
Lab 1 Part 2

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2.1 - Construction of the Bach Fugue

```
load bach_fugue.mat
song = playSong(theVoices);
audiowrite('bach_fugue.wav', song/max(song), 11024);
```

2.2 - Musical Tweaks - Enveloping

```
type ADSR
type playSongWithADSR

load bach_fugue.mat
song = playSongWithADSR(theVoices);
audiowrite('bach_fugue_ADSR.wav', song/max(song), 11024);

function tone = ADSR(tone)
    %{
    ADSR: Apply an envelope to a particular note.
    Input Args:
    -tone: the tone to apply the ADSR envelope to.
    Output:
    -tone: the tone that was supplied as a parameter, with the ADSR
    envelope.
    Usage:
    envelopedTone = ADSR(tone);
    %}

    A = linspace(0.0, 0.9, (length(tone)*0.25)); % rise 25%
    D = linspace(0.9, 0.7, (length(tone)*0.05)); % drop 5%
    S = linspace(0.7, 0.7, (length(tone)*0.40)); % maintain 40%
    R = linspace(0.7, 0.0, (length(tone)*0.30)); % drop 30%
    ADSR = [A D S R];

    x = zeros(size(tone));
    x(1:length(ADSR)) = ADSR;
    tone = tone .* x;
end

function song = playSongWithADSR(theVoices)
    %{
```

```

PLAYSONG: Produce a sinusoidal waveform containing the combination
of the different notes in theVoices
Input Args:
    -theVoices: structure contains noteNumbers, durations, and
startpulses vectors for multiple voices.
Output:
    -song: vector that represents discrete-time version of a musical
waveform
Usage: song = playSong()
%}

fs = 11024;
bpm = 120;
bps = bpm / 60;
spb = 1 / bps;
spp = spb / 4; %seconds per pulse, theVoices is measured in pulses
with 4 pulses per beat

maxIndex = 1;
for i = 1:length(theVoices)
    lastNoteNumber = length(theVoices(i).noteNumbers);
    lastNote = key_to_note(0.5,
theVoices(i).noteNumbers(lastNoteNumber),
theVoices(i).durations(lastNoteNumber)*spp);
    currentIndex = spp*fs*theVoices(i).startPulses(lastNoteNumber)
+ length(lastNote) - 1;
    if currentIndex > maxIndex
        maxIndex = currentIndex;
    end
end

song = zeros(1, maxIndex); %Create a vector of zeros with length
equal to the total number of samples in the entire song

%Then add in the notes
for i = 1:length(theVoices)
    for j = 1:length(theVoices(i).noteNumbers)
        keynum = theVoices(i).noteNumbers(j);
        dur = theVoices(i).durations(j)*spp;
        note = ADSR(key_to_note(0.5, keynum, dur)); %Create
sinusoid of correct length to represent a single note
        locstart = spp*fs*theVoices(i).startPulses(j); % Index of
where note starts
        locend = locstart + length(note) - 1; % index of where
note ends
        song(locstart:locend) = song(locstart:locend) + note;
    end
end
song = song/max(song);
soundsc(song, fs);
end

```

2.3 - Musical Tweaks - Fourier Series of a Trumpet

```

type playSongWithTrumpet
type key_to_trumpet_note

load bach_fugue.mat
song = playSongWithTrumpet(theVoices);
audiowrite('bach_fugue_trumpet_ADSR.wav', song/max(song), 44100);

function song = playSongWithTrumpet(theVoices)
    %{
        PLAYSONG: Produce a sinusoidal waveform containing the combination
        of the different notes in theVoices
        Input Args:
        -theVoices: structure contains noteNumbers, durations, and
        startpulses vectors for multiple voices.
        Output:
        -song: vector that represents discrete-time version of a musical
        waveform
        Usage: song = playSong()
    %}

    fs = 44100;
    bpm = 120;
    bps = bpm / 60;
    spb = 1 / bps;
    spp = spb / 4; %seconds per pulse, theVoices is measured in pulses
    with 4 pulses per beat

    maxIndex = 1;
    for i = 1:length(theVoices)
        lastNoteNumber = length(theVoices(i).noteNumbers);
        lastNote =
key_to_trumpet_note(theVoices(i).noteNumbers(lastNoteNumber),
theVoices(i).durations(lastNoteNumber)*spp);
        currentIndex = spp*fs*theVoices(i).startPulses(lastNoteNumber)
+ length(lastNote) - 1;
        if currentIndex > maxIndex
            maxIndex = currentIndex;
        end
    end

    song = zeros(1, ceil(maxIndex)); %Create a vector of zeros with
length equal to the total number of samples in the entire song

    %Then add in the notes
    for i = 1:length(theVoices)
        for j = 1:length(theVoices(i).noteNumbers)
            keynum = theVoices(i).noteNumbers(j);
            dur = theVoices(i).durations(j)*spp;

```

```

        note = ADSR(key_to_trumpet_note(keynum, dur)); %Create
        sinusoid of correct length to represent a single note
        locstart = spp*fs*theVoices(i).startPulses(j); % Index of
        where note starts
        locend = locstart + length(note) - 1; % index of where
        note ends
        % floor is included here to remove the warning "Integer
        operands are required for colon operator when used as index."
        song(floor(locstart):floor(locend)) =
        song(floor(locstart):floor(locend)) + note;
    end
end
song = song/max(song);
soundsc(song, fs);
end

function xx = key_to_trumpet_note(keynum, dur)
%{
    KEY_TO_TRUMPET_NOTE: Produce a sinusoidal waveform corresponding
    to a given piano key number
    Input Args:
    -X: amplitude (default = 1)
    -keynum: number of the note on piano keyboard -dur: duration of
    the note (in seconds)
    Output:
    -xx: sinusoidal waveform of the note
%}
    harmonics.amplitudes = [0.1155, 0.3417, 0.1789, 0.1232, 0.0678,
    0.0473, 0.0260, 0.0045, 0.0020];
    harmonics.phases = [-2.1299, 1.6727, -2.5454, 0.6607, -2.0390,
    2.1597, -1.0467, 1.8581, -2.3925];

    fs = 44100;
    tt = 0:(1/fs):dur-1/fs;
    freq = 440 * ( 2^( (keynum-49)/12 ) );
    xx = zeros(1,length(tt));

    for k = 1:length(harmonics.amplitudes)
        A = harmonics.amplitudes(k);
        phi = harmonics.phases(k);
        xx = xx + real( A*exp(j*2*pi*freq*k*tt)*exp(j*phi) );
    end
end
end

```

Question 1: Suppose the maximum frequency in the Bach Fugue is 1200 Hz. What is the minimum sampling frequency needed to synthesize, without aliasing, a trumpet sound containing nine harmonics?

According to the Nyquist Theorem, we need a sampling frequency of at least $1200 \text{ Hz} * 2 + 1 = 2401 \text{ Hz}$ to avoid aliasing.