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Macroeconomic Approach to Point in Time Probability of Default Modeling – IFRS 9 Challenges¹

Abstract: This paper aims to present one possible retail estimation framework of lifetime probability of default in accordance with IFRS 9. The framework rests on “term structure of probability of default” conditional to given forward-looking macroeconomic dynamics. Due to the one of the biggest limitation of forward-looking modeling – data availability, model averaging technique for quantification of macroeconomic effect on default probability is explained.

Key words: IFRS 9, Term Structure of Probability of Default, Point in Time Probability of Default, Forward-looking, Macroeconomic approach, Model averaging

JEL: G11, G23, C41

Introduction

In 2014, the International Accounting Standards Board (IASB) issued the completed version of International Financial Reporting Standard 9 (IFRS 9) which under impairment requirements requires the measurement of impairment loss provisions to be based on an expected credit loss (ECL) accounting model rather than on an incurred loss accounting model. Additionally, banks were to measure the loss allowance equal to lifetime ECL for all financial instruments for which there have been significant increases in credit risk since initial recognition.

¹ The views expressed in this paper are those of the author and do not necessarily reflect those of the employer.

The key components of estimation *ECL* frameworks are term structure of probability of default (*TsPD*), loss given default (*LGD*), exposure at default (*EAD*) and dynamic state of conditional variable (e.g. macroeconomic indicators). This paper focuses on perhaps the most important component of lifetime *ECL* - *TsPD*. Even though historical information is an important anchor or base from which to measure expected credit losses, an entity is to adjust historical data such as credit loss experience on the basis of current observable data to reflect the effects of the current conditions and its forecasts of future conditions that did not affect the period on which the historical data is based, and to remove the effects of the conditions in the historical period that are not relevant to the future contractual cash flows (B5.5.52, details of these requirements can be found in IASB [2014]). Translated to the main component of the paper, this means that historical unadjusted *PD* through the cycle (*TTC PD*) should be modelled conditional to state variables, in order to forecast so called point-in-time *PD* (*PIT PD*).

Concept of *PIT PD* is not new in credit risk literature. It can be dated back to Belkin et al (1998) that proposed one-parameter representation of credit risk and transition matrices, and with the application of survival models for credit risk analysis started with the paper by Narain (1992) and, later, was developed by Carling et al (1998), Roszbach (2003), Glennon and Nigro (2005), Allen and Rose (2006), Baba and Goko (2006), and Malik and Thomas (2006).

Based on lessons learned from the financial crisis, Breeden (2010) proposed a reinvented approach for retail analytics utilizing from analysis of all available vintages simultaneously. He stated that consumer's risk of default exhibits strong lifecycle effects and decomposes vintage performance on maturation, exogenous (macroeconomic) and vintage quality effect. In response to upcoming regulatory standards, new age literature rapidly increases. Thus, Conze (2015) explores *PIT PD* modelling based on Asymptotic Single Risk Factor Model providing generalization of one-parameter model. Xu (2016) presents general framework estimation for lifetime *ECL*, discussing popular modelling strategies for the key components of this framework. Brunel (2016) provides a comprehensive survey of *PD* analytics methodology, clearly emphasizing the difference in approaches between retail and corporate analytics.

Selection of any proposed modelling technique is highly dependent on data availability. Concretely for macroeconomic *PIT PD* modelling, limitations can exist on *TTC PD* calibration side and on macroeconomic indicators availability. In situation where the ratio of data points to number of variables (macroeconomic indicators) is small, standard variable selection methods can often be misleading. This phenomenon is known as Freedman's paradox (Freedman, 1983) and cur-

rently presents one of the biggest limitations for *IFRS9* forward looking modelling. In order to overcome this problem, different statistical variations of model averaging estimators are proposed.

Lukacs et al (2010) proposed model averaging estimator based on model selection with Akaike's AIC used with linear regression. They found that the proposed model estimator reduces bias introduced while using data to select a single seemingly "best model" from a set of models employed in many predictor variables.

Similarly, Clemen (1989) and Stock and Watson (2001, 2004) undertook an extensive study across numerous economic and financial variables using linear and nonlinear forecasting models and found that, on average, pooled forecasts outperform predictions from the single best model. Timmermann (2005) exposed two main reasons for using forecast combinations. First, individual forecasts may be very differently affected by structural breaks caused, for example, by institutional change or technological developments. Some models may adapt quickly and will only temporarily be affected by structural breaks, while others have parameters that only adjust very slowly to new post-break data. The second reason is that individual forecasting models may be subject to misspecification bias of an unknown form (underlying data generating process and variable selection bias).

Finally, compliance with professional and legal regulations is not sufficient guarantee for ensuring quality of financial reporting. Ethical behavioural in the process of providing desired quality is recognized with its inescapable role (Todorović, 2018).

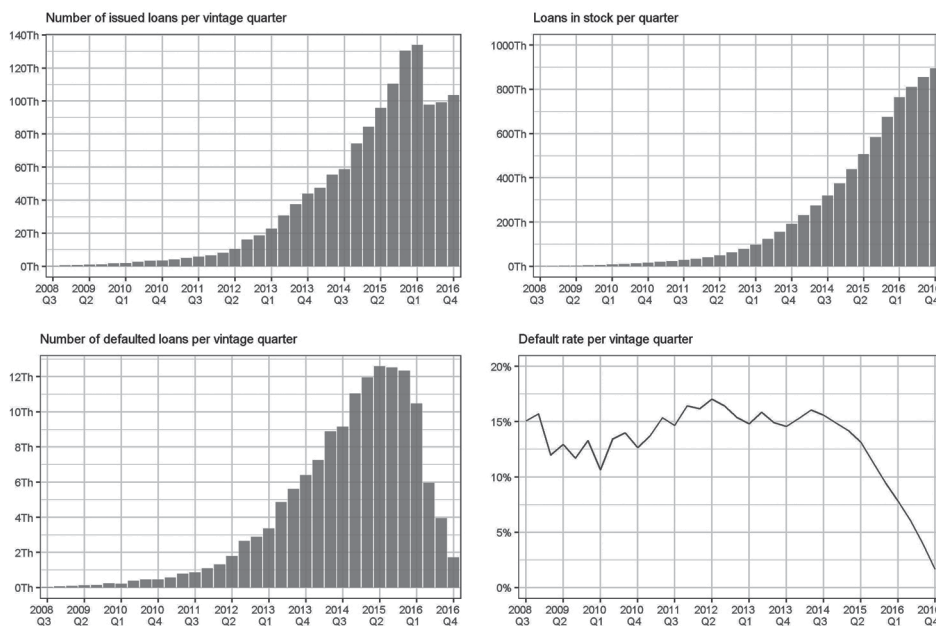
This paper provides an illustrative example of one possible approach to retail *PIT PD* statistical modelling technique for different macroeconomic scenarios. It is motivated by credit risk analysis and requirements of *IFRS 9*. The remainder of the paper is organized as follows. Section 2 presents a data description and its development over years. Section 3 and 4 present the methodology applied and empirical results. Finally, conclusions are presented.

Data description

In this article, we analysed loans issued in the period from 2008 Q3 to 2016 Q4, from the world's largest USA online credit marketplace Lending Club. Since Lending Club allows for delinquency status, all loans with current status Late (31- 120 days), Default, Charged off are marked as defaulted.

Total number of issued loans in analysed period is 1,317,974. The number of loans with defaulted status is 142,125. Figure 1 presents development of the analysed portfolio.

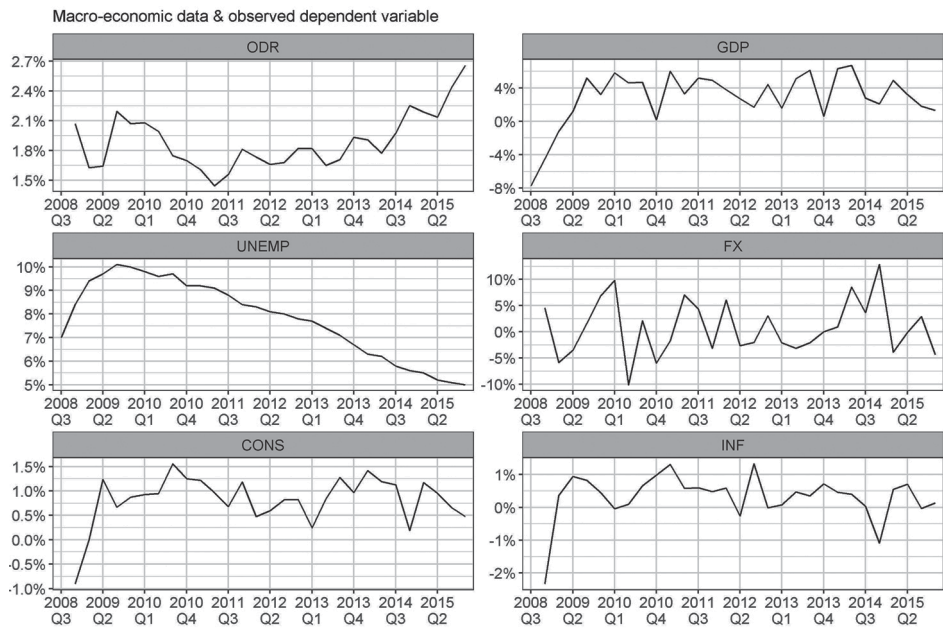
Figure 1: Modelling portfolio development



In 2016, the number of issued loans registered a decrease after a significant increase in 2015. An increase in the number of issued loans until 2016 was followed by an increase in the number of defaults but at quite steady default rate per quarter of around 14%.

The USA macroeconomic indicators used for modelling are GDP growth rate, unemployment rate, FX rate, consumption, and consumer price index. They are downloaded from Federal Reserve Economic Database (FRED) for the period from 2008 Q3 to 2016 Q4.

Quarter-on-quarter observed default rate (*ODR*) and development of macroeconomic indicators are presented in Figure 2.

Figure 2: Observed default rate and macroeconomic indicators

Methodology

TTC framework

Term structure of *PD* presents the product of two components: the conditional *PD* and the survival rate (*SR*). Conditional *PD* is calculated as the ratio between the number of defaults (*D*) and population at risk (*R*) for a certain period of time:

$$PD_t = \frac{\sum_{i=t-1}^t D_i}{R_{t-1}} \quad (1)$$

The survival rate expresses the probability that a certain loan is still at risk at any given period *t*. Depending of the *ECL* modelling approach, the survival rate can include all possible exits from the population at risk or only exits based on already defaulted accounts. We use the latter approach to calculate the survival rate employing the product-limit estimator. Survival function is given by following formula:

$$SR_t = \prod_{t_i < t} (1 - PD_{ti}) \quad (2)$$

Both parameters, PD and SR , are estimated using cohort analysis based on “loans in stock”, all loans at snapshot date that are not defaulted. Cohorts are formed on quarterly bases and $TTC\ PD$ is calculated as an average of cohorts PD for all available quarters. In total we have 36 cohorts with time window from 36 to one quarter. Tables 1 to 5 present the examples of the parameters calculation:

Table 1: Number of defaults in horizon view

Snapshot	Q1	Q2	Q3	Q4	...	Q36
2008 Q3	10	15	17	8		1
2008 Q4	12	20	25	17		
...						

Table 2: Population at risk in horizon view

Snapshot	Q1	Q2	Q3	Q4	...	Q36
2008 Q3	2000	1750	1400	1200		100
2008 Q4	2500	2350	2100	1950		
...						

Table 3: Conditional probability of default

Snapshot	Q1	Q2	Q3	Q4	...	Q36
2008 Q3	0.50%	0.86%	1.21%	0.67%		1.00%
2008 Q4	0.48%	0.85%	1.19%	0.87%		
...						

Table 4: TTCPD

Q1	Q2	Q3	Q4	...	Q36
0.49%	0.85%	1.20%	0.77%		1.00%

Table 5: TTC SR

Q1	Q2	Q3	Q4	...	Q36
100%	99.51%	98.66%	97.96%

PIT (forward-looking) framework

In the next step we adjust *TTC PD* to *PIT PD* based on changes of macroeconomic indicators. For this purpose we calibrate the “alpha” parameter which measures where we are in the credit cycle and drives how much we shift the *PIT PD* from *TTC PD* (Cheong et al, 2017):

$$ODR_q = \frac{1}{1 + \left\{ \frac{ODR_{LT}}{1 - ODR_{LT}} \right\}^{-\alpha}} \quad (3)$$

where ODR_q presents short term (quarterly) observed default rate and ODR_{LT} presents long-term default rate. The lowest possible value of the alpha parameter indicates that recent defaults significantly exceed long-term defaults and the credit cycle is in a steep downturn.

TTC PD is mapped to *PIT PD* using calculated alpha parameter for all forecasted periods:

$$PIT PD_t = \frac{1}{1 + \left\{ \frac{TTC PD_t}{1 - TTC PD_t} \right\}^{-\alpha}} \quad (4)$$

and finally, *PIT TsPD_t* given *PIT PD_t* is:

$$PIT TsPD_t = \prod_{t_i < t} (1 - PIT PD_{t_i}) * PIT PD_t \quad (5)$$

In order to obtain forecast of ODR_q we estimate linear regression models where we use the following macroeconomic indicators as independent variables: yearly GDP growth (GDP), unemployment rate (UNEMP), quarterly consumption change (CONS), quarterly change of FX rate (FX), quarterly inflation (INF). All possible linear models of one, two, and three independent variables combination, with time lags from one to four quarters, are fit. Variables are modelled in the first difference due to non-stationarity property of ODR_q (KPPS p-value 4%, PP p-value 70%, ADF p-value 96%)². If the estimated model has Durbin-Watson p-value less than 5%, heteroscedasticity and autocorrelation consistent standard errors are calculated and coefficient significance is reviewed based on this standard errors. Out of all estimated models, we selected only the models that fulfil the following criteria:

² KPPS - Kwiatkowski–Phillips–Schmidt–Shin tests, PP - Phillips–Perron test, ADF - Augmented Dickey–Fuller test

1. Estimated sign of independent variable is in line with economic expectations: GDP – negative, UNEMP– positive, CONS – negative, FX – positive, INF – positive.
2. All estimated coefficients are statistically significant at 5% significance level.
3. Shapiro-Wilk p-value test for residual normality is lower than 5%.
4. No multicollinearity exists measured by variance inflation factor less than 5.

Based on selected models and assumed forecasts of macroeconomic indicators, we forecast ODR_q for n quarters ahead. Further, we calculate the weighted average of each model forecast, following the approach of Lukacs et al (2010) except that the original AIC value is used.

Weights calculation starts with an estimate of Kullback-Leibler information loss:

$$\Delta_j = AIC_j - \min(AIC_j) \quad (6)$$

Then Akaike weight for selected model j is calculated as:

$$w_j = \frac{\exp(-\frac{1}{2}\Delta_j)}{\sum_{j=1}^R \exp(-\frac{1}{2}\Delta_j)} \quad (7)$$

Finally, weighted ODR_q is obtained:

$$\widehat{ODR}_q = \sum_{j=1}^R w_j * ODR_{q,j,t} \quad (8)$$

After we obtain ODR_q , the alpha parameter is calibrated and final *PIT PD* adjustment is done (Eq. 4).

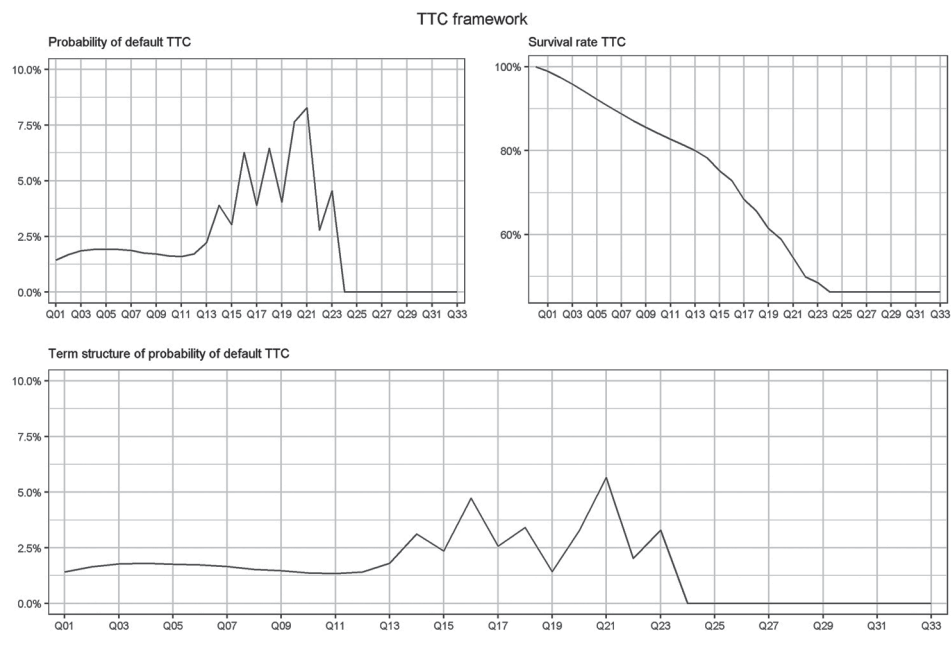
Since forecast of macroeconomic indicator is beyond the aim of this paper and for the sake of simplicity, we split data on estimation and forecasting data set. Forecasting data set consists of last four observations (four quarters of 2016) and the baseline scenario is equal to observed figures of macroeconomic indicators. Pessimistic scenario is simulated based on the last four observed figures. GDP is assumed to decrease by 1%, UNEMP increased by 20%, FX increases by 20% or remain at 0% change (depending on previous year changes), while INF increases by 20% for each quarter. Table 6 summarises assumed forecasted figures:

Table 6: Assumed macroeconomic forecasts for baseline and pessimistic scenarios

Quarter	GDP	UNEMP	FX	CONS	INF	Scenario
2016 Q1	3.70%	5.00%	2.55%	1.56%	0.34%	Base
2016 Q2	5.00%	5.00%	-0.52%	1.10%	0.41%	Base
2016 Q3	4.20%	4.80%	5.88%	1.37%	0.75%	Base
2016 Q4	3.40%	4.70%	-1.40%	0.67%	1.02%	Base
2016 Q1	-1.00%	6.00%	3.06%	1.25%	0.40%	Pessimistic
2016 Q2	-1.00%	6.00%	0.00%	0.88%	0.50%	Pessimistic
2016 Q3	-1.00%	5.76%	7.06%	1.10%	0.90%	Pessimistic
2016 Q4	-1.00%	5.64%	0.00%	0.54%	1.22%	Pessimistic

Empirical results

Figure 3 presents *TTC* parameters calibrated within framework explained in methodology section: conditional *PD*, survival rate *SR* and *TsPD*.

Figure 3: TTC framework

Due to the high prepayment rate after 11th quarter, certain noise is easy noticeable in calibrated parameters. This phenomenon confirms specificity of retail loans compared to corporate loans already noticed by Brunel (2016) and Breeden (2010). In addition to prepayment specificity, maturation effect is present as well even though conditional *PD* is calibrated based on “loans in stock”.

Out of all estimated models, only three single factor models fulfil the selected criteria and they are presented in Table 7.

Table 7: Selected candidate models

Model_ID	Coefficients	Estimate	StdError	t-value	Prt	R squared	SW p-value	AIC	DW p-value
d(ODR)-1-Model:15	lag(d(INF), -2)	0.11	0.04	2.80	0.97%	23.86%	12.09%	- 256.29	78.60%
d(ODR)-1-Model:21	lag(d(GDP), -4)	- 0.02	0.01	- 2.65	1.40%	22.64%	61.72%	- 255.19	66.80%
d(ODR)-1-Model:4	d(CONS)	- 0.17	0.07	- 2.51	1.85%	18.87%	59.94%	- 271.09	83.00%

Figures 4 and 5 present forecast of default rate as the weighted average of selected models and forecast of default rate for each model separately.

Figure 4: Forecast of observed default rate for base and pessimistic scenario

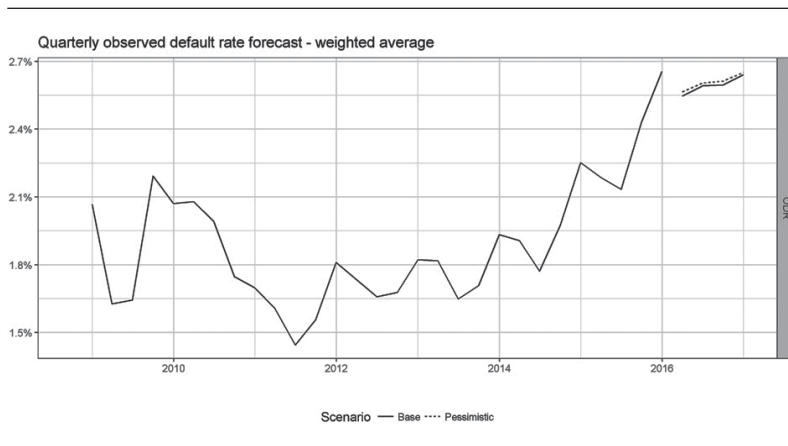
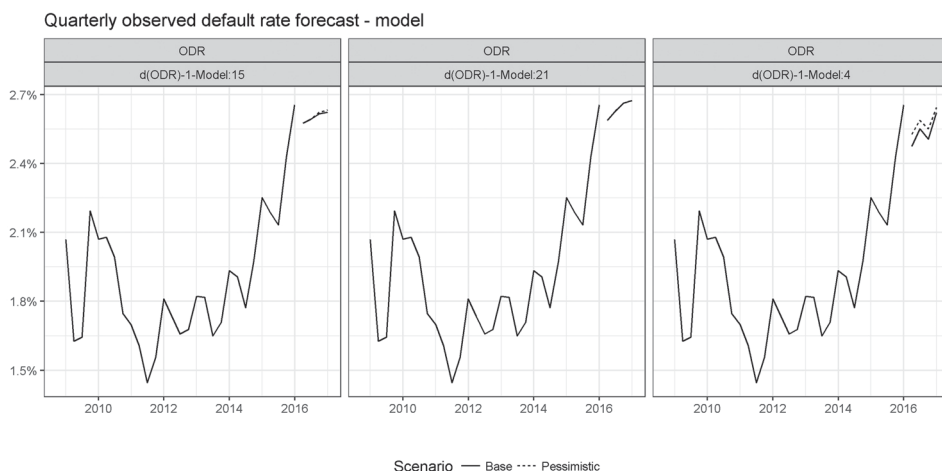


Figure 5: Forecast of observed default rate for each model and two scenarios

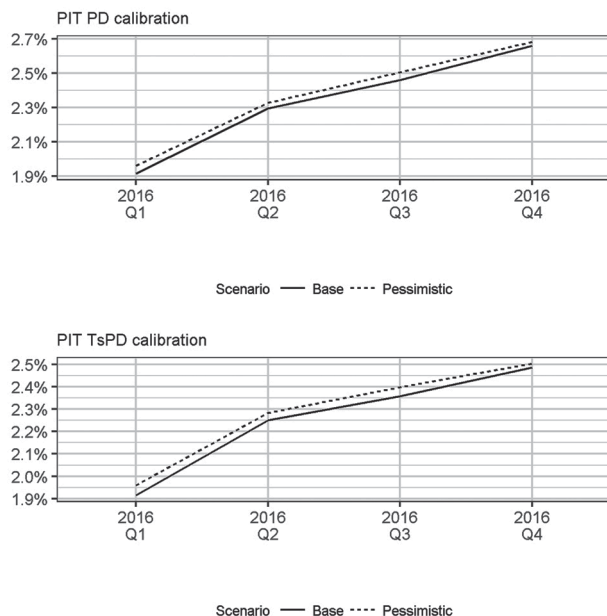
Due to the low sensitivity of ODR_q to macro environment, forecasts of both scenarios are close to each other despite the fact of assumed high change in pessimistic scenario. The main reason for this is the fast growing and changing Lending Club portfolio, so the more important effect on default rate have internal changes over macro environment.

Once the forecast of ODR_q are obtained, $PIT PD_t$ and $PIT TsPD_t$ can be calibrated. Under assumption that macro environment has the same effect on the portfolio regardless of the portfolio maturity, calibrated $PIT PD_t$ and $PIT TsPD_t$ are presented in Table 8 and Figure 6.

Table 8: $PIT PD_t$ and $PIT TsPD_t$ calibration

Scenario	Quarter	Forecast	ODRLT	alpha	TTC PD	PIT PD	PIT TsPD
Base	2016-03-31	2.48%	1.89%	0.9303	1.43%	1.92%	1.92%
Base	2016-06-30	2.55%	1.89%	0.9224	1.68%	2.29%	2.25%
Base	2016-09-30	2.51%	1.89%	0.9271	1.85%	2.46%	2.36%
Base	2016-12-31	2.62%	1.89%	0.9153	1.92%	2.66%	2.49%
Pessimistic	2016-03-31	2.53%	1.89%	0.9249	1.43%	1.96%	1.96%
Pessimistic	2016-06-30	2.59%	1.89%	0.9187	1.68%	2.33%	2.28%
Pessimistic	2016-09-30	2.55%	1.89%	0.9224	1.85%	2.50%	2.40%
Pessimistic	2016-12-31	2.65%	1.89%	0.9130	1.92%	2.68%	2.50%

Figure 6: $PIT PD_t$ and $PIT TsPD_t$ calibration based on model average approach



Conclusion

The upcoming *IFRS9* standard requires each entity to adjust historical data on the basis of current observable data to reflect the effects of the current conditions and its forecasts of future conditions. In line with that, the aim of this paper was to provide an illustrative example of one possible macroeconomic approach to retail *PIT PD* statistical modelling technique. For that purposes we used data from the world's largest USA online credit marketplace Lending Club and USA macroeconomic indicators.

We presented the modelling approach proposed by Clemen (1989), Stock and Watson (2001, 2004), Timmermann (2005) and Lukacs et al. (2010) for the situation of limited data availability and possible structural break existence. Also, we take into account the specificity of retail loans (prepayment and maturation effect) already emphasized by Brunel (2016) and Breeden (2010). These specificities are incorporated in the *TTC* calibration framework.

Finally, we found low effect of macro environment on *PD* development mainly due to fast changing marketplace and a constant increase in the number of participants on this market.

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