# Reactive Scheduling of Computational Resources in Control Systems

#### Hodai Goldman

Ben-Gurion University of the Negev Department of Computer Science

January 1, 2018

- Overview
- 2 Automata-based Scheduling
  - Motivation
  - Component-based Architecture
  - Büchi Games Interface
- 3 Integration with Kalman
  - Guiding Concept
  - Guided Tour Simulation
- Experiment with real-life case-study
  - The Mission
  - Vision Component
  - Simplifying the Kalman Filter with Complementary Filter
  - Test and Results
- Conclusion
  - Conclusion
  - Related Work



## Overview - TODO: clean this slide

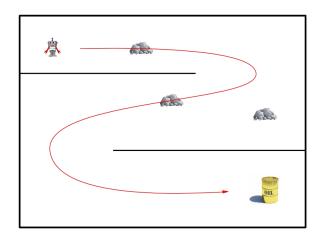
#### **Contributions**

- Development of control and scheduling co-design framework
- Reactive scheduling (environment condition adaptation)
- Independent, adaptive, and composable interface (Based on automata theory)
- What we do better?
- Prepare the ground for automata-based scheduling tool
- Development of scheduling technique based on Kalman filter

#### Achievements of this thesis

- Continue the work of RTComposer
- Proof of concept with simulation
- Proof of concept with real-life case-study
- Bridge the gaps between control and software engineering

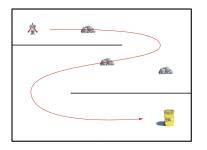
## An control problem example



Robot navigation



## An control problem example

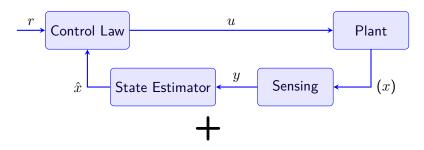


#### The Objectives

- The robot need to reach the target point fast and safely
- The robot have on-board camera for obstacle-avoidance
- The robot use GPS for general navigating



## The Traditional Solution



Constant time steps + periodic tasks					
time steps					
Task	Period	Deadline			
Check for obstacles	10ms	1.5ms			
Check GPS position	10ms	0.5ms			
Control Law	2ms	0ms			
	Task Check for obstacles Check GPS position Control Law	Task Period Check for obstacles 10ms Check GPS position 10ms Control Law 2ms	Task Period Deadline Check for obstacles 10ms 1.5ms Check GPS position 10ms 0.5ms Control Law 2ms 0ms		

## The Main Software Design Problems

Task	Period	Deadline		
Check for obstacles	10ms	1.5ms		
Check GPS position	10ms	0.5ms		
Control Law	2ms	0ms		
•••				

## The design problems from our point of view

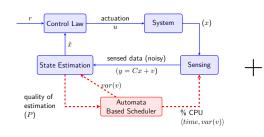
- All the tasks are highly coupled: any change or addition of some task require to consider all other tasks requirements
- Static and inefficient scheduling: the table is defined for the worst case talk about related work on this direction
- No consideration of the environmental conditions: it is a cyber-physical system after all

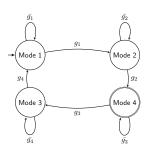


In this thesis we design an **reactive** scheduling framework for real-time systems

#### Required features:

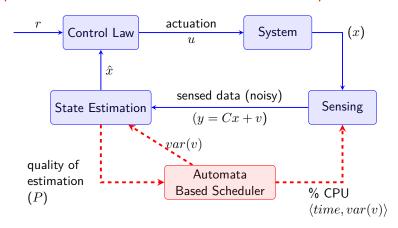
- Independent and composable requirements
- Control objective based requirement interface
- Environment adoptive scheduler





## System Design The Proposed Architecture

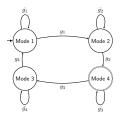
#### Explain that the scheduler is involve in the control loops



## Automata-Based Specification Interface

The Proposed Architecture

#### maybe add a word about RTcomposer and GameComposer

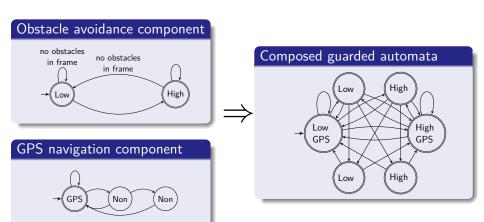


#### Why Automata

- Lite: minimal resource consumption at run-time
- Composable: easy to compose independent components
- Automata theory built in: allows for tools such GOAL
- Expressiveness

## Example of Guarded Automata

#### The Proposed Architecture



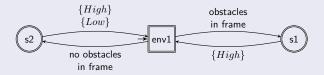
## Simplifying the Guarded Automata

The Proposed Architecture

# Mode-based guarded automata (for good intuition) no obstacles in frame in frame Low High

1

### The automata in practice (best match $\omega$ -word theory)

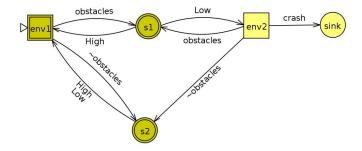


Q: How to create the guarded automata? By wining Büchi

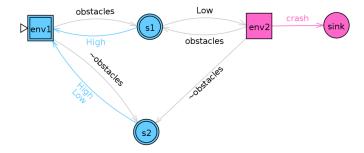
games



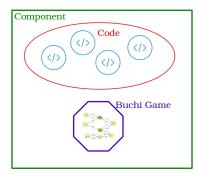
## Büchi game remainder



## Büchi game remainder



## A Component in the System

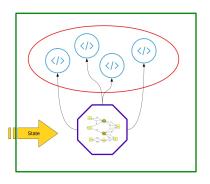


## Component Definition $(\langle T, G \rangle)$

- A set of subroutines (functions code)
- A Generalize Büchi Game



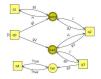
## A Component in the System



## The Büchi game $(G = \langle A, \langle P_{sched}, P_{env} \rangle \rangle)$

- Is played in turns by the environment and the scheduler
- Represent the interaction between the scheduler and the environment reaction

#### A Component in the System



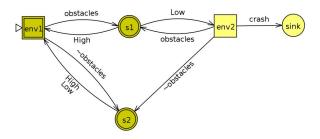
#### Scheduling Büchi Game

- Alternating turns
- Scheduler alphabet is  $\Sigma_{schd} = 2^T$
- ullet Environment alphabet is  $\Sigma_{env}=\mathbb{R}^n$  (scheduler feedback variables)
- There is an Edge for any possible environmental outcome
- The scheduler feedback variables can be any environment-depended value
- Environment player plays first

## Example - Büchi Game

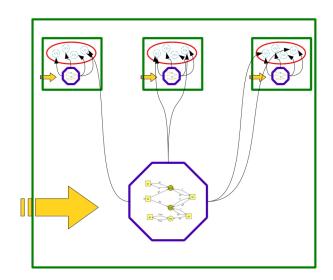
A Component in the System

The Büchi Game of the obstacles avoidance component:

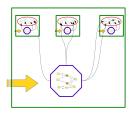


- The objectives of the component is to avoid obstacles
- The scheduler win  $\Leftrightarrow$  the corresponding word  $\omega \in \mathcal{L}(A) \Leftrightarrow$  the component achieved his **objectives**

## Component Composition



## Component Composition



#### Requirements

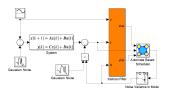
- A game  $(G = \langle A, \langle P_s, P_e \rangle)$  correspond to all the components
- The game of Component is  $G_i = \langle A_i, \langle P_s^i, P_e^i \rangle \rangle$
- $\omega \in \mathcal{L}(A) \Leftrightarrow \forall i : \omega(i) \in \mathcal{L}(A_i)$



TODO: how to present the composition details?

TODO: show the scheduler work: 1. find wining strategy 2. simultaneously walk through the strategy automata

## Integration with Kalman



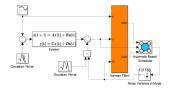
Kalman filter figure

#### Resource utilization with Kalman filter

- Novel technique for on-line trade-off between estimation quality and resource consumption
- Evaluate the overall errors using Kalman filter
- Schedule sensing-tasks based on the estimation quality

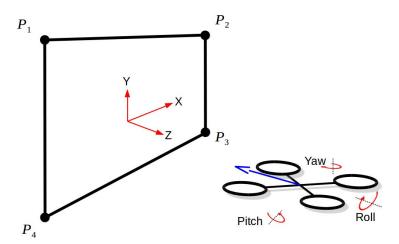
## Integration with Kalman

### Explain the concept of estimate the errors

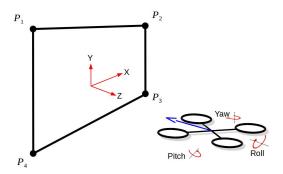


## Mission Definition

#### Explain the window motivation



## Concrete Control Objectives

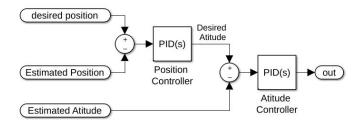


### Control & Scheduling Objectives

- Minimize the x-deviation
- Minimize the CPU usage of image processing task



## Traditional Controller Design

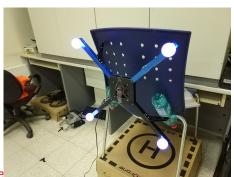


#### Attitude and position controller

- **vision** component estimate the x-position
- Position controller output a desired roll angle
- Attitude controller is a traditional attitude controller



## Vision Component



front picture

#### Image Processing Algorithm

- Find the window corners (brute force search)
- 2 Calculate the drone position

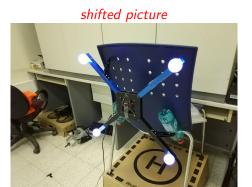


# Calculate the Drone Position



$$V_d = \frac{((y_1 - y_4) - (y_2 - y_3))}{((y_1 - y_4) + (y_2 - y_3))}$$

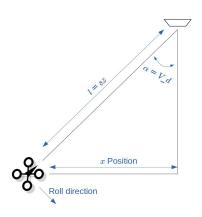
# Calculate the Drone Position Center of Mass



$$S_x = \frac{x_1 + x_2 + x_3 + x_4}{4}$$

## Calculate the Drone Position

#### Aproximate x Position



$$x = l \cdot \sin(V_d) \approx l \cdot V_d$$



## Two Step Filter

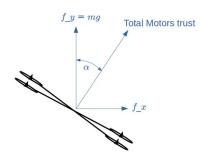
#### Why not Kalman filter

- It's a Non-linear system
- The process noise distribution is unknown, and unstable
- Kalman filter adds complexity in the code

#### Two step filter

- Predicts with a linearized model
- Update with the vision and other sensors

## The Linearized Model



$$A = \begin{pmatrix} 1 & dt & 0 \\ 0 & 1 & dt \\ 0 & 0 & 0 \end{pmatrix}$$
$$B = \begin{pmatrix} 0 \\ 0 \\ g \end{pmatrix}$$

#### Basic equations of motion on x axis

Assume stable hover:

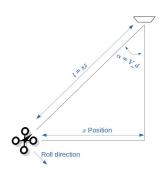
• Position:  $\bar{r_x}[k+1] = r_x[k] + dt \cdot v_x[k]$ 

• Velocity:  $\bar{v_x}[k+1] = v_x[k] + dt \cdot a_x[k]$ 

• Acceleration:  $\bar{a_x}[k+1] = \Sigma F_x/m \approx roll \cdot g$ 



### The Measurement vector



$$C = \left(\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1/g \end{array}\right)$$

#### Measurement vector

Position: from vision algorithm

• Velocity:  $\frac{\partial r_x}{\partial t}$ 

Acceleration: roll angle from the AHRS of APM



## $x[k] = K \cdot \bar{x}[k] + (1 - K) \cdot C^{-1} \cdot y[k]$

$$x_r = K_r \cdot \bar{x_r}[k] + (1 - K_r) \cdot y_r[k]$$
  

$$x_v = K_v \cdot \bar{x_v}[k] + (1 - K_v) \cdot y_v[k]$$
  

$$x_a = \bar{x_a}$$

#### Overall noise estimation

$$\tilde{y}_{k|k} = \bar{x_r}[k] - y_r[k]$$

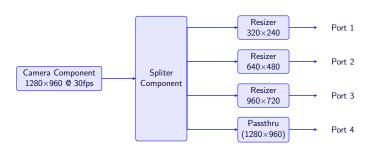


# Experiment Setup

this slide is needed?

Overview Scheduler Kalman Filter Experiment Conclusion The Mission Vision Component Filtering Results

### Vision Mode



#### Image resolution switching

- Change camera resolution in run time adds large delay
- Use hardware resizer for fast mode switch



### Constant Vision Mode

#### Always low quality mode

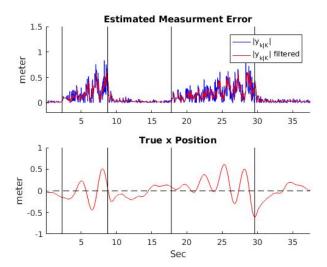
- 240p resolution
- mean error tolerance of 30cm ( not really stable)
- 2.1% CPU usage

#### Always high quality mode

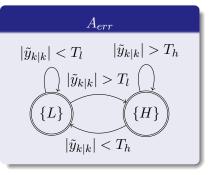
- 960p resolution
- mean error tolerance of 9.5cm
- 30% CPU usage

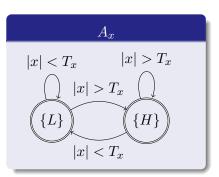
Overview Scheduler Kalman Filter Experiment Conclusion The Mission Vision Component Filtering Results

# Manual Mode flight

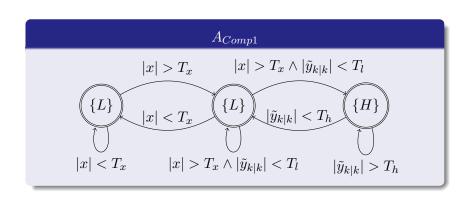


## Reactive Schedulers

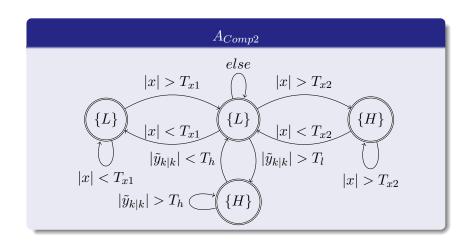




### Reactive Schedulers



### Reactive Schedulers



Schedule	% CPU	mean( $ x $ ) (cm)
Only High	30.9%	9.5
Only Low	2.1%	30.0
$A_x (T_x = 10)$	16.6%	10.9
$A_x (T_x = 20)$	14.0%	14.1
$A_x (T_x = 30)$	8.9%	17.4
$A_{err}$ $(T_l = 10, T_h = 20)$	10.3%	14.9
$A_{err}$ $(T_l = 10, T_h = 15)$	11.7%	11.3
$A_{comp1} \ (T_x=10 \; ,  T_l=10 \; ,  T_h=15)$	8.8%	12.9
$A_{comp2}$ $(T_{x1}=10$ , $T_{x2}=30$ , $T_{l}=10$ , $T_{h}=15)$	10.4%	12.7



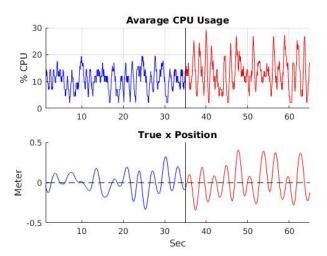
# Adaptive Results

$$\begin{split} |\tilde{y}_{k|k}| < T_l & |\tilde{y}_{k|k}| > T_h \\ & \underbrace{\left| \tilde{y}_{k|k} \right| > T_l \left( \underbrace{\left\{ H \right\}} \right)}_{|\tilde{y}_{k|k}| < T_h} \end{split}$$

conditions	% CPU	mean( $ x $ ) (cm)
Fan off	11.7%	11.3
Fan on	13.2%	11.8

Overview Scheduler Kalman Filter Experiment Conclusion The Mission Vision Component Filtering Results

# Adaptive Results



# **Thanks**