HWZ- Glen Hocky
(1) Garma function

$$\Gamma(z) = \int_{0}^{\infty} x^{z-1} e^{-x} dx$$

a)
$$M(1) = \int_{0}^{\infty} x^{0} e^{-x} dx = \int_{0}^{\infty} e^{-x} dx$$

= $-e^{-x} \int_{0}^{\infty} e^{-x} dx$

b)
$$\Pi(z+1) = \int_{0}^{\infty} x^{z} e^{-x} dx$$

$$= -x^{z} e^{-x} \Big|_{0}^{\infty} + \int_{0}^{\infty} e^{-x} \cdot z \cdot x^{z-1} dx = z \cdot x^{z-1} \Big[\int_{0}^{\infty} u dv = uv - \int_{0}^{\infty} v dv \Big]$$

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$$= > S_{d-1} = \frac{1}{2} \prod_{d/2} (d/2) \cdot S_{d-1}$$

$$= > S_{d-1} = 2\pi^{d/2}$$

$$= \sum_{d/2} \prod_{d/2} (d/2)$$

$$|V| \qquad V_{d} = \frac{S_{d-1}}{d}$$

$$= \frac{R^{d/2}}{d \Gamma(d/2)} = \frac{R^{d/2}}{(d/2) \Gamma(d/2)} = \frac{R^{d/2}}{\Gamma(d/2) \Gamma(d/2)}$$

$$|\Gamma(k)| = \int_{0}^{\infty} dx e^{-x} + \frac{1}{2}$$

$$= \frac{R^{d/2}}{R^{d/2}} = \frac{R^{d/2}}{R^{d/2}} = \frac{R^{d/2}}{R^{d/2}}$$

$$|\Gamma(k)| = \int_{0}^{\infty} dx e^{-x} + \frac{1}{2} = \int_{0}^{\infty} 2r dr e^{-r^{2}} = \frac{1}{2}$$

$$= \frac{R^{d/2}}{R^{d/2}} = \frac{R^{$$

3) Microconstant ideal gas

$$S(N, v, E) = \frac{E_0 V}{h^{3N} N!} \int_{-D_0}^{\infty} dy^3 N S\left(\frac{3v}{2} \frac{p^2}{km} - E\right)$$
 $= \frac{E_0 V}{h^{3N} N!} \int_{-D_0}^{3N/2} dy^3 N S\left(\frac{2v}{2} \frac{p^2}{km} - E\right)$
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b)
$$\int_{0}^{\infty} S(r^{2}-\epsilon)r^{2} = \frac{1}{2\sqrt{\epsilon}} \cdot \left(\int_{0}^{\infty} (r-\sqrt{\epsilon})r^{2} + \int_{0}^{\infty} (r+\sqrt{\epsilon})r^{2}\right)$$

$$= 0, -\sqrt{\epsilon} \text{ outside raye}$$

$$SO \int_{0}^{\infty} dr S(r^{2}-\epsilon)r^{2} = \frac{1}{2\sqrt{\epsilon}} \int_{0}^{\infty} S(r-\sqrt{\epsilon})r^{2} dr$$

$$= \frac{1}{2\sqrt{\epsilon}} (\sqrt{\epsilon})^{2} = \frac{1}{2\sqrt{\epsilon}} \int_{0}^{\infty} S(r-\sqrt{\epsilon})r^{2} dr$$

$$= \frac{1}{2\sqrt{\epsilon}} (\sqrt{\epsilon})^{2} = \frac{1}{2\epsilon} \cdot \frac{(3N)^{2}}{2\epsilon}$$
thursful
$$S(N,V,\epsilon) = \frac{\epsilon}{2\sqrt{\epsilon}} \int_{0}^{\infty} (\sqrt{2m})^{2N/2} \frac{(3N)}{2\epsilon} \int_{0}^{\infty} \frac{(3N/2)}{2\epsilon} dr$$

$$= \frac{1}{\sqrt{3N}N!} \int_{0}^{\infty} \frac{(3N)}{2\sqrt{2}} \int_{0}^{\infty} \frac{(3N/2)}{2\epsilon} dr$$

$$\int (N, V, E) = \frac{E}{E} \int (Z_{M})^{3N/2} \frac{(3N)}{2\pi} \int \frac{1}{2E} \frac{(3N/2)}{2E}$$

$$= \frac{E}{E} \int \frac{V^{N}(Z_{M})^{3N/2}}{V^{3N/2}} \frac{I(Z_{M})^{3N/2}}{I(Z_{M})^{3N/2}} \frac{3N/2}{I(Z_{M})^{3N/2}}$$

$$\int (Z_{M})^{N/2} \frac{I(Z_{M})^{3N/2}}{I(Z_{M})^{3N/2}} \frac{I(Z_{M})^{3N/2}}{I(Z_{M})^{3N/2}} \int \frac{1}{2E} \frac{E}{E} \int \frac{1}{V^{N/2}} \frac{I(Z_{M})^{3N/2}}{I(Z_{M})^{3N/2}} \frac{I(Z_{M})^{3N/2}}{I(Z_{M})^{3N/2}} \int \frac{1}{I(Z_{M})^{3N/2}} \frac{I(Z_{M})^{3N/2}}{I(Z_{M})^{3N/2}} \frac{I(Z_{M})^{3N/2}}{$$

$$\int (|v_1 v_1 \varepsilon|)^2 = \frac{\varepsilon_0}{\varepsilon} \frac{1}{N! \Gamma'(3N)} \left[U \left(\frac{2\pi m \varepsilon}{h^2} \right)^{3/2} \right]^{N}$$

$$\Pi\left(\frac{3N}{2}\right) = \left(\frac{3N}{2} - 1\right)! \approx \left(\frac{3N}{2}\right)! \approx \left(\frac{3N}{2}\right)! \approx \left(\frac{3N}{2}\right)^{\frac{3N}{2}} e^{-3N/2}$$
And $e^{3N/2 - 1} \approx e^{3N/2}$

So
$$\mathcal{L}(\nu, \nu, \varepsilon) \approx \frac{\varepsilon_0}{\nu!} \cdot \frac{1}{(3\nu)^{\frac{3\nu}{2}}} = \frac{5\nu}{2} \cdot \left[\sqrt{2\pi\alpha\varepsilon} \right]^{\frac{3\nu}{2}}$$

S=
$$k_B \ln \Omega \approx N k_B \ln \left[v \left(\frac{2\pi m k_B T}{n^2} \right) \right] + \frac{3N}{2} k_B - k_B \ln N! \sqrt{\frac{2\pi m k_B T}{n^2}} + \frac{3N}{2} k_B - k_B \ln N! \sqrt{\frac{2\pi m k_B T}{n^2}} + \frac{5N}{2} k_B \sqrt{\frac{2\pi m k_B T}{n^2}} + \frac{3N}{2} k_B \sqrt{\frac{2\pi m k_B T}{n^2}} + \frac{3N}$$

