



# HUST

**ĐẠI HỌC BÁCH KHOA HÀ NỘI**  
HANOI UNIVERSITY OF SCIENCE AND TECHNOLOGY

ONE LOVE. ONE FUTURE.





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# WEB MINING

## LECTURE 08: RECOMMENDATION SYSTEM

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# Agenda

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1. Introduction tp Recommender System
2. Evaluation methods
3. Colaborative filtering using k-Nearest Neightbors
4. Colaborative filtering using Maxtrix Factorization
5. Neural Colaborative Filtering
6. Session-based Recommender System

# 1. Summary

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Why we need recommender system?

- Users are overloaded with information on the web
- Sellers need to offer the right product to
  - Increase sale revenue
  - Improve serving quality
- The trend of personalization and digitization is inevitable

# Recommender vs Information retrieval

- Information retrieval: Users express their wishes through a query
- Recommender System : Users do not know what they want

# Applications

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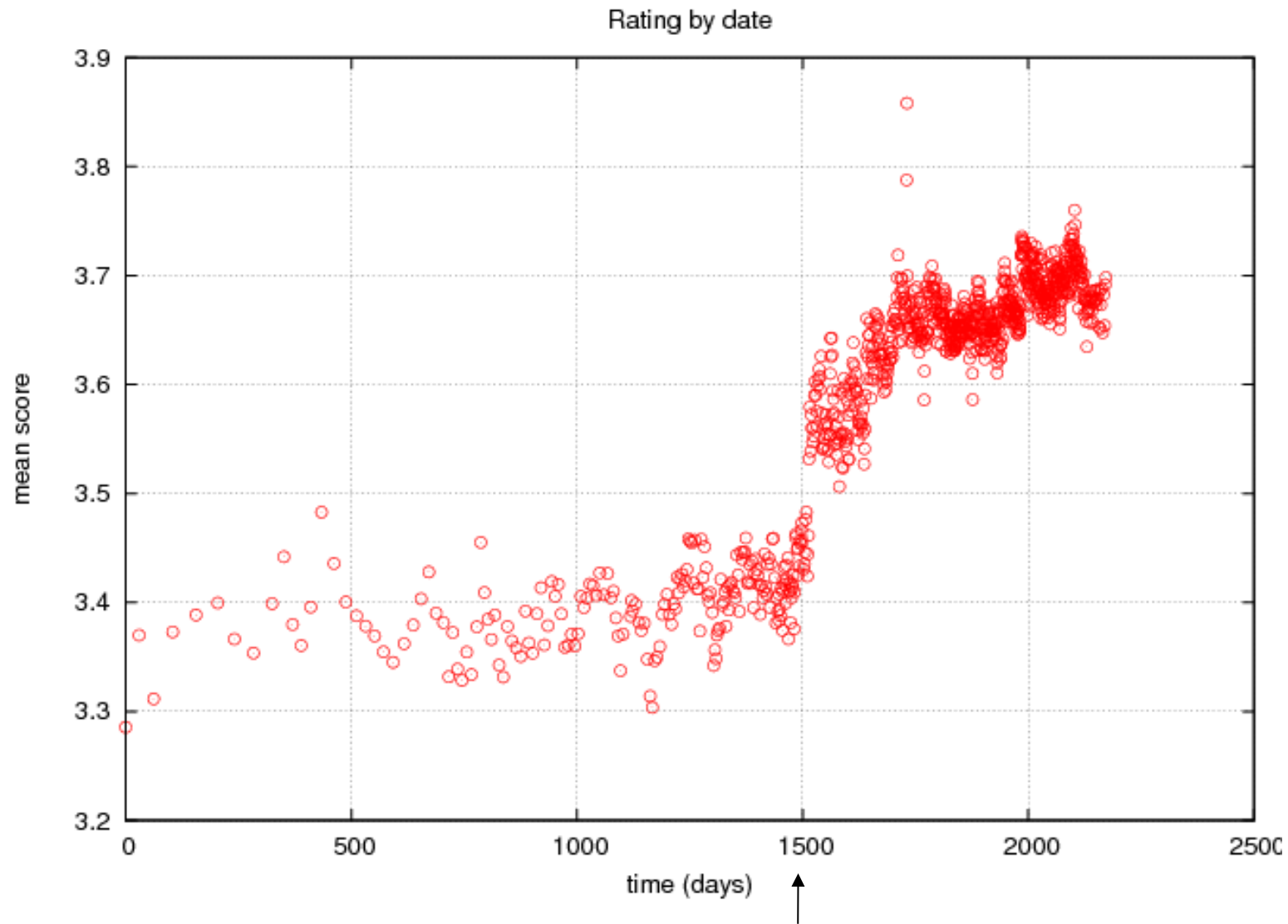
- Ecommerce
- Online entertainment
- Online News
- Forums, social networks
- Scientific research
- Online Dating

# Applications

- *Amazon:*
  - Recommend products
  - More than 30% increase in revenue
- *Netflix:*
  - Recommend movies, TV shows
  - Bring in \$1B per year
- *Google News:*
  - News Suggestions
  - Nearly 40% increase in traffic



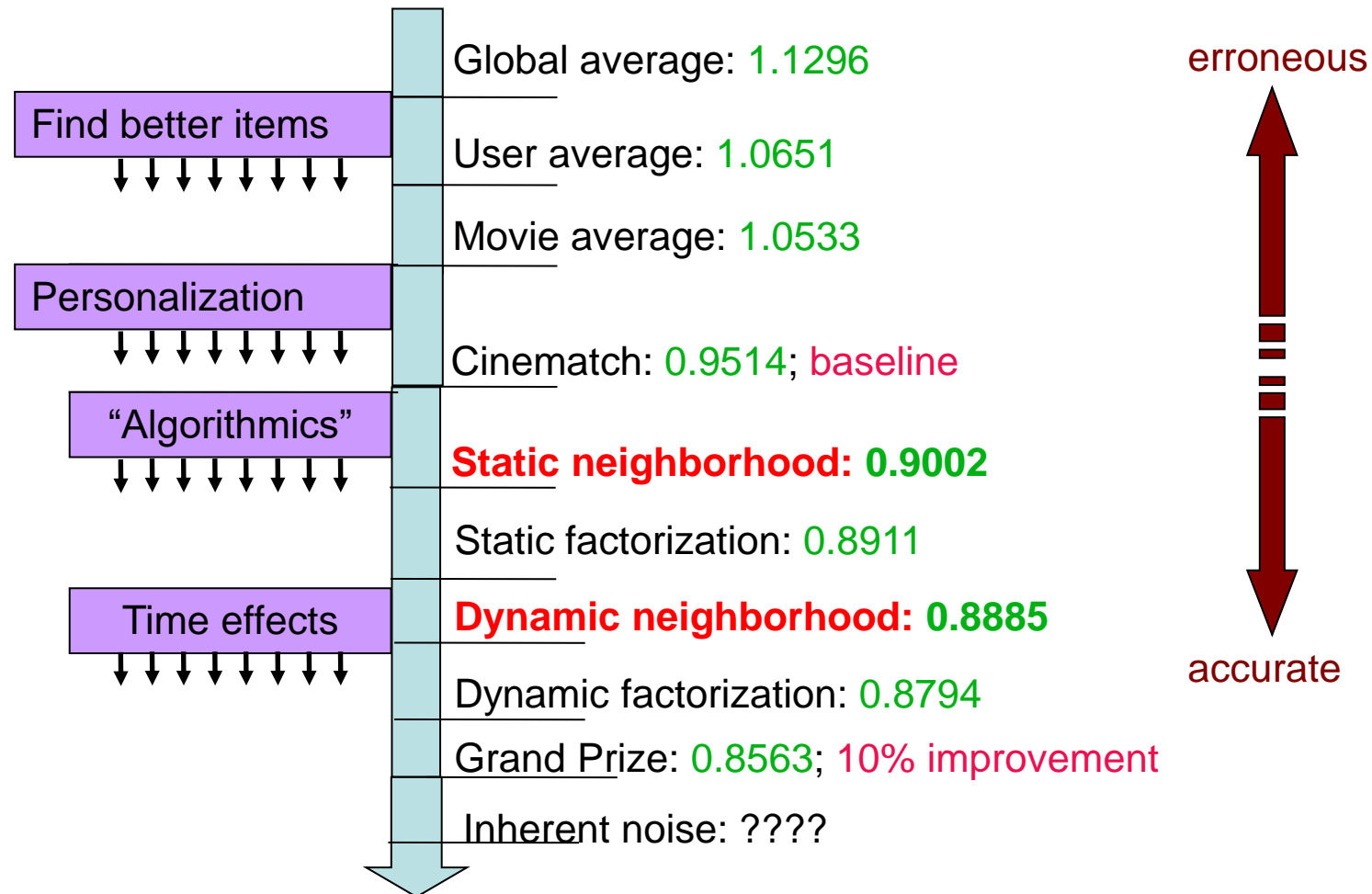
# Applications



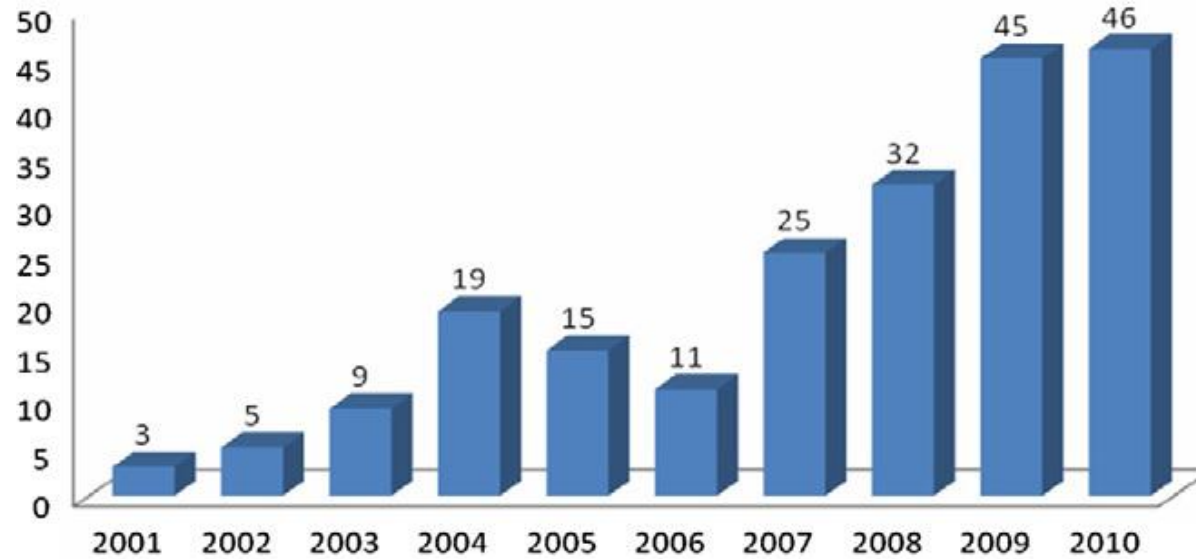
# Recommendation methods

- Content-based:
  - Suggestions based on user's transaction history
- Collaborative filtering:
  - Suggestions based on users with similar interests
- Session-based:
  - Suggestions based on transaction chains
- Hybrid methods

# Netflix challenge

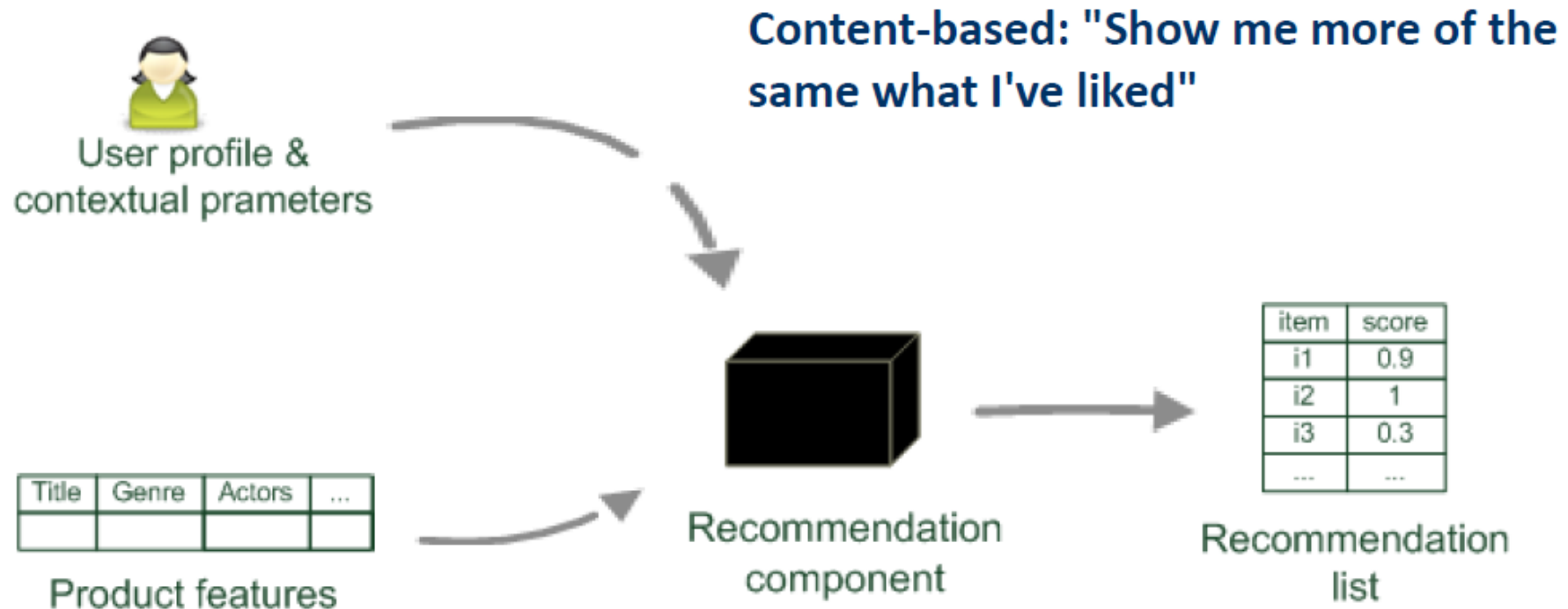


# Netflix challenge (cont.)

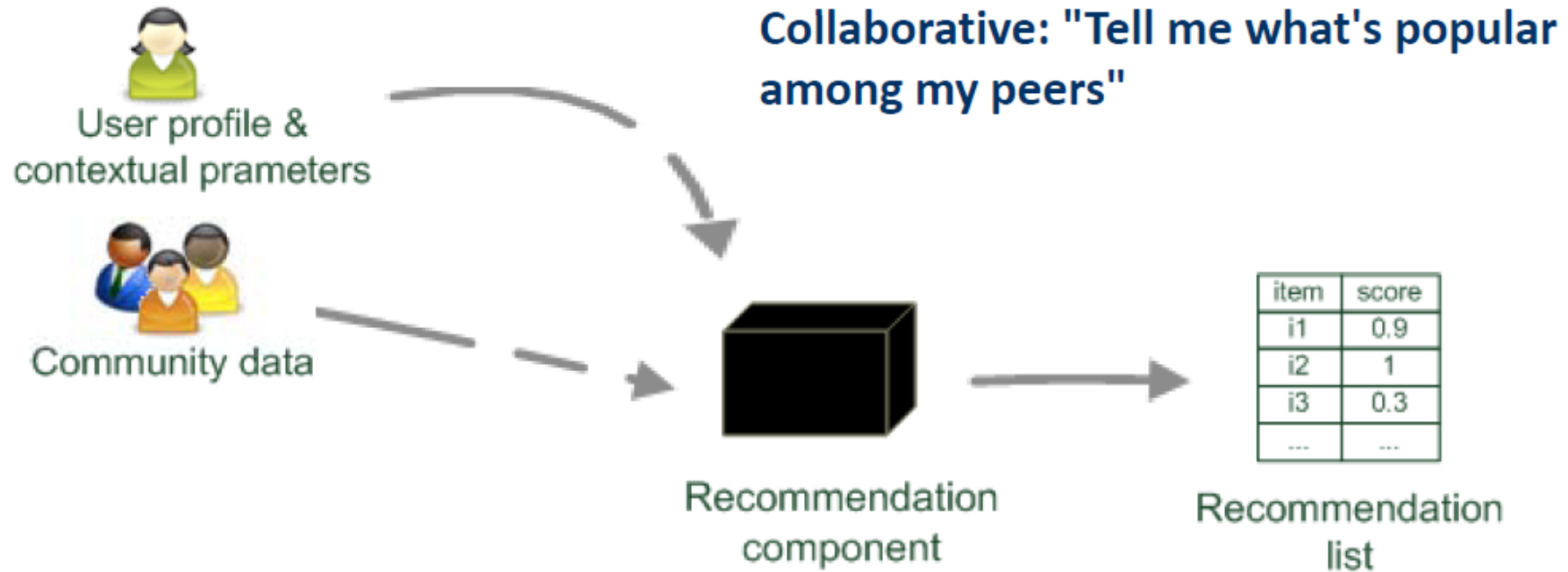


Number of papers on recsys by years

# Content-based approach



# Collaborative Filtering



# Challenges of recommender system

- The number of transactions is very small compared to the actual number of users and products
- Not enough information about new users and products
- Users and products change over time, seasonally
- Consumption habits change over time, seasonally
- Real-time recommendation

## 2. Evaluation methods

- Give
  - User set  $U$
  - Item set  $I$
- Dataset of transactions  $(u, i, r_{ui}, t)$ 
  - $u$ : user  $u \in U$
  - $i$ : item  $i \in I$
  - $r_{ui}$ : ratings of user  $u$  to item  $i$
  - $t$ : rating time



- $r_{ui}$ 
  - 5-stage scale (1, 2, 3, 4, 5)
  - Binary scale (0, 1)
- Dataset separated into train set and test set
- RS is trained on train set
- On test set, RS predict ratings  $p_{ui}$  of user  $u$  to item  $i$

|       | $i_1$ | $i_2$ | $i_3$ | $i_4$ |
|-------|-------|-------|-------|-------|
| $u_1$ | -     | 5     | 3     | -     |
| $u_2$ | 4     | -     | 2     | 3     |
| $u_3$ | 4     | 1     | -     | 5     |

|       | $i_1$ | $i_2$ | $i_3$ | $i_4$ |
|-------|-------|-------|-------|-------|
| $u_1$ | -     | 5     |       | -     |
| $u_2$ |       | -     | 2     | 3     |
| $u_3$ | 4     | 1     | -     |       |

train

|       | $i_1$ | $i_2$ | $i_3$ | $i_4$ |
|-------|-------|-------|-------|-------|
| $u_1$ | -     |       | 3     | -     |
| $u_2$ | 4     | -     |       |       |
| $u_3$ |       |       | -     | 5     |

test

- (N)MAE
- RMSE
- Ranking:
  - Precision/Recall/F-score

$$MAE = \frac{\sum_{ui} |p_{ui} - r_{ui}|}{n}$$

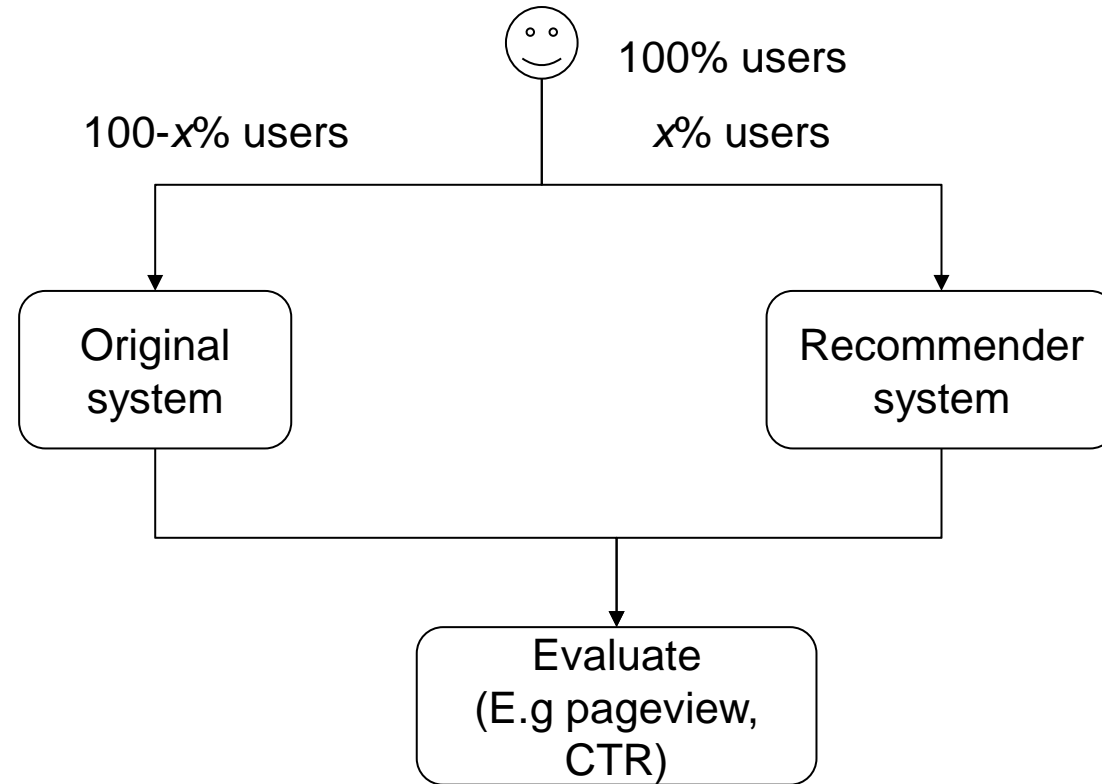
- $p_{ui}$ : prediction of model on ratings of user  $u$  to item  $i$
- $r_{ui}$ : ratings of user  $u$  to item  $i$
- $n$ : number of examples in test set

$$NMAE = \frac{MAE}{r_{max} - r_{min}}$$

- $r_{max}$ : User's maximum ratings value
- $r_{min}$ : User's minimum ratings value

$$RMSE = \sqrt{\frac{1}{n} \sum_{ui} (p_{ui} - r_{ui})^2}$$

# A/B testing

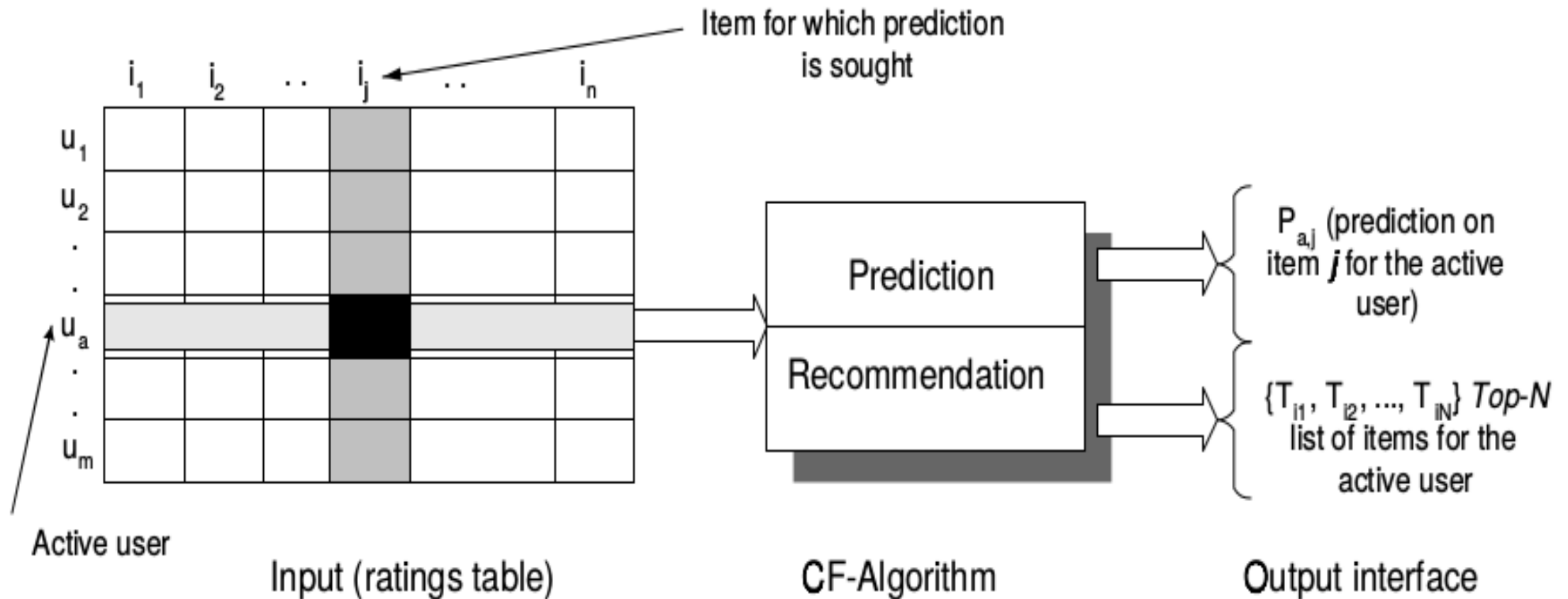


### 3. Collaborative Filtering using kNN

- Based on product user interaction matrix
- No training
- Recommend based on users
  - Find set  $V$  of similar users to user  $u$
  - Compute ratings for item  $i$  based on ratings of user in  $V$  to item  $i$



# User-based recommendation



# User similarity

- $C$ : set of item on that both user  $u$  and user  $v$  rated
- $r_u$ : Average ratings of user  $u$  (only counting for items that  $u$  rated)

$$\text{sim}(\mathbf{u}, \mathbf{v}) = \frac{\sum_{i \in C} (r_{ui} - \bar{r}_{\mathbf{u}})(r_{vi} - \bar{r}_{\mathbf{v}})}{\sqrt{\sum_{i \in C} (r_{ui} - \bar{r}_{\mathbf{u}})^2} \sqrt{\sum_{i \in C} (r_{vi} - \bar{r}_{\mathbf{v}})^2}}$$

# Predict ratings

- $V$ : top  $k$  similar users to user  $u$

$$p_{\mathbf{u}i} = \bar{r}_{\mathbf{u}} + \frac{\sum_{\mathbf{v} \in V} \text{sim}(\mathbf{u}, \mathbf{v})(r_{vi} - \bar{r}_{\mathbf{v}})}{\sum_{\mathbf{v} \in V} |\text{sim}(\mathbf{u}, \mathbf{v})|}$$

## Example ( $k = 2$ )

|       | $i_1$ | $i_2$ | $i_3$ | $i_4$ |
|-------|-------|-------|-------|-------|
| $u_1$ | 5     | 4     | 4     | 1     |
| $u_2$ | 2     | 1     |       |       |
| $u_3$ | 5     | 4     | 4     | ?     |
| $u_4$ |       | 1     | 2     | 5     |

$$\begin{aligned} r_1 &= 14/4 & \text{sim}(u_3, u_1) &= \sim 0.492 & p(u_3, i_4) &= \sim 6.67 \\ r_2 &= 3/2 & \text{sim}(u_3, u_2) &= \sim 0.948 & & \\ r_3 &= 13/3 & \text{sim}(u_3, u_4) &= \sim 0.919 & & \\ r_4 &= 8/3 & & & & \end{aligned}$$

# Disadvantages

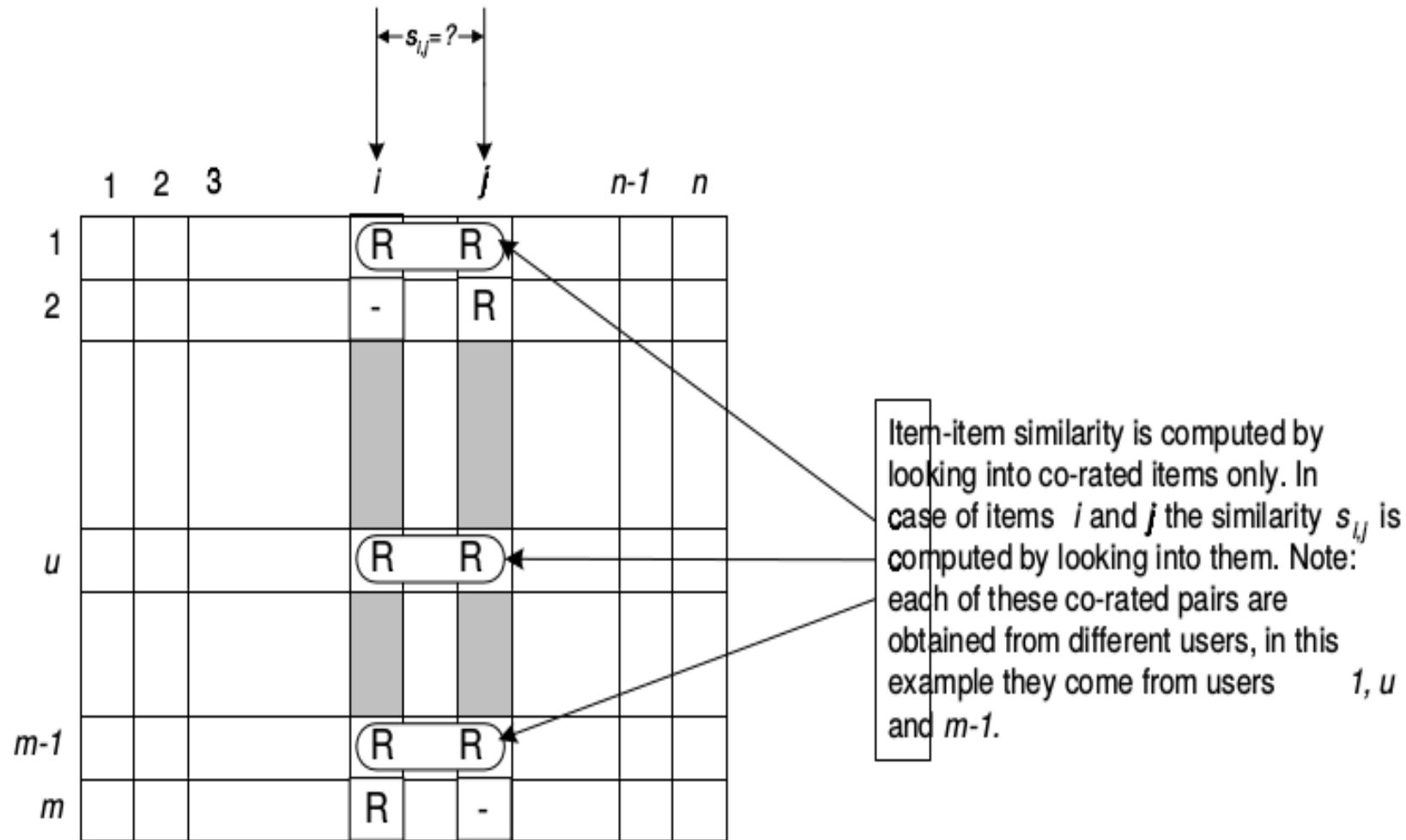
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- Regularly update the user vector when the user has a new transaction
- Requires computation on the entire set of users

# Item-based recommendation

- Product representation based on user-product interaction matrix
- Suitable for systems with product number  $\ll$  number of users
- Lower update frequency of product vectors
- Can calculate product-product similarity in advance

# Item-based recommendation



# Item similarity

- $U$ : set of users rated both item  $i$  and item  $j$

$$sim(i, j) = \frac{\sum_{\mathbf{u} \in U} (r_{ui} - \bar{r}_{\mathbf{u}})(r_{uj} - \bar{r}_{\mathbf{u}})}{\sqrt{\sum_{\mathbf{u} \in U} (r_{ui} - \bar{r}_{\mathbf{u}})^2} \sqrt{\sum_{\mathbf{u} \in U} (r_{uj} - \bar{r}_{\mathbf{u}})^2}}$$

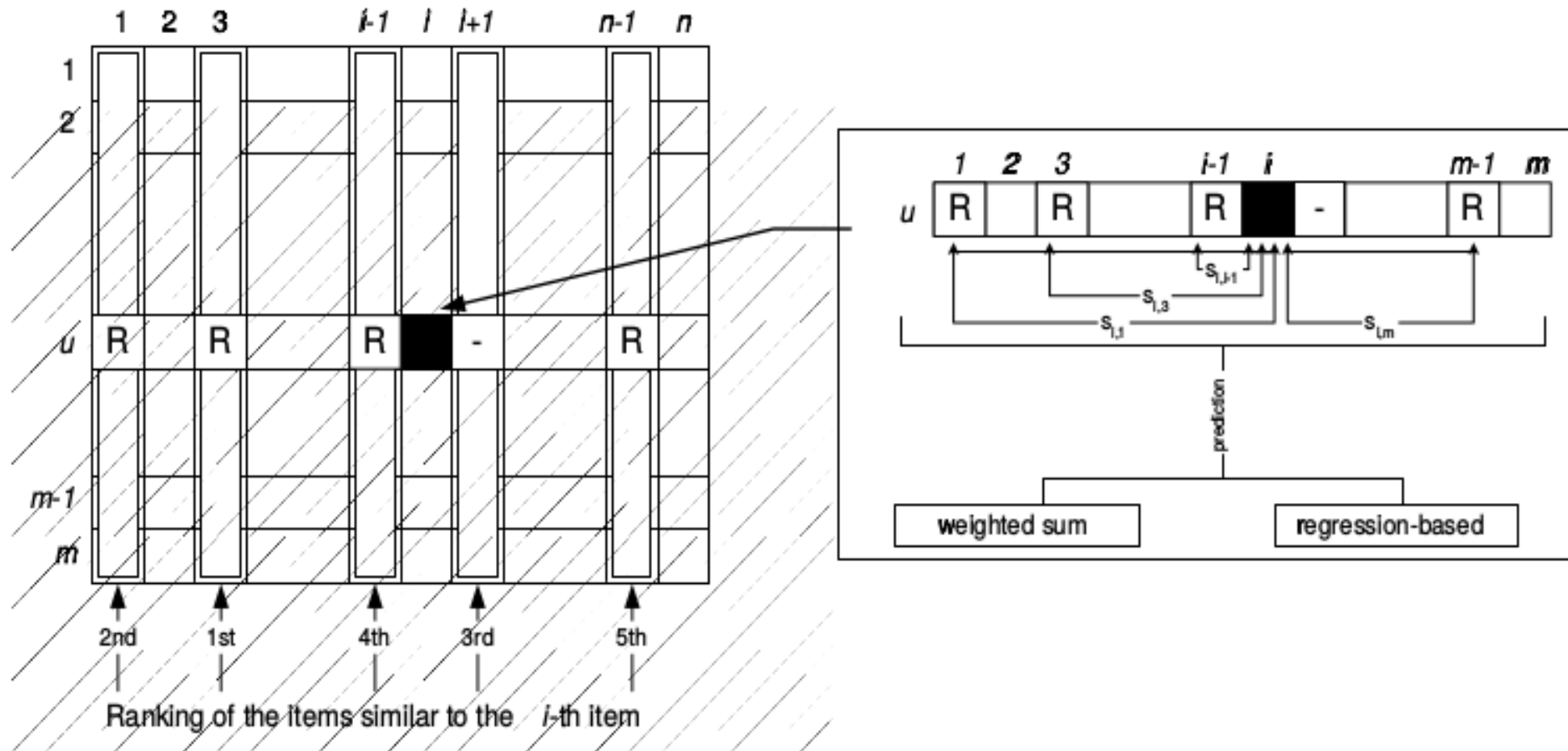


# Ratings prediction

$J$ : top  $k$  similar items to item  $i$

$$p(\mathbf{u}, i) = \frac{\sum_{j \in J} r_{\mathbf{u}, j} \times \text{sim}(i, j)}{\sum_{j \in J} \text{sim}(i, j)},$$

# Example



## 4. Collaborative Filtering using MF

- Based on the overall context of the user-product interaction
- Representing users, products in latent aspects
- Using Matrix Factorization technique
- Based on user and product vectors to make predictions

- User – movies matrix  $R$
- Factorize  $R$  into user-aspect matrix  $U$  and movies-aspect matrix  $M$
- Each user is represented by a K-dimensional vector, where K is the number of latent aspect
- Each movie is represented by a K-dimensional vector

$$R \approx U^T M . \quad r_{ij} \approx \mathbf{u}_i^T \mathbf{m}_j = \sum_{k=1}^K u_{ki} \times m_{kj} ,$$

# Ratings predictions

$$p_{ij} = \sum_{k=1}^K u_{ki} \times m_{kj} .$$

- $p_{ij}$ : predict ratings of user  $i$  to movie  $j$
- $u_i$ : User vector  $i$
- $m_j$ : movie vector  $j$

Loss function:  $e_{ij}^2$

$$e_{ij} = r_{ij} - p_{ij} .$$

- U, M is learning parameters
- R is training dataset
- Mean Square Error:  $E_{ij} = e_{ij}^2 = (p_{ij} - r_{ij})^2$
- Learning technique: Gradient Descent

Derivative of the error  
function wrt  $u_{ki}$

$$\frac{\partial (e_{ij})^2}{\partial u_{ki}} = 2e_{ij} \frac{\partial e_{ij}}{\partial u_{ki}}.$$

$$\frac{\partial e_{ij}}{\partial u_{ki}} = -\frac{\partial p_{ij}}{\partial u_{ki}}.$$

$$\frac{\partial (e_{ij})^2}{\partial u_{ki}} = 2e_{ij}(-m_{kj}) = -2(r_{ij} - p_{ij})m_{kj}.$$

Derivative of the error  
function wrt  $m_{kj}$

$$\frac{\partial (e_{ij})^2}{\partial m_{kj}} = 2e_{ij}(-u_{ki}) = -2(r_{ij} - p_{ij})u_{ki}.$$

$$u_{ki}^{t+1} = u_{ki}^t - \gamma \frac{\partial (e_{ij})^2}{\partial u_{ki}} = u_{ki}^t + 2\gamma(r_{ij} - p_{ij})m_{kj}^t.$$

$$u_{ki}^{t+1} = u_{ki}^t + 2\gamma(r_{ij} - p_{ij})m_{kj}^t,$$

$$m_{kj}^{t+1} = m_{kj}^t + 2\gamma(r_{ij} - p_{ij})u_{ki}^t.$$



# Gradient Descent (cont.)

Update  $u_{ki}$ :

$$u_{ki}^{t+1} = u_{ki}^t + \gamma(2(r_{ij} - p_{ij})m_{kj}^t - \lambda u_{ki}^t),$$

Update  $m_{kj}$ :

$$m_{kj}^{t+1} = m_{kj}^t + \gamma(2(r_{ij} - p_{ij})u_{ki}^t - \lambda m_{kj}^t).$$

$\lambda$ : regularize parameter

$\gamma$ : learning rate

## 5. Neural Collaborative Filtering

- Representing the user, product in a hidden aspect level may not fully capture the complex nature of the user-product interaction
- Deep neural networks allow automatic learning of latent aspect levels from basic to abstract
- MF is basic form of neural network

# Limitations of MF

- MF preserve similarity of user vectors
- Assume that user similarity is measured using Jaccard metric
- User vector and item vector are both represented in the K-dimensional latent aspect space

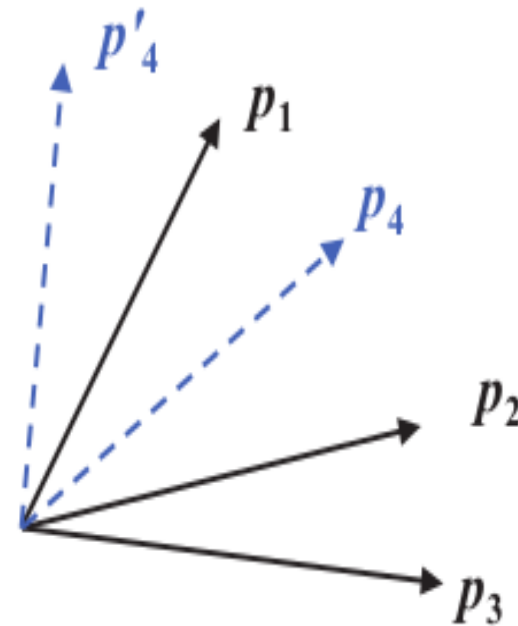
# Limitations MF (cont.)

- $s_{23} (0.66) > s_{12} (0.5) > s_{13} (0.4)$
- $s_{41} (0.6) > s_{43} (0.4) > s_{42} (0.2)$

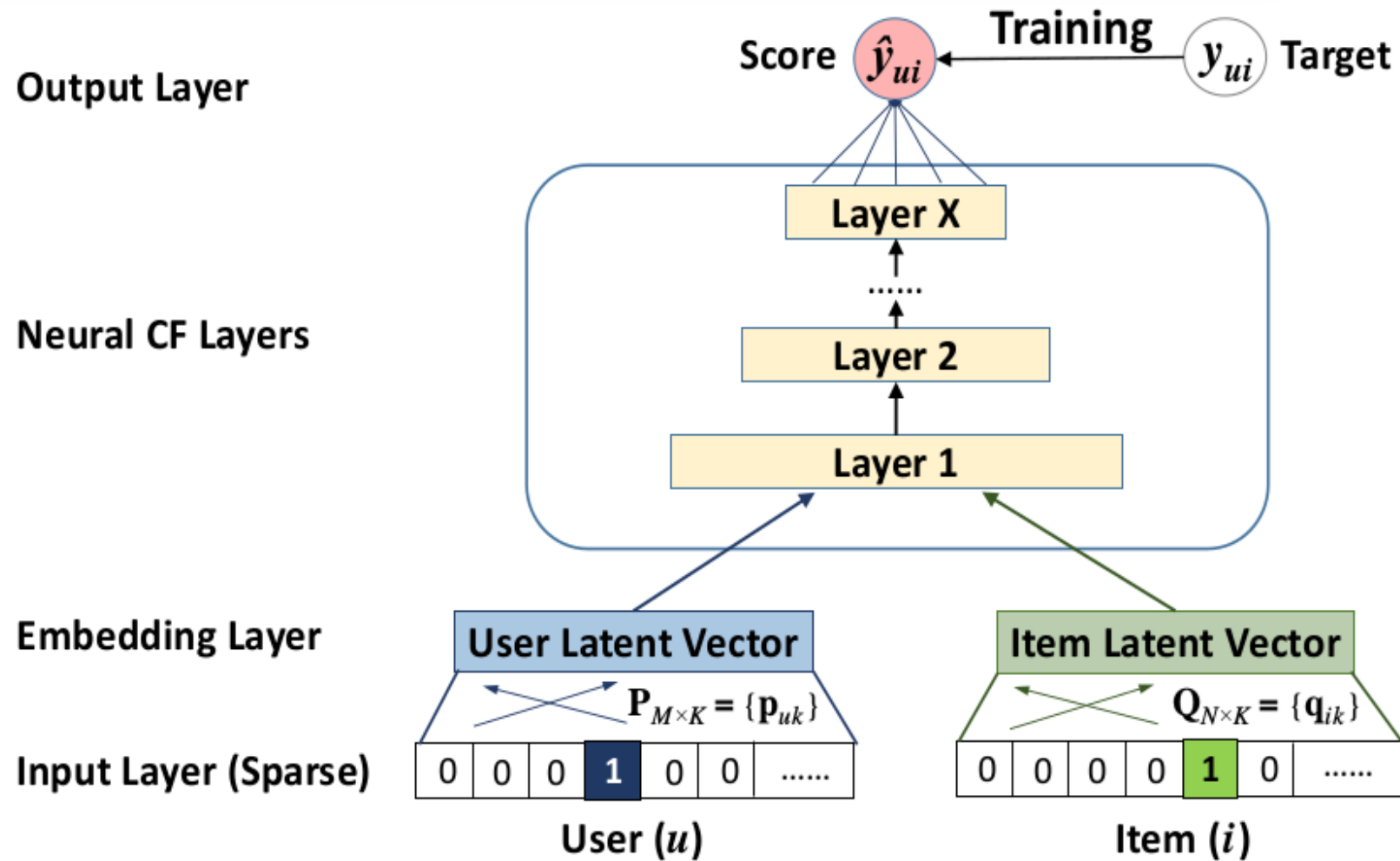
|       | $i_1$ | $i_2$ | $i_3$ | $i_4$ | $i_5$ |
|-------|-------|-------|-------|-------|-------|
| $u_1$ | 1     | 1     | 1     | 0     | 1     |
| $u_2$ | 0     | 1     | 1     | 0     | 0     |
| $u_3$ | 0     | 1     | 1     | 1     | 0     |
| $u_4$ | 1     | 0     | 1     | 1     | 1     |

↑ users

← items →



# NCF architecture



# Input layer

- The user is represented by a  $M$ -dimension one-hot vector
  - $M$  is number of users
- Item are represented by a  $N$ -dimension one-hot vector where  $N$  is the number of products

# Embedding layer

- Independently represent users and products
- $M \times K$  connection weight to represent user
- $N \times K$  connection weights to represent item
- E.g:  $K = 16$

- User and item representations are feeded into a multi-layered MLP network to learn complex user and product interactions
- E.g:
  - *ReLU* activation function
  - 3 layers with decreasing size  $32 \rightarrow 16 \rightarrow 8$



# Loss function

- Implicit feedback:
  - 1: user interacts with item
  - 0: user do not interacts with item
- Binary classification problem with probability factor
- Using the cross entropy loss function

$$- \sum_{(u,i) \in \mathcal{Y} \cup \mathcal{Y}^-} y_{ui} \log \hat{y}_{ui} + (1 - y_{ui}) \log(1 - \hat{y}_{ui}).$$

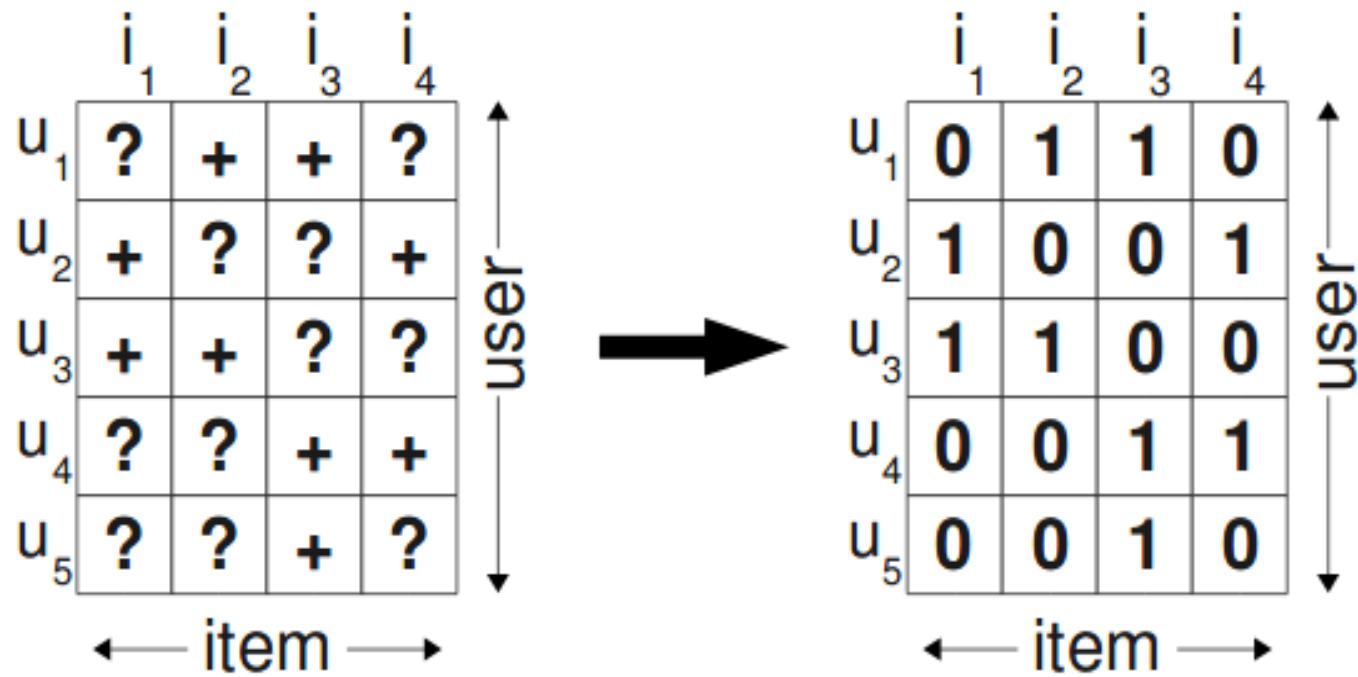
## 6. Session-based recommendation

- In many cases, it is difficult to identify users and collect reviews.
  - Small commercial websites
  - News sites
- Session-based recommendation
  - Does not require user identification
  - Each transaction, including transaction order, is used as model training data

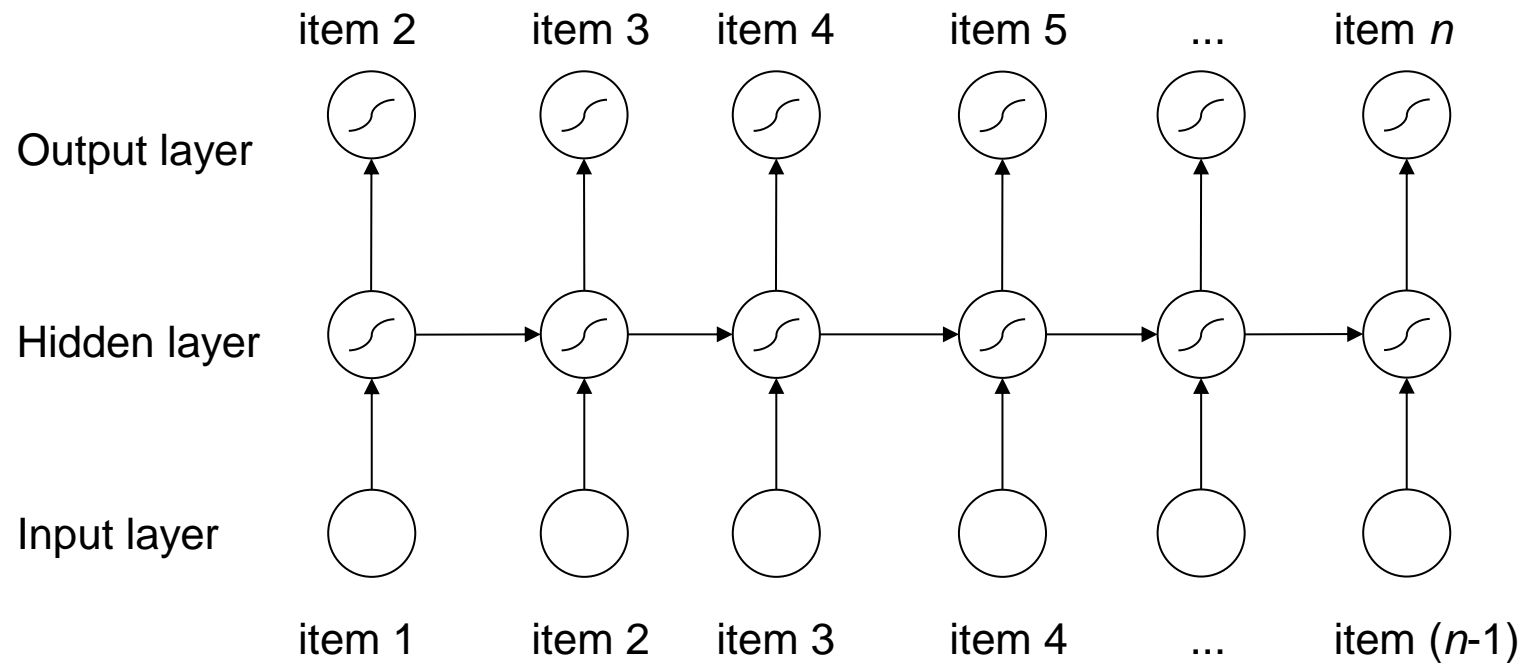
# Problem definition

- Input: Stream of items  $i_1, i_2, \dots, i_{n-1}$
- Output: suggest next item
- Given a list of products with the highest probability  $\Pr(i_n | i_1, i_2, \dots, i_{n-1})$
- Suitable for implicit feedback

# Implicit feedback



# RNN architecture



# Input layer

- Represent each item at a time  $t$  as  $V$ -dimension one-hot vector
  - 1 at position of item, otherwise 0
  - $V$ : number of distinct

# Embedding layer

- Transform one-hot into K-dimension representation
  - $K$  number of neural in embedding layer
  - Number of connection weight between input and embedding layer  $V \times K$

# Recurrent layer

- The recurrent layer stores historical information through recurrent links
- Many recurrent layer stacked together to learn high level abstract features
- Advanced model: LSTM or GRU



# MLP layer

- The output of the recurrent layer is used as the input of the MLP layer to generate the prediction
- The MLP layer can include hidden layers to learn the nonlinear function
- The MLP has  $V$  neurons corresponding to  $V$  products

# Loss function

- Pair-wise rank loss function

$$L = -\frac{1}{N} \sum_{j=1}^N \log(\sigma(\hat{r}_i - \hat{r}_j))$$

- $N$ : number of negative sample
- $\hat{r}_i$ : ratings of positive sample  $i$
- $\hat{r}_j$ : ratings of negative sample  $j$
- Implicit feedback hypothesis: item  $i$  is selected so  $i$ 's priority is higher than any other item  $j$

A large graphic on the left side of the slide. It features a dark blue background with a circular pattern of red dots of varying sizes, creating a sense of depth and movement. The word "HUST" is centered within this graphic in a bold, white, sans-serif font.

# HUST

# THANK YOU !