# Programming Assignment 1

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### Grade For a B

We randomly create vector p containing either 4 or 11 data bits by calling makeMessage.

$$p = \begin{pmatrix} d_1 \\ d_2 \\ d_3 \\ d_4 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \\ 1 \end{pmatrix}$$

Listing 1: makeMessage

def makeMessage(n):
 return np.random.randint(2, size=(n, 1))

Then we encode p by pre-multiplying p by G modulo 2 in the encode function.

$$x = Gp = \begin{pmatrix} 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \\ 1 \\ 2 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix}$$

encode returns the encoded message x which is the result of a matrix multiply modulo 2.

Listing 2: encode

 $\mathbf{def}$  encode(G,p):

return np.matmul(G,p) & 1

Sometimes we create an error (flip a bit) in p using the makeError function. We choose a random number between 0 and 1, like tossing a coin, and if the number is 1, we don't create an error in p, otherwise we do. When creating an error we choose a random bit in the message p and flip its bit with an XOR operation.

$$r = x + e_5 = \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 1 \\ 1 \\ 1 \end{pmatrix}$$

Listing 3: makeError

```
def makeError(p):
   if random.randint(0,1): return p
   rdm=random.randint(0,p.shape[0]-1)
   p[rdm,0]=p[rdm,0]^1;
   return p
```

We check to see where errors occured by pre-multiplying r by the parity-check matrix H to produce the syndrome vector z.

$$z = Hr = \begin{pmatrix} 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ 4 \\ 2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

ParityCheck returns the syndrome vector z which is result of a matrix multiply modulo 2.

Listing 4: parityCheck

```
def parityCheck(H,r):
   return np.matmul(H,r) & 1
```

Correct the error by flipping the bit that was incorrect according to the syndrome vector z.

Listing 5: correctError

```
def correctError(z,r):
    loc=0
    for i in range(0,z.shape[0]):
        loc+=z[i,0]*pow(2,i)
    if loc==0: return r
    r[loc-1,0]=r[loc-1,0]^1;
    return r
```

Finally, we decode the message by pre-multipling the encoded message r by a decoding matrix R.

$$p_r = Rr = \begin{pmatrix} 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \\ 1 \end{pmatrix}$$

decodeMessage returns the original message p which is the result of a matrix multiply modulo 2.

Listing 6: decodeMessage

```
def decodeMessage(R, r):
   return np.matmul(R, r)
```

Below is our main function. We hardcoded G, H, and R according to which mode was entered by the user. Then these three matrices are passed to functions encode, parityCheck, and decode, respectively. I created the (15,11) matrices by looking at the bit patterns in the table in the writeup.

Listing 7: main

```
def main():
  \# enter mode: either (7,4) or (15,11)
  mode=input ("Enter_mode: _")
  if mode="H1511":
    pLen=11
   G=np.array([
      [1,1,0,1,1,0,1,0,1,0,1]
      [1,0,1,1,0,1,1,0,0,1,1]
      [1,0,0,0,0,0,0,0,0,0,0]
       [0,1,1,1,1,0,0,0,1,1,1,1],
       [0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0]
      [0,0,1,0,0,0,0,0,0,0,0]
      [0,0,0,0,1,0,0,0,0,0,0,0]
       [0,0,0,0,0,1,1,1,1,1,1,1,1]
       [0,0,0,0,0,1,0,0,0,0,0,0],
      [0,0,0,0,0,1,0,0,0,0,0]
      [0,0,0,0,0,0,0,1,0,0,0,0]
       [0,0,0,0,0,0,0,0,0,0,0,0]
       [0,0,0,0,0,0,0,0,0,1,0,0],
      [0,0,0,0,0,0,0,0,0,1,0]
      [0,0,0,0,0,0,0,0,0,0,0,1]]
    H = np.array([ \ \ \ \ \ \ \ \ )
      [1,0,1,0,1,0,1,0,1,0,1,0,1,0,1]
      [0,1,1,0,0,1,1,0,0,1,1,0,0,1,1]
      [0,0,0,1,1,1,1,0,0,0,0,1,1,1,1]
      [0,0,0,0,0,0,0,0,1,1,1,1,1,1,1,1]
      ])
    [0,0,1,0,0,0,0,0,0,0,0,0,0,0,0]
     [0,0,0,0,0,1,0,0,0,0,0,0,0,0,0,0]
     [0,0,0,0,0,0,0,0,0,0,0,0,0,0,0]
     [0,0,0,0,0,0,0,1,0,0,0,0,0,0,0,0]
```

```
[0,0,0,0,0,0,0,0,0,1,0,0,0,0,0,0],
   [0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0]
   [0,0,0,0,0,0,0,0,0,0,0,0,0,0,0]
   [0,0,0,0,0,0,0,0,0,0,0,0,0,0,0]
   [0,0,0,0,0,0,0,0,0,0,0,0,1,0,0]
   [0,0,0,0,0,0,0,0,0,0,0,0,0,0,1,0]
   [0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0]]
else:
  pLen=4
  G=np.array([
    [1,1,0,1],
    [1,0,1,1],
    [1,0,0,0]
    [0,1,1,1],
    [0,1,0,0]
    [0,0,1,0],
    [0,0,0,1]
 [1,0,1,0,1,0,1],
    [0,1,1,0,0,1,1],
    [0,0,0,1,1,1,1]
  [0,0,1,0,0,0,0]
    [0,0,0,0,1,0,0],
    [0,0,0,0,0,1,0],
    [0,0,0,0,0,0,1]
\# generate random message vector, p, of length 4 or 11
p=makeMessage(pLen);
\mathbf{print} ("Message ____: _"+\mathbf{str} (p. transpose ()[0]))
# encode (make send vector)
x=encode(G, p)
\mathbf{print} ("Send_Vector___:_"+\mathbf{str} (x. transpose ()[0]))
# modify the vector to simulate an error or not
r=makeError(x)
print ("Received _ Message _ : _ "+str (r. transpose ()[0]))
```

```
# Parity Check
z=parityCheck(H,r)
print("Parity_Check____:_"+str(z.transpose()[0]));

# Error Correction
corrected=correctError(z,r)
print("Corrected_Message:_"+str(corrected.transpose()[0]))

# Decode Message
pr=decodeMessage(R,x)
print("Decoded_Message.__:_"+str(pr.transpose()[0]));
```

# Usage

Hamming.py can be run in Ubuntu using the python3 command in the terminal.

```
Listing 8: main
> python3 Hamming.py
```

#### Libraries Used

I used the Python 3 random, math, and numpy libraries.

# Testing and Verification

I tested the program by running the program multiple times on the command line and manually checking whether the output was expected.

## First-Person vs Third-Person

Earlier in this document I spoke in the third-person (we, our) because I was describing a mostly mathematical process. However, toward the end of this document I began speaking in the first person (I, my). At the possibility of any confusion, I wanted to clarity that I worked on this project independently. I'll work on being more consistent with my English in the future.