

# Programming Assignment 1

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We randomly create vector  $p$  containing either 4 or 11 data bits by calling `makeMessage`.

$$p = \begin{pmatrix} d_1 \\ d_2 \\ d_3 \\ d_4 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \\ 1 \end{pmatrix}$$

Listing 1: `makeMessage`

```
def makeMessage(n):
    return np.random.randint(2, size=(n, 1))
```

Then we encode  $p$  by pre-multiplying  $p$  by  $G$  modulo 2 in the `encode` function.

$$x = Gp = \begin{pmatrix} 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \\ 1 \\ 2 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix}$$

Listing 2: `encode`

```
def encode(G,p):
    return np.matmul(G,p) & 1
```

We sometimes create an error (flip a bit) in  $p$  using the `makeError` function.

Listing 3: `makeError`

```
def makeError(p):
    if random.randint(0,1): return p
    rdm=random.randint(0,p.shape[0]-1)
    p[rdm,0]=p[rdm,0]^1;
    return p
```

We check to see where errors occurred by pre-multiplying  $x$  by the parity-check matrix,  $H$ . This is done in parityCheck function.

$$z = Hr = \begin{pmatrix} 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ 4 \\ 2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$

Listing 4: parityCheck

```
def parityCheck(H,r):
    return np.matmul(H,r) & 1
```

Correct the error by flipping the bit that was incorrect according to the syndrome vector  $z$ .

Listing 5: correctError

```
def correctError(z,r):
    loc=0
    for i in range(0,z.shape[0]):
        loc+=z[i,0]*pow(2,i)
    if loc==0: return r
    r[loc-1,0]=r[loc-1,0]^1;
    return r
```

Finally, we decode the message by pre-multiplying the encoded message by a decoding matrix  $R$ .

$$p_r = Rr = \begin{pmatrix} 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \\ 1 \end{pmatrix}$$

Listing 6: decodeMessage

```
def decodeMessage(R, r):
    return np.matmul(R, r)
```

Below is our main function. We hardcoded  $G$ ,  $H$ , and  $R$  according to which mode was entered by the user. Then these three matrices are passed to functions encode, parityCheck, and decode, respectively. I created the (15,11) matrices by looking at the bit patterns in the table in the writeup.

Listing 7: main

```
def main():
    # enter mode: either (7,4) or (15,11)
    mode=input("Enter mode: ")
    if mode=="H1511":
        pLen=11
        G=np.array([
            [1,1,0,1,1,0,1,0,1,0,1], \
            [1,0,1,1,0,1,1,0,0,1,1], \
            [1,0,0,0,0,0,0,0,0,0,0], \
            [0,1,1,1,0,0,0,1,1,1,1], \
            [0,1,0,0,0,0,0,0,0,0,0], \
            [0,0,1,0,0,0,0,0,0,0,0], \
            [0,0,0,1,0,0,0,0,0,0,0], \
            [0,0,0,0,1,1,1,1,1,1,1], \
            [0,0,0,0,1,0,0,0,0,0,0], \
            [0,0,0,0,0,1,0,0,0,0,0], \
            [0,0,0,0,0,0,1,0,0,0,0], \
            [0,0,0,0,0,0,0,1,0,0,0], \
            [0,0,0,0,0,0,0,0,1,0,0], \
            [0,0,0,0,0,0,0,0,0,1,0], \
            [0,0,0,0,0,0,0,0,0,0,1]])
        H = np.array([ \
            [1,0,1,0,1,0,1,0,1,0,1,0,1], \
            [0,1,1,0,0,1,1,0,0,1,1,0,0,1,1], \
            [0,0,0,1,1,1,1,0,0,0,0,1,1,1,1], \
            [0,0,0,0,0,0,0,1,1,1,1,1,1,1,1], \
            ])
        R = np.array([ \
```

```

[0,0,1,0,0,0,0,0,0,0,0,0,0,0], \
[0,0,0,0,1,0,0,0,0,0,0,0,0,0], \
[0,0,0,0,0,1,0,0,0,0,0,0,0,0], \
[0,0,0,0,0,0,1,0,0,0,0,0,0,0], \
[0,0,0,0,0,0,0,1,0,0,0,0,0,0], \
[0,0,0,0,0,0,0,0,1,0,0,0,0,0], \
[0,0,0,0,0,0,0,0,0,1,0,0,0,0], \
[0,0,0,0,0,0,0,0,0,0,1,0,0,0], \
[0,0,0,0,0,0,0,0,0,0,0,1,0,0], \
[0,0,0,0,0,0,0,0,0,0,0,0,1,0], \
[0,0,0,0,0,0,0,0,0,0,0,0,0,1]])
else :
    pLen=4
    G=np.array([ \
        [1,1,0,1], \
        [1,0,1,1], \
        [1,0,0,0], \
        [0,1,1,1], \
        [0,1,0,0], \
        [0,0,1,0], \
        [0,0,0,1]])
    H = np.array([ \
        [1,0,1,0,1,0,1], \
        [0,1,1,0,0,1,1], \
        [0,0,0,1,1,1,1]])
    R = np.array([ \
        [0,0,1,0,0,0,0], \
        [0,0,0,0,1,0,0], \
        [0,0,0,0,0,1,0], \
        [0,0,0,0,0,0,1]])

# generate random message vector, p, of length 4 or 11
p=makeMessage(pLen);
print("Message: "+str(p.transpose()))

# encode (make send vector)
x=encode(G,p)
print("Send_Vector: "+str(x.transpose()))

```

```

# modify the vector to simulate an error or not
r=makeError(x)
print("Recieved_Message:_" + str(r.transpose()))

# Parity Check
z=parityCheck(H,r)
print("Parity_Check:_" + str(z.transpose()));

# Error Correction
corrected=correctError(z,r)
print("Corrected_Message:_" + str(corrected.transpose()))

# Decode Message
pr=decodeMessage(R,x)
print("Decoded_Message:_" + str(pr.transpose()));

```

## Usage:

Hamming.py can be run in Ubuntu using the python3 command in the terminal.

Listing 8: main

```
$ python3 Hamming.py
```