

# Reactive Scheduling of Computational Resources in Control Systems

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## ABSTRACT

### 1. INTRODUCTION

Cyber-physical systems (CPS) technologies of integrating software and control are at the heart of many critical applications (c.f. [10]). These technologies aim at handling issues that emerge when the integration of software and hardware breaks the traditional abstraction layers: when researchers and practitioners are required to consider a unified view that includes both software and hardware. An example of such an issue is the challenge of dynamic assignment of computational resources to software based controllers discussed in, e.g., [1, 17, 19]. While the computation burden required by the control loops can be ignored in many situations, this is not always the case. A main motivating example studied in this paper is vision based control, where computer vision algorithms acquire state information to be used in a physical feedback loop (c.f. [5, 7, 15]). Unlike conventional sensors such as accelerometers, gyros, compasses, etc., a visual sensor requires significant processing of the acquired image to prepare the state information for feedback. Since typical cyber-physical application, such as robot control, consist of many control loops, responsible for different aspects of the system, that run simultaneously and share the same computational resources, the computer vision algorithms cannot always be invoked in full power. Alternatively, we propose in this paper a mechanism to dynamically trade CPU consumption vs. measurement accuracy so that data acquisition algorithms run in full power only when the control loop requires accurate data and provides less accurate data otherwise.

A main challenge in forming mechanisms for the integration of software and control lies in the design of efficient interfaces for integrating the engineering disciplines involved (c.f. [19]). Components with clearly specified APIs, such as Java library classes, allow designers to build complex systems effectively in many application domains. The key to such modular development is that an individual component can be designed, analyzed, and tested without the knowledge of other components or the underlying computing platform. When the system contains components with real-time requirements, the notion of an interface must include the requirements regarding resources, and existing programming languages provide little support for this. Consequently, current development of real-time embedded software requires significant low-level manual effort for debugging and component assembly (cf. [8, 9, 14]). This has motivated many researchers to develop compositional approaches and interface notions for real-time scheduling (cf. [3, 4, 6, 11–13, 16, 18]).

### 2. ARCHITECTURE: AUTOMATA BASED SCHEDULER

Sections go here.

### 3. SIMULATIONS

### 4. PROPOSED METHODOLOGY

1. **Controller design:** Based on the separation principle, we propose to design the controller to achieve the control objectives assuming a perfect observation. In practice, this may not be feasible because controller designs such as PID require a system to experiment with. In this case, as demonstrated in the case-study below (see Section 5), we propose to work with one of the observation modes. If the system is close to linear, this should result with a near optimal design.
2. **Observers design:** Specification of sensor modes and observers design

3. **Performance analysis:** Now, we can perform some experiments with the different observer modes and analyze transient behaviors. Specifically, as shown in the case study ??, we can measure how long it takes for the error to accumulate after switching to a lesser observation mode and formulate how this error affects the control objectives.
4. **Scheduling automata design:** Base on the analysis we can specify the resource scheduling requirements in the form of *specification automaton*. The goal is to design flexible specification that allow dynamic scheduling in order to adapt the environment and the system state, this will improve the system efficient.

## 5. APPLICATION: STABILIZING A QUADROTOR IN FRONT OF A WINDOW

The case study we used to test our concept is the development of a controller that stabilizes a quadrotor [?] in front of a window. We implement an autonomous controller for that task and evaluated its performance.

The part of the controller that we focused on is the vision based position controller. Specifically, the main controller, that we will describe below, uses a standard low-level angular controller and a simple image processing algorithm that identifies the position of the corners of the window in the image plane<sup>1</sup>. Its goal is to regulate the position of the quadrotor by tilting it. Note that rotations of the quadrotor generate a more-or-less proportional accelerations in a corresponding direction. A main challenge for this controller is that the computer vision algorithm takes significant time to compute relative to the fast control loop. We can decrease computation time by lowering the resolution, but this also increase the measurement noise. We will demonstrate how adaptive scheduling of the resolution can serve for balancing resource consumption vs. control performance.

### 5.1 Observer Design

We first implemented an observer based on the work of Hanoach [?]. The observer gets the positions of the widow corners, enumerated clockwise starting from the top left corner noted by  $p_1, p_2, p_3, p_4$ , and extract 4 quantities based on the shape and location of the window corners in the image plane:  $S_x, s_y, V_d$  and  $sz$ . **center of mass:**  $S_x$  and  $S_y$  represent the window “center of mass” in the image plane along the image  $x$  and  $y$  axes, respectively.  $S_x$  and  $S_y$  are normalized to the range of  $[-1, 1]$ .  $S_x$  is used to measure the roll angle of the window center (for stabilize the roll axis), and  $S_y$  is used to measure the altitude of the drone (for stabilizing the

throttle). **window size:**  $sz$  is the sum of the vertical edges of the window,  $sz$  is used to measure the distance of the drone from the window and then to regulate the roll angle<sup>2</sup>. **Vertical difference:**  $V_d = \frac{y_1 - y_4 - (y_2 - y_3)}{y_1 - y_4 + (y_2 - y_3)}$ , where  $y_i$  is the vertical position of  $p_i$  in the range of  $[-1, 1]$  (0 is the center of the image) first is used to measure the angular position of the drone in relation to the window ( $\theta$ ), then  $\theta$  and  $sz$  are used to calculate the horizontal position parallel to the window surface ( $x$  position) of the drone (see Figure ??).

After measuring the relative position and yaw attitude as usual we add estimator (filter) to get the best state estimation. As shown in the simulation at Section 3 we should use Kalman filter estimator, in our case we have non-linear system... For simplicity, inspiring from linear Kalman filter [?], we use two steps estimator that *predict* the current state evolved from the previous state using a linearized model of the system ( $\hat{x}_{k|k-1}$ ) and then *update* the prediction with current state measurement from image explained before, noted by  $z_k$ . This is a simplified kalman filter, a known technique as show in [?], where The result estimation (noted by  $\hat{x}_{k|k}$ ) is a complementary filter of the prediction ( $\hat{x}_{k|k-1}$ ) and the measurement ( $z_k$ ):  $\hat{x}_{k|k} = K\hat{x}_{k|k-1} + (1 - K)z_k$ .

As describe in Section ??, the image processing have few different operation modes, every mode use different image resolution, better image resolution results in more accurate measurement but consume more processing time, changing operation modes allows us to control the trade off between mesurment quality and processing time as shown in Table ??. The  $K$  gain is tuned different for each mode (resolution) for achieving the best estimation in each mode. For simplicity, we examine only two modes, *High quality* with resolution of 960p and *Low quality* with resolution of 240p.

### 5.2 Controller Design

We used a simple Proportional Integral Derivative (PID [2]) controller that we tuned by experimenting with the quadrotor in our lab. Based on the separation principle [?], we tuned the parameters of our controller only with the highest resolution observer and used them for all the other observers without any modification.

### 5.3 Analysis and Specification Automata

The objective of the system is to maintain stable hovering in front of the window. Hence, the performances of the system is measured by the amount of deviation from the center line of the window in the critical axis  $x$  (see Figure ??). Our goal is to achieve maximum performance with minimal amount of processing (CPU per-

<sup>1</sup>In the experiment, to simplify the image processing algorithm, we marked the corners of the window with led lights.

<sup>2</sup>we use fixed size window and convert  $sz$  to distance (in meter in our case) based on this window, in the general case the distance is relative to the window size

centage). The main consumer of computation resources in this system is the heavy observation tasks.

Analyzing the test results shown in Table ?? we see that High quality observation mode provide 0.4 meter error tolerance meaning we can fly this mode in 1.2 meter wide corridor<sup>3</sup>, with the cost of 30% CPU usage. With adaptive scheduling specification we lower the CPU usage without significant worsening of High quality performances.

From the Low quality experiment graph we can see that measurement post-fit residual ( $\tilde{y}_{k|k}$ ) is accumulate proportional to the deviation from the center of  $x$  axis, and we can use  $\tilde{y}_{k|k}$  vales to predict

TODO - position ( $x_{k|k}$ ) derived schedulers  
 TODO - complex / aggregated schedulers  
 TODO - gyro derived??

## 5.4 Results

TODO - graphs and tables

## 6. EXPERIMENT SETUP

The drone is controlled by a Raspberry pi with the navio [?, ?] that runs a modified ArduPilot [?] software.

## 7. CONCLUSIONS

Conclusion goes here.

## Acknowledgments

Acknowledgement goes here.

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<sup>3</sup>Experiments was done with 0.4 meter wide quad-rotor

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## **APPENDIX**

Appendix goes here.