

### **2D Minimum Algorithm**



- Consider applying a 2D window to a 2D array of elements
  - Each output element is the minimum of input elements within the window



- 2D operations like this are found in many fundamental algorithms
  - Interpolation, Convolution, Filtering
- Applications in seismic processing, weather simulation, image processing, etc

### 2D Minimum: C Version



```
#define WIN SIZE 16
#define N 20000
int main() {
                                       Allocate
 int size=N*N*sizeof(int);
                                     Resources
 int i, j, x, y, temp;
 //allocate resources
 int *cell=(int *)malloc(size); //input
 int *node=(int *)malloc(size); //output
                                       Initialize
 initializeArray(cell,N);
                                         data
 initializeArray(node,N);
```

```
Loop over
for(i=0;i<N;i++)
                                  dataset
   for(j=0;j<N;j++)
  //find minimum in window
                                      Loop over
                                       window
     temp = node[i][j];
     for(x=0;x<WIN_SIZE;x++)</pre>
      for(y=0;y<WIN\_SIZE;y++)
           if (temp> cell[i+x][j+y])
                                             Find
                                             min
              temp = cell[i+x][j+y];
      node[i][j] = temp;
//free resources
                                 Cleanup
 free(cell); free(node);
```

### 2D Minimum: C Version

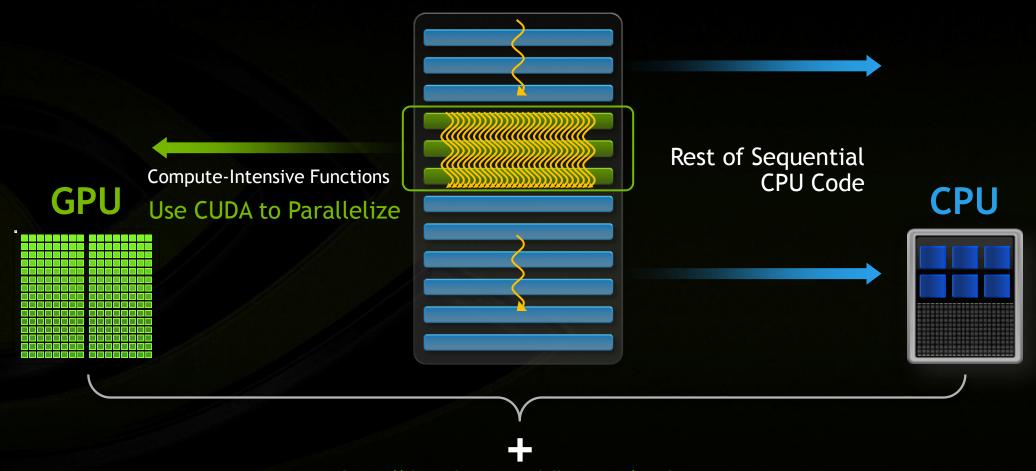


```
#define WIN SIZE 16
                                                      for(i=0;i<N;i++)
#define N 20000
                                                         for(j=0;j<N;j++)
int main() {
                                                         //find minimum in window
 int size=N*N*sizeof(int);
 int i, j, x, y, temp;
                                                           temp = node[i][j];
 //alloca
        Algorithm
                              Device
                                                   Compute
                                                                         Speedup
 int *cel
                              Xeon X5650
 int *noc C (serial)
                                                   96.1sec
                                                                    temp = cell[i+x][j+y];
 initializeArray(cell,N);
                                                            node[i][j] = temp;
 initializeArray(node,N);
                                                       //free resources
                                                       free(cell); free(node);
```

# CPU + GPU = Big Speedup



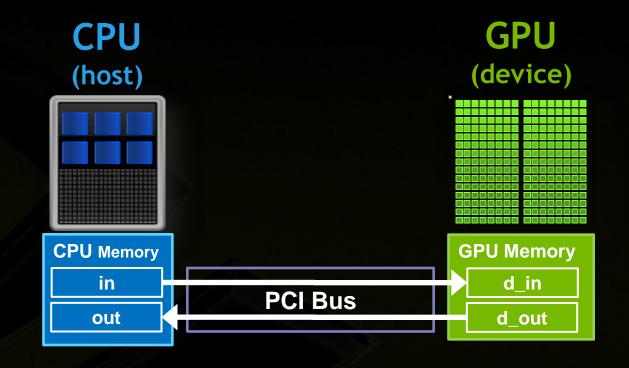




http://developer.nvidia.com/cuda

# **Explicit Data Movement**







C

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(int*)malloc(size); //input
 int *node=(int*)malloc(size); //output
 initializeArray(cell,N);
 initializeArray(node,N);
// nested for loops
 for...
  for ...
   for ...
     for ....
//free resources
 free(in); free(out);
```

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(float*)malloc(size);
 int *node=(float*)malloc(size);
 int *d cell; cudaMalloc(&d cell,size);
 int *d_node; cudaMalloc(&d_node,size);
 initializeArray(cell,N); initializeArray(node,N);
 cudaMemcpy(d_cell,cell,size,cudaMemcpyHostToDevice);
 cudaMemcpy(d_node,node,size,cudaMemcpyHostToDevice);
 compute_win2D<<<nblocks, nthreads>>>(d_node,d_cell);
 //free resources
 free(cell); free(node);
 cudaFree(d_cell); cudaFree(d_node);
```



C

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(int*)malloc(size); //input
 int *node=(int*)malloc(size); //output
 initializeArray(cell,N);
 initializeArray(node,N);
// nested for loops
 for...
  for ...
   for ...
     for ....
//free resources
 free(in); free(out);
```

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
                                              Allocate
 int *cell=(float*)malloc(size);
                                               Device
 int *node=(float*)malloc(size);
                                              Memory
 int *d cell; cudaMalloc(&d cell,size);
 int *d_node; cudaMalloc(&d_node,size);
 initializeArray(cell,N); initializeArray(node,N);
 cudaMemcpy(d_cell,cell,size,cudaMemcpyHostToDevice);
 cudaMemcpy(d_node,node,size,cudaMemcpyHostToDevice);
 compute_win2D<<<nblocks, nthreads>>>(d_node,d_cell);
 //free resources
 free(cell); free(node);
 cudaFree(d_cell); cudaFree(d_node);
```



C

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(int*)malloc(size); //input
 int *node=(int*)malloc(size); //output
 initializeArray(cell,N);
 initializeArray(node,N);
// nested for loops
 for...
  for ...
   for ...
     for ....
//free resources
 free(in); free(out);
```

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(float*)malloc(size);
 int *node=(float*)malloc(size);
 int *d cell; cudaMalloc(&d cell,size);
 int *d_node; cudaMalloc(&d_node,size);
                                                Copy Data to
 initializeArray(cell,N); initializeArray(node,N
                                                 the Device
 cudaMemcpy(d_cell,cell,size,cudaMemcpyHostToDevice);
 cudaMemcpy(d_node,node,size,cudaMemcpyHostToDevice);
 compute_win2D<<<nblocks, nthreads>>>(d_node,d_cell);
 //free resources
 free(cell); free(node);
 cudaFree(d_cell); cudaFree(d_node);
```



```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(int*)malloc(size); //input
 int *node=(int*)malloc(size); //output
 initializeArray(cell,N);
 initializeArray(node,N);
// nested for loops
                                        Call Cuda
 for...
                                        Function
  for ...
   for ...
    for ....
//free resources
 free(in); free(out);
```

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(float*)malloc(size);
 int *node=(float*)malloc(size);
 int *d cell; cudaMalloc(&d_cell,size);
 int *d_node; cudaMalloc(&d_node,size);
 initializeArray(cell,N); initializeArray(node,N);
 cudaMemcpy(d_cell,cell,size,cudaMemcpyHostToDevice);
 cudaMemcpy(d_node,node,size,cudaMemcpyHostToDevice);
 compute_win2D<<<nblocks, nthreads>>>(d_node,d_cell);
 //free resources
 free(cell)
              Launch
                                                  Device
 cudaf
                              _node);
            Parameters
                                                  Pointers
```



C

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(int*)malloc(size); //input
 int *node=(int*)malloc(size); //output
 initializeArray(cell,N);
 initializeArray(node,N);
// nested for loops
 for...
  for ...
   for ...
     for ....
//free resources
 free(in); free(out);
```

```
int main() {
 int size=N*N*sizeof(int);
 //allocate resources
 int *cell=(float*)malloc(size);
 int *node=(float*)malloc(size);
 int *d cell; cudaMalloc(&d cell,size);
 int *d_node; cudaMalloc(&d_node,size);
 initializeArray(cell,N); initializeArray(node,N);
 cudaMemcpy(d_cell,cell,size,cudaMemcpyHostToDevice);
 cudaMemcpy(d_node,node,size,cudaMemcpyHostToDevice);
 compute_win2D<<<nblocks, nthreads>>>(d_node.d_cell);
 //free resources
                                                 Cleanup
 free(cell); free(node);
 cudaFree(d_cell); cudaFree(d_node);
```

### **Parallel Execution Model**



- A CUDA C function is executed by many parallel threads
- Threads are organized as a grid of independent thread blocks



# 2D Window: CUDA – Kernel Function



C

```
for(i=0;i<N;i++)
   for(j=0;j<N;j++)
   //find minimum in window
     temp = node[i][j];
     for(x=0;x<WIN_SIZE;x++)</pre>
       for(y=0;y<WIN_SIZE;y++)</pre>
            if (temp> cell[i+x][j+y])
              temp = cell[i+x][j+y];
      node[i][j] = temp;
```

```
<u>__global</u>__ <u>void</u> compute_win2D(<u>int</u> knode[][N], <u>int</u> kcell[][N])
int idx=blockIdx.x*blockDim.x+threadIdx.x;
    idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx<N)&&(idy<N)) {</pre>
//find minimum in window
     temp = knode[idx][idy];
     for(x=0;x<WIN_SIZE;x++)
      for(y=0;y<WIN_SIZE;y++)</pre>
           if (temp> kcell[idx+x][idy+y])
              temp = kcell[idx+x][idy+y];
     knode[i][j] = temp;
```

### 2D Window: CUDA – Kernel Function



C

```
Add
for(i=0;i<N;i++)
                                          global
   for(j=0;j<N;j++)
                                         Keyword
   //find minimum in window
     temp = node[i][j];
     for(x=0;x<WIN_SIZE;x++)</pre>
       for(y=0;y<WIN_SIZE;y++)</pre>
           if (temp> cell[i+x][j+y])
              temp = cell[i+x][j+y];
      node[i][j] = temp;
```

```
global void compute_win2D(int knode[][N], int kcell[][N])
int idx=blockIdx.x*blockDim.x+threadIdx.x;
    idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx<N)&&(idy<N)) {</pre>
//find minimum in window
    temp = knode[idx][idy];
    for(x=0;x<WIN_SIZE;x++)
      for(y=0;y<WIN_SIZE;y++)</pre>
          if (temp> kcell[idx+x][idy+y])
             temp = kcell[idx+x][idy+y];
     knode[i][j] = temp;
```

### 2D Window: CUDA – Kernel Function



**Replace Outer Loops With an** Index

```
void compute_win2D(int knode[][N], int kcell[][N])
                                  Calculation
for(i=0;i<N;i++)
                                                           int idx=blockIdx.x*blockDim.x+threadIdx.x;
                                                               idy=blockIdx.y*blockDim.y+threadIdx.y;
   for(j=0;j<N;j++)
                                                           int temp, x, y;
                      blockldx.x
                                                           if((idx<N)&&(idy<N)) {</pre>
                                                           //find minimum in window
                                                               temp = knode[idx][idy];
                                                                for(x=0;x<WIN_SIZE;x++)</pre>
                                                                 for(y=0;y<WIN_SIZE;y++)</pre>
                         •••
                                                                     if (temp> kcell[idx+x][idy+y])
                                                255
                                                                        temp = kcell[idx+x][idy+y];
                                                                knode[i][j] = temp;
       threadldx.x
                                   threadIdx.x
```

# 2D Window: CUDA – Kernel Function C CUDA C



```
<u>void</u> compute_win2D(int knode[][N], int kcell[][N])
                                                      idx=blockIdx.x*blockDim.x+threadIdx.x;
for(i=0;i<N;i++)
                                                      idy=blockIdx.y*blockDim.y+threadIdx.y;
   for(j=0;j<N;j++)
               Algorithm
                                     Device
                                                          Compute
                                                                                Speedup
  //find minimum
    temp = nod
                C (serial)
                                     X5650
                                                          96.1sec
    for(x=0;x<V)
      for(y=0;y<
                                                                                11.5x
                                     M2090
                                                          8.33sec
            temp = cell[i+x][j+y];
                                                            if (temp> kcell[idx+x][idy+y])
     node[i][j] = temp;
                                                               temp = kcell[idx+x][idy+y];
                                                       knode[i][j] = temp;
```

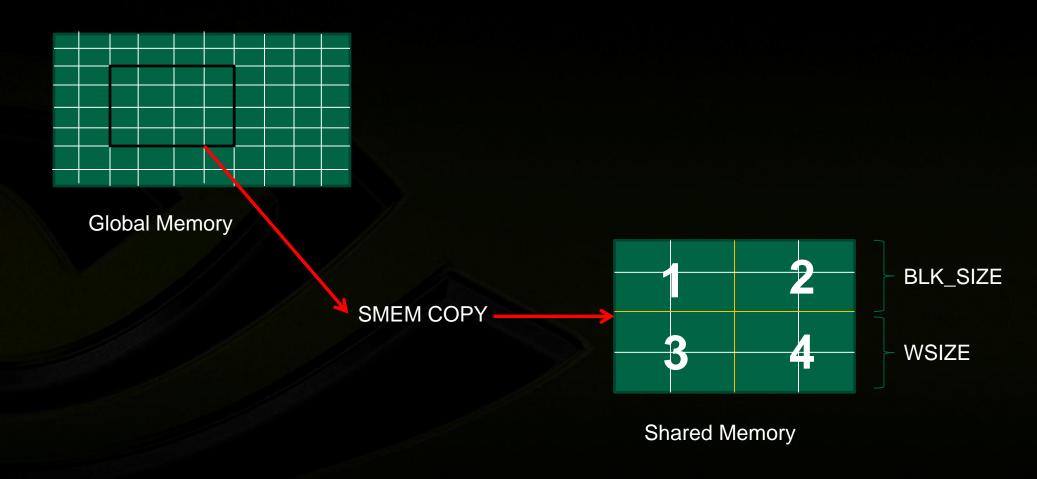
### **Observation: Data Reuse**





# **Optimization: Use Shared Memory**





http://developer.nvidia.com/cuda

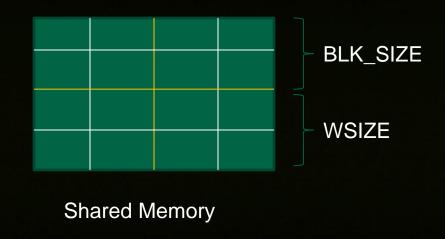


```
global void compute win2D(int knode[][N], int kcell[][N])
 __shared__ int smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx < N) & (idy < N)) 
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
  smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x >(N-WSIZE))
  smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
 __syncthreads();
```

```
//find minimum in window
 temp = knode[idx][idy];
 for(x=0;x<WSIZE;x++)
   for(y=0;y<WSIZE;y++)
     if (temp> smem[threadIdx.x+x][threadIdx.y+y])
      temp = smem[threadIdx.x+x][threadIdx.y+y];
     knode[i][j] = temp;
```

```
OVIDIA
```

```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
 <u>__shared___ int</u> smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
                                                    Allocate Shared
int temp, x, y;
                                                       Memory for
if((idx < N) & (idy < N)) 
                                                       Each Block
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
 smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
 smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```



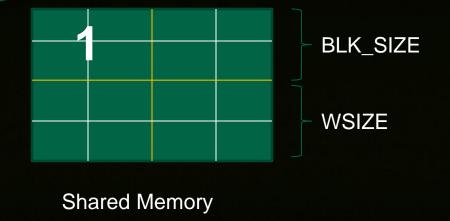


```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
 <u>shared</u> int smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
                                                        Calculate Global
                                                         Memory Indices
if((idx < N) & (idy < N)) 
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
 smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
 smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```





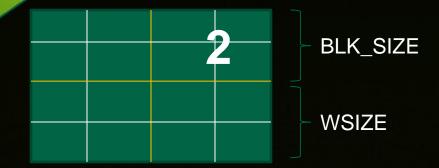
```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
 <u>_shared</u> <u>int</u> smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
                                                         Load Interior
int temp, x, y;
                                                      Region 1 to Shared
if((idx < N) & (idy < N)) 
                                                            Memory
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
 smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
 smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```





```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
 <u>_shared</u> <u>int</u> smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx < N) & (idy < N)) 
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
  smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
  smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```

Load Halo Region 2 to Shared Memory



**Shared Memory** 

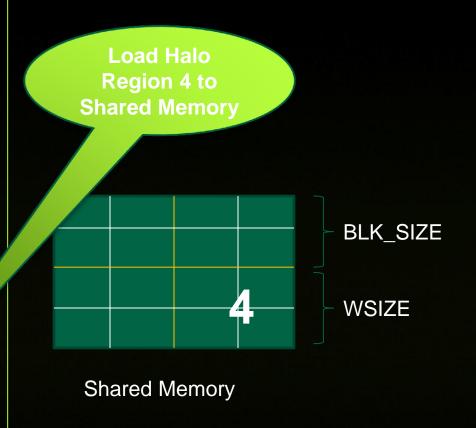


```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
 <u>_shared</u> <u>int</u> smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx < N) & (idy < N)) 
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
  smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
  smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```

Load Halo Region 3 to **Shared Memory** BLK SIZE WSIZE **Shared Memory** 

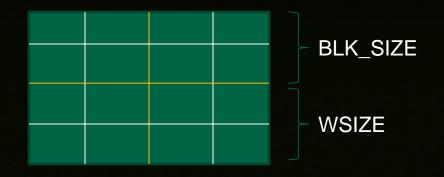


```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
 <u>shared</u> int smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx < N) & (idy < N)) 
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
 smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
 smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```





```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
 <u>shared</u> int smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx < N) & (idy < N)) 
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
 smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
 smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
                                               Wait for All Threads to
//wait for all threads to finish read
                                                  Finish Writing to
__syncthreads();
```



**Shared Memory** 

**Shared Memory** 



```
<u>_global___ void</u> compute_win2D(int knode[][N], int kcell[][N])
<u>_shared</u> <u>int</u> smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx<N)&&(idy<N)) {</pre>
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
  smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
  smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```

```
//find minimum in window
 temp = knode[idx][idy];
 for(x=0;x<WSIZE;x++)
   for(y=0;y<WSIZE;y++)</pre>
     if (temp> smem[threadIdx.x+x][threadIdx.y+y])
      temp = smem[threadIdx.x+x][threadIdx.y+y];
     knode[i][j] = temp;
                       Find Minimum:
                      Read Input from
                      Shared Memory,
                     Accumulate into a
                          Register
```



```
qlobal void compute_win2D(int knode[][N], int kcell[][N])
<u>__shared</u>__ int smem[BLK_SIZE+WSIZE][BLK_SIZE+WSIZE];
int idx=blockIdx.x*blockDim.x+threadIdx.x;
int idy=blockIdx.y*blockDim.y+threadIdx.y;
int temp, x, y;
if((idx < N) & (idy < N)) 
smem[threadIdx.x][threadIdx.y]=kcell[idx][idy];
if (threadIdx.y > (N-WSIZE))
 smem[threadIdx.x][threadIdx.y + WSIZE]=kcell[idx][idy+WSIZE];
if (threadIdx.x > (N-WSIZE))
 smem[threadIdx.x + WSIZE][threadIdx.y]=kcell[idx+WSIZE][idy];
if ((threadIdx.x > (N-WSIZE)) && (threadIdx.y > (N-WSIZE)))
 smem[threadIdx.x+WSIZE][threadIdx.y+WSIZE]=
               kcell[idx+WSIZE][idy+WSIZE];
//wait for all threads to finish read
__syncthreads();
```

```
//find minimum in window
 temp = knode[idx][idy];
 for(x=0;x<WSIZE;x++)
   for(y=0;y<WSIZE;y++)
    if (temp> smem[threadIdx.x+x][threadIdx.y+y])
      temp = smem[threadIdx.x+x][threadIdx.y+y];
     knode[i][j] = temp;
                  Write
               Minimum
               to Global
                Memory
```

