# This is A Tribute To The Best TN of All Time

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#### Abstract

This is the abstract

7	Contents											
8	1	Introduction										
9		1.1	BANFF Treatment of ND Constraint									
10			1.1.1 Constructing a Likelihood									
11			1.1.2 BANFF Likelihood									
12			1.1.3 Flux, Cross Section, and Detector Systematics									
13		1.2	Usage of ND280 PSYCHE Software									
14	<b>2</b>	PØ	D Event Selection And Cuts 12									
15		2.1	The PØD									
16		2.2	Global Reconstruction									
17		2.3	Data Sets									
18		2.4	PØD Selection Cuts									
19			2.4.1 Pre-Selection Cuts									
20			2.4.2 CC-Inclusive in FHC									
21			2.4.3 CC-Inclusive in RHC									
22		2.5	PØD Water-Out Samples									
23			2.5.1 CC-Inclusive									
24			2.5.2 CC-1 Track (CCQE Enhanced)									
25			2.5.3 CC-N Tracks (CCnQE Enhanced)									
26		2.6	PØD Water-In Samples									
27			2.6.1 CC-Inclusive									
28			2.6.2 CC-1 Track (CCQE Enhanced)									
29			2.6.3 CC-N Tracks (CCnQE Enhanced)									
30			2.6.4 Differences Between Water-Out and Water-In Samples									

eferences	30
omenclature	31

ist (	of Figures
1.1	BANFF ND280 NuMu and ANuMu Flux Binning Parameters
1.2	BANFF Pre-fit Flux Covariance Matrix
1.3	Cross Section Parameters Pre-fit Correlation Matrix
2.1	Cartoon of the PØD
2.2	Cartoon of an Individual PØDule
2.3	Momentum: True Particle
2.4	Angle: True Particle
2.5	Momentum: NEUT Interaction
2.6	Angle: NEUT Interaction
2.7	Momentum: True Topology
2.8	Angle: True Topology
2.9	Momentum: True Particle
2.10	Angle: True Particle
2.11	Momentum: NEUT Interaction
2.12	Angle: NEUT Interaction
2.13	Momentum: True Topology
2.14	Angle: True Topology
	1.1 1.2 1.3 2.1 2.2 2.3 2.4 2.5 2.6 2.7 2.8 2.9 2.10 2.11 2.12 2.13

List of Tables					
	2.1	PØD WT FV and Corridor Definition	17		

### Introduction

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#### 1.1 BANFF Treatment of ND Constraint

The primary goal of an oscillation experiment is to measure the parameters in a neutrino 55 mixing matrix. All other parameters, while having some theoretical importance to fundamental physics, are nuisance parameters that must be accounted for. To understand the 57 methodology of BANFF, it is relevant to understand the number of nuisance parameters that go into a ND+FD fit. The BANFF implementation aims to reduce the dimensionality, and hence complexity, of the problem by performing a separate analysis on the nuisance 60 parameters that only the ND can measure. Then that information is propagated to the oscil-61 lation analysis for the FD data. Conceptually this approach has computational advantages 62 and should provide the same result with a joint ND+FD analysis. However, information 63 encoded in the ND measurements for shared nuisance parameters is inevitably lost in this 64 'divide-and-conquer" approach. 65

The BANFF ND-only constraint between 2015 and 2018 is described in detail in T2K-TN-220[7]. While subsequent updates to the BANFF analysis increase the sample sizes and systematic parameterizations, the method has remained unchanged. It uses a frequentist approach to find the best nuisance parameter set to maximize a binned likelihood. The sets of nuisance, also called systematic, parameters in BANFF are

- cross section physics model parameters hereby denoted by  $\vec{x}$ ,
- $\bullet$  neutrino flux binned in neutrino energy hereby denoted by  $\vec{b},$  and
- detector systematics response weights that affect detector observables hereby denoted by  $\vec{d}$ .

A priori (prior) knowledge of  $\vec{x}$  and  $\vec{b}$  are available from external measurements and experiments. The  $\vec{d}$  parameters are penalty terms whose effect can be understood and mitigated

with control samples.

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#### 1.1.1 Constructing a Likelihood

We can define a binned likelihood for the ND280-only constraint with the nuisance parameters as

$$\mathcal{L}\left(\vec{x}, \vec{b} \left| \vec{N}_{\text{ND280}}^{\text{Data}} \right.\right) = \mathcal{P}\left(\vec{x}, \vec{b}, \vec{d} \left| \vec{N}_{\text{ND280}}^{\text{Data}} \right.\right) = \frac{\mathcal{P}\left(\left. \vec{N}_{\text{ND280}}^{\text{Data}} \right| \vec{x}, \vec{b}, \vec{d}\right)}{\mathcal{P}\left(\vec{N}_{\text{ND280}}^{\text{Data}}\right)} \pi\left(\vec{x}\right) \pi\left(\vec{b}\right) \pi\left(\vec{d}\right), \tag{1.1}$$

where  $\vec{N}_{\rm ND280}^{\rm Data}$  are the binned data measurements,  $\pi\left(\vec{y}=\vec{x},\vec{b},\vec{d}\right)$  are prior distributions which are assumed Gaussian distributions

$$\pi(\vec{y}) = \left(\frac{1}{(2\pi)^k \det(V_y)}\right)^{\frac{1}{2}} e^{\left(-\frac{1}{2}\Delta \vec{y} \cdot V_y^{-1} \cdot \Delta \vec{y}^T\right)},\tag{1.2}$$

with  $V_y$  being the covariance matrix for  $\vec{y}$  and  $\Delta \vec{y} = \vec{y} - \vec{y}_{\mathrm{Nominal}}$  is the difference between

the current and nominal set of vector parameters, and  $\mathcal{P}\left(\vec{N}_{\mathrm{ND280}}^{\mathrm{Data}}\right)$  is a normalization. We

85 have used Bayes' theorem

$$\mathcal{P}(AB) = \mathcal{P}(B)\mathcal{P}(A|B) \tag{1.3}$$

to evaluate (1.1) as

$$\mathcal{P}\left(\underbrace{\vec{x}, \vec{b}, \vec{d}}_{A} \middle| \underbrace{\vec{N}_{\text{ND280}}^{\text{Data}}}_{B}\right) = \frac{\mathcal{P}\left(\vec{N}_{\text{ND280}}^{\text{Data}}, \left(\vec{x}, \vec{b}, \vec{d}\right)\right)}{\mathcal{P}\left(\vec{N}_{\text{ND280}}^{\text{Data}}\right)}$$
(1.4)

which we can further manipulate since the data are independent of the nuisance parameters

$$\mathcal{P}\left(\vec{N}_{\text{ND280}}^{\text{Data}}, \left(\vec{x}, \vec{b}, \vec{d}\right)\right) = \mathcal{P}\left(\underbrace{\left(\vec{x}, \vec{b}, \vec{d}\right)}_{A}, \underbrace{\vec{N}_{\text{ND280}}^{\text{Data}}}_{B}\right) = \pi\left(\vec{x}\right) \pi\left(\vec{b}\right) \pi\left(\vec{d}\right) \mathcal{P}\left(\vec{N}_{\text{ND280}}^{\text{Data}} \middle| \vec{x}, \vec{b}, \vec{d}\right)$$
(1.5)

resulting in Equation (1.1). The assumption of a Gaussian prior in Equation (1.2) while not always truly Gaussian, allows for the use of a covariance matrix to describe the uncertainties and correlations in parameters. Once a maximum of the likelihood is found after marginalizing the effects of the systematics  $\vec{d}$ , the best fit values for  $\vec{b}$  and  $\vec{x}$  can be propagated to the oscillation analysis.

#### 1.1.2 BANFF Likelihood

In practice maximizing the log-likelihood (LLH) is performed instead of maximizing the likelihood function. In addition, multiplying the LLH by -2 turns the maximization problem into a minimization one which programs like MINUIT are designed to find. To obtain the best set of parameters  $\vec{x}$  and  $\vec{b}$  from the ND280 data that minimize the  $-2\times$ LLH, we need to predict how they affect our detector observables. Consider binned samples that select different charged current topologies. A convenient choice of observables for all the samples are the outgoing charged lepton l momentum  $P_l$  and angle  $\cos\theta_l$  as mesaured in the ND since all the nuisance parameters affect these quantities. BANFF also uses an event-by-event weighting scheme to rapidly vary the event observables from detector systematics. With this treatment, the detector systematics  $\vec{d}$  are treated with a response  $\vec{r}$  and thus  $P_l \to P_l(\vec{r})$  and  $\cos\theta_l \to \cos\theta_l(\vec{r})$ . We have the pieces needed to define the likelihood function used in ND-only BANFF analysis. For each  $(P_l, \cos\theta_l)$  bin  $i=1,2,\ldots,M-1,M$ , the likelihood for the ND-constraint is a ratio of the predicted events  $(\vec{N}^p)$  likelihood to the likelihood of the data events  $(\vec{N}^d)$ 

$$\Lambda_{\text{ND280}}^{r} = \frac{\mathcal{L}\left(\vec{N}^{p}\left(\vec{x}, \vec{b}, \vec{r}\right) \middle| \vec{N}^{d}\right)}{\mathcal{L}\left(\vec{N}^{d}\left(\vec{x}, \vec{b}, \vec{r}\right) \middle| \vec{N}^{d}\right)}$$

$$= \left(\prod_{\vec{y}=\vec{x}, \vec{b}, \vec{r}} \frac{\pi\left(\vec{y}\right)}{\pi\left(\vec{y}_{\text{Nom}}\right)}\right) \left(\prod_{i=1}^{M}\left(\vec{N}_{i}^{p}\right)^{\vec{N}_{i}^{d}} \frac{e^{-\vec{N}_{i}^{p}}}{\vec{N}_{i}^{d}!}\right) \left(\prod_{j=1}^{M}\left(\vec{N}_{i}^{d}\right)^{\vec{N}_{i}^{d}} \frac{e^{-\vec{N}_{i}^{d}}}{\vec{N}_{i}^{d}!}\right)^{-1} \tag{1.6}$$

where constant terms have been dropped for brevity. When taking  $-2\log$  of both sides, we use Wilks' theorem to define a chi-squared  $\Delta\chi^2_{\text{ND280}} = -2\log\Lambda^r_{\text{ND280}}$  which is

$$\Delta \chi_{\text{ND280}}^{2} = 2 \sum_{i=1}^{M} \left[ \vec{N}_{i}^{p} \left( \vec{x}, \vec{b}, \vec{r} \right) - \vec{N}_{i}^{d} + \vec{N}_{i}^{d} \log \left( \frac{\vec{N}_{i}^{d}}{\vec{N}_{i}^{p} \left( \vec{x}, \vec{b}, \vec{d} \right)} \right) \right]$$

$$+ \Delta \vec{x} \cdot V_{x}^{-1} \cdot \left( \Delta \vec{x} \right)^{T} + \Delta \vec{b} \cdot V_{b}^{-1} \cdot \left( \Delta \vec{b} \right)^{T} + \Delta \vec{r} \cdot V_{r}^{-1} \cdot \left( \Delta \vec{r} \right)^{T}$$

$$(1.7)$$

where again constants were dropped from before. Since  $\vec{N}_i^p$  is a function the nuisance parameters, this is most generally written as

$$\vec{N}_{i}^{p}\left(\vec{x}, \vec{b}, \vec{r}\right) = \sum_{j=1}^{N_{i}^{\text{MC}}} \vec{b}_{j}\left(E_{\nu}\right) \times w_{j}^{\text{norm}} \times w_{j}^{\vec{x}}\left(\vec{x}\right) \times w_{j}^{\vec{d}}\left(\vec{r}\right) \times \delta_{i}\left(P_{j}\left(\vec{r}\right), \cos\theta_{j}\left(\vec{r}\right), s_{j}\left(\vec{r}\right)\right)$$
(1.8)

where  $\vec{b}_j$  is the flux weight as a function of  $E_{\nu}$ ,  $w_j^{\text{norm}}$  is the POT normalization this the POT weight? Originally denoted as xnorm in TN-166 which denotes cross section,  $w_j^{\vec{x}}(\vec{x})$  is the weight function for the interaction cross section,  $w_j^{\vec{d}}(\vec{r})$  is the detector systematics weights that are stored in the response functions  $\vec{r}$ , and  $\delta_i\left(P_j(\vec{r}), \cos\theta_j(\vec{r}), s_j(\vec{r})\right)$  is a general delta function that indicates the correct observable bin if the event belongs in sample  $s_j(\vec{r})$ .

#### 1.1.3 Flux, Cross Section, and Detector Systematics

The minimization of the LLH is attempted by exploring the multidimensional parameter space to as best as possible match the data and prediction. To understand the response of each systematic, a covariance matrix is built for each source. A combined covariance matrix is used in used the BANFF analysis where each submatrix is initially uncorrelated with each other. The parameters in the covariance matrix are usually given a nominal value of one (1) unless a special value is needed with an uncertainty extracted using the Cholesky decomposition method. The development of each systematic uncertainty is briefly discussed below.

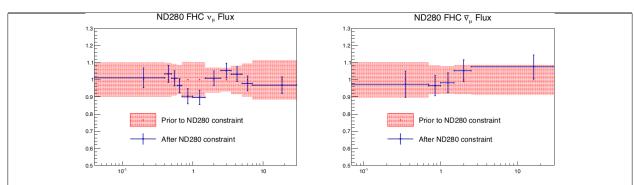


Figure 1.1: BANFF ND280 flux  $\nu_{\mu}$  and  $\overline{\nu}_{\mu}$  binning parameters from T2K-TN-324 data post-fit results. The uncertainties are extracted from the pre-fit and post-fit covariance matrices.

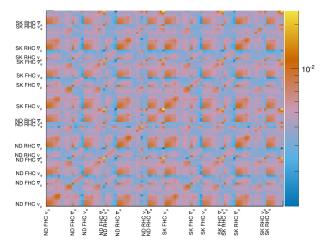


Figure 1.2: BANFF pre-fit flux covariance matrix shown with respective detector, horn current, and neutrino flavor.

Flux: The flux weight is binned as a function of neutrino energy  $E_{\nu}$  and divided by horn current (RHC or FHC) and neutrino flavor  $(\nu_{\mu}, \overline{\nu}_{\mu}, \nu_{e}, \text{ and } \overline{\nu}_{e})$ . Each flux bin has a preset width with parameter that describes the weight and its uncertainty as shown in Figure 1.1 . Each parameter has a nominal value of one (1) and an increase of 10% (1.1) indicates the corresponding bin increases by 10% also. There are 50 ND and 50 SK parameters with a flux covariance matrix is shown in Figure 1.2 .

Cross Section: There are a number of cross section models and weight functions implemented in BANFF. A technical description of the models and weight functions is given in T2K-TN-315[2]. In general, there are model parameters that describe CC-0 $\pi$ , CC-1 $\pi$ , FSI

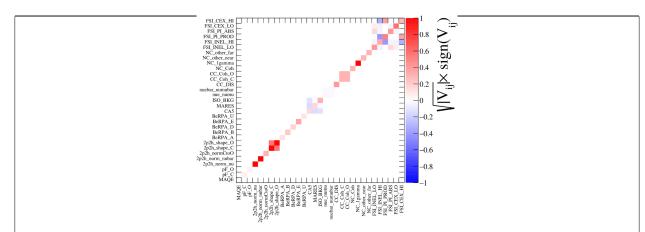


Figure 1.3: Cross section parameters pre-fit correlation matrix from the 2017 BANFF analysis.

(FSI: final state interactions, and smaller T2K effects. There are 25 cross section parameters as shown in Figure 1.3 [1]. While most parameters are set to a nominal value of one (1), some are different like the 2p2h (MEC) parameters. Also other parameters are unconstrainted like MAQE due to limitations of the dipole form factor model.

**Detector Systematics**: Detector systematics are implemented as normalization changes to event kinematics as well as sample migration. Variations are stored in the event-by-event response vector  $\vec{r}$ . In order to understand how the detector systematics correlate for a set of samples with varying kinematic bins, BANFF employs what are called observable normalization (obsnorm) parameters. Since the event can change from sample-to-sample and in kinematic normalization, obsnorms correlations are understood by examining how kinematics vary over many fake experiments, also called toy experiments or just toys. A detector covariance matrix is contructed using all toy experiments. The drawback to this method is that not all detector systematics have Gaussian responses to the observables, and so the correlations are not fully accurate.

### 1.2 Usage of ND280 PSYCHE Software

### 2 PØD Event Selection And Cuts

This section describes the development of  $\nu_{\mu}$  and  $\overline{\nu}_{\mu}$ CC-Inclusive selections in both FHC and RHC beam configuration for PØD-based analyses. These selections are the continuation of previous works that developed  $\nu_{\mu}$  CC-Inclusive selections between the PØD and TPC1. The first such analyses were T2K-TN-80 and T2K-TN-100 which described the  $\nu_{\mu}$  CC-Inclusive event selection and, later, cross-section analysis using ND280 Production 5 software, respectively[4, 5]. These analyzes relied on each sub-detector's reconstruction software and developed a track matching algorithm since the ND280 "Global" reconstruction matching was problematic in Production 5. As the inter-detector matching reconstruction improved in "Global", two CC-0 $\pi$  cross section analyzes, T2K-TN-258 and T2K-TN-328, were developed that also used the CC-Inclusive selection as pre-selection cuts[10, 3]. The selections described in this technical note also employ the same pre-selection cuts. What follows from here in this section is a layout of the following topic discussions.

The first topic discussed in this section is a description of the  $\pi^0$  Detector (PØD). The next topic is the event reconstruction using the "Global" reconstruction software. Following that is the pre-selection cut flow. With the pre-selection cuts established, each of the three CC-Inclusive selection's cut flow is described. Concluding this section is a discussion of the three samples in the following order:  $\nu_{\mu}$  in FHC mode,  $\overline{\nu}_{\mu}$  in RHC, and  $\nu_{\mu}$  in RHC.

### 2.1 The PØD

The PØD, short for  $\pi^0$  Detector, is a plastic scintillator based tracking calorimeter inside the ND280 basket. The PØD is constructed as many sandwiches of active and inactive materials designed to fully contain  $\pi^0$ decay photons. The four primary regions inside the PØD in order of upstream to downstream of the neutrino beam are the upstream ECal (USECal), upstream water target (WT), central WT, and central ECal (CECal). A representation

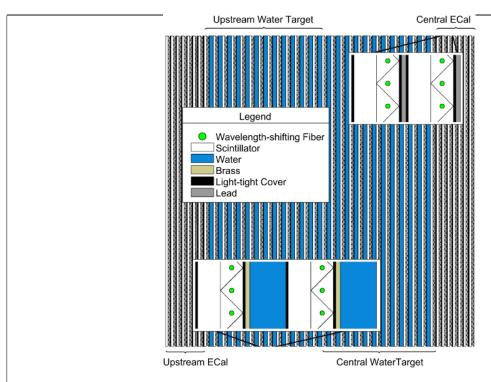


Figure 2.1: This cartoon illustrates the concept design of the  $P\emptyset D$  where the neutrino beam is approaching from the left.

of the entire PØD can be seen in Figure 2.1. Each active module, also called a PØDule, consists of two orthogonally oriented sheets of triangular, scintillator-doped plastic bars as shown in Figure 2.2. The ECal regions are designed to contain decay photons inside the PØD by alternating the scintillator planes with lead sheets. The WT regions, as compared to the lead sheets in the ECals, alternate a thin brass sheet and water filled bags between the PØDules. A unique feature of the PØD is that the water can be drained out resulting in two detector configurations: water-in and water-out.

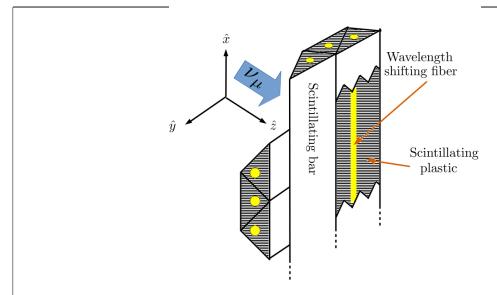


Figure 2.2: This cartoon illustrates the design of a PØDule with orthogonal layers of scintillating, triangular bars. When a charged particle travels through the bar such as a muon from CC interaction, the scintillation light is captured and wavelength shifted inside a fiber bored in the center of each bar. The wavelength shifted light is later observed by a photon counter.

#### 2.2 Global Reconstruction

The task of the Global reconstruction is to combine ND280 sub-detector reconstruction into an single reconstructed object. It was originally designed to analyze "CCQE-like" events in the Tracker region and has been extended with all of ND280. Global attempts to match and re-fit individual sub-detector objects using a Kalman filter while correcting for energy loss and multiscattering. A vertex associated with the re-fit object is also extracted using a different Kalman filter. A detailed description of the track matching and vertex finding algorithms for Global is described in T2K-TN-46[9].

#### 2.3 Data Sets

The data sets used in this analysis are runs 2-8.

#### 2.4 PØD Selection Cuts

The selection of CC-Inclusive events use a series of cuts to select the primary lepton. The pre-selection cuts ("precuts") are applied first to extract events that start in the PØD FV.

A MIP is more likely to reach TPC1 from the PØD FV since the PØD is constructed out of heavy materials especially in the CECal. So the main track each selection is designed to select a muon.

This following sections will describe the precuts common to all CC-Inclusive selections and the branching of different cuts, after the precuts, to select the main track.

#### 2.4.1 Pre-Selection Cuts

The pre-selection ("precuts") were initially developed to select  $\nu_{\mu}$ CC-Inclusive using the PØD and TPC sub-detector reconstruction softwares separately[4]. They were then used with the Global reconstruction software for the  $\nu_{\mu}$ CC-0 $\pi$  selection in the FHC beam configuration as described in technical note T2K-TN-258[10]. The description and flow of the precuts are described here as well since there is an incomplete description of the selection precuts.

The precuts are performed on each bunch per beam spill as follows

- 1. The event has a "good" data quality flag.
  - An event is rejected if any sub-detector or electronics in ND280 reported as "bad" during that bunch.
- 2. There is at least one (1) track reconstructed in TPC1.
  - There are no restrictions on the number of tracks fully contained in the PØD or exiting into other sub-detectors.
- 3. The track in TPC1 must have more than 18 nodes.

- The TPC reconstruction gathers vertical and horizontal hits into clusters of hits. The charge distribution of the cluster is used to get a vertical (horizontal) position that is more accurate than the individual readout pads. A node is constructed out of each cluster with associated track state information. The set of nodes are used to fit the track helix[8].
- 4. The reconstructed vertex is within the PØD WT FV.

- The PØD FV is defined to include as much as the WT regions as possible. Its X and Y borders are 25 cm away from the PØDule edges while its Z borders intersect the last and first half downstream PØDule in the USECal and CECal, respectively. The enumerated volume edges are shown in table 2.1. This volume, while used for track-based analyzes in the past, was optimized for  $\pi^0$  and  $\nu_e$  analyzes [6].
- 5. All tracks that enter TPC1 pass the veto cut
  - An event is rejected if any PØD track enters TPC1 from outside the "corridor" volume. This cut was designed to eliminate broken tracks between the PØD and TPC1 when the separate sub-detector reconstructions were used[4]. In practice, this cut ensures that Global tracks entering TPC1 away from its X and Y edges. The corridor definition is the same as defined in T2K-TN-208 and shown in Table 2.1.

PØD	WT F	V	Corridor Volume			
-836 <					< X <	
-871 <	< Y <	869	-	-1020	< Y <	1010
-2969 <	< Z <	1264	-	3139	< Z <	-900

Table 2.1: The PØD WT FV (left) and veto corridor volume (right) in the ND280 coordinate system. The corridor spans from the 5th (8th) to 40th (80th) PØDule (scintillator layer). All the units are given in millimeters.

After passing all the precuts, a single, global track, which is observed in TPC1, is assigned as the "main track" of a selection. The main track for  $\nu_{\mu}$  selections is the highest momentum, negatively-charged track (HMNT). Similarly the highest momentum, positively-charged track (HMPT) is assigned the main track for  $\overline{\nu}_{\mu}$  selections.

This concludes the application of precuts to all the CC-Inclusive selections. The following subsubsections describe the CC-Inclusive selection cuts, first in FHC mode and then RHC mode.

#### 2.4.2 CC-Inclusive in FHC

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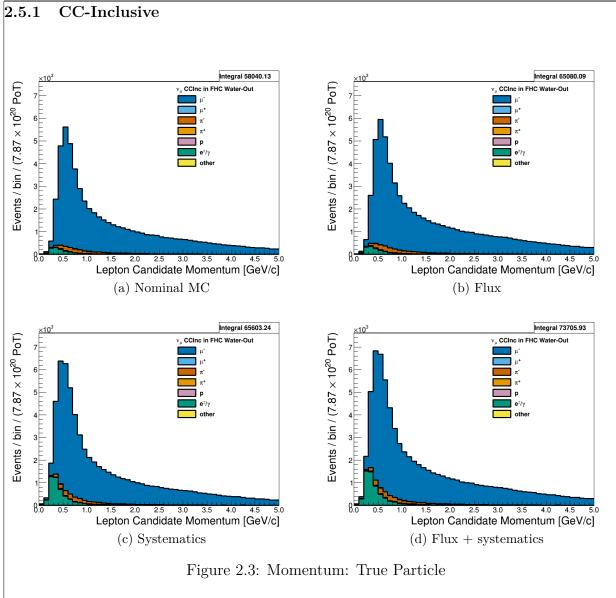
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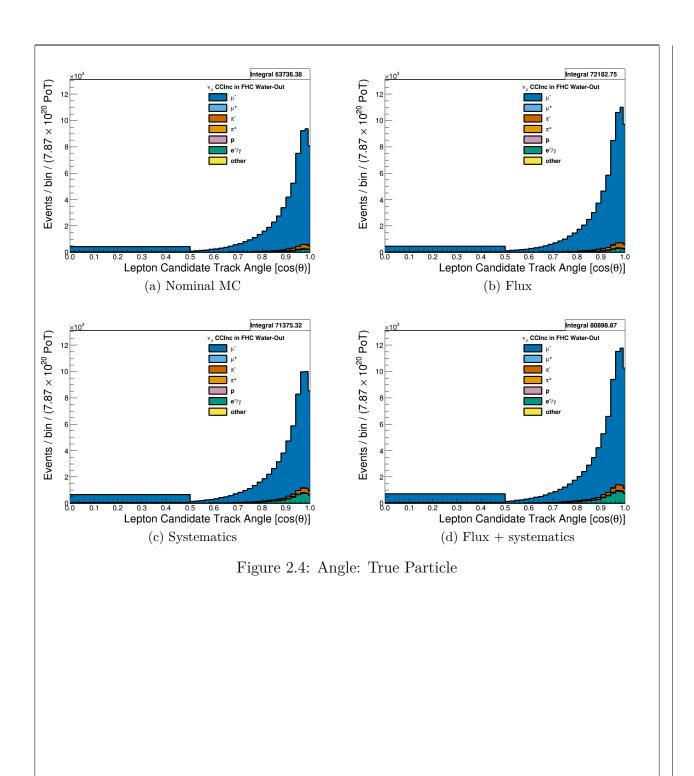
As discussed in Section 2.4.1 on page 15, this selection is the basis for the  $\nu_{\mu}$  CC-0 $\pi$ PØD+TPC1 analysis. This is FHC mode selection and so the lack of a negatively charged track is the final cut for the CC-Inclusive selection.

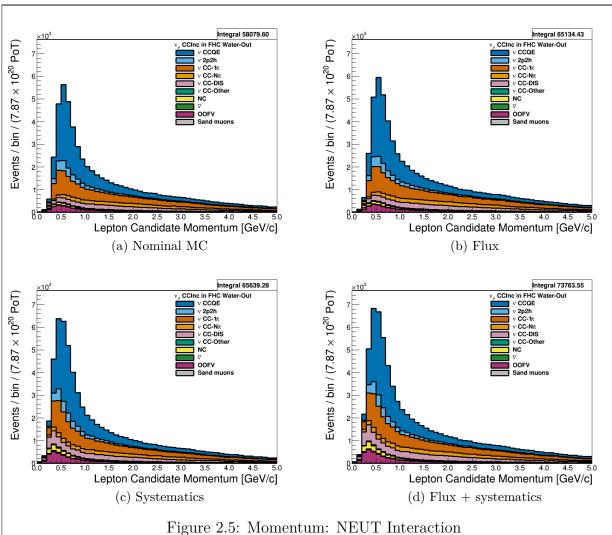
#### 2.4.3 CC-Inclusive in RHC

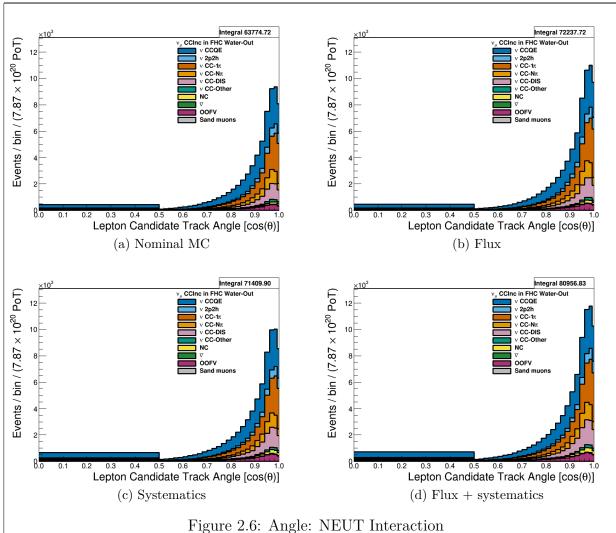
### 2.5 PØD Water-Out Samples

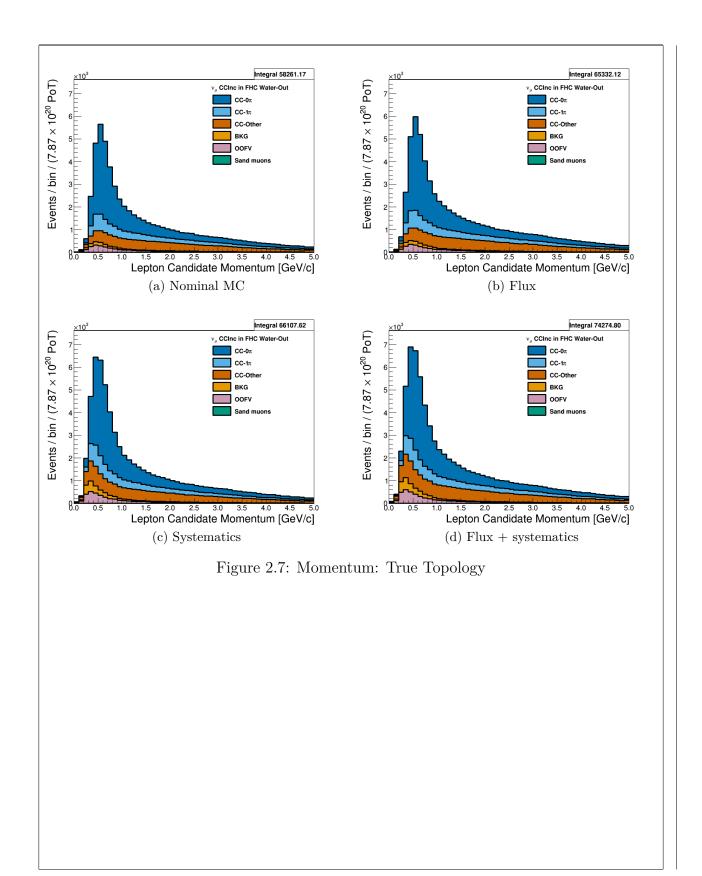
This section shows the kinematic distributions for the  $P\emptyset D$  water-out samples. First an examination of the CC-Inclusive samples and the effects of the systematic weights will be explored. The samples are then examined as CC 1-track and CC N-tracks.











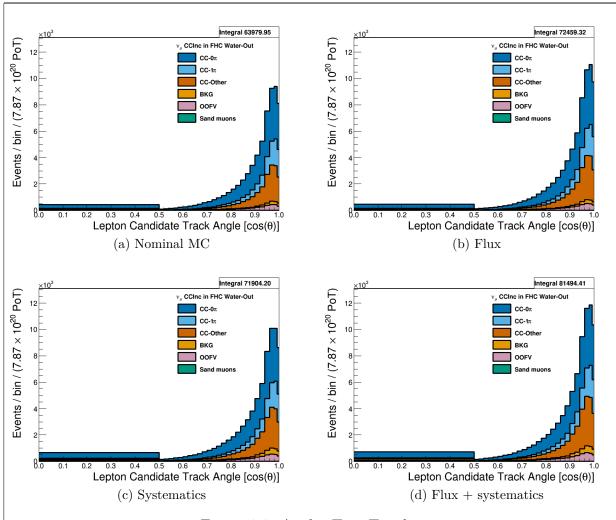


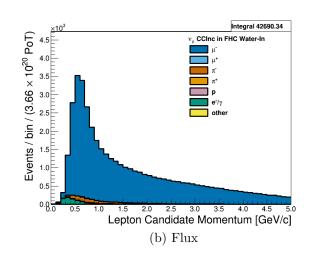
Figure 2.8: Angle: True Topology

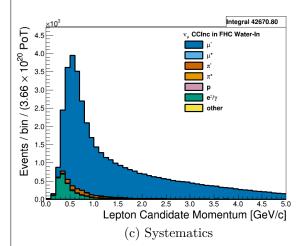
#### 2.5.2 CC-1 Track (CCQE Enhanced)

#### 2.5.3 CC-N Tracks (CCnQE Enhanced)

## 2.6 PØD Water-In Samples

This section shows the kinematic distributions for the PØD water-in samples. These samples will demonstrate the similarities between it and water-out modes. First an examination of the CC-Inclusive samples and the effects of the systematic weights will be explored. The samples are then examined as CC 1-track and CC N-tracks.





(a) Nominal MC

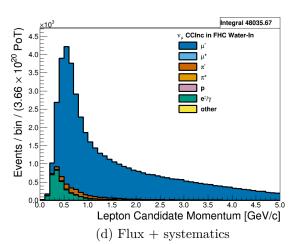
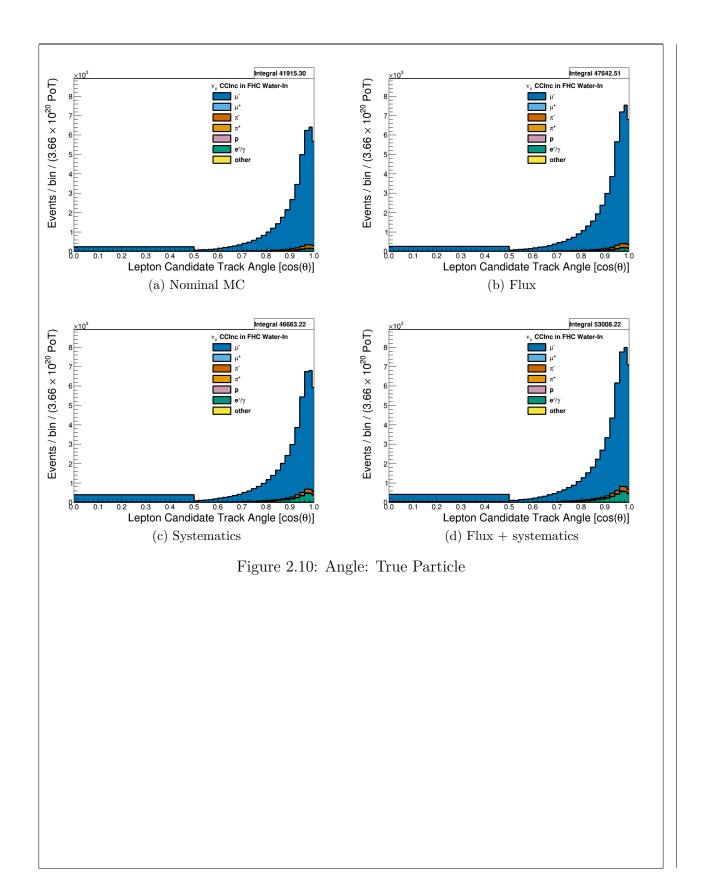


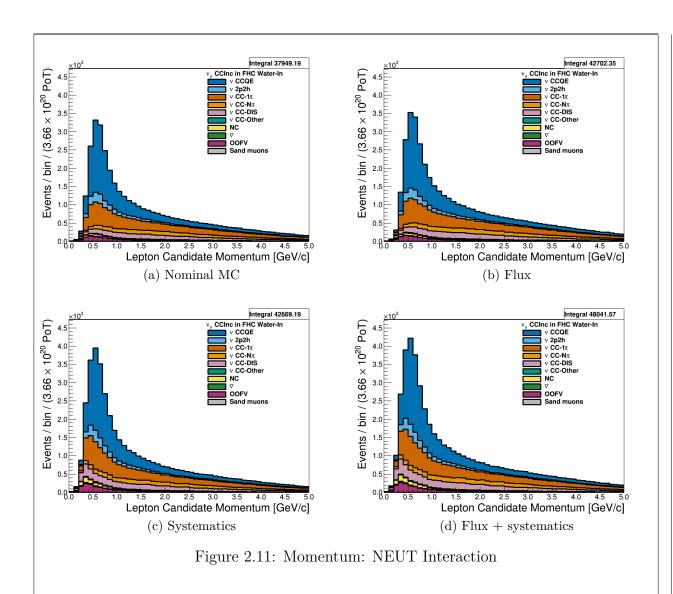
Figure 2.9: Momentum: True Particle

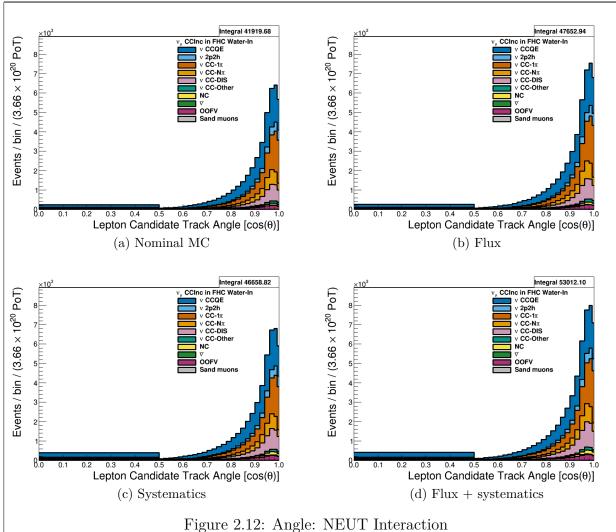
Integral 37942.47

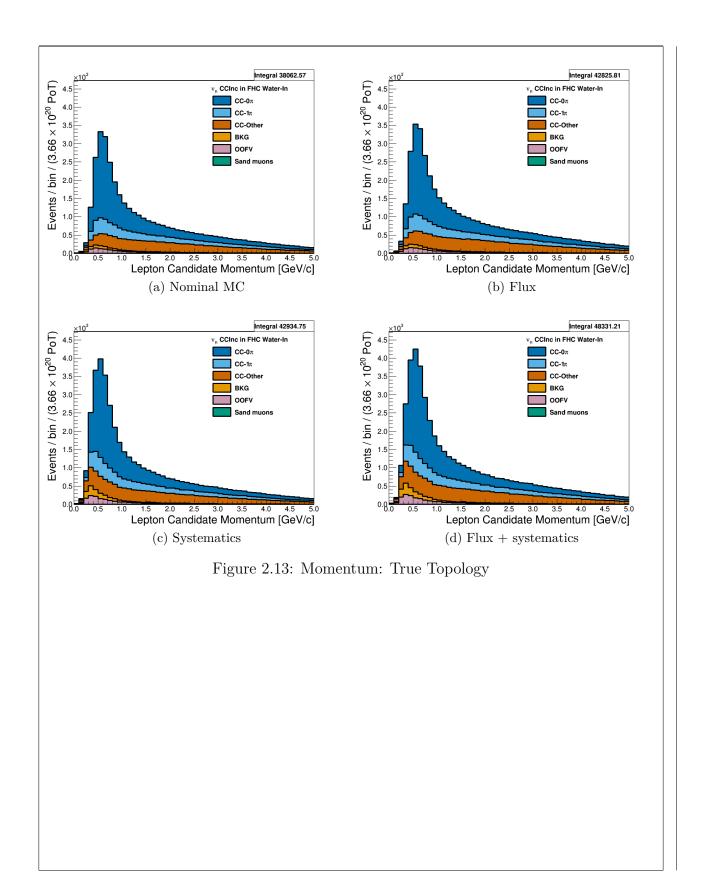
4.0

ν<sub>μ</sub> CCInc in FHC Water-In









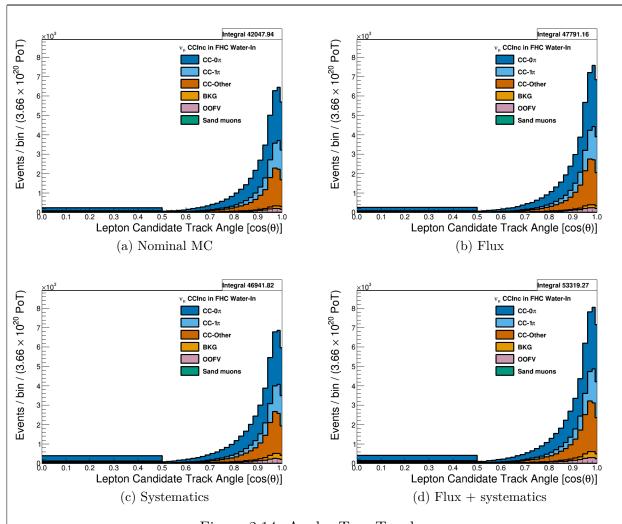


Figure 2.14: Angle: True Topology

2.6.2 CC-1 Track (CCQE Enhanced)

257

- 2.6.3 CC-N Tracks (CCnQE Enhanced)
- 2.6.4 Differences Between Water-Out and Water-In Samples

# References

- [1] S. Bienstock and Others. Constraining the Flux and Cross Section Models with Data from the ND280 Detector using FGD1 and FGD2 for the 2017 Joint Oscillation Analysis, August 2017. T2K-TN-324 v3. 11
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# Nomenclature $CC-0\pi$ A charged current zero pion selection is an exclusive selection that selects neutrino 283 interaction topologies only one MIP-like particle. 284 CC-Inclusive A charged current event selection that selects all neutrino interaction topolo-285 gies with an outgoing charged lepton. 286 A fine grain detector is a detector made of closely spaced, small scintillating bars 287 designed to provide precise resolution of charged particle tracks 288 FHC The forward horn current beam configuration that focuses positively charged particles 289 into the particle decay pipe. This configuration produces a very pure $\nu_{\mu}$ neutrino 290 beam 291 HMNT The highest momentum negatively-charged track in the bunch 292 HMPT The highest momentum positively-charged track in the bunch MIP A minimum ionizing particle 294 ND280 The Near Detector of T2K which is 280 meters away from the neutrino source. 295 CECal The Central ECal detector which is a part of the $P\emptyset D$ inside ND280 296 PØD The $\pi^0$ detector (**p**i-**Ø** detector) 297 PØDule A collection of two active scintillator bar layers inside the PØD

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with a significant  $\nu_{\mu}$  contribution.

RHC The reverse horn current beam configuration that focuses negatively charged particles

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into the particle decay pipe. This configuration produces a  $\overline{\nu}_{\mu}$  enriched neutrino beam

