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IN PRAGUE

**F3**

**Faculty of Electrical Engineering  
Department of Control Engineering**

**Master's Thesis**

# **Indoor localization system for automated vehicles based on Ultra-Wideband technology**

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Cybernetics and robotics

**May 2021**

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# MASTER'S THESIS ASSIGNMENT

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## II. Master's thesis details

Master's thesis title in English:

**Indoor localization system for automated vehicles based on Ultra-Wideband technology**

Master's thesis title in Czech:

**Interiérový lokalizační systém pro autonomní prostředky s využitím technologie Ultra-Wideband**

Guidelines:

1. Study the state of the art data fusion principles used for pose estimation. Study principles of Inertial navigation systems (INS)
2. Propose a localization system for autonomous vehicles based on fusion of data from Ultra-Wideband (UWB) positioning system and on-board dead-reckoning sensors such as Inertial measurement unit (IMU)
3. Evaluate proposed localization system for use in industrial environments.

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## Acknowledgement / Declaration

  Lorem ipsum sit amet, thanks to  
  TACR (TACR project with the correct  
  name and number)

I hereby declare that I wrote the presented thesis on my own and that I cited all the used information sources in compliance with the Methodical instructions about the ethical principles for writing an academic thesis.

.....  
Prague, May 21, 2021

## Abstrakt / Abstract

Lorem ipsum sit amet

**Klíčová slova:** ultra-wideband, imu, ins, localization, indoor, kalman-filtr, ekf

**Překlad titulu:** Interiérový lokalizační systém pro autonomní prostředky s využitím technologie Ultra-Wideband

The most awesome abstract

**Keywords:** ultra-wideband, imu, ins, localization, indoor, kalman-filter, ekf

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# Chapter 1

## Introduction

- problem indoor lokalizace a proc je treba to resit - cim je prace motivovana -> TACR
- co my od lokalizace chceme za features, jakou cestou pujdeme - jake sekce nas cekaji, co se v nich dozvime a k cemu jsou dulezite

### 1.1 Indoor localization

### 1.2 Motivace - projekt TACR

### 1.3 Key features of localization for TACR

### 1.4 Overview of chapters in thesis

# Chapter 2

## Indoor localization methods

### 2.1 Absolute and relative localization

In the field of localization systems, plenty of technologies have been investigated. These technologies can be divided into two significant subgroups according to a process, how the location is described. **Absolute** localization refers to the system, where the position is given in some coordinate system, and in **relative** localizations, the location is described with respect to other locations or landmarks. Typically, in the absolute localization system, the position should not significantly drift over time but can change in discrete jumps. That means that this system is not continuous but serves good as a long-term global reference. In the relative localization system, the position drifts over time but does not suffer for discrete jumps, as it is continuous.

It can be seen that the best approach for designing the localization system is to combine both principles to counter their negative aspects. The combination is given by state estimations algorithms briefly described in Chapter 4. But before that, the different technologies for position estimation are briefly introduced in the next section.

### 2.2 A brief overview of localization technologies

- lokalizace z kamery (to chci rozebrat kvuli referenci - apriltag a vicon - laserova lokalizace - lokalizace v prumyslu nyni

### 2.3 State of the art in fusion UWB a IMU

- jake jsou trendy ve fuzi uwb a neco?

Jednim z nejvetsich problemu indoor lokalizace je nemoznost pouzit absolutni lokalizaci pomocí GNSS, jelikoz ted pro sve spravne fungovani potrebuje primy pohled na oblohu. Dnes se tedy indoor lokalizace robotu resi ruznymi druhy technologii, vetsinou i ve spravne fuzi. Pristupy lokalizace se daji delit bud podle pouzite technologie nebo Obecne se da lokalizace rozdelit na dve kategorie a to lokalizace absolutni a lokalizace relativni. Vyznam absolutni a relativni lokalizace. Dnes se

# Chapter 3

## Sensors

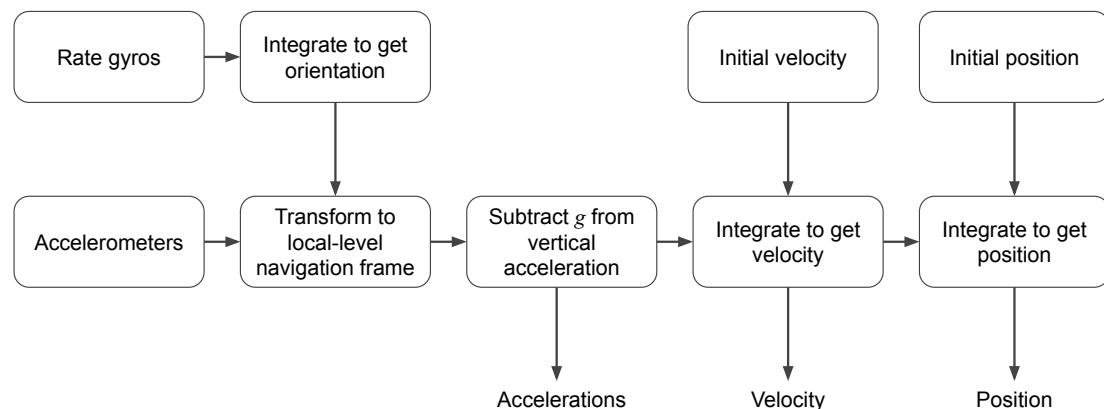
In chapter 3 the overview of used sensors and their properties is given. The main aim is to describe an localization method based on ultra-wideband technology(UWB), an inertial measurement unit (IMU) and an odometry. The UWB TODO. The IMU section mainly focuses on the unit overview, a short description of gyroscopes and accelerometers used in it, the errors of these sensors, its analysis and outcomes for the localization unit. The odometry TODO.

### 3.1 Localization based on Ultra-wideband

### 3.2 Inertial measurement unit

An inertial measurement unit (IMU) is a device that utilizes measurement systems such as gyroscopes and accelerometers to estimate the relative position, velocity and acceleration of a vehicle in motion[1]. The unit is typically integrated with an on-board computational unit and may contain more sensors as a magnetometer or thermometer.

The gyroscopes measure angular velocities and accelerometers specific forces, which can be easily transformed into linear accelerations [1]. The IMU typically contains three orthogonal accelerometers and three orthogonal gyroscopes. Because of that, it can measure angular velocities and specific forces in each axis to maintain a 6-DOF estimate of the pose of the vehicle (position ( $x, y, z$ ) and orientation ( $roll, pitch, yaw$ )). The process of the computation can be seen in Figure 3.1.



**Figure 3.1.** IMU block diagram[1].

There are two basic ways how to mount the IMU to a vehicle, also called mechanization architectures [1–2].

- In **gimbaled systems**, the IMU is attached to a stabilized platform that maintains its inertial orientation as the vehicle manoeuvres.
- In **strap-down systems**, it is rigidly attached to the vehicle.

The mechanization determines the conversion between measurements of IMU and estimation of linear accelerations and angular velocities of the vehicle. It means the transformations IMU body frame to local frame. The conversion is called navigation (mechanization) equations and they are briefly summarized in Section 3.2.5.

IMU's are extremely sensitive to measurement errors given by properties of used gyroscopes, accelerometers and their mounting. As the data are once or twice integrated, any error in measurement causes a linear or quadratic error in the pose estimation. Even with a small measurement error, the IMU's drift becomes significant, and it needs to be externally compensated. The IMU provides a short-term stable solution, which is not affected by external environment [2], and it has a high data rate (100 Hz - 200 Hz). That makes the IMU measurement complementary to the UWB localization measurement.

### 3.2.1 Accelerometers

Accelerometers can measure external forces acting on the vehicle. They measure a specific force relatively to a non-rotating inertial space in a specific direction. They are sensitive to all forces, including gravity and fictitious forces [1].

**Mechanical accelerometers** use a spring-mass-damper system. The force acts on the mass, and it causes displacement of the spring. The system is limited by physical properties of real spring.

**Microelectromechanical systems (MEMS) based accelerometers** are made of at least three components, namely a proof mass, a suspension to hold the mass and a pickoff, which relates an output signal to the induced accelerations [3]. MEMS accelerometers are then classified by the type of converting the mechanical displacement of the proof mass to an electrical signal. In most common principles belong to piezoresistive, capacitive sensing, piezoelectric, optical sensing and tunnelling current sensing. Unlike the others, the piezoelectric MEMS sensors can not be used for navigation because their output rate is too low [3].

The current accelerometers used technology according to an application is summarized in Figure 3.2.

### 3.2.2 Gyroscopes

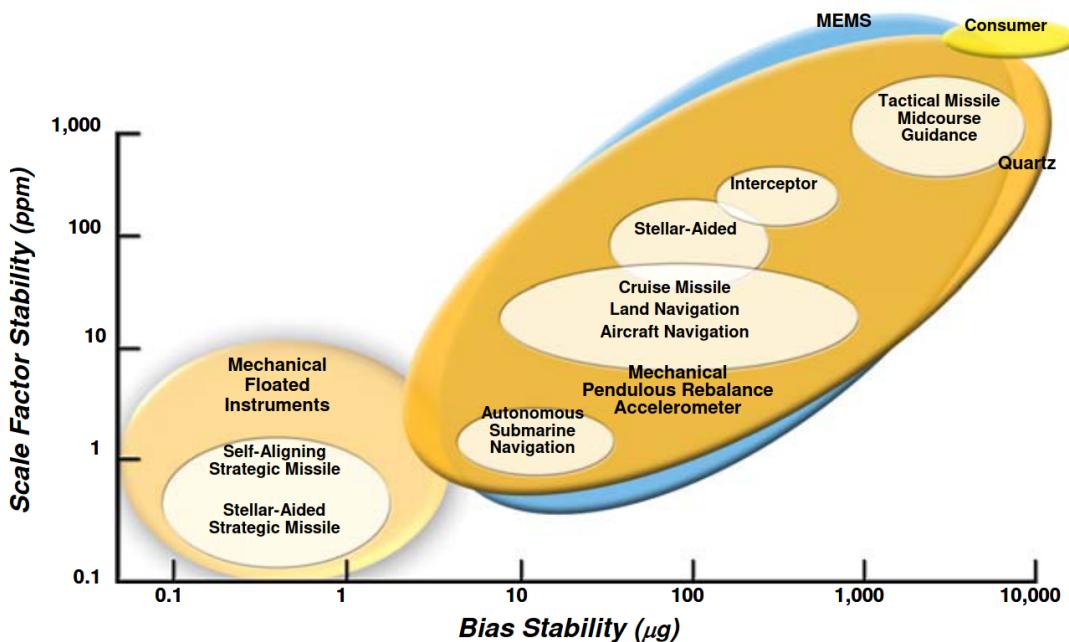
Gyroscopes are used for estimating a rotational motion of a body, each gyroscope measures angular rate  $\omega$  (inertial angular rotation) relatively to a non-rotating inertial space in one axis. There are basically three main categories of gyroscopes [1].

**Mechanical gyroscopes** have a mass spinning steadily with respect to a free movable axis, they are not used a lot anymore, but they can be found in very old submarines.

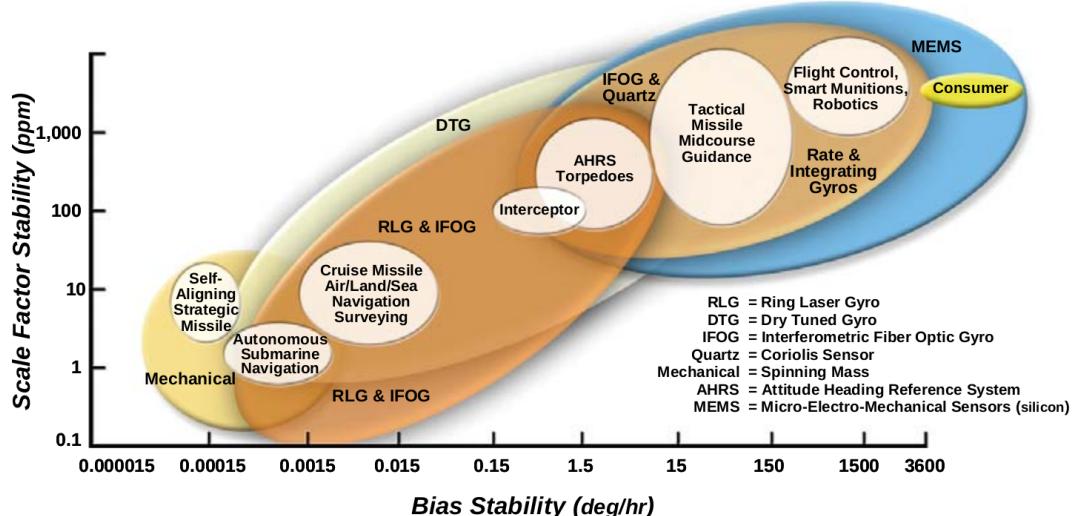
**Optical gyroscopes** are based on the Sagnac effect, which states that frequency/phase shift between two waves counter-propagating in a rotating ring interferometer is proportional to the loop angular velocity. As a light source, laser is typically used. Currently, this technology gives the best performance. Examples can be ring laser gyroscopes (RLG) or fibre optic gyroscopes (FOG).

**Vibrating gyroscopes** are based on the Coriolis effect that induces a coupling between two resonant modes of a mechanical resonator. Typically, vibrating gyroscopes are based on MEMS technology[3] and they play significant role in robotics, because of their simplicity. They are small, cheap, have no rotating parts and furthermore have low power consumption.

The performance and application of each technology is demonstrated in Figure 3.3.



**Figure 3.2.** Accelerometers technology plotted by bias instability and scale factor stability[4].



**Figure 3.3.** Gyroscopes technology plotted by bias instability and scale factor stability[4].

### 3.2.3 IMU's errors and Allan variance analysis

**IMU errors** IMUs faces several error sources, which are always related to the specific sample unit and its technology. In this thesis, the main focus is given to MEMS-based IMUs as they are used in experiments. These sensors are typically small and low cost. In this section, the most significant errors for MEMS sensors and analysis of these errors with Allan variance are summarized. This analysis is applied to a specific IMU, which is used during experiments.

Errors can be divided into two categories [3]

- stochastical errors, which can be described as random processes,
- and systematic errors are basically caused by manufacturing imperfections or not ideal handling with IMU. These errors can be corrected by proper calibration.

Nevertheless, errors need to be analysed and reduced according to application requirements, next following subset of errors are the most significant according to the topic of this thesis.

*Biases* of accelerometers and gyroscopes used in IMU are examples of systematic errors and can be divided into

- bias instability<sup>1</sup>, which represents drift of the sensor during a time,
- and initial bias<sup>2</sup> is a static offset, which can vary during each start-up of the device, but during a run, it is static.

Biases are typically represented in  $^{\circ}/hr$  or  $^{\circ}/s$  for gyroscopes and  $mg$  for accelerometers.

*A scale factor* and *a misalignment error*, both systematic errors, could also be significant. The scale factor is connected to imperfection while converting the real measurement input value and output value. The nonorthogonality of all sensors gives the misalignment error in IMU and it is caused during the production.

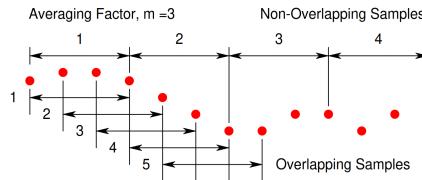
*Angle or velocity random walks* belong to stochastic errors. The measurement of gyroscopes and accelerometers are subject to white noises (the noise represented by Gaussian distribution). During the estimation of angles and velocities, integration needs to be done. Then the white noise starts to manifest itself by angle or velocity random walk,  $(^{\circ}/s/\sqrt{Hz})$  and  $(m^2/s/\sqrt{Hz})$  respectively.

**Allan variance(AVAR)** is widely used to analyse a random error of inertial sensors in time-domain. The brief introduction and important outcomes from AVAR, the most common time domain measure of frequency stability, is given [5].

The AVAR  $\sigma_A^2(\tau)$  is a function of the averaging time  $\tau$ , computed as

$$\sigma_A^2(\tau) = \frac{1}{2(N-1)} \sum_{i=1}^{N-1} (\bar{y}_\tau(i+1) - \bar{y}_\tau(i))^2, \quad (1)$$

where  $N$  represents the number of clusters in the dataset ( $N = \text{floor}(M/n)$ ),  $n$  is the number of samples in the cluster,  $M$  is the total number of samples in dataset,  $\tau$  is the time length of the cluster ( $\tau = m \times T_s$ ),  $T_s$  is the sampling period,  $\bar{y}_\tau(i+1)$  and  $\bar{y}_\tau(i)$  are mean values of certain cluster of  $i+1$ -th and  $i$ -th cluster respectively. [6].



**Figure 3.4.** The difference between non-overlapping and overlapping sample [7].

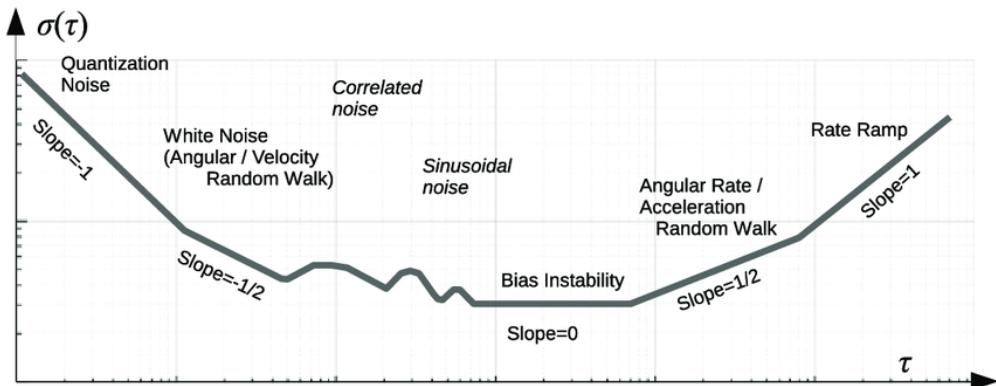
The samples in a cluster can be both non-overlapping and overlapping. The difference is illustrated in 3.4. The overlapping samples improve the confidence of the resulting estimate. That is the reason why this method is the most common for a measure of time-domain frequency stability in general [5].

<sup>1</sup> also called in-run bias

<sup>2</sup> repeatability bias

The process of measuring AVAR consist of collecting 24-48 hours long dataset when the inertial sensor is not moving, and it is in not vibrating environments (no trains, subways that would cause vibration). The sampling values are angular rate or accelerations.

If the dataset is valid and the AVAR is correctly computed, the plot copies the example plot seen in Figure 3.5. It is typically plotted on a log/log scale. A different slope of the graph describes each noise component by that the graph can be easily divided into specific parts.



**Figure 3.5.** An example of Allan variance plot[8].

The most significant outcome for navigation purposes is when the bias instability is reached (slope is zero). At this time, the sensor model contains only a white (Gaussian) noise [9]. After that period, the external reset needs to be done.

### 3.2.4 Performance of IMUs according to their application

IMUS can be used in various application, which differs by IMUs performance. The overview of each sensor's precision for a given application is summarized in Figure 3.6.

### 3.2.5 Navigation (mechanization) equations

Both gyroscopes (see section 3.2.2) and accelerometers (see section 3.2.1) measure in IMU inertial frame, typically called body frame. That means they need to be converted to a reference frame. In that frame, the state (positions, orientations, velocities, ...) is estimated and it is the output of the localization method.

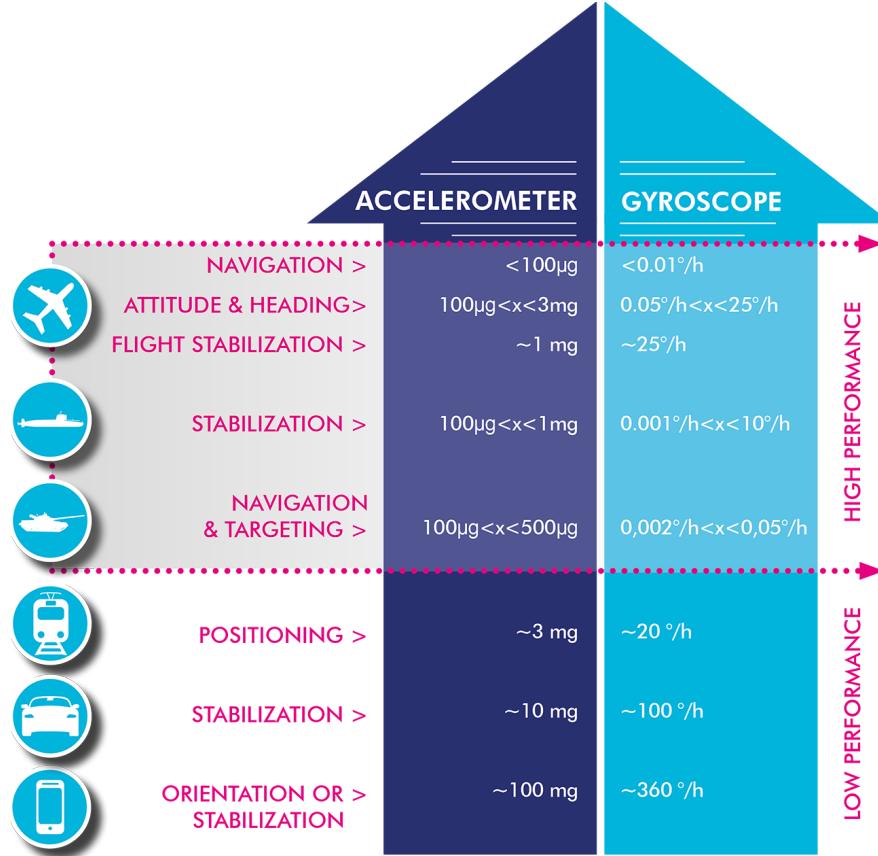
Navigation equations implement the transforms between the body frame and the reference frame, either a local-level frame (as North-East-Down or East-North-Up), a reference to a specific point at planet Earth, or an Earth-fixed frame as ECEF [3].

These equations are known and can be found in the book MEMS-based Integrated Navigation [3].

## 3.3 Inertial navigation system

### 3.4 Odometry

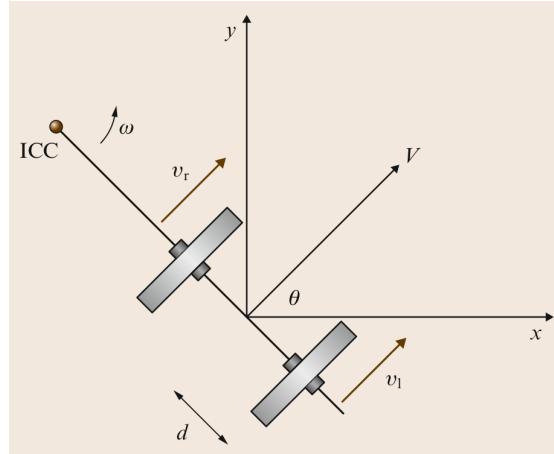
The odometry of a device contains its pose and velocity based on its motion, it can be obtained from various sources as IMU, lidars, cameras or wheel encoders[1], and it is an example of a dead reckoning system.



**Figure 3.6.** A performance of IMU per application[10].

Both IMU and wheel encoders are used in the suggested localisation system since they can counter each other's negative characteristics because wheel encoders drift over travelled distance and IMU drift over time[1].

The details of odometry information varies with vehicle design and during experiments the differential type is used (illustrated in Figure 3.7).



**Figure 3.7.** A differential drive kinematics scheme[1].

## Chapter 4

### State estimations algorithms for localization

The localisation is the problem of estimating a robot's coordinates in an external reference frame from sensor data. In particular, probabilistic approaches are typically more robust in the face of sensor limitations, sensor noise or environment dynamics[11]. Moreover, they often scale much better to complex and unstructured environments, where the ability to handle uncertainty is of even greater importance[11].

For that reason, only probabilistic methods for state estimation are described in the next chapter. The basis of each technique briefly described in this thesis is Bayes filter[11]. The first section discusses the difference between Kalman and Particle filter for state estimation. The following section introduces advanced concepts derived from the Kalman filter algorithm as extended Kalman filter and unscented Kalman filter. The third and fourth sections go deeply into the Error state extended Kalman filter and introduces the benefits of using it, as it is the core of the localization system of this thesis.

#### 4.1 Kalman and particle filter

Both Kalman and particle filter are the first implementations of Bayes filter in the continuous time[11], and in both filters, the state is represented by belief, which corresponds to a distribution. For the Kalman filter it is a multivariate normal distribution, but for particle filter, the distribution is represented by all particles[11–12].

Both algorithms work with a prediction and correction step, which works with the system and sensor model, respectively. Firstly, it predicts the state based on the internal system model, and secondly, it corrects itself by external measurements and sensor model. Kalman and particle filter algorithms for localization are well described in a referenced Probabilistic robotics[11].

There are a few limitations for both algorithms. For the Kalman filter, the state transitions and measurements need to be linear with added Gaussian noise, and the initial state must have normal distribution[11]. There is no such requirement for linearity for the particle filter, and it works fine with nonlinear or multi-modal systems too[11]. But the algorithm can be more computation demanding as a high number of particles needs to be generated in each sample time for a robust estimation[11].

I decided to use an algorithm based on the Kalman filter for several reasons. First, the localization system will be used for the navigation of vehicles. For these kinds of tasks, the update rate has to be relatively high. Second, the state transition and measurements are approximately linear. And third, these algorithms are typically used in the fusion of IMU and GNSS, as I already mentioned in Chapter TODO.

#### 4.2 Algorithms based on Kalman filter

There have been many modifications and extensions of the standard Kalman filter since the 1950s when the filter was invented, because the assumptions of the linear system

and sensor model with added Gaussian noise are rarely fulfilled in practice[11]. In these cases, the state transition or sensor model are described by nonlinear functions.

There exist many techniques for linearizing nonlinear functions. The most popular tool, called Extended Kalman filter, use (first-order) Taylor expansion[11]. This approximation has its limitations, which correspond to a degree of nonlinearity of the functions and a degree of uncertainty. The higher these degrees are, the further the approximation deviates from true belief. In general, the Extended Kalman filter has its benefits in simplicity, optimality and robustness[11], but in practice, it is reliable for the system, which is almost linear in one-time step[13].

The Unscented Kalman filter is a tool that appears superior to the EKF linearization[11, 13]. The linearization is given by carefully selected sample points from nonlinear functions. Also, this approach does not assume that the distribution of noise source is Gaussian[13].

In conclusion, the degree of nonlinearity of the system is critical for the state estimation by algorithms based on the Kalman filter. Thus, the relatively recent but promising tool Error state Extended Kalman filter was introduced. In this concept, the error of the state is estimated, as it is more likely correctly modelled by a linear function[14–16].

### 4.3 Error state Extended Kalman filter

Error state Extended Kalman filter belongs to a group of Indirect Kalman filters because it does not estimate the state itself, but the error of the state[14].

The main idea is that the true state, which should be the output of the system, is computed as a suitable composition of nominal state and the error state

$$x_t = x_n \bigoplus \delta x \quad (1)$$

where

- $\bigoplus$  is a suitable composition as linear sum or matrix product,
- $x_t$  is the true state,
- $x_n$  is the nominal state
- and  $\delta x$  is the error state.

The nominal state is considered a large signal, which can be integrated in its nonlinear form and the error state as a small signal, which is a nearly linear function, ideal for Extended Kalman filtering[15].

The algorithm can be illustrated in the following equations in prediction, correction, injection and resetting steps. In **the prediction step** the nominal state and its covariance is estimated by following equation[14–15]

$$\begin{aligned} x_t &= f(x_{t-1}, u_t) \\ P_t &= FP_{t-1}F^T + BQB^T \end{aligned} \quad (2)$$

where

- $f(x_{t-1}, u_t)$  is the nonlinear function described the current state of the system based on previous state and current input,
- $x_t$  is the nominal state in time  $t$ ,
- $x_{t-1}$  is the true state in time  $t - 1$ ,

- $u_t$  is the input of the system,
- $P_t$  is the state covariance matrix (also called system covariance),
- $F$  is the state transition matrix given by  $F = \frac{\delta f(x_{t-1}, u_t)}{\delta x_{t-1}}$ ,
- $B$  is the input matrix,
- and  $Q$  is the input noise covariance matrix.

In **the correction step** the state is corrected based on measurement according to equations[14–15]

$$\begin{aligned} K &= P_{t-1} H^T (H P H^T + R)^{-1} \\ e_t &= K(y_t - h(x_{t-1})) \\ P_t &= (I - K H) P_{t-1} (I - K H)^T + K R K^T \end{aligned} \quad (3)$$

where

- $K$  is Kalman gain,
- $H$  is the measurement transition matrix given by  $H = \frac{\delta h(x_t)}{\delta x_t}$ ,
- $R$  is the covariance of the measurement,
- $e_t$  current estimated error of the state,
- $y_t$  is the measurement in time  $t$ ,
- and  $h(x_{t-1})$  is the measurement model based on previous state  $x_{t-1}$ .

In **the injection and resetting step** the state is compensated by error, and the error state and state covariance matrix need to be reseted[14–15]. The injection of error is given by

$$x_t = x_{t-1} + e_t \quad (4)$$

and the resetting can be illustrated

$$\begin{aligned} e_t &= g(e_t) \\ P_t &= G P_{t-1} G^T \end{aligned} \quad (5)$$

where

- $g(e_t)$  is reseting function of error state
- and  $G$  is the Jacobian matrix defined as  $G = \frac{\delta g(e_t)}{\delta e_t}$ .

## 4.4 Chosen approach for the state estimation

This thesis aims to design a prototype of the localization system of vehicles based on the fusion of the UWB positioning system and onboard dead-reckoning sensors. As I already mentioned in Chapter TODO, the system should be used for the localization of indoor vehicles in an industrial environment. However, each such vehicle (and terrain, where it is moving) can differ in its dynamics. Because of that, I decided to use an approach, which can replace these dynamics. The Inertial navigation system(INS) meets these requirements and gives us the state independent of a specific vehicle and specific terrain where it is moving. The estimation is accurate for a short time (see Section 3.2). Thus it needs to be corrected via other measurements as the UWB positioning system and odometry. I decided to estimate the error of the INS in the Error state Extended Kalman filter for the following reasons.

- The correction of INS can be done at a lower rate than the state estimation for localization purposes itself[14–15],
- The unscented Kalman filter or Particle filter algorithms have high computational load, that usually prevents them to be used in real time system[17].
- The model for estimation of the error is linear, as the error is
  - close to the origin,
  - and small, so higher orders can be neglected[14–15].
- numerical stability of the solution[14],
- even if the error estimation has a temporary computer failure, the INS is not affected, and some emergency procedures can come into account[14].

To sum up, the state estimation is given by INS, and the ES-EKF estimates the errors in the state using the difference between the INS and external sources of data, which are odometry and the UWB positioning system. The INS can estimate high-frequency motions of the vehicle accurately, so these dynamics are not in the filter explicitly modelled. The ES-EKF use a model of error propagation in INS, which are at low frequency and very well modelable by linear functions[14, 18, 16]. This approach is also known as Aided navigation systems and is briefly described in Aided navigation: GPS with high rate sensors[16]. The following Chapter 5 introduce the localization system design and implementation in detail.

# Chapter 5

## Localization system design and implementation

In this chapter, the design of the architecture is described along with the used tools for its solution.

The first part is proposed the system architecture design, the system kinematics equations follow in the second part. In the third part, the equations for the Error state extended Kalman filter are introduced. The fourth part is dedicated to injecting the estimated error into the estimated state and resetting the injected error. In the fifth and final part, the implementation tools are discussed.

To sum up, this chapter gives the reader a detail introduction to the proposed localization system with all equations and tools used in the final implementation.

### 5.1 System architecture design

Various approaches for state estimation were introduced in Chapter 4. The chosen approach is the Error state extended Kalman filter(ES-EKF). According to ES-EKF is the error in the states estimated using a Kalman filter rather than the state itself. The benefits of this approach are briefly summarized in Chapter 4.

The system consists of three crucial steps. The first is the inertial navigation system (INS), where the state is estimated based on IMU measurements. This state estimation leads to a dead-reckoning system, where the drift grows with time and needs to be corrected.

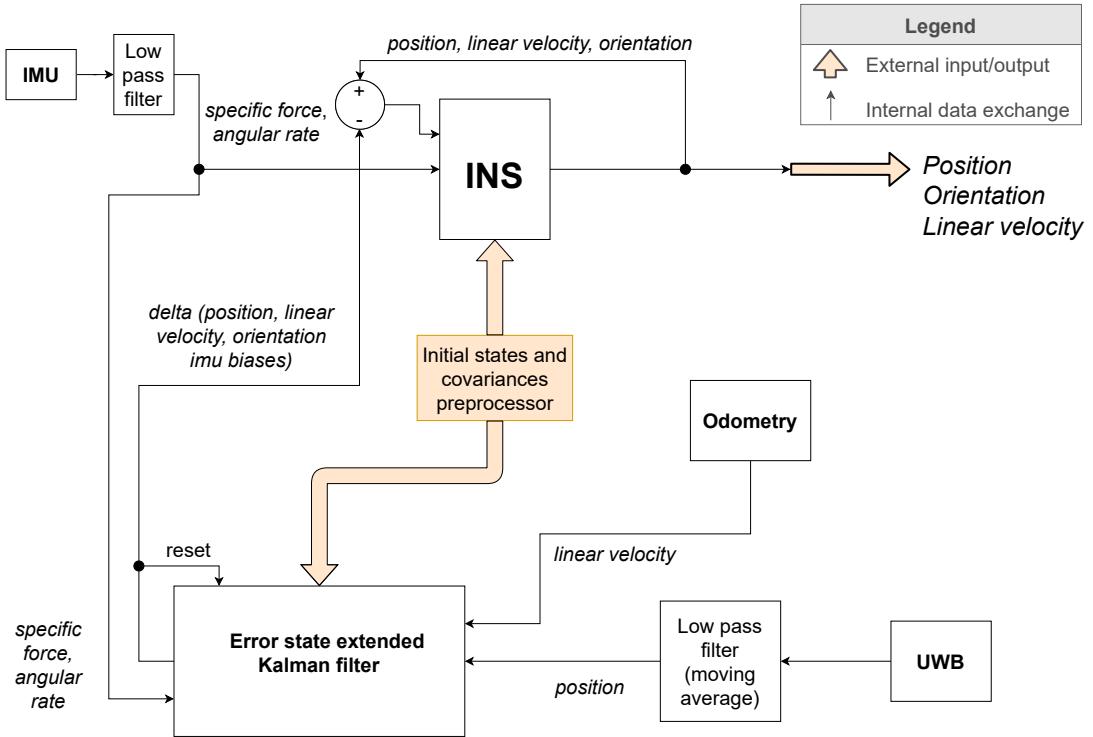
The second step is the ES-EKF itself. The error of the state is calculated and is then corrected using measurements from UWB localization and odometry. Measurements from UWB localization and odometry observe the error. The UWB localization gives us the absolute position, which can reduce the drift in step one.

The third part is injecting error into INS estimation and resetting the ES-EKF while the injection is done. Finally, the output of the whole system is given by the INS solution. The system requires initial states with covariances for INS and ES-EKF set up first. The simplified architecture is illustrated in Figure 5.1 and described in the following section in detail[15].

For navigation purposes, the regular rate of pose estimation is hundreds of Hertz[19]. The INS provides a full state estimate with the IMU update rate, which usually satisfies this requirement. Furthermore, it gives us the state estimation utterly independent of external factors, for example, slipping wheels[19].

As UWB localization and odometry measurements cannot give us a much higher rate than tens Hertz, they are used only in the correction step.

In other words, the most dynamic part of the estimation is somehow independent of Kalman filtering. On the one hand, the state estimation in INS is simple and fast. On the other hand, the error estimation can be more computationally demanding as the computation of Jacobians needs to be done. Therefore the separation of state



**Figure 5.1.** The proposed architecture of the localization system.

estimation and error estimation cause that the calculation of state is sufficiently fast. The error state is estimated separately in ES-EKF and is injected into the state only if another measurement than IMU comes in. The only requirement is that the correction needs to be applied before non-gaussian noise in IMU measurement is significant. That correction reduces the drift of the dead-reckoning system.

In conclusion, the benefit of this architecture is state estimation at a high rate, independent of external events. The state is corrected at a lower rate but faster than the non-gaussian noise becomes significant in state estimation. That brings us the best aspects of all types of sensors, which are used in the architecture.

In the following sections, the output of the system is called the navigation state (i.e., position, linear velocity, and attitude).

## 5.2 System kinematics

For a more detailed introduction to system architecture, the system kinematics equations need to be announced. But before I enter that itself, let me describe an important topic, which represents attitude and rotation in 3D space.

### 5.2.1 Representation of 3D attitude and rotation in space

There are many ways how to represent 3D attitude and rotation in space. The most commonly used representations in the field of robotics are

- rotation matrices,

- Euler angles,
- axis-angle
- and quaternions[1].

To not go into much detail, each representation has its pros and cons and applications, where it has its purpose. The rotation matrix is chosen as the internal representation of orientation and the quaternion as an output.

There are several reasons why to pick this representation[20–21]. Firstly, quaternions and rotation matrices do not suffer from singularities as Euler and fixed angles do[20]. Secondly, quaternion gives us a compact representation. And finally, these two are the most recommended representation in ROS standard rep-103[21]. As quaternions have many internal models in different libraries (Eigen library in C++[22], geometry messages library[23] or the transform library tf2 in ROS[24]) and the representation is not easy to imagine, I decided to use the quaternions only as an output and rotation matrix as the internal representation.

## 5.2.2 The kinematics equations in continuous time

The kinematics formulas in continuous time, that relates the inertial sensor measurements to the **true navigation state**, is well-known [15–16, 3, 2]. Therefore, I did not have to derive equations myself and used the one derived in [quaternion\_kinematics] equation 235. The only difference is that orientation is in the rotation matrix and not quaternion. Equations are

$$\begin{aligned}
 \dot{p}_t &= v_t \\
 \dot{v}_t &= R_t(a_m - a_{bt} - a_n) + g_t \\
 \dot{R}_t &= R_t(\Omega_t) \\
 \dot{a}_{bt} &= a_w \\
 \dot{\omega}_{bt} &= \omega_w \\
 \dot{g}_t &= 0,
 \end{aligned} \tag{1}$$

where

- $p_t$  is true position in 3D [m],
- $v_t$  is true linear velocity in 3D [ $m \cdot s^{-2}$ ],
- $R_t$  is true rotation matrix of orientation,
- $a_m$  is specific force given by accelerometers [ $m \cdot s^{-2}$ ],
- $a_{bt}$  is true accelerometer bias [ $m \cdot s^{-2}$ ],
- $a_n$  is accelerometers white Gaussian noise [ $m \cdot s^{-2}$ ],
- $a_w$  is white Gaussian noise accelerometers bias [ $m \cdot s^{-2}$ ],
- $g_t$  is true gravity vector [ $m \cdot s^{-2}$ ],
- $\Omega_t = [(\omega_m - \omega_{bt} - \omega_n)_{\times}] = \begin{bmatrix} 0 & -(\omega_{m3} - \omega_{bt3} - \omega_{n3}) & \omega_{m2} - \omega_{bt2} - \omega_{n2} \\ \omega_{m3} - \omega_{bt3} - \omega_{n3} & 0 & -(\omega_{m1} - \omega_{bt1} - \omega_{n1}) \\ -(\omega_{m2} - \omega_{bt2} - \omega_{n2}) & \omega_{m1} - \omega_{bt1} - \omega_{n1} & 0 \end{bmatrix}$  is true skew-symmetric matrix (a tensor of angular velocity) [ $\frac{rad}{s}$ ],
- $\omega_m$  is angular rate given by gyroscopes [ $\frac{rad}{s}$ ],
- $\omega_{bt}$  is true bias of gyroscopes [ $\frac{rad}{s}$ ],
- $\omega_n$  is gyroscopes white Gaussian noise [ $\frac{rad}{s}$ ],
- and  $\omega_w$  is white Gaussian noise gyroscopes bias [ $\frac{rad}{s}$ ].

The state  $x_t$ , is governed by IMU noisy reading  $u_m$  and perturbed by white Gaussian noise  $w$ , defined by

$$\begin{aligned} x_t &= [p_t, v_t, R_t, a_{bt}, \omega_{bt}, g_t]^T \\ u_t &= [a_m - a_n]^T \\ w_t &= [a_w, w_w]^T. \end{aligned} \quad (2)$$

The output of the localization system is **navigation state** (also called nominal), which corresponds to the system kinematics, but does not take into account the noise terms  $w_t$  and other possible model imperfections (see equation 237 in [15], hence it is simplified to

$$\begin{aligned} \dot{p} &= v \\ \dot{v} &= R(a_m - a_b) + g \\ \dot{R} &= R(\Omega) \\ \dot{a}_b &= 0 \\ \dot{\omega}_b &= 0, \\ \dot{g} &= 0, \end{aligned} \quad (3)$$

where

- $p$  is position in 3D [ $m$ ],
- $v$  is linear velocity in 3D [ $m \cdot s^{-2}$ ],
- $R$  is the rotation matrix of orientation,
- $a_m$  is specific force given by accelerometers [ $m \cdot s^{-2}$ ],
- $a_b$  is accelerometer bias [ $m \cdot s^{-2}$ ],
- $g$  is gravity vector [ $m \cdot s^{-2}$ ],
- $\Omega = [(\omega_m - \omega_b)_{\times}] = \begin{bmatrix} 0 & -(\omega_{m3} - \omega_{b3}) & \omega_{m2} - \omega_{b2} \\ \omega_{m3} - \omega_{b3} & 0 & -(\omega_{m1} - \omega_{b1}) \\ -(\omega_{m2} - \omega_{b2}) & \omega_{m1} - \omega_{b1} & 0 \end{bmatrix}$  is skew-symmetric matrix (a tensor of angular velocity) [ $\frac{rad}{s}$ ],
- $\omega_m$  is angular rate given by gyroscopes [ $\frac{rad}{s}$ ],
- $\omega_b$  is bias of gyroscopes [ $\frac{rad}{s}$ ].

The linearized dynamics (see equation 238 in [15]) of the **error state** are

$$\begin{aligned} \dot{\delta p} &= \delta v \\ \dot{\delta v} &= -R[a_m - a_b]_{\times} \delta \Theta - R \delta a_b + \delta g - R a_n \\ \dot{\delta \Theta} &= -[\omega_m - \omega_b]_{\times} \delta \Theta - \delta \omega_b - \omega_n \\ \dot{\delta a}_b &= a_w \\ \dot{\delta \omega}_b &= \omega_w \\ \dot{\delta g} &= 0, \end{aligned} \quad (4)$$

where

- $\delta p$  is the position error in [ $m$ ],
- $\delta v$  is the linear velocity error in [ $m \cdot s^{-2}$ ],
- $\delta \Theta$  is the orientation error,
- $\delta a_b$  is acceleration bias error [ $m \cdot s^{-2}$ ],
- $\delta \omega_b$  is gyroscope bias error [ $\frac{rad}{s}$ ],
- $\delta g$  is gravity vector error [ $m \cdot s^{-2}$ ],
- $R$  is rotation matrix given by nominal state,

- $a_m$  is specific force given by accelerometers [ $m \cdot s^{-2}$ ],
- $a_b$  is accelerometer bias [ $m \cdot s^{-2}$ ],
- $a_n$  is accelerometers white Gaussian noise [ $m \cdot s^{-2}$ ],
- $a_w$  is white Gaussian noise accelerometers bias [ $m \cdot s^{-2}$ ],
- $\omega_m$  is angular rate given by gyroscopes [ $\frac{rad}{s}$ ],
- $\omega_b$  is bias of gyroscopes [ $\frac{rad}{s}$ ],
- $\omega_n$  is gyroscopes white Gaussian noise [ $\frac{rad}{s}$ ],
- and  $\omega_w$  is white Gaussian noise gyroscopes bias [ $\frac{rad}{s}$ ]. .

Note that higher orders in linearization are neglected since the error state is small compared to the navigation state.

During **filter correction phase**, measurements from UWB localization and odometry comes into account. Usual, the sensor delivers measurements that depend on the state, such as

$$y = h(x_t) + \rho, \quad (5)$$

where  $h(t)$  is a general nonlinear function of the system state (the true navigation state), and  $\rho$  is a white Gaussian noise with covariance. For *UWB localization* the function is simple as it is

$$y_1 = p_t + \rho_1, \quad (6)$$

with covariance  $R_1$ . But for *odometry* it is a little bit complicated

$$y_2 = R_t^{-1}v_t + \rho_2 \quad (7)$$

with covariance  $R_1$ . This difference is important in the computation of Jacobian for the ES-EKF algorithm.

### 5.2.3 The kinematics equations in discrete time

As the equations in continuous time are derived from book [15], where their representation in discrete time is also presented, I decided to write down only parts, which are different. For more detail see equations 260 in [15]. The equation 260c is slightly different since I am using rotation matrix for orientation representation and not quaternion. This equation is changed to

$$R \leftarrow R + (R\Omega)\Delta t, \quad (8)$$

where

- $R$  is the rotation matrix of orientation,
- $\Omega = [(\omega_m - \omega_b)_{\times}] = \begin{bmatrix} 0 & -(\omega_{m3} - \omega_{b3}) & \omega_{m2} - \omega_{b2} \\ \omega_{m3} - \omega_{b3} & 0 & -(\omega_{m1} - \omega_{b1}) \\ -(\omega_{m2} - \omega_{b2}) & \omega_{m1} - \omega_{b1} & 0 \end{bmatrix}$  is skew-symmetric matrix (a tensor of angular velocity) [ $\frac{rad}{s}$ ],
- $\omega_m$  is angular rate given by gyroscopes [ $\frac{rad}{s}$ ],
- $\omega_b$  is bias of gyroscopes [ $\frac{rad}{s}$ ].

This integration is happening in the INS box in Figure 5.1.

## 5.3 Error state extended Kalman filter implementation

Algorithm and equations for general extended Kalman filter are briefly described in Chapter 4. In this section, these equations are concretized.

The **error state system** is now

$$\delta x \leftarrow f(x, \delta x, u_m, i) = F_x(x, u_m) \cdot \delta x + F_i \cdot i, \quad (9)$$

where

- $i$  is a perturbation vector (usually modelled as white Gaussian noise).

The **Es-EKF prediction part** is given by

$$\begin{aligned} \hat{\delta x} &\leftarrow F_x(x, u_m) \cdot \hat{\delta x} \\ \hat{P} &\leftarrow F_x P F_x^T + F_i Q F_i^T, \end{aligned} \quad (10)$$

where

- $P$  is a process covariance matrix,
- $F_x$  is transition matrix,
- $F_i$  is Jacobian of error state system by impulses,
- $Q$  is covariances of process noise,

The **transition matrix** (also called system matrix)  $F_x$  is error state Jacobian and it is simple determined by error state kinematics equations  $f(\delta x_t)$  in discrete time in Section 5.2.3,

$$F_x = \frac{\partial f(\delta x, u_m)}{\partial \delta x} = \begin{bmatrix} I & I\Delta t & 0 & 0 & 0 & 0 \\ 0 & I & -R[a_m - a_b] \times \Delta t & -R\Delta t & 0 & I\Delta t \\ 0 & 0 & R\{\omega_m - \omega_b\}^T \Delta t & 0 & -I\Delta t & 0 \\ 0 & 0 & 0 & I & 0 & 0 \\ 0 & 0 & 0 & 0 & I & 0 \\ 0 & 0 & 0 & 0 & 0 & I \end{bmatrix}. \quad (11)$$

$F_i$  is given by

$$F_i = \frac{\partial f}{\partial i} \Big|_{x, u_m} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ I & 0 & 0 & 0 \\ 0 & I & 0 & 0 \\ 0 & 0 & I & 0 \\ 0 & 0 & 0 & I \\ 0 & 0 & 0 & 0 \end{bmatrix}, \quad (12)$$

The covariances matrix is given by random impulses applied to the velocity, orientation and bias estimates, modelled by white Gaussian noise [15]

$$Q = \begin{bmatrix} \sigma_{a_n}^2 \Delta t^2 I & 0 & 0 & 0 \\ 0 & \sigma_{\omega_n}^2 \Delta t^2 I & 0 & 0 \\ 0 & 0 & \sigma_{a_w}^2 \Delta t^2 I & 0 \\ 0 & 0 & 0 & \sigma_{\omega_w}^2 \Delta t^2 I \end{bmatrix}, \quad (13)$$

where

- $\sigma_{a_n}$  is standard deviation of accelerometers [ $m \cdot s^{-2}$ ],
- $\sigma_{\omega_n}$  is standard deviation of accelerometers [ $\frac{rad}{s}$ ]
- $\sigma_{a_w}$  is velocity random walk [ $\frac{rad}{s\sqrt{s}}$ ],
- $\sigma_{\omega_w}$  is angular random walk [ $\frac{rad}{s\sqrt{s}}$ ].

This information can be obtained from the datasheet or AVAR (see Section 3.2.3).

The **ES-EKF correction part** is given by

$$\begin{aligned} K &\leftarrow P H^T (H P H^T + R)^{-1} \\ \delta x &\leftarrow K(y - h(\hat{x})) \\ P &\leftarrow (I - K H) \hat{P} (I - K H)^T + K R K^T \end{aligned} \quad (14)$$

where

- $K$  is Kalman gain,
- $H$  is observation matrix,
- $R$  is covariances of observation noise,
- $P$  is process covariance,
- $y$  is an observation,
- $h(\hat{x})$  is an observation model,
- $\delta x$  is a error state.

The bf observation matrices differs for *UWB localization* ( $H_1$ ) and *odometry* ( $H_2$ )

$$\begin{aligned} H_1 &= [I \ 0 \ 0 \ 0 \ 0 \ 0] \\ H_2 &= [0 \ R_t^T \ -R_t^T [v_t]_{\times} J_r(\Theta) \ 0 \ 0 \ 0], \end{aligned} \quad (15)$$

where

- $R_t$  is orientation in navigation state,
- $v_t$  is linear velocity in navigation state,
- $\Theta$  is orientation  $R_t$  in rotation vector form,
- $J_r$  is right jacobian of rotation group  $SO(3)$  (see equation 183 in [15]).

To obtain  $H_2$  from Equation (7), a reader should notice a Jacobian with respect to the rotation vector in section 4.3.4 and equation 188 in [15].

## 5.4 Injection the error state into the navigation state

While the correction phase is done, the estimated error state comes into account in the navigation state

$$x \leftarrow x \bigoplus \delta x, \quad (16)$$

where

$\bigoplus$  appropriate composition of sums or rotation product.

The equations are

$$\begin{aligned} p &\leftarrow p + \delta p \\ v &\leftarrow v + \delta v \\ R &\leftarrow R * R\{\delta\Theta\} \\ a_b &\leftarrow a_b + \delta a_b \\ \omega_b &\leftarrow \omega_b + \delta \omega_b \\ g &\leftarrow g + \delta g \end{aligned} \quad (17)$$

where

$R\{\delta\Theta\}$  orientation error in rotation matrix.

The injection of the error state is essential, but the resetting of the error state must also be done.

## 5.5 Implementation tools

This section briefly introduces tools used for implementation: the ROS2[25] framework, C++ and Python languages.

**ROS2[25]** is a set of software libraries and tools for building robot applications. It is open-source, and it consists of drivers for hardware, state-of-the-art algorithms, tools for debugging, visualisation, simulation, communications overall processes. All applications created in ROS2 are easy to share and used in the community. It supports all most known and most used programming languages like C++, Python, Java, Lua or Lisp. ROS2 distributions are released to work on operating systems like Ubuntu, MacOs or Windows. Nevertheless, as it is open-source, users usually use it with one Ubuntu distributions, such as 20.04 or 18.04.

The newest version of ROS is ROS2, introduced in 2014 at the conference ROSCon 2014 in Chicago[25], but the first distribution was released in May 2019. There are several distributions of ROS2 yet, the localisation system and experiments are implemented using Foxy Fitzroy<sup>1</sup> which was released in June 2020<sup>2</sup>.

ROS2 has defined code style and languages version which are recommended to use. The implementation sticks to these rules and uses C++17 and Python3. As the localisation needs to be implemented as a real-time application, it is implemented in C++17. Python3 is used for the visualisation of experiments results and supporting scripts.

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<sup>1</sup> The documentation to ROS2 Foxy Fitzroy <https://docs.ros.org/en/foxy/index.html>

<sup>2</sup> The list of all distributions of ROS2 <https://docs.ros.org/en/galactic/Releases.html>

# Chapter 6

## Experiments

This chapter is dedicated to the experimental evaluation of the proposed localization system.

TODO dopsat pouzite metriky v experimentech a co nas vlastne zajima. - co nas zajima pro evaluaci lokalizace ve 2D prostoru - jake metriky budou pouzite (inspirace u Halodove)

Localization system was implemented on a robotic platform CART2, where inertial measurement unit and ultra-wideband localization tag were mounted. Specific hardware and the robotic platform are introduced in first section.

Next two sections are dedicated to experiments at two different experimental environments. First experiments, described in second section, were realized in a lab at Datavision s. r. o. company with an external localization system based on an AprilTag detection with camera. The external localization system was developed in this thesis for evaluation of the proposed localization system.

Additional experiments took place in a Intelligent and mobile robotics lab at Czech Technical University in Prague – Czech Institute of Informatics, Robotics, and Cybernetics, where Vicon reference system is used for evaluation. These experiments are summarized in third section of this chapter.

### 6.1 Used hardware description

In this section, overview of used sensors for the proposed localization is given as well as a description of CART2 robotic platform used during experiments.

#### 6.1.1 Sensors specification

The onboard sensors of interest are Inertial Measurement Unit, ultra-wideband localization tag, april tag and encoders on motors.

**Inertial measurement unit** used during experiments is Epson M-G365PDF1 (loaner sample). Epson M-G365 is used in a number of various applications ranging from stabilization systems (as camera gimbal) or navigation systems.



**Figure 6.1.** IMU used in experiments Epson M-G365PDF1.



**Figure 6.2.** Experimental setup for static data acquisition of Epson M-G365PDF1.

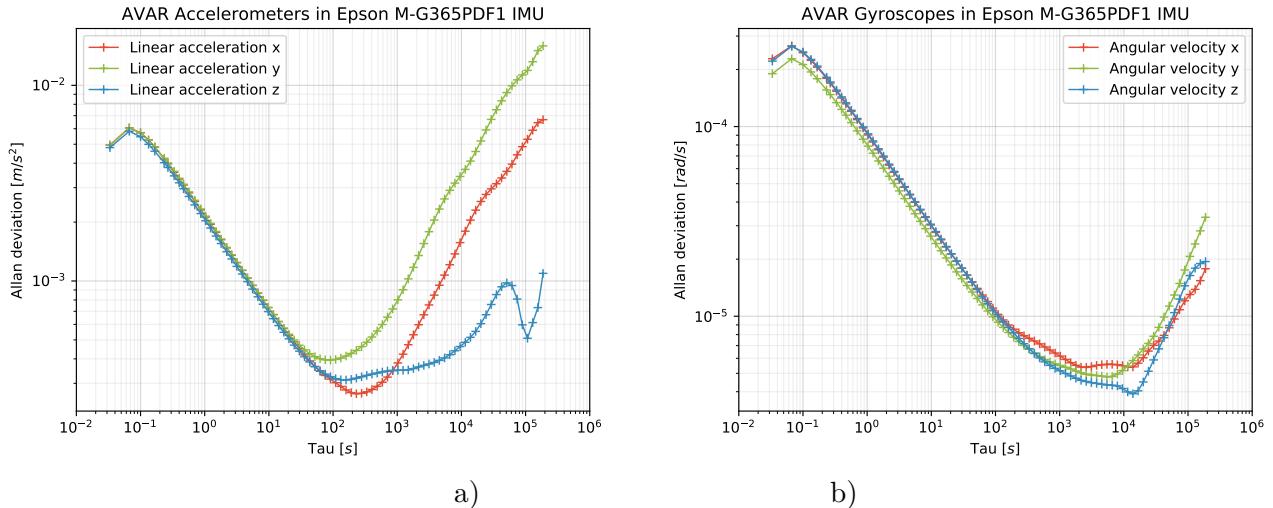
The IMU has six degrees of freedom and measures angular rates and linear accelerations in three axis. It is factory calibrated and the calibration data are stored in the memory of the unit. Technical specifications of Epson M-G365 can be found at <sup>1</sup>, while summary is included in Table 6.1

Specification	Value
Triple gyroscopes	$\pm 450^\circ/\text{sec}$
Gyroscopes bias instability	$1.2^\circ/\text{hr}$
Gyroscopes initial bias error	$0.1^\circ/\text{s}$
Angular random walk	$0.08^\circ/\sqrt{\text{hr}}$
Tri-axis accelerometers	$\pm 10\text{ G}$
Accelerometers bias instability	$16\text{ }\mu\text{G}$
Accelerometers initial bias error	$3\text{ mG}$
Velocity random walk	$0.033\text{ (m/s)}/\sqrt{\text{hr}}$

**Table 6.1.** Technical specifications of Epson M-G365PDF1[7].

As I already mentioned in Chapter 3.2.3, the AVAR analysis of IMU sensors can give us a brief overview of IMU's specification. Experimental setup for static data acquisition can be seen in Figure 6.2. The sensor is mounted on two sponge and fixed with cartboard. The static data were recorded for 48 hours at frequency of 30.0 Hz. The experiment took place at a village without any subway, trams or trains to reduce external vibrations on measurement (to reduce potential outliers) and at standard room temperature (about  $23^\circ\text{C}$ ).

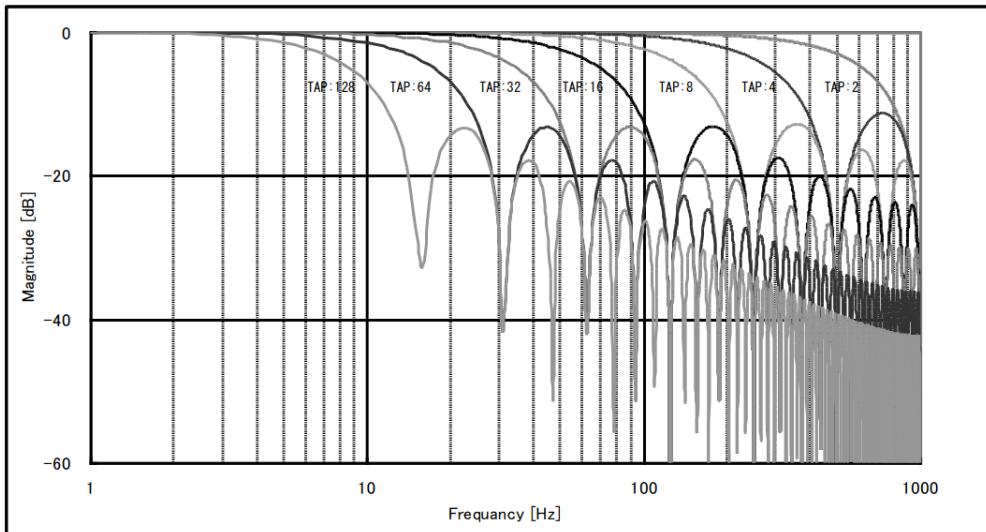
For AVAR computation I used a python library named AllanTools, for purposes of this thesis the overlapping Allan deviation function is used.



**Figure 6.3.** Overlapping Allan variance plot for Epson M-G365PDF1.

As you can see in the Figure 6.3, the external reset of integration of IMU measurement must be performed at 0.01 Hz at the latest. After that period, non gaussian noise of accelerometers comes into account. The UWB localization system works at 10 Hz, that should be enough for the resetting.

<sup>1</sup> Datasheet of Epson M-G365 [https://global.epson.com/products\\_and\\_drivers/sensing\\_system/download\\_hidden/pdf/m-g365pd\\_datasheet\\_e\\_rev20201007.pdf](https://global.epson.com/products_and_drivers/sensing_system/download_hidden/pdf/m-g365pd_datasheet_e_rev20201007.pdf)



**Figure 6.4.** Moving average filter characteristics for Epson M-G365PDF1[7].

For the final experiments, the IMU is setup to publish delta angle and delta velocity at 100 Hz with moving average filter with tap 64. Because of that, higher frequencies than 10 Hz are filtered as can be seen in Figure 6.4.

**UWB localization system** is provided by Qorvo's MDEK1001 ultra-wideband development kit. This kit includes 12 DWM1001-DEV development boards in plastic enclosures (see Figure 6.5).



**Figure 6.5.** DWM1001-DEV development boards[26].

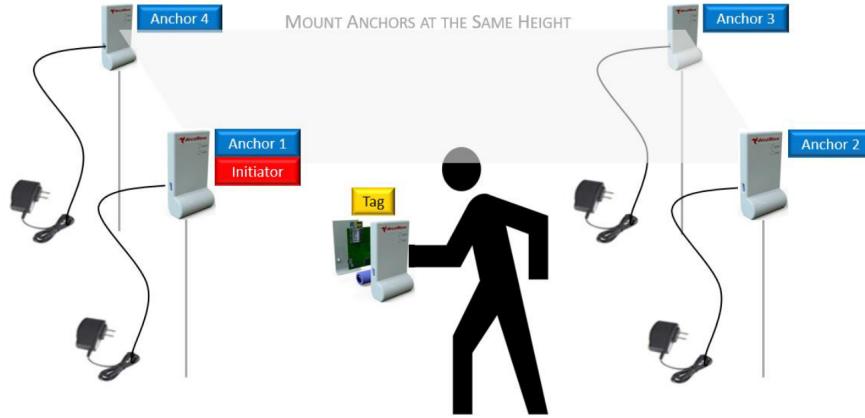
Each can be configured as an anchor, tag or bridge node. The system is installed with 6 anchors fixedly mounted and one tag which can be moved. The anchors are higher than tag. According to the initiator anchor, the tag's position gives the coordinates frame's origin. The set up of the system can be seen in Figure 6.6.

The anchors should be mounted at the same height and higher than the operating area of the moving tag. They also should not be mounted close to any metal to get the best accuracy. The configuration of the whole network is done via their mobile application and positions of the anchors are estimated manually.

Technical specification of MDEK1001 and DWM1001-DEV can be found in documents [26], the summary is listed in Table 6.2.

**The odometry** is computed according to measurement of encoders in Maxon EPOS4 positioning controllers for Maxon brushless DC motors.

**AprilTag** serves as a global reference of pose of the CART2 platform. The AprilTag detection software computes the precise 3D position, orientation, and identity of the tags



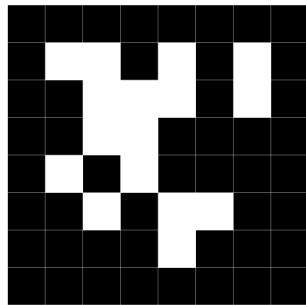
**Figure 6.6.** Positioning of anchors and tags[26].

Specification	Value
Maximum tag location rate	10 Hz
X-Y location accuracy	< 10 cm
Point to point range	up to 60 m in line of sight conditions
Scheme range	25 - 30 m between anchors

**Table 6.2.** System performance of MDEK1001[26].

relative to the camera[27]. This tag is similar to QR codes (a type of two-dimensional bar code), but it encodes smaller data payloads (between 4-12 bits) and it can be detected more robustly.

**Camera** used for detection of AprilTag is Niceboy Stream Pro with Full HD (1920 x 1080) resolution, 30 FPS, 90 ° field of vision and f/1.8 lens aperture[28].



**Figure 6.7.** AprilTag used for detection of CART2 position at Datavision s. r. o.

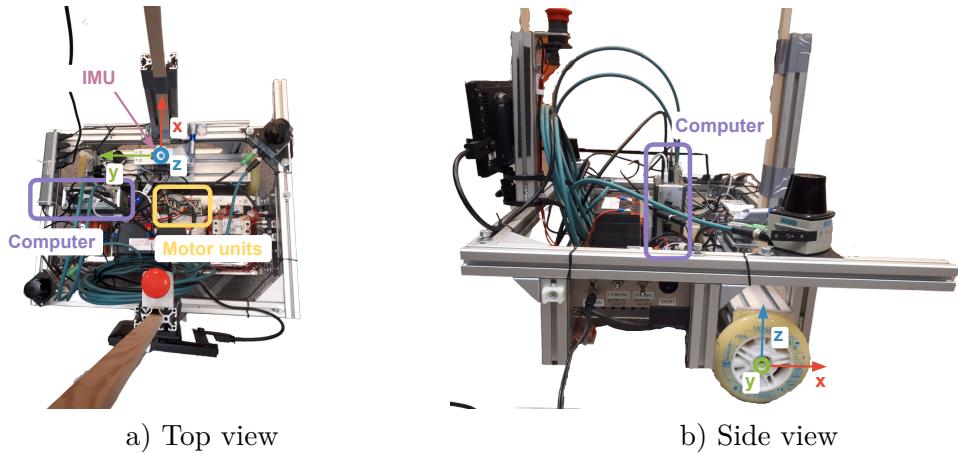


**Figure 6.8.** Camera used for AprilTag detection Niceboy Stream Pro[28].

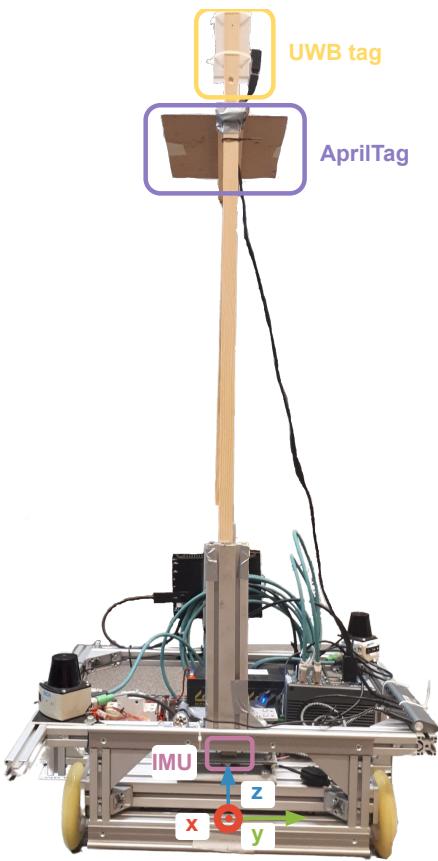
### 6.1.2 CART2 platform description and sensors placements

An image of the utilized CART2 platform can be seen in Figure 6.9. The coordinate frame of CART2 called `baselink` is illustrated in all Figures 6.9 and 6.10. The CART2 used for a various robotic competitions is a differential drive and is equipped with the ADlink MXE-210 computer.

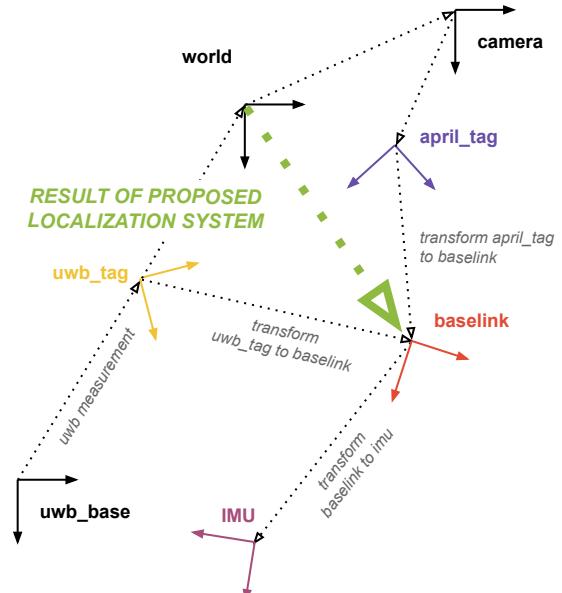
The onboard sensors placements are illustrated in Figure 6.10. The vehicle uses Maxon brushless DC motor (Maxon EC-imotor), which is controlled by Maxon EPOS4 control units.



**Figure 6.9.** A photo of the utilized CART2 platform.



**Figure 6.10.** A photo of sensors placements on CART2.



**Figure 6.11.** Illustration of coordinate systems at CART2.

The UWB tag is mounted on a wooden stick approximately one meter upon the CART2 platform to reduce reflections of UWB wave from surfaces and negative influence of any metal part. The AprilTag is mounted below the UWB tag to not become a barrier in UWB wave. When the AprilTag was mounted on top of the CART2 platform, the wooden stick obstructs the camera detection of AprilTag in some position of CART2 in a room, thus I decided to mount it as high as possible to reduce these situations.

Transform	Translation [x, y, z] in [m]	Rotation in quaternion [x, y, z, w]
uwb_tag to baselink	[0.0, 0.0, 1.192]	[0.0, 0.0, 0.0, 1.0]
apriltag to baselink	[0.0, -0.171, 1.071]	[0.707107, -0.707107, 0.0, 0.0]
imu to baselink	[0.0, 0.0, 0.05]	[0.0, 0.0, -0.7071068, 0.7071068]

**Table 6.3.** Summary of transforms for experiments with CART2.

**Coordinate systems of CART2 and sensors placements** are illustrated in Figure 6.11 and described in Table 6.3. Note, that world, camera and uwb\_base frames are fixed with environment and explained in Section 6.2.

## 6.2 Experiments in the lab at Datavision s. r. o.

### 6.2.1 Experimental lab description

For first experiments I created an experimental setup at Datavision s. r. o. with global reference given by camera detection of AprilTag mounted at CART2 platform. The address of the building is Ukrajinská 1487/2a, 101 00 Prague 10 - Vršovice. Dimensions of the room for experiments are approximately 4 x 6 [m] and the camera view area is approximately 2.5 x 4.5 [m]. The setup can be seen in Figure 6.12.

Firstly, UWB anchors need to be mounted and measured their poses according to the world coordinate system. These poses need to be set in the mobile application, where all the uwb network can be set up. The world frame coincides to uwb\_base frame in rotation and only differs in z coordinate in translation.

Transform	Translation [x, y, z] in [m]	Rotation in quaternion [x, y, z, w]
world to uwb_base	[0.0, 0.0, 2.58]	[0.0, 0.0, 0.0, 1.0]
world to camera	[1.089, 2.024, 2.625]	[0.707107, -0.707107, 0.0, 0.0]

**Table 6.4.** Summary of transforms for experiments setup at Datavision s. r. o..

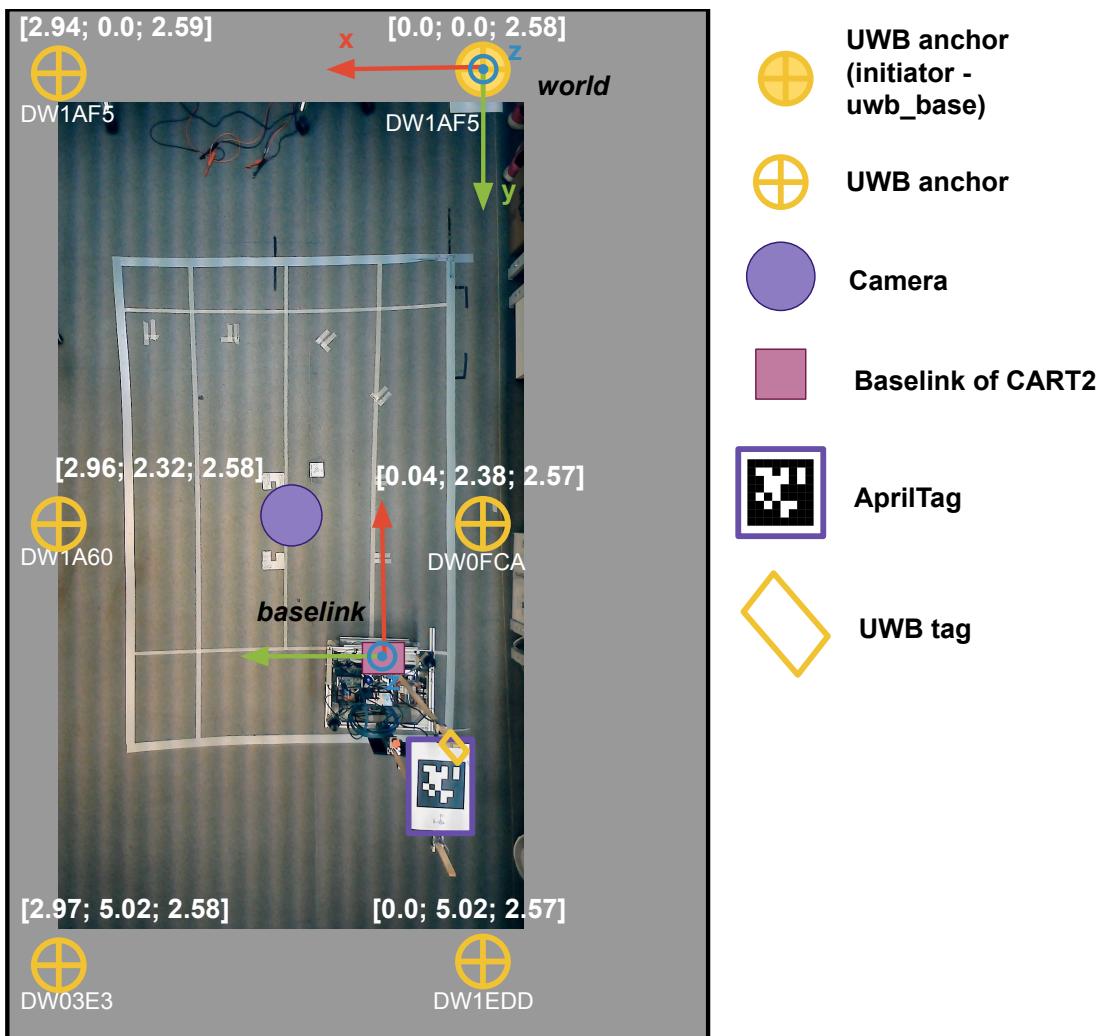
Secondly, the camera need to be mounted and measured its position according to the world coordinate system. The transform between world and camera is not trivial, because of that I decided to use transformation mentioned in Table 6.4 and then computed a camera homography according to a few positions measured by camera detection and by hand. The homography defines the transformation between a planar surface (ground) and camera image plane. The camera homography is then applied to the AprilTag detection pose and this pose is considered as global reference. These frames are illustrated in 6.11.

### 6.2.2 Description of experiments

The area for experiments is not big, but I decided that these experiments serve as a proof of concept of the localization idea.

Experiments can be divided based on six simple trajectories of CART2 into

- stationary test (stationary test),
- rotation above 360 degrees in one direction at one place test (rotation test),
- moving in x direction (x test),

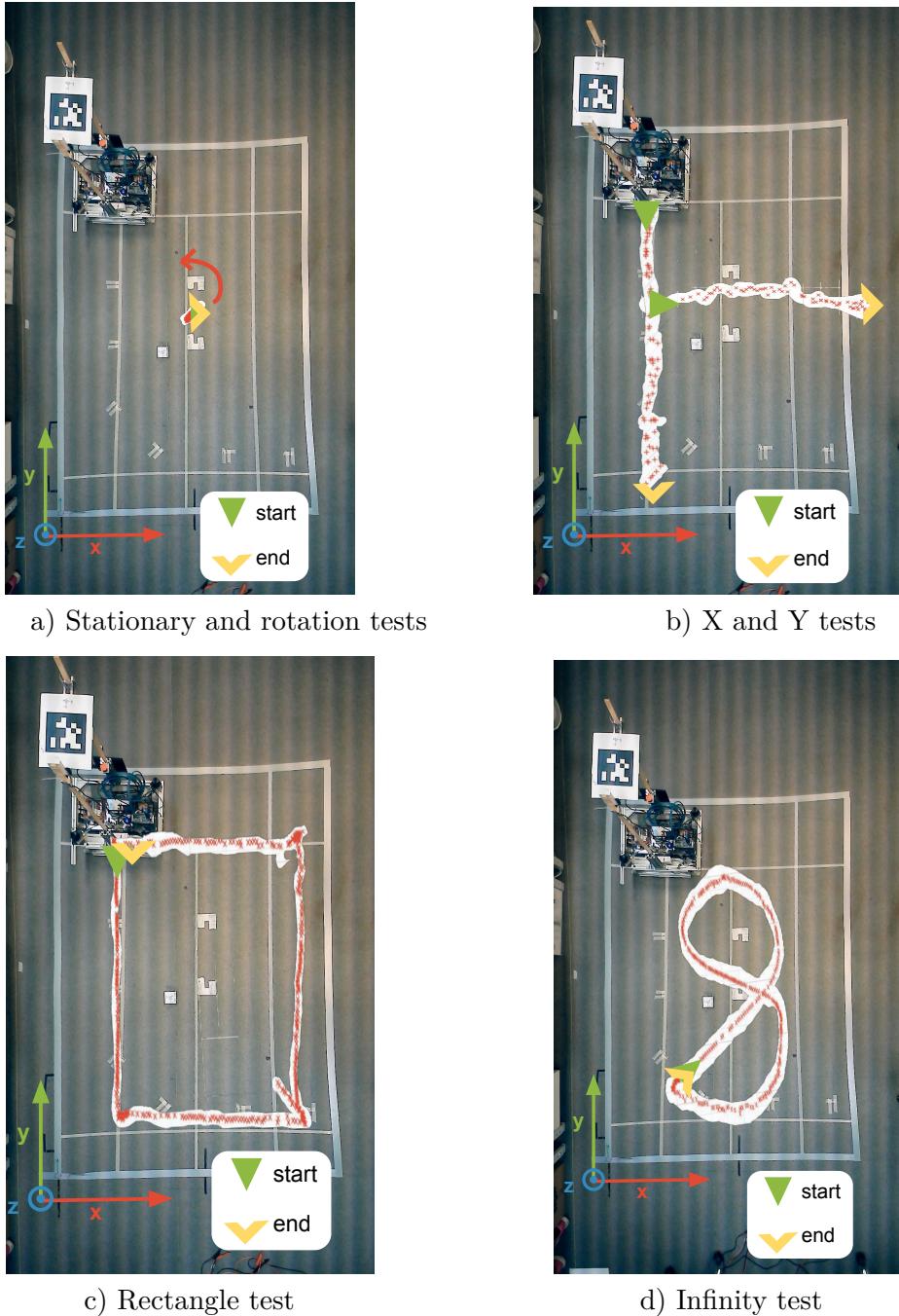


**Figure 6.12.** Experimental setup at Datavision s. r. o..

- moving in y direction (y test),
- moving in rectangle shape (rectangle test)
- and moving in infinity shape (infinity test).

For each testing trajectories I picked specific initial pose to be possible to make these tests repetitively in very similar conditions. Also rotation, rectangle and infinity tests ran several times in a row without start/stop of the system to see, how it behaves in a long term.

Trajectories of these tests as well as the starting and ending positions of CART2 performing the movement are illustrated in Figure 6.13. CART2 platform was controlled via keyboard and joystick during experiments. The controlling via keyboard has a benefit of control velocity in each direction easily, thus I used it for constant velocity during simple moving in single axis and simple rotation around single axis. With that I controlled all tests, except infinity test, where the movement is more complicated. During rectangle test, CART2 drove forward (moving in single axis) then stopped and turned at one place above 90 degrees (rotating above single axis). In infinity movement I drove the CART2 platform with joystick and tried to move similar velocities as in constant movements. The summary of velocities during experiments is given in Table 6.5.



**Figure 6.13.** Trajectories for experiments at Datavision s. r. o..

### ■ 6.2.3 Evaluation of experiments

TODO

## ■ 6.3 Experiments at CIIRC

### ■ 6.3.1 Experiments at CIIRC description

Next experimental environment was placed at Czech Technical University in Prague – Czech Institute of Informatics, Robotics, and Cybernetics (CIIRC) in the lab Intelligent

Test	Description	Speed [m/s]	Turn [rad/s]
stationary	Constant velocities	0.0	0.0
rotation	Constant velocities	0.0	0.1094
x	Constant velocities	0.0750	0.0
y	Constant velocities	0.0750	0.0
rectangle	Constant velocities	0.0750 or 0.0	0.0 or 0.1094
infinity test	non constant (control via joystick)	approx. 0.0750	approx. 0.1094

**Table 6.5.** Velocities during experiments in Datavision s. r. o..

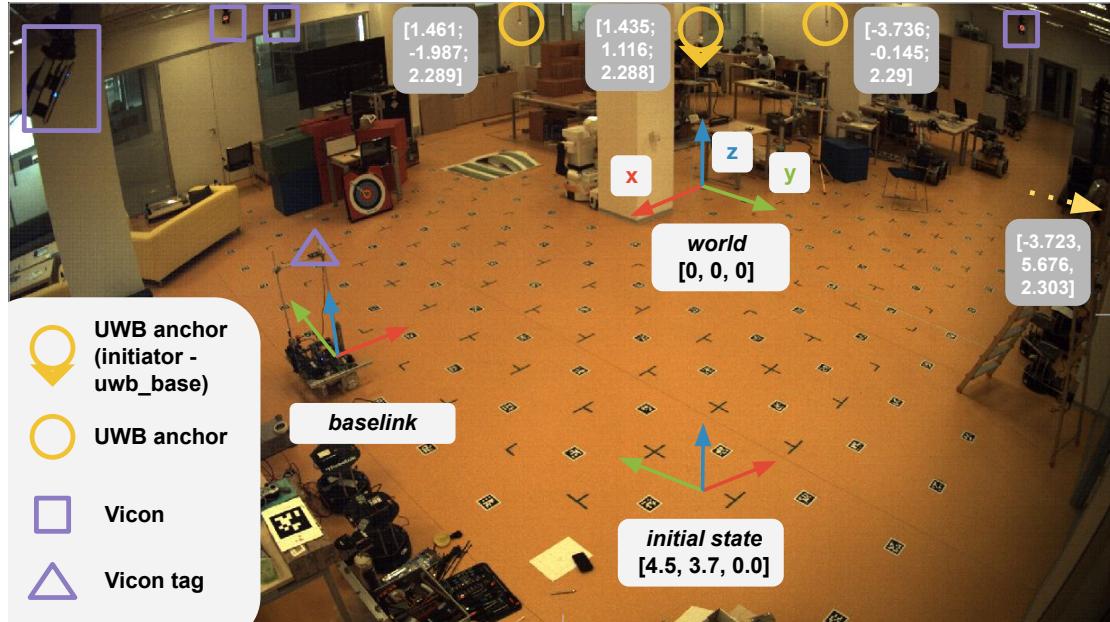
and mobile robotics. Here, the localization system was evaluated using the the VICON external camera localization system [29]. The world frame is defined by the VICON. UWB localization is installed with six anchors and their positions are defined in a world frame. The setup is illustrated in Figure 6.14. The benefit of this environment is size of the laboratory, the minimal distance between two anchors is bigger then 3,5 meters, thus the accuracy of UWB localization should be increased.

Experiments here are more complex, because they are longer both in terms of duration or in terms of travelled distance. These experiments promised to evaluate possible drift caused by the use two relative localization based on IMU and odometry. As I already mentioned in previous chapters, localization based on pure IMU drift with time and odometry drift with travelled distance. Performed experiments can be divided based on 3 simple trajectories of CART2 into

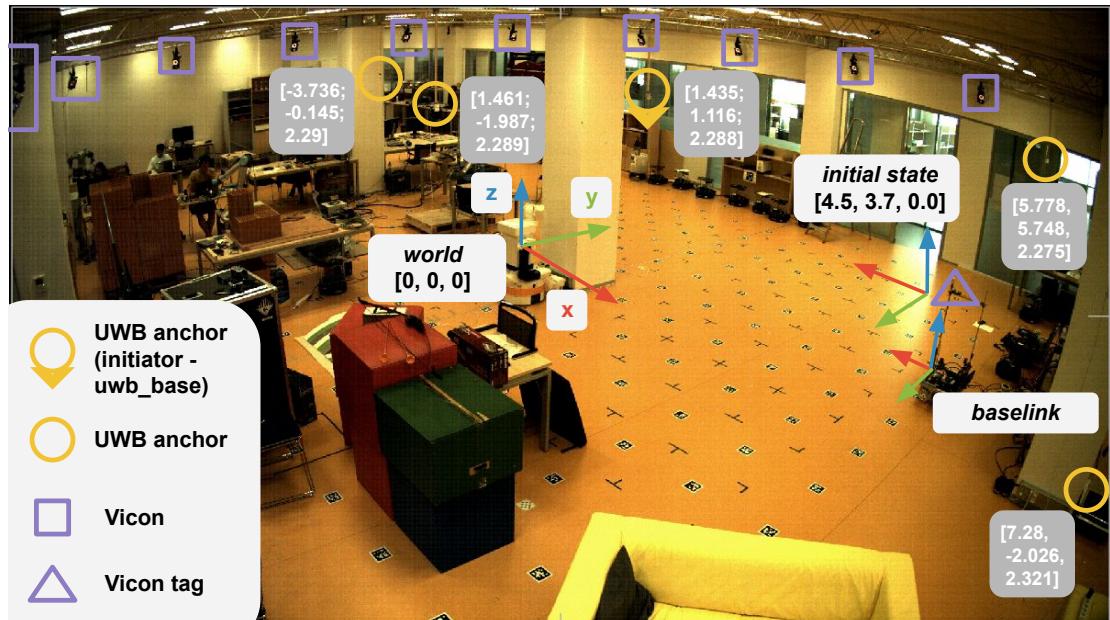
- moving in rectangle shape (rectangle test),
- moving in infinity shape (infinity test)
- and moving in bean shape (bean test).

For each testing trajectories I picked specific initial pose to be possible to make these tests repetitively in very similar conditions. Also rotation, rectangle and infinity tests ran several times in a row without start/stop of the system to see, how it behaves in a long term.

### ■ 6.3.2 Evaluation of experiments at CIIRC



a) View from camera 1



b) View from camera 2

**Figure 6.14.** Experimental setup at Intelligent and mobile robotics lab (CIIRC).

## Chapter 7

### Conclusion and future work

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#### 7.1 Evaluace vysledku z experimentu celkova

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#### 7.2 Možné využití této fuze v průmyslu

#### 7.3 Future work

- kalibrace sensoru poradna - použití virtuálních sensorů (robot stojí, robot jede jen rovně...) k tomu, aby estimace byla lepsi - jak to rozšírit pro fungování na dronech - lepsi hardware pro realtime aplikace

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# Appendix A

## Abbreviations and symbols

### A.1 A list of abbreviations

All abbreviations used in this thesis are listed below.

- AVAR Allan variance.
- DOF Degrees of freedom.
- ES-EKF Error state extended Kalman filter.
- IMU Inertial measurement unit.
- INS Inertial navigation system.
- MEMS Microelectromechanical systems.
- UWB Ultra-wideband.
- ROS2 Robot Operating System 2.
- CTU Czech Technical University in Prague.
- CIIRC Czech Institute of Informatics, Robotics and Cybernetics.