## A Note on The Dynamic Effects of Supply and Demand Shocks in the Crude Oil Market

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## Online Appendix

## A Prior distribution

Let  $\Theta = \{\theta_{1:k,0}, \Sigma_{\theta,1:k}, \Sigma_{h,1:k}, \theta_{1:k,1:T}, \mathbf{h}_{1:k,0:T}\}$  be the parameter set of the hybrid TVP-VAR model. We assume vague but proper prior distributions. For example, the prior for the degree of freedom is  $\nu_i \sim \mathcal{G}(2,0.1)$ . The prior for the variance of shock to the volatility and time-varying parameters are  $\sigma_{h,1:k}^2 \sim \mathcal{G}(\frac{1}{2},\frac{1}{2\mathbf{V}_h})$  and  $\sigma_{\theta,1:k}^2 \sim \mathcal{G}(\frac{1}{2},\frac{1}{2\mathbf{V}_\theta})$  where  $\mathbf{V}_h = \mathbf{V}_\theta = 1$ , this prior is less influential in comparison to the conjugated inverse gamma prior especially when the true value is small. The priors of the initial volatility and  $\mathbf{h}_0$  and initial regression coefficients  $\theta_{i,0}$  are  $\mathbf{h}_0 \sim N(\mathbf{a}_{h_0}, \mathbf{V}_{h_0})$  where  $\mathbf{a}_{h_0} = \log \hat{\Sigma}_{OLS}$  is the estimated residual variance of a univariate AR(p) model using the ordinary least square method, and  $\mathbf{V}_{h_0} = 4\mathbf{I}_k$ , see Clark (2011);  $\theta_{0,i}$  follows a Minnesota prior with the overall shrinkage  $l_1 = 0.2$  and the cross-variable shrinkage  $l_2 = 0.5$ , see Koop and Korobilis (2010).

## References

- T. E. Clark. Real-time density forecasts from Bayesian vector autoregressions with stochastic volatility. *Journal of Business and Economic Statistics*, 29(3):327–341, 2011.
- G. Koop and D. Korobilis. Bayesian multivariate time series methods for empirical macroeconomics. Now Publishers Inc, 2010.