#### Code ▼

# Bayes Factors (BFs) in the TADA model

- Dataset
- Create a function to calculate numerical integration
- Compare between two approaches

Inside the previous version of TADA, BFs for de novo mutations (DNMs) are calculated by using a negative binomial distribution (as a Poisson distribution with a Gamma prior). This approach uses the function dnbinom inside the R language. This approach can reduce computing time, but does rely on the function dnbinom. [1]

One possible question: the way TADA uses parameters for the dnbinom in R may create an error for BFs and downstream analyses.

- To answer this question, and also to test if there are any differences in analysis results or/and possible bugs inside the package extTADA/TADA from that function, we use a traditional way to calculate BFs.

We calculate BFs by using a numerical integration approach as in Calculus 1.

```
Bayes Factors = P(X|H_1)/P(X|H_0) [2]
```

in which  $P(X|H_1 = \int Poisson(X|2N\mu\gamma)Gamma(\gamma|\bar{\gamma}\beta,\beta)d\gamma$ 

and  $P(X|H_0) = Poissson(X|2N\mu)$ .

Note: Numerical integration is an approximation, and might not be the same as analytical integration.

We will test [1] and [2] to see any differences by using some steps below.

### **Dataset**

We will use the dataset from De Rubeis et al., (2015) [1]

[1]. https://www.ncbi.nlm.nih.gov/pmc/articles/PMC4402723/ (https://www.ncbi.nlm.nih.gov/pmc/articles/PMC4402723/)

Read the data frame into R.

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#### Warning message:

R graphics engine version 14 is not supported by this version of RStudio. The Plots tab will be di sabled until a newer version of RStudio is installed.

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```
x <- read.table("test_Data_from_ASD.txt", header = TRUE, as.is = TRUE)
##https://www.nature.com/articles/nature13772#Sec9
Ntrio = 3871</pre>
```

· Print some lines of this dataset

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head(x)

Gene	mut.rate	dn.LoF
<chr></chr>	<dbl></dbl>	<int></int>

	Gene <chr></chr>	mut.rate <dbl></dbl>	dn.LoF <int></int>
1	SCN2A	0.00007400	4
2	SYNGAP1	0.00006600	5
3	CHD8	0.00009200	3
4	ARID1B	0.00009000	4
5	ANK2	0.00014923	3
6	SUV420H1	0.00003500	3
6 ro	ws		

## Create a function to calculate numerical integration

We write a function for the Gamma prior.

```
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```

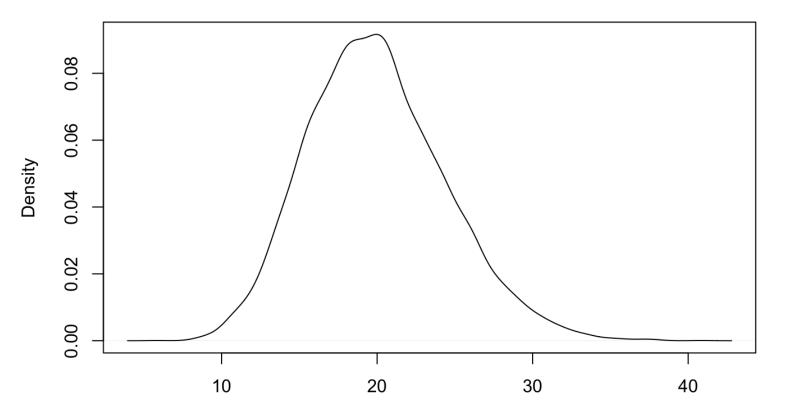
```
gamma0 = 20
beta0 = 1
f1 <- function(x.gamma){dgamma(x.gamma, shape = gamma0*beta0, rate = beta0)}

f2 <- function(x.gamma){dpois(xdn, lambda = 2*Ntrio*10^-6*x.gamma)*dgamma(x.gamma, shape = gamma0*beta0, rate = beta0)}</pre>
```

and have a look at its density distribution with parameters from the paper.

```
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```

```
xGamma <- rgamma(10000, shape = gamma0*beta0, rate = beta0)
plot(density(xGamma), main = '', xlab = '')</pre>
```



```
gammaMin = min(xGamma)
gammaMax = max(xGamma)
```

## Compare between two approaches

We will test [1] and [2] by using three examples.

## Example 1

• We test for X = 0.

```
##numerical integration
xdn = 0
(dpois(xdn, lambda = 2*Ntrio*10^-6*gamma0)*integrate(f1, gammaMin, gammaMax, subdivisions = 200L)
$value)/dpois(xdn, lambda = 2*Ntrio*10^-6)
```

```
[1] 0.8631131
```

```
gamma0 = 20
beta0 = 1
mu0 = 10^-6
fM1 <- function(x.gamma){dpois(xdn, lambda = 2*Ntrio*mu0*x.gamma)*dgamma(x.gamma, shape = gamma0*b eta0, rate = beta0)}
integrate(fM1, gammaMin, gammaMax, subdivisions = 200L)$value/dpois(xdn, lambda = 2*Ntrio*mu0)</pre>
```

```
[1] 0.8636426
```

```
[1] 0.8637243
```

### Example 2

• We test for X=2.

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```
##numerical integration

xdn = 2

fM1 <- function(x.gamma){dpois(xdn, lambda = 2*Ntrio*mu0*x.gamma)*dgamma(x.gamma, shape = gamma0*b eta0, rate = beta0)}

integrate(fM1, gammaMin, gammaMax, subdivisions = 200L)$value/dpois(xdn, lambda = 2*Ntrio*mu0)</pre>
```

```
[1] 357.0694
```

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```
[1] 357.2117
```

## Example 3

We test for all genes from the dataset.

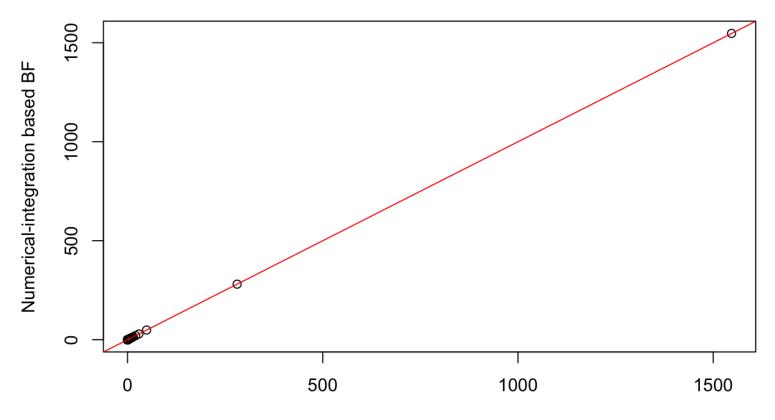
```
##numerical integration

x.bf.numericalIn <- apply(data.frame(x$mut.rate, x$dn.LoF), 1, function(y){

fM1 <- function(x.gamma){dpois(y[2], lambda = 2*Ntrio*y[1]*x.gamma)*dgamma(x.gamma, shape = gamm a0*beta0, rate = beta0)}
   integrate(fM1, gammaMin, gammaMax, subdivisions = 200L)$value/dpois(y[2], lambda = 2*Ntrio*y[1])
})</pre>
```

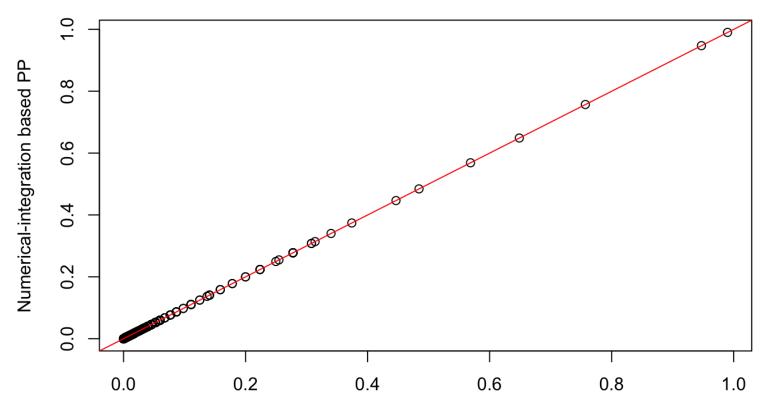
Compare between the two methods.

```
plot(x.bf, x.bf.numericalIn, xlab = 'Analytical-integration based BF (Negative binomial distribution)', ylab = 'Numerical-integration based BF') abline(a = 0, b = 1, col = 'red')
```



Analytical-integration based BF (Negative binomial distribution)

```
plot(x.pp, x.pp.numericalIn, xlab = 'Analytical-integration based PP (Negative binomial distributi
on)', ylab = 'Numerical-integration based PP')
abline(a = 0, b = 1, col = 'red')
```



Analytical-integration based PP (Negative binomial distribution)

Gene <chr></chr>	x.pp <dbl></dbl>	x.pp.numericalIn <dbl></dbl>
2 SYNGAP1	0.9471226	0.9471223
7 DYRK1A	0.9899745	0.9899744
2 rows		

Those results are similar, especially for posterior probability > 0.6.