

Lecture 15 Conformational Equilibrium



v_i

$$\Delta \bar{G}_{rxn} = \bar{G}_{products} - \bar{G}_{reactants}$$

$$\Delta \bar{G}_{rxn} = \sum_i v_i \mu_i \quad (@ \text{ const } P, T)$$

$$\mu_i = \mu_i^\circ + RT \ln [i]$$

$$\Delta \bar{G}_{rxn} = \Delta \bar{f}_{rxn}^\circ + RT \ln Q \quad \leftarrow Q = \prod_i [i]^{v_i}$$

$$Q = \prod_i [i]^{v_i} = [A]^{\nu_A} [B]^{\nu_B} [C]^{\nu_C} \dots$$

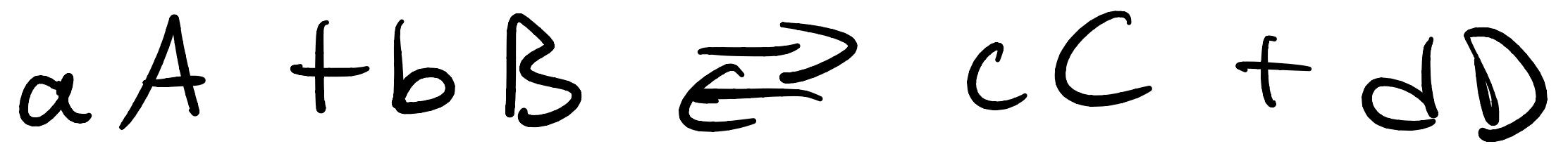
$$\ln(\pi) = \sum \ln$$

$$@ \text{Eq} \quad \Delta \bar{G}_{rxn}^{\circ} = 0$$

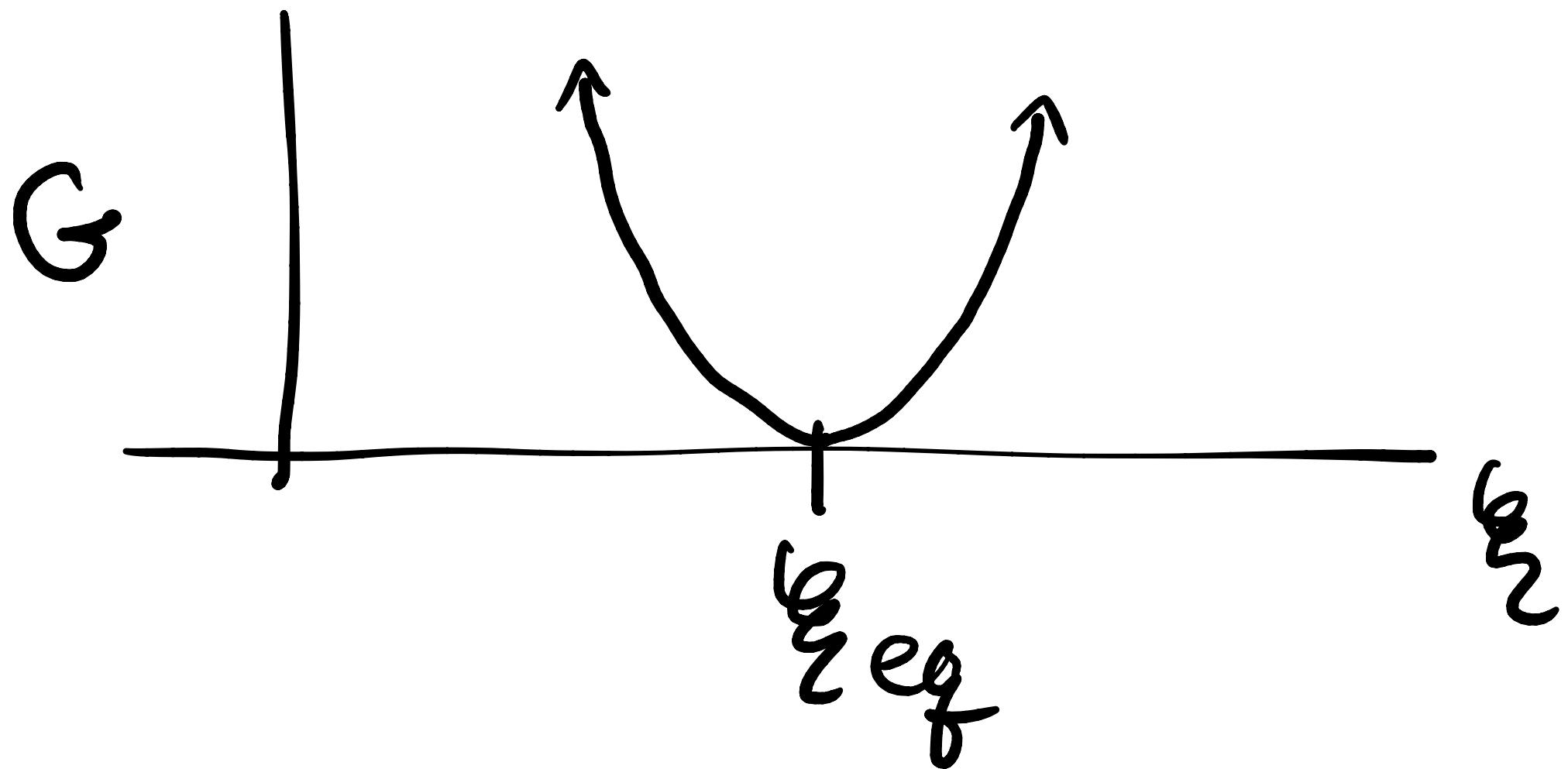
$$\Delta \bar{G}^{\circ} = -RT \ln(K_{eq})$$

$$\Delta \bar{G}_{rxn} = \Delta \bar{G}^{\circ} + RT \ln Q$$

$$= -RT \ln K + RT \ln Q = RT \ln(Q/K_{eq})$$



$$a\dot{\xi} = b\dot{\xi} = -c\dot{\xi} = -d\dot{\xi}$$



$$A \geq 2B$$

IM OM

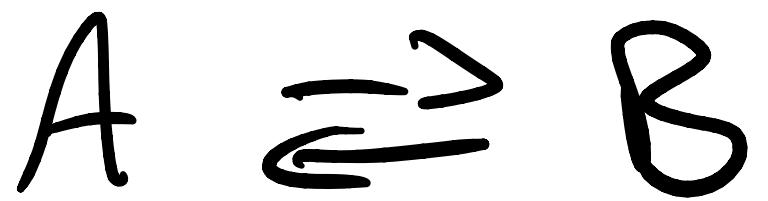
IM - x OM + 2x

know K_{eq}

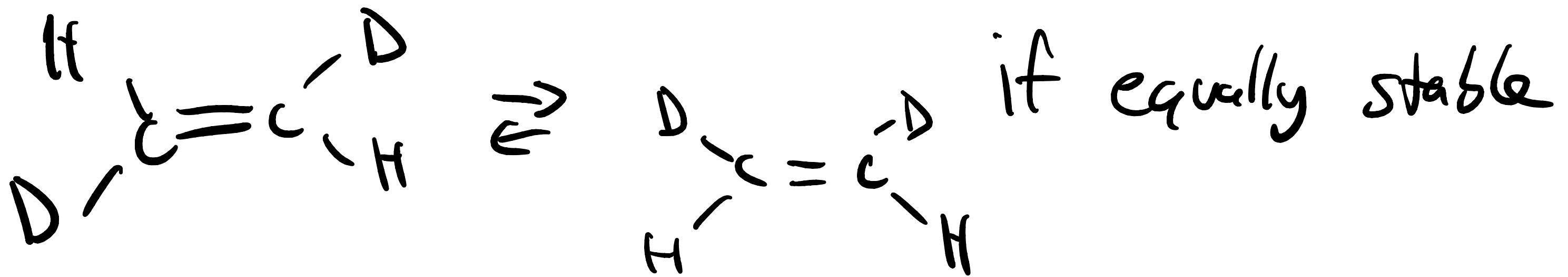
$$K_{eq} = \frac{(2x)^2}{1-x} \Rightarrow K - Kx = 4x^2$$

$$4x^2 + Kx - K = 0$$

$$x = \frac{-K \pm \sqrt{K^2 + 16K}}{8}$$



$$K(T,P) = \frac{[B]}{[A]} = 1$$



$$\frac{x}{1-x} = 1$$

$$x = 1 - x$$

$$2x = 1 \Rightarrow x = \frac{1}{2}$$

Dependence on temperature

$$-RT \ln(K_{eq}) = \bar{\Delta G}^\circ = \bar{\Delta H}^\circ - T \bar{\Delta S}^\circ$$

diff btwn

Reactants & products

$\bar{\Delta H} < 0$

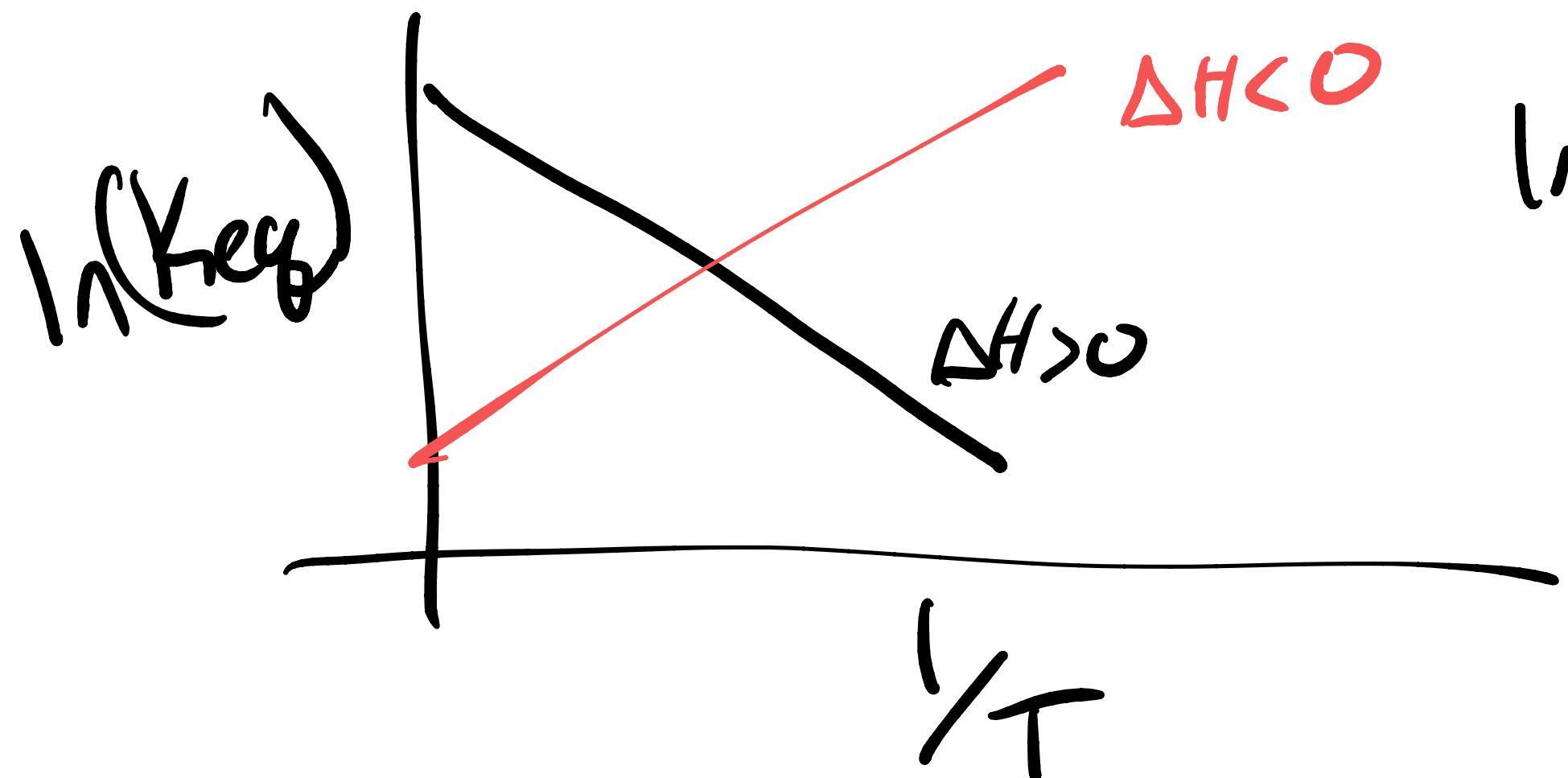
diff in entropy

Exothermic reaction if heat is produced

Endothermic reaction, $\bar{\Delta H} > 0$

$$\ln(K_{eq}) = \frac{\bar{\Delta S}^\circ}{R} - \frac{\bar{\Delta H}^\circ}{k_B T}$$

Vant Hoff
Equation



$$\ln K = \frac{\bar{S}}{R} - \frac{\bar{H}}{R} \cdot \left(\frac{1}{T}\right)$$

(no phase transition)



$A \geq B$
water ice

Dependence on pressure

$$d(\Delta G_{\text{rxn}}) = -\bar{\Delta S} dT + \bar{\Delta V} dP$$

$$\bar{\Delta V}^{\circ} = \left(\frac{\partial \Delta G^{\circ}}{\partial P} \right)_T \quad (\text{standard cond.'ns})$$

$$\Delta G^{\circ}(P) = \Delta G^{\circ}(P^{\text{ref}}) + (P - P^{\text{ref}}) \bar{\Delta V}^{\circ}$$

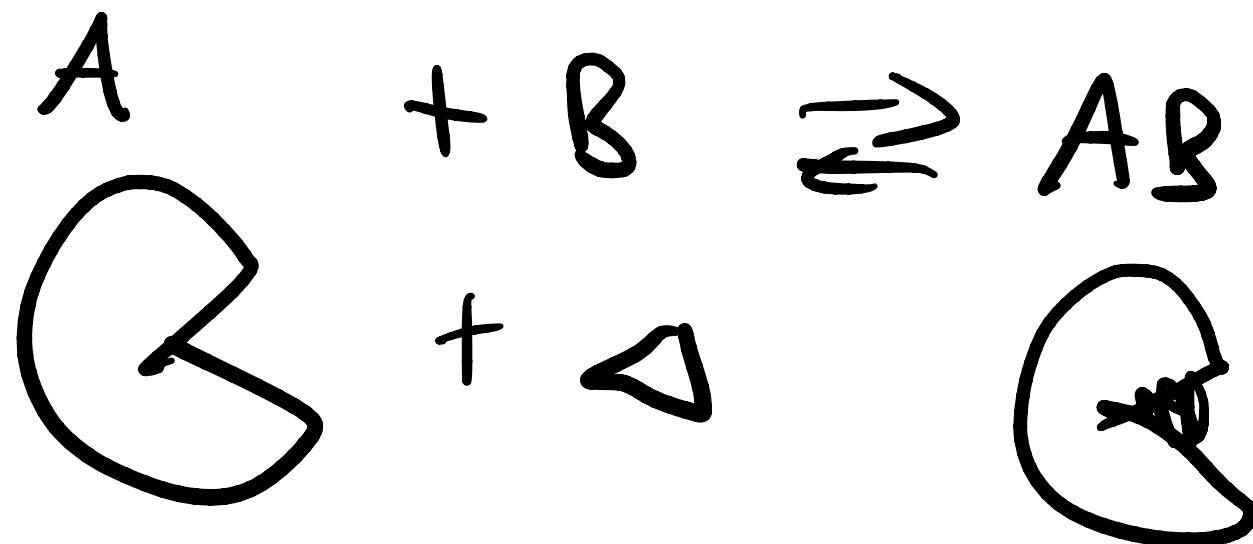


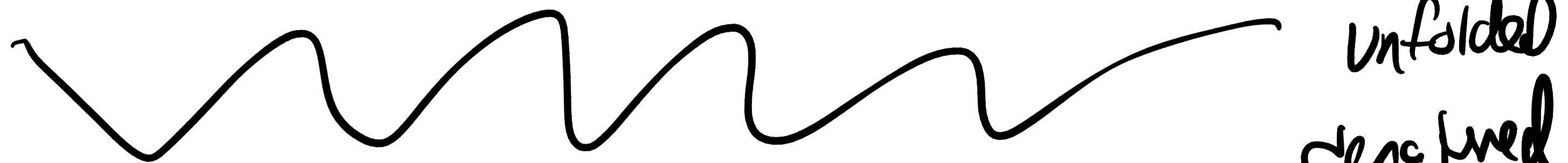
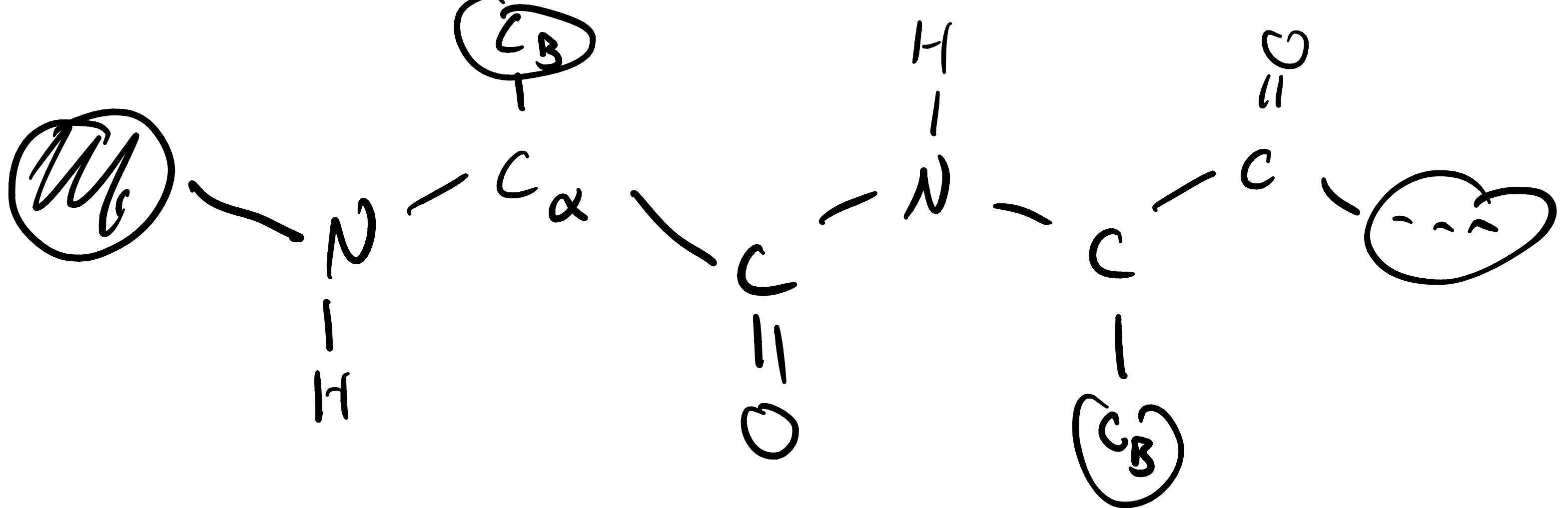
$$-RT \ln K_{\text{eq}}(P) = -RT \ln K_{\text{eq}}(P^{\text{ref}}) + (P - P^{\text{ref}}) \bar{\Delta V}^{\circ}$$

Conformational Equilibrium

$$A \rightleftharpoons B$$

Example: folded & unfolded state
of a protein





$\Delta H < 0$

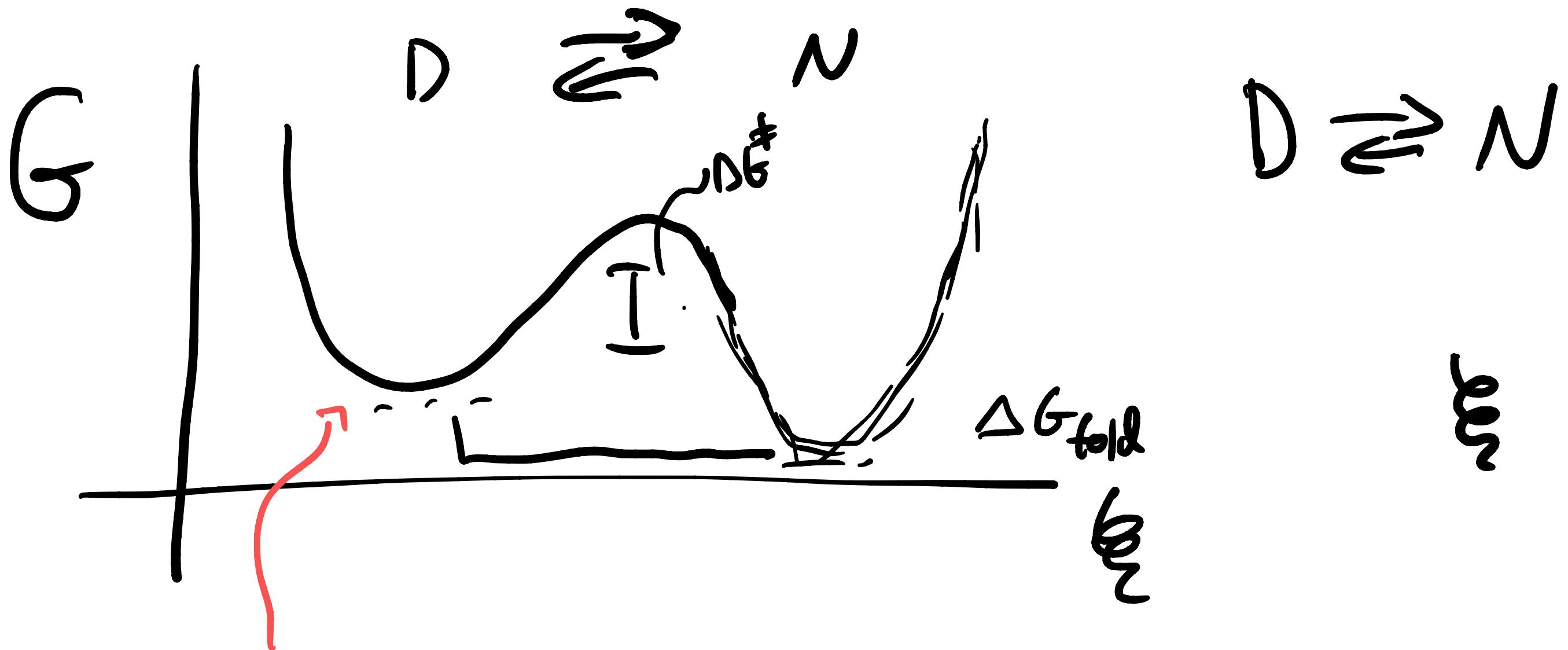
α Helix

$\Delta S < 0$ usually

ΔG folding ~ -10 kcal/mol

$U \geqslant$ Folded
 $D_{\text{denatured}} \geqslant$ Native
(@ room temp)

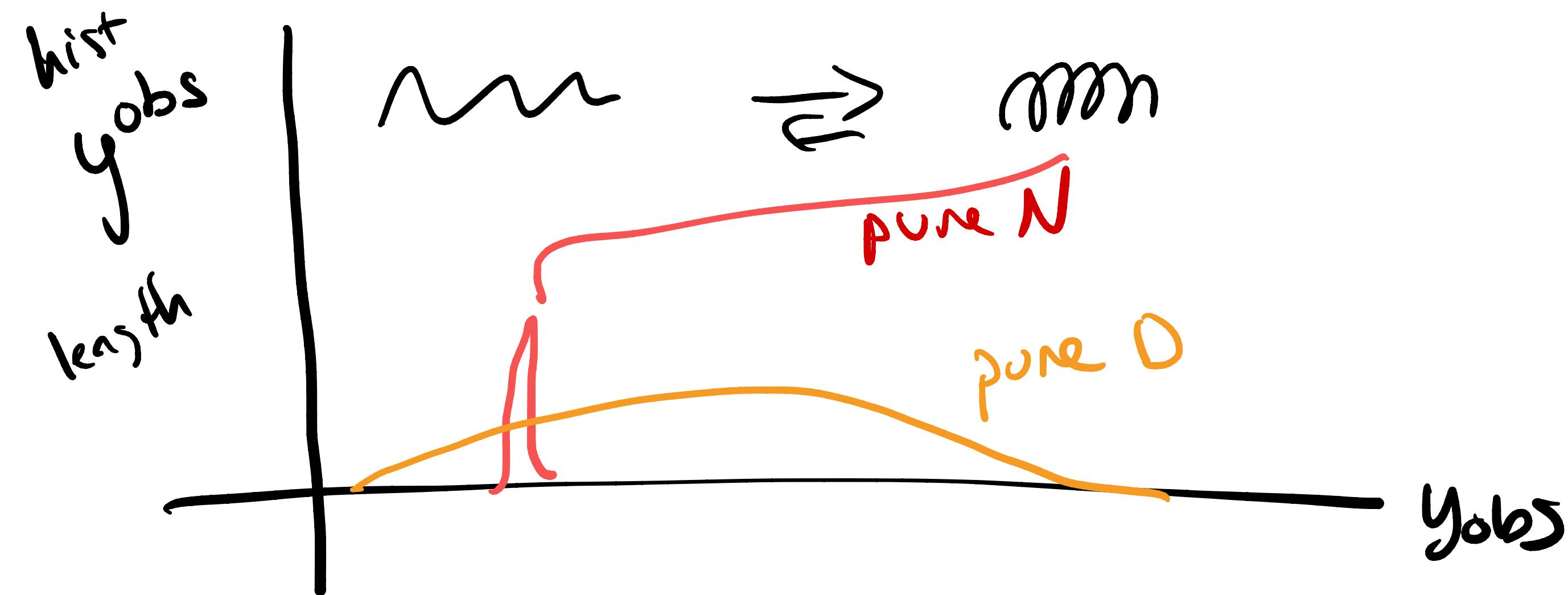
How to measure ΔH_{fold} , $\Delta S_{\text{folding}}$



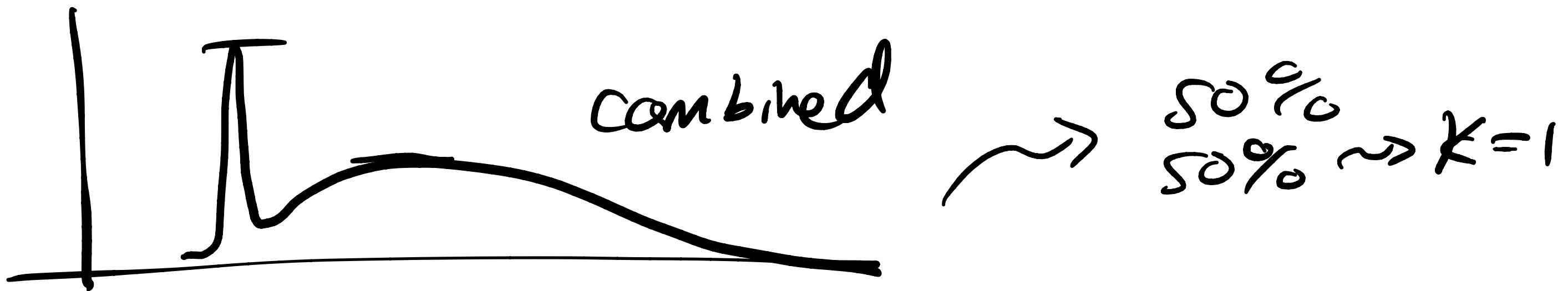
"metastable" $\xrightarrow{-10 \text{ kcal/mole}}$

$$K_{eq} = e^{-\frac{\Delta G^\circ}{kT}}$$

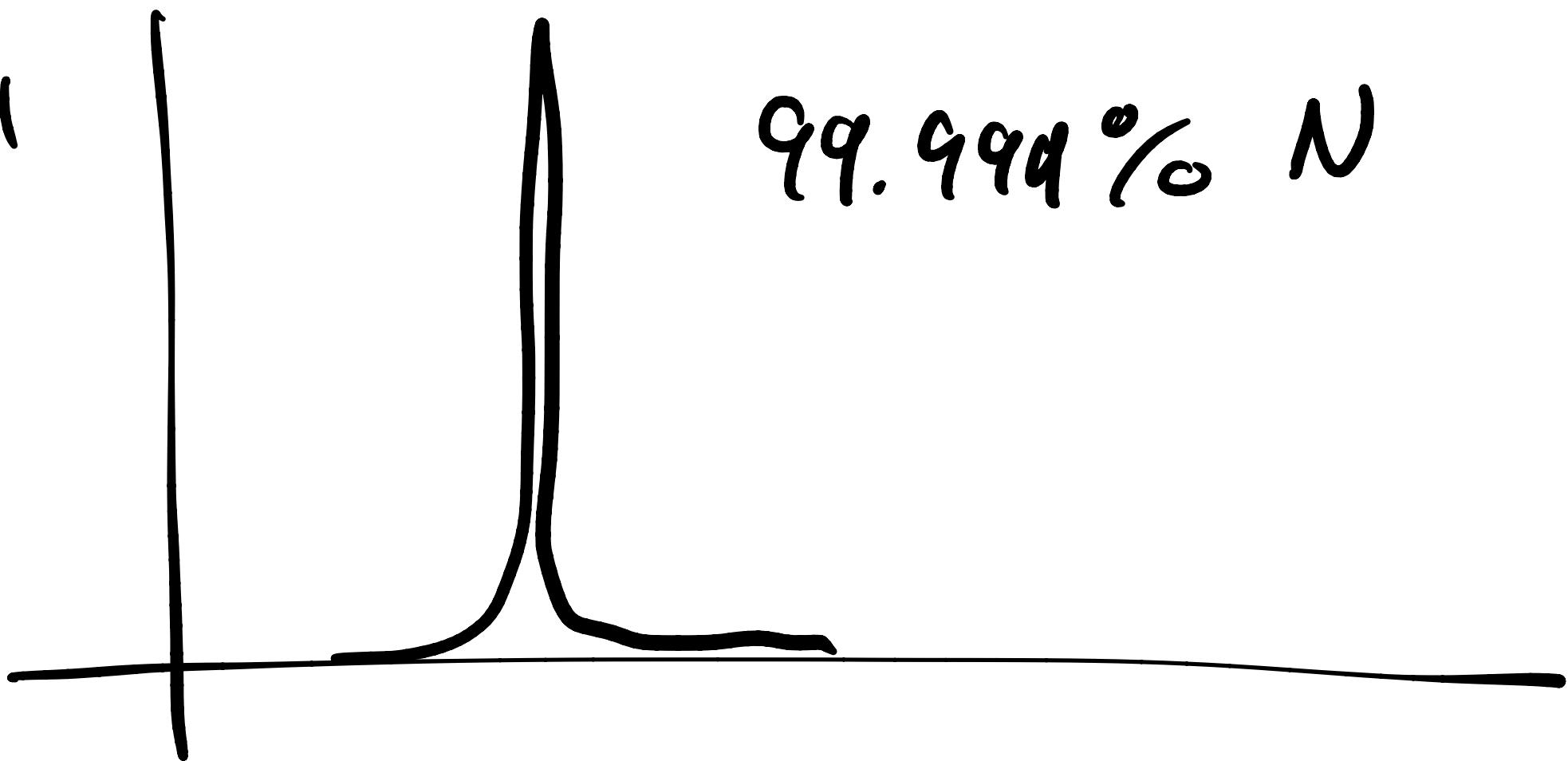
$\xrightarrow{0.6 \text{ kcal/mole}}$



If 50/50 mixture



typical



how can we tell 98 from 99
from 99.9

Key is change conditions

