dots + \frac{n}{2^{i-1}} + T\left(\frac{n}{2^i}\right)\right)$$

$$\begin{aligned} \text{Khi } i = \log_2(n) \Rightarrow T(n) &= c\left(n + \frac{n}{2} + \dots + \frac{n}{2^{i-1}} + c'\right) \\ &= cn\left(1 + \frac{1}{2} + \dots + \frac{1}{2^{i-1}}\right) + c' \\ &= c * 2n + c' \in O(n) \end{aligned}$$

\Rightarrow Do phuc tap là $O(n)$