

Economic Order Quantity

Reference: Hopp, Wallace J., and Mark L. Spearman. Factory physics. Waveland Press, 2011.

Economic order quantity (EOQ) expresses the fundamental tradeoff between setup costs and holding costs. Small lot sizes have large setup costs per unit, but large lot sizes incur holding costs.

The variables are:

```
D = Variable("D", "count/year", "Demand rate")
c = Variable("c", "USD/count", "per unit production cost")
A = Variable("A", "USD", "setup cost")
h = Variable("h", "USD/count/year", "holding cost")
Q = Variable("Q", "count", "lot size")
Y = Variable("Y", "USD/year", "cost per year")
```

The cost per year is simply the sum of holding, setup, and production costs,

$$Y(Q) = \frac{hQ}{2} + \frac{AD}{Q} + cD$$

Or in gpkit,

```
from gpkit.constraints.set import ConstraintSet
eoq = ConstraintSet([Y >= h*Q/2 + A*D/Q + c*D])
```

Now create a model that minimizes cost and substitute in the values given in Factory Physics.

```
from gpkit import Model, units
m = Model(Y, [eoq])
m.substitutions.update({D: 1000, # /units("year"),
                        c: 250, # *units("USD"),
                        A: 500, # *units("USD"),
                        h: 35}) # *units("USD/year"))

sol = m.solve()
# would like to assert here that
# sol.subinto((2*A*D/h)**0.5 == sol.subinto(Q)
```

Cost — 2.559e+05 [USD/year]

Free Variables	Value	Units	Description
Q	169	[count]	lot size
Y	2.559e+05	[USD/year]	cost per year

Constants	Value	Units	Description
A	500	[USD]	setup cost

D	1000	[count/year]	Demand rate
c	250	[USD/count]	per unit production cost
h	35	[USD/count/year]	holding cost

Sensitivities	Value	Units	Description
D	0.9884		Demand rate
c	0.9769		per unit production cost
h	0.01156		holding cost
A	0.01156		setup cost

Now sweep Q to see the tradoff curve from Factory Physics

```
import numpy as np
m.substitutions.update({
    Q: ("sweep", np.logspace(np.log10(10), np.log10(500), 25)))
sol = m.solve()
```

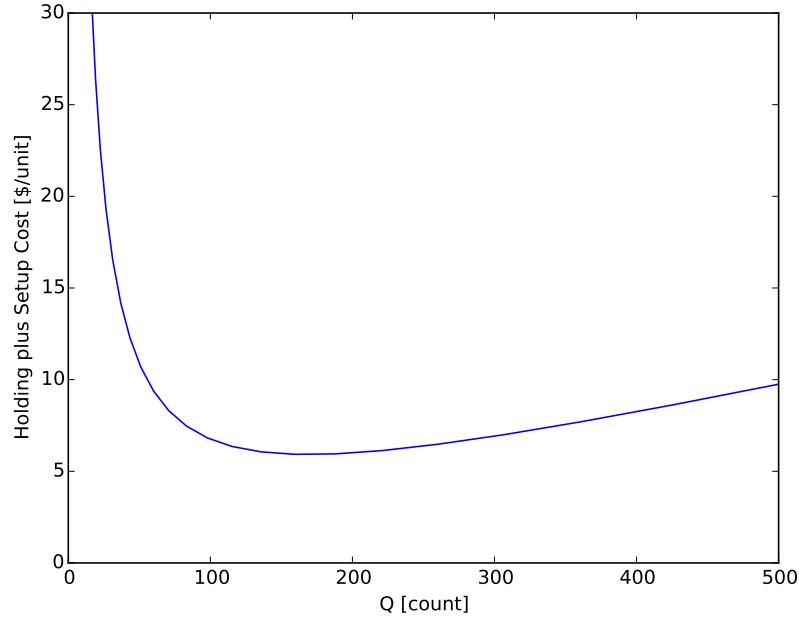


Figure 1: Cost vs Order Quantity