

# Reactive Scheduling of Computational Resources in Control Systems

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# Overview - *TODO: clean this slide*

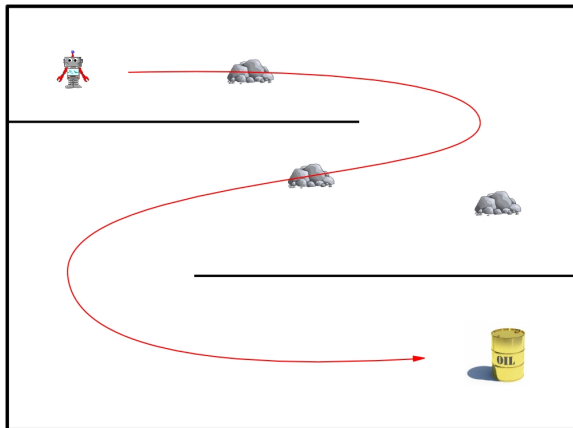
## Contributions

- Development of control and scheduling co-design framework
- **Reactive** scheduling (environment condition adaptation)
- **Independent**, **adaptive**, and **composable** interface (Based on automata theory)
- *What we do better?*
- Prepare the ground for automata-based **scheduling tool**
- Development of scheduling technique based on **Kalman filter**

## Achievements of this thesis

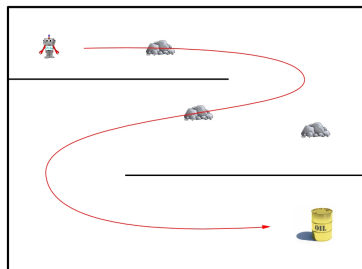
- Continue the work of **RTComposer**
- Proof of concept with **simulation**
- Proof of concept with **real-life case-study**
- **Bridge** the gaps between control and software engineering

# An control problem example



Robot navigation

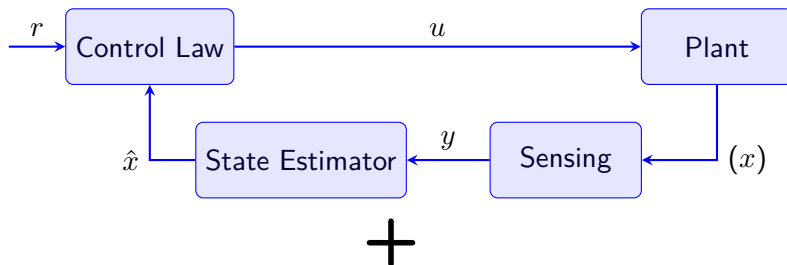
# An control problem example



## The Objectives

- The robot need to reach the target point **fast** and **safely**
- The robot have on-board camera for **obstacle-avoidance**
- The robot use GPS for general **navigating**

# The Traditional Solution



Constant time steps + periodic tasks

*time steps*

*figure*+

Task	Period	Deadline
Check for obstacles	10ms	1.5ms
Check GPS position	10ms	0.5ms
Control Law	2ms	0ms
...		

# The Main Software Design Problems

Task	Period	Deadline
Check for obstacles	10ms	1.5ms
Check GPS position	10ms	0.5ms
Control Law	2ms	0ms
...		

## The design problems from our point of view

- **All the tasks are highly coupled:** *any change or addition of some task require to consider all other tasks requirements*
- **Static and inefficient scheduling:** *the table is defined for the worst case talk about related work on this direction*
- **No consideration of the environmental conditions:** *it is a cyber-physical system after all*

# The Goal

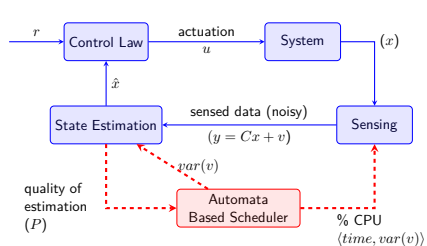
In this thesis we design an **reactive** scheduling framework for real-time systems

## Required features:

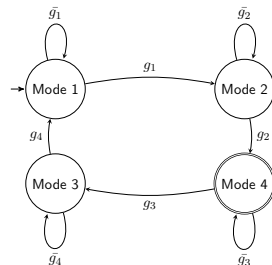
- **Independent** and **composable** requirements
- **Control objective based** requirement interface
- Environment **adoptive** scheduler



# The Proposed Architecture



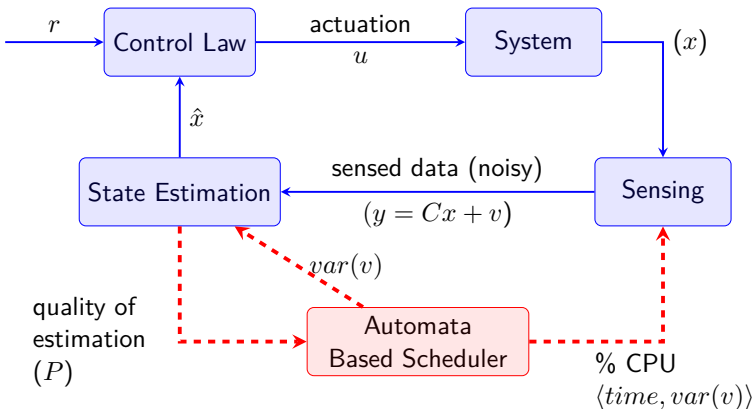
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# System Design

## The Proposed Architecture

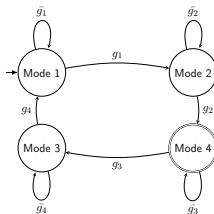
*Explain that the scheduler is involve in the control loops*



# Automata-Based Specification Interface

## The Proposed Architecture

*maybe add a word about RTcomposer and GameComposer*

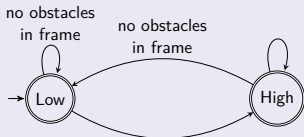


## Why Automata

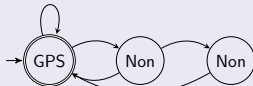
- **Lite:** minimal resource consumption at run-time
- **Composable:** easy to compose independent components
- **Automata theory built in:** allows for tools such *GOAL*
- **Expressiveness**

## The Proposed Architecture

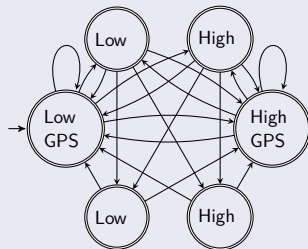
## Obstacle avoidance component



## GPS navigation component



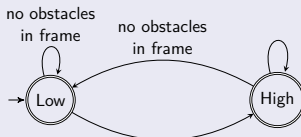
## Composed guarded automata



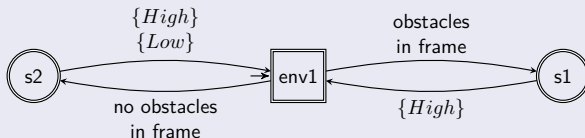
# Simplifying the Guarded Automata

## The Proposed Architecture

### Mode-based guarded automata (for good intuition)

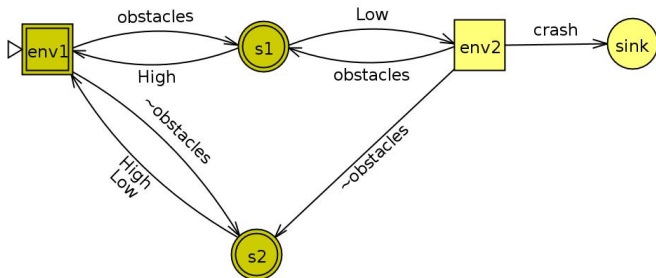


### The automata in practice (best match $\omega$ -word theory)

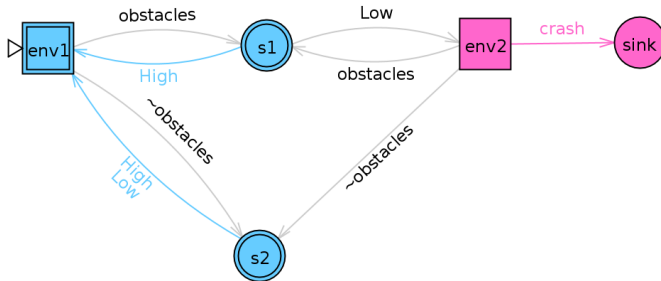


**Q: How to create the guarded automata?** By winning Büchi games

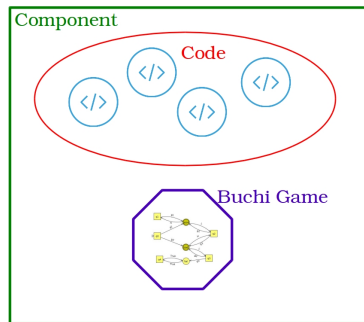
# Büchi game remainder



# Büchi game remainder



# A Component in the System

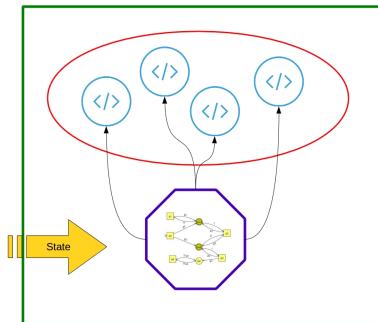


## Component Definition $\langle T, G \rangle$

- A set of subroutines (functions code)
- A Generalize Büchi Game



# A Component in the System

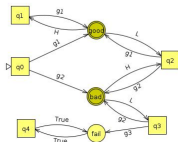


The Büchi game ( $G = \langle A, \langle P_{sched}, P_{env} \rangle \rangle$ )

- Is played in turns by the **environment** and the **scheduler**
- Represent the **interaction** between the scheduler and the environment reaction

# Scheduling Büchi Game

A Component in the System



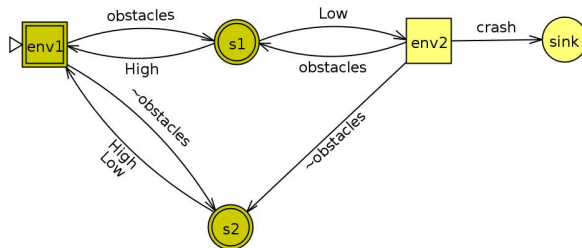
## Scheduling Büchi Game

- **Alternating turns**
- Scheduler alphabet is  $\Sigma_{schd} = 2^T$
- Environment alphabet is  $\Sigma_{env} = \mathbb{R}^n$  (scheduler feedback variables)
- There is an Edge for any **possible** environmental outcome
- The **scheduler feedback variables** can be any environment-depended value
- Environment player plays first

# Example - Büchi Game

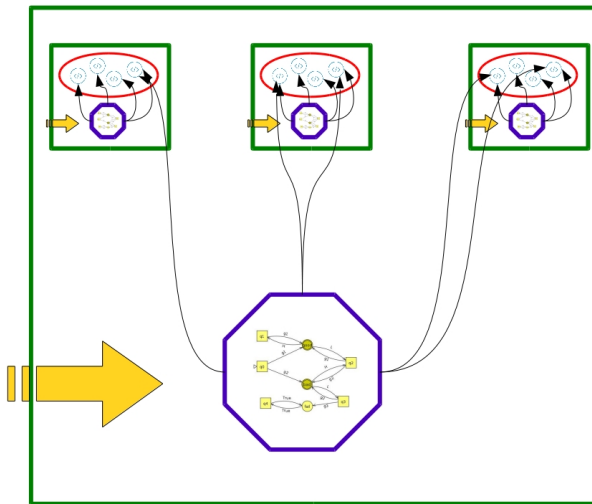
## A Component in the System

The Büchi Game of the obstacles avoidance component:

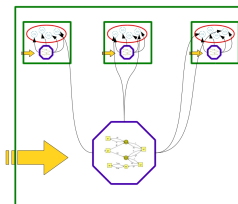


- The objectives of the component is to avoid obstacles
- The scheduler **win**  $\Leftrightarrow$  the corresponding word  $\omega \in \mathcal{L}(A) \Leftrightarrow$  the component achieved his **objectives**

# Component Composition



# Component Composition



## Requirements

- A game  $(G = \langle A, \langle P_s, P_e \rangle \rangle)$  correspond to all the components
- The game of Component is  $G_i = \langle A_i, \langle P_s^i, P_e^i \rangle \rangle$
- $\omega \in \mathcal{L}(A) \Leftrightarrow \forall i : \omega(i) \in \mathcal{L}(A_i)$

*TODO: how to present the composition details?*

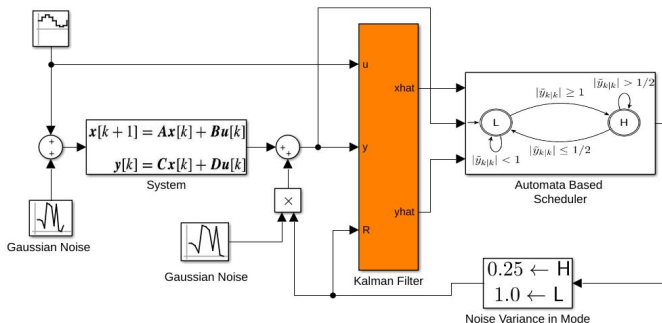
*TODO: show the resource component*

*TODO: show the scheduler work: 1. find winning strategy 2. simultaneously walk through the strategy automata*



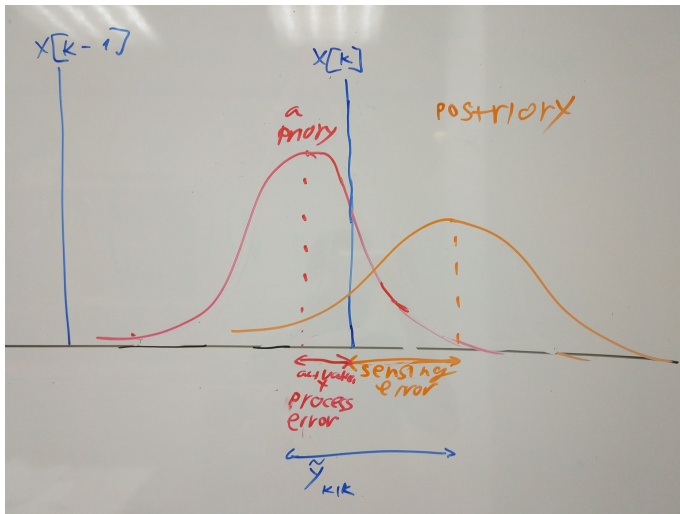
# Simulation

Schedule sensing-tasks based on the estimation quality



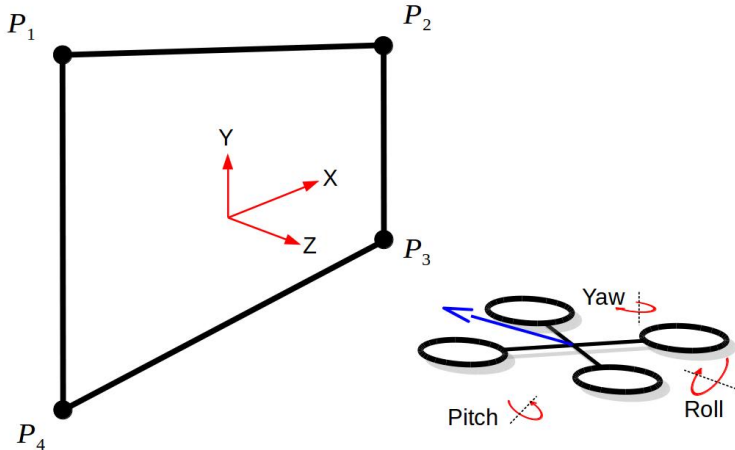
	High	Low	Aut. Based
%CPU	85	10	46
mean of $ x - \hat{x} $	0.97	1.24	1.08

# Integration with Kalman

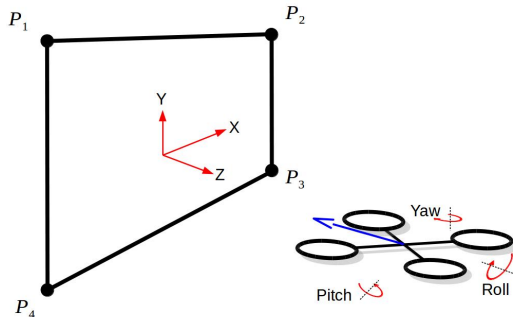


# Mission Definition

*Explain the window motivation*



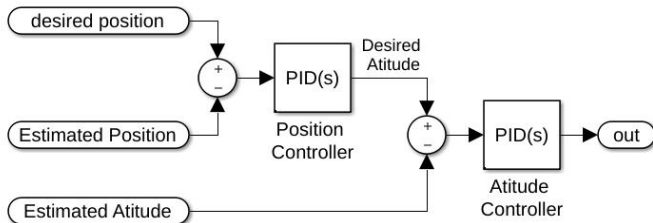
# Concrete Control Objectives



## Control & Scheduling Objectives

- Minimize the  $x$ -deviation
- Minimize the CPU usage of image processing task

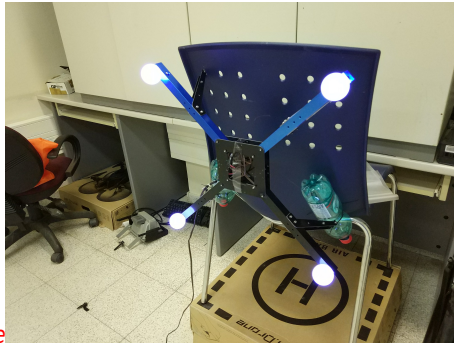
# Traditional Controller Design



## Attitude and position controller

- **vision** component estimate the  $x$ -position
- Position controller output a desired roll angle
- Attitude controller is a traditional attitude controller

# Vision Component



*front picture*

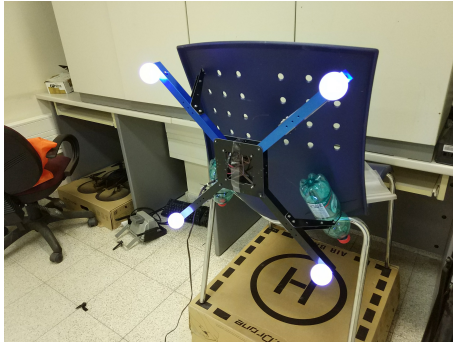
## Image Processing Algorithm

- 1 Find the window corners (brute force search)
- 2 Calculate the drone position

# Calculate the Drone Position

## Vertical Difference

*side picture*

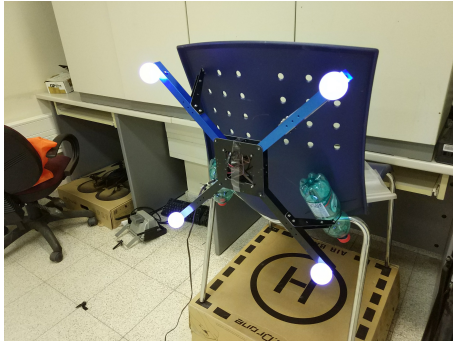


$$V_d = \frac{((y_1 - y_4) - (y_2 - y_3))}{((y_1 - y_4) + (y_2 - y_3))}$$

# Calculate the Drone Position

## Center of Mass

*shifted picture*

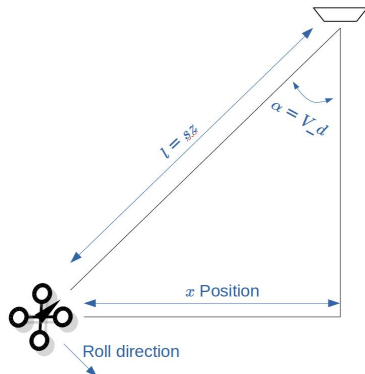


$$S_x = \frac{x_1 + x_2 + x_3 + x_4}{4}$$



# Calculate the Drone Position

Aproximate  $x$  Position



$$x = l \cdot \sin(V_d) \approx l \cdot V_d$$

# Two Step Filter

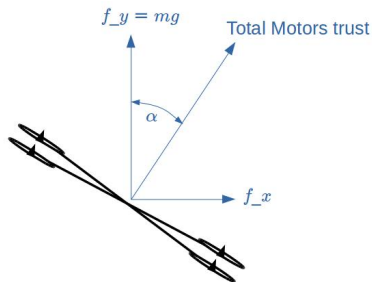
## Why not Kalman filter

- It's a Non-linear system
- The process noise distribution is unknown, and unstable
- Kalman filter adds complexity in the code

## Two step filter

- 1 Predicts - with a linearized model
- 2 Update - with the vision and other sensors

# The Linearized Model



$$A = \begin{pmatrix} 1 & dt & 0 \\ 0 & 1 & dt \\ 0 & 0 & 0 \end{pmatrix}$$

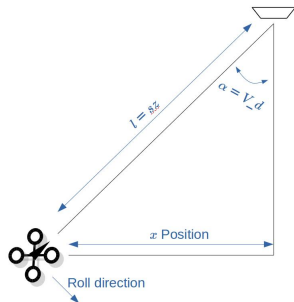
$$B = \begin{pmatrix} 0 \\ 0 \\ g \end{pmatrix}$$

## Basic equations of motion on $x$ axis

Assume stable hover:

- **Position:**  $\bar{r}_x[k+1] = r_x[k] + dt \cdot v_x[k]$
- **Velocity:**  $\bar{v}_x[k+1] = v_x[k] + dt \cdot a_x[k]$
- **Acceleration:**  $\bar{a}_x[k+1] = \Sigma F_x / m \approx roll \cdot g$

# The Measurement vector



$$C = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1/g \end{pmatrix}$$

## Measurement vector

- **Position:** from vision algorithm
- **Velocity:**  $\frac{\partial r_x}{\partial t}$
- **Acceleration:** roll angle from the AHRS of APM

# The Update Step

$$x[k] = K \cdot \bar{x}[k] + (1 - K) \cdot C^{-1} \cdot y[k]$$

$$x_r = K_r \cdot \bar{x}_r[k] + (1 - K_r) \cdot y_r[k]$$

$$x_v = K_v \cdot \bar{x}_v[k] + (1 - K_v) \cdot y_v[k]$$

$$x_a = \bar{x}_a$$

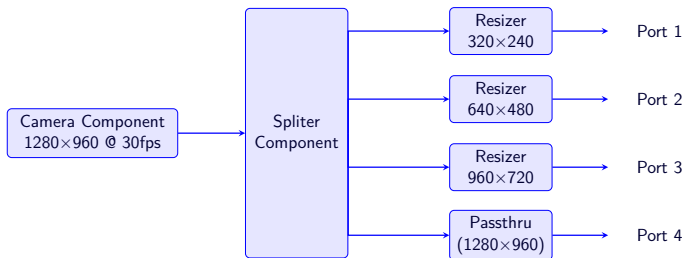
## Overall noise estimation

$$\tilde{y}_{k|k} = \bar{x}_r[k] - y_r[k]$$

# Experiment Setup

*this slide is needed?*

# Vision Mode



## Image resolution switching

- Change camera resolution in run time adds large **delay**
- Use **hardware resizer** for fast mode switch

# Constant Vision Mode

## Always low quality mode

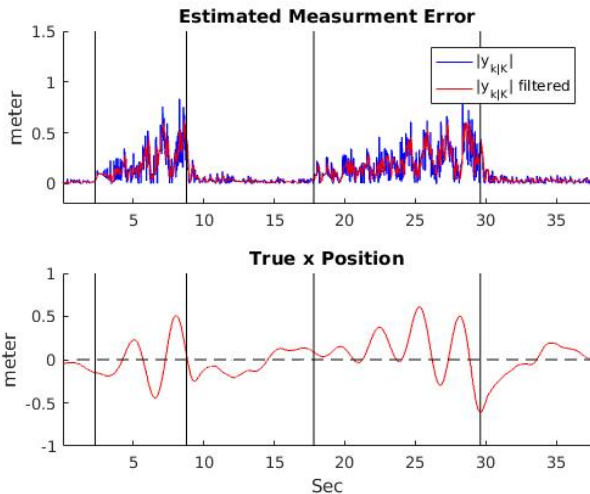
- 240p resolution
- mean error tolerance of 30cm ( *not really stable* )
- 2.1% CPU usage

## Always high quality mode

- 960p resolution
- mean error tolerance of 9.5cm
- 30% CPU usage



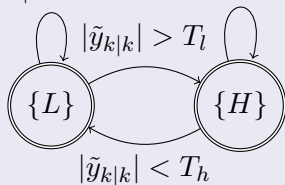
# Manual Mode flight



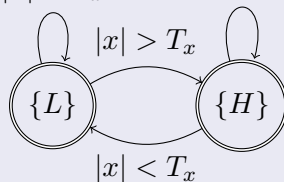
# Reactive Schedulers

 $A_{err}$ 

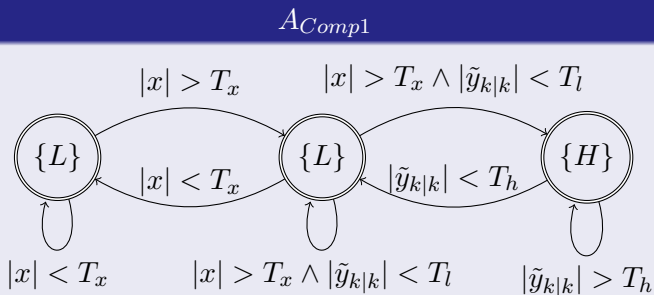
$$|\tilde{y}_{k|k}| < T_l \quad |\tilde{y}_{k|k}| > T_h$$


 $A_x$ 

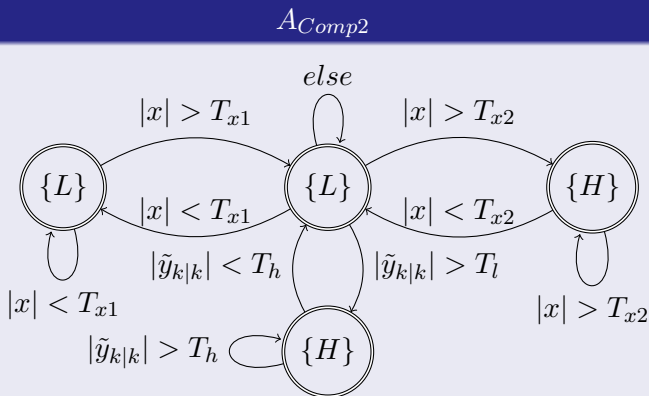
$$|x| < T_x \quad |x| > T_x$$



# Reactive Schedulers



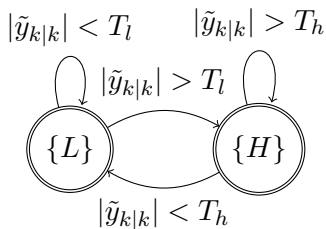
# Reactive Schedulers



## Results

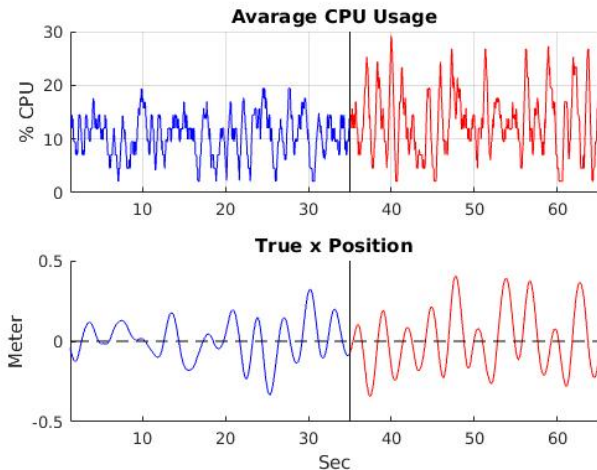
Schedule	% CPU	mean( $ x $ ) (cm)
Only High	30.9%	9.5
Only Low	2.1%	30.0
$A_x (T_x = 10)$	16.6%	10.9
$A_x (T_x = 20)$	14.0%	14.1
$A_x (T_x = 30)$	8.9%	17.4
$A_{err}$ ( $T_l = 10, T_h = 20$ )	10.3%	14.9
$A_{err}$ ( $T_l = 10, T_h = 15$ )	11.7%	11.3
$A_{comp1}$ ( $T_x = 10, T_l = 10, T_h = 15$ )	8.8%	12.9
$A_{comp2}$ ( $T_{x1} = 10, T_{x2} = 30, T_l = 10, T_h = 15$ )	10.4%	12.7

# Adaptive Results



conditions	% CPU	mean( $ x $ ) (cm)
Fan off	11.7%	11.3
Fan on	13.2%	11.8

# Adaptive Results



*instead of with Related Work   review of similar papers: A table with few papers*



# Thanks