# IMPLEMENTING AES-256 ON FPGA

19th June 2021

Ho Hai Cong Thuan Student, Computer Engineering, University of Information Technology, HCMC, Vietnam hohaicongthuan@gmail.com

Abstract—In the modern days, the amount of data grow exponentially, including classified and sensitive data that need to be kept secured. For this reason, many cryptographic techniques have been invented for the purpose. AES is one of them. It provides fast and secure data encryption which are the reasons this algorithm is chosen for this project.

The goal of this project is to implement a fully functional AES encryption and decryption system using 256-bit key on FPGA.

Keywords—AES-256; cryptography; data security; FPGA; encryption; decryption.

# 1 INTRODUCTION

The Advanced Encryption Standard (AES), also known as Rijndael is a specification for encrypting electronic data first introduced by the U.S. National Institute of Standards and Technology (NIST) in 2001. It provides a fast and secure way to encrypt data and uses symmetric keys encryption which means both the encryption and decryption processes using the same key. The key length for AES could be 128, 192 and 256 bits. This paper concentrates on AES using 256-bit key which will be referred to as AES-256 for the rest of this paper.

Pouting used to generate a series

## 1.1 Concepts used in AES-256

Van aman	Routine used to generate a series
$Key\ expan-sion$	of Round Keys from the Cipher
51011	Key.
	Intermediate Cipher result that
State	can be pictured as a rectangular
Diale	array of bytes, having four rows
	and $Nb$ columns.
	Non-linear substitution table
	used in several byte substitution
S- $box$	transformation and in the Key
5-00x	Expansion routine to perform
	a one-for-one substitution of a
	byte value.
	A group of 32 bits that is treated
Word	either as a single entity or as an
	array of 4 bytes.

# 1.2 Abbreviations and Symbols used in AES-256

Nb	Number of columns (32-bit words) comprising the State. For this standard, $Nb = 4$ .
Nk	Number of 32-bit words comprising the Cipher Key. For this standard, $Nk = 8$ .
Nr	Number of rounds, which is a function of $Nk$ and $Nb$ (which is fixed). For this standard, $Nr = 14$ .
XOR	Exclusive-OR operation
$\oplus$	Exclusive-OR operation
$\otimes$	Multiplication of two polynomials (each with degree $< 4$ ) modulo $x^4 + 1$
•	Finite field multiplication

# 2 AES-256

## 2.1 Key Expansion

The Key Expansion routine in AES-256 takes a 256-bit cipher key and generate a set of Nb(Nr+1) (which is 60) words. These words are smaller parts that make up round keys, each round key has four words. These round keys involve in the  $Add\ Round\ Key$  in the encryption and decryption process.

There are 3 functions that participate in the key scheduling process:

RotWord	Takes a four-byte word $[a_0, a_1, a_2, a_3]$ and performs rotation one byte to the left and returns $[a_1, a_2, a_3, a_0]$ .
SubWord	Takes a four-byte word and substitute each byte with the corresponding byte in the S-box.
Rcon	The round constants, which is given in the form $[rc_i, 00_{16}, 00_{16}, 00_{16}]$ with $i$ starts from 1. $rc_i$ is defined as in (1)
	in the S-box.  The round constants, which is give in the form $[rc_i, 00_{16}, 00_{16}, 00_{16}]$ with

$$rc_{i} = \begin{cases} 1 & \text{if } i = 1\\ 2 \cdot rc_{i-1} & \text{if } i > 1 \text{ and } rc_{i-1} < 80_{16} \\ (2 \cdot rc_{i-1}) \oplus 11B_{16} & \text{if } i > 1 \text{ and } rc_{i-1} \ge 80_{16} \end{cases}$$
(1)

In AES-256, the first two round keys (first 8 words) are filled with the cipher key. For the rest, w[i] word is generated using w[i-1] word.

Loop through the following steps until we have generated Nb(Nr+1) words.

If i is divisible by Nk, w[i-1] is rotated by the function RotWord and then substituted by the function SubWord. The final result is XOR-ed with Rcon[i/Nk] and assigned to w[i]. Otherwise, if i dividing by Nk results in 4 as the remainder, only SubWord is performed on w[i-1].

w[i] will then be XOR-ed with w[i-Nk] and the result is assigned back to itself. i is incremented by 1.

After finishing the algorithm, a set of Nb(Nr+1) words is generated. Round Keys are created by grouping four words each sequentially. At this point, we have one round key for the initial round and 14 round keys for 14 rounds during the encryption or decryption processes, with the total of 15 round keys.

# 2.2 AES-256 Encryption

The AES-256 Encryption process comprises of fourteen rounds plus the initial round. In the initial round, the input data will be added with the initial round key. In the next thirteen rounds, all the SubBytes, ShiftRows, MixColumns, and AddRoundKey transformations will be performed on the State, respectively. In the last round, only SubBytes, ShiftRows, and AddRoundKey are performed.

#### 2.2.1 Bytes Substitution

Bytes Substitution transformation is denoted by *Sub-Bytes* function. This independently replaces all the bytes in the *State* with the corresponding bytes using a *substitution* box (or *S-Box*), which is shown in the figure 1.

		У															
		0	1	2	3	4	5	6	7	8	9	a	b	С	d	е	f
	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	с9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	£7	aa	34	a5	e5	f1	71	d8	31	15
	3	04	с7	23	с3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	<b>a</b> 0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7£	50	3с	9f	a8
l <sub>x</sub> l	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
1^	8	cd	0с	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	ф
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	С	ba	78	25	2e	1c	<b>a</b> 6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3е	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	е	e1	f8	98	11	69	d9	8e	94	9b	1e	87	е9	ce	55	28	df
	f	8c	a1	89	0d	bf	е6	42	68	41	99	2d	0f	ъ0	54	bb	16

Figure 1: Substitution Box (S-Box) used in SubBytes transformation.

The higher 4 bits determine the coordinate of the row and lower 4 bits determine the coordinate of the column. For example, the byte  $\mathbf{5A}$ , we have x=5 & y=A, these values point to the new value in the table, which is  $\mathbf{BE}$ . So  $\mathbf{5A}$  will be substituted by  $\mathbf{BE}$ .

#### 2.2.2 Shift Rows

In the *ShiftRows* transformation, the last three row of the *State* will be rotated to the left with different byte offsets.

The first row of the *State* is unaffected. The second row will be rotated to the left by one byte, two bytes for the third row, and three bytes for the fourth row. Therefore,

$$\begin{bmatrix} a_0 & a_4 & a_8 & a_{12} \\ a_1 & a_5 & a_9 & a_{13} \\ a_2 & a_6 & a_{10} & a_{14} \\ a_3 & a_7 & a_{11} & a_{15} \end{bmatrix}$$
(2)

will become

$$\begin{bmatrix} a_0 & a_4 & a_8 & a_{12} \\ a_5 & a_9 & a_{13} & a_1 \\ a_{10} & a_{14} & a_2 & a_6 \\ a_{15} & a_3 & a_7 & a_{11} \end{bmatrix}$$

$$(3)$$

after ShiftRows transformation.

#### 2.2.3 Mix Columns

MixColumns transformation operates column-by-column on the State. Each column is multiplied with a fixed matrix which results in a new column with new values.

The fixed matrix used in *MixColumns* is shown below:

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix}$$

$$(4)$$

The multiplication operation performed in this *Mix-Columns* transformation is not ordinary integer multiplication but multiplication in  $GF(2^8)$ , which can be performed at byte level as left shift operation followed by the conditional XOR operation with the number  $1\mathbf{B}$  in hexadecimal.

## 2.3 AES-256 Decryption

The AES-256 Decryption process is the inverse of the AES-256 Encryption process. Basically, it is the same as the encryption process but in reverse. Round keys used in the decryption process are also in reverse order. However, the SubBytes, ShiftRows, and MixColumns transformations are replaced with InvSubBytes, InvShiftRows, and InvMixColumns, respectively. Details of those transformations are discussed in the following sub-sections.

#### 2.3.1 Inverse Bytes Substitution

		У															
		0	1	2	3	4	5	6	7	8	9	a	b	С	d	е	f
	0	52	09	6a	d5	30	36	<b>a</b> 5	38	bf	40	a3	9e	81	f3	d7	fb
	1	7c	e3	39	82	9b	2f	ff	87	34	8e	43	44	c4	de	е9	cb
	2	54	7b	94	32	a6	c2	23	3d	ee	4c	95	0ъ	42	fa	с3	4e
	3	08	2e	a1	66	28	d9	24	b2	76	5b	a2	49	6d	8ъ	d1	25
	4	72	f8	f6	64	86	68	98	16	d4	a4	5с	cc	5d	65	b6	92
	5	6c	70	48	50	fd	ed	b9	da	5e	15	46	57	a7	8d	9d	84
	6	90	d8	ab	00	8c	bc	d3	0a	£7	e4	58	05	b8	b3	45	06
x	7	d0	2c	1e	8f	ca	3f	0f	02	c1	af	bd	03	01	13	8a	6b
^	8	3a	91	11	41	4f	67	dc	ea	97	f2	cf	ce	f0	b4	е6	73
	9	96	ac	74	22	e7	ad	35	, 85	e2	f9	37	e8	1c	75	df	6e
	а	47	f1	1a	71	1d	29	c5	89	6f	<b>b</b> 7	62	0e	aa	18	be	1b
	b	fc	56	3е	4b	с6	d2	79	20	9a	db	c0	fe	78	cd	5a	f4
	С	1f	dd	a8	33	88	07	с7	31	b1	12	10	59	27	80	ec	5f
	d	60	51	7£	<b>a</b> 9	19	b5	4a	0d	2d	e5	7a	9f	93	с9	9c	ef
	е	a0	e0	3ъ	4d	ae	2a	f5	ь0	с8	eb	bb	3с	83	53	99	61
	f	17	2b	04	7e	ba	77	d6	26	e1	69	14	63	55	21	0c	7d

Figure 2: Inverse S-Box

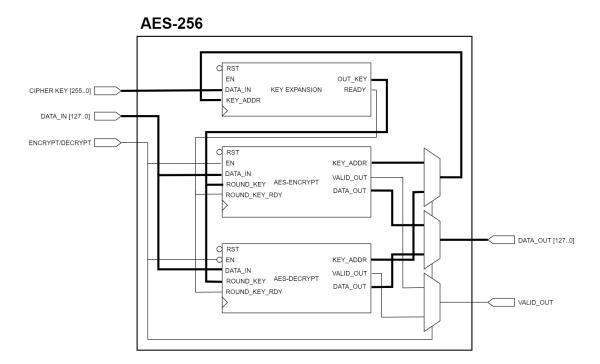


Figure 3: Top-level design of AES-256.

In the *Inverse Bytes Substitution* transformation, which is denoted as *InvSubBytes*, all bytes from the *State* will be replaced by the corresponding bytes from the inverse S-Box, which is shown in figure 2.

# 2.3.2 Inverse Shift Rows

Inverse Shift Rows denoted as InvShiftRows is the inverse of ShiftRows transformation. Each row from the State is rotated with different offsets to the right instead of left. According to that, the first row is untouched, the second row is rotated one byte to the right, rotated two bytes to the right for the third row, and three bytes for the fourth row. Suppose (2) as the example input, after InvShiftRows transformation, the input will become

$$\begin{bmatrix} a_0 & a_4 & a_8 & a_{12} \\ a_{13} & a_1 & a_5 & a_9 \\ a_{10} & a_{14} & a_2 & a_6 \\ a_7 & a_{11} & a_{15} & a_3 \end{bmatrix}$$
 (5)

#### 2.3.3 Inverse Mix Columns

Inverse Mix Columns denoted as InvMixColumns is the inverse of MixColumns transformation. Each column from the State is multiplied with the inverse matrix of the matrix (4), which is shown in (6), using the multiplication in  $GF(2^8)$ . Note that all numbers in the matrix are written in hexadecimal.

$$\begin{bmatrix}
0e & 0b & 0d & 09 \\
09 & 0e & 0b & 0d \\
0d & 09 & 0e & 0b \\
0b & 0d & 09 & 0e
\end{bmatrix} (6)$$

# 2.4 Add Round Keys

Round keys generated from *Key Expansion* rountine will be used in this transformation. It takes two 128-bit input data and output 128-bit data. Round keys are added to the *State* by bitwise *XOR* operations with the corresponding bytes.

# 3 IMPLEMENTATION

The top-level design for AES-256, including encryption and decryption, is shown in figure 3. The implementation of smaller modules are discussed in the following sub-sections.

# 3.1 Key Expansion

The design of the Key Expansion routine is shown in figure 4. As in the design, the total of 15 round keys, including round key for the initial round, will be created firstbefore they could involve in the *Add Round Key* function in the encryption and decryption process.

This circuit will generate words that make up the Round Key one-by-one and store them in the *Register File*. The *Register File* has the total amount of 64 registers but only 60 of them are used because we only need to generate 60 words. The module *Rcon* and *SubWord* are implemented in the form of look-up tables (LUTs).

In order for the circuit to work, the *reset* signal must be pulled low (the *reset* signal is active low) and then the *enable* signal is pulled high. The cipher key can be passed through *Input Data*. After reset, the counter's value will be set to zero and increased by 1 after each clock cycle. In the meantime, the inputted cipher key will be broken up into words, which are 32 bits each, and stored in eight registers from  $w_0$  to  $w_7$ .

In the next eight clock cycles each of the word will be saved into the Register File sequentially from the address

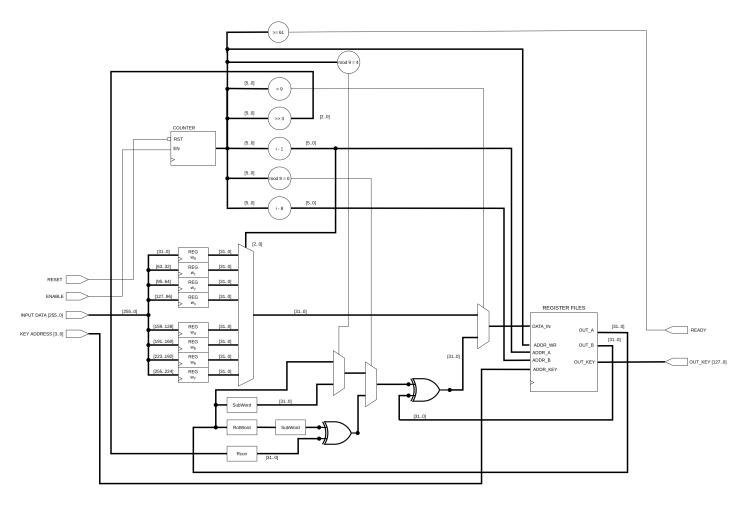


Figure 4: Diagram of Key Expansion.

1 to 8. After that, to generate the  $i^{th}$  word,  $(i-1)^{th}$  and  $(i-Nk)^{th}$  words are required, which can be accessed through Register File's Out\_A & Out\_B ports respectively, with the addresses are selected by i-1 & i-8 blocks in the circuit.

Depend on which word is generating, RotWord, SubWord can all be performed or just SubWord is performed or neither of those. This is controlled by signals from  $mod\ 9=4$  &  $mod\ 9=0$  blocks. Basically, the  $mod\ 9=4$  block checks if a input number dividing by 9 has 4 as the remainder. If it is, the output will be pulled high and pulled low if it is not. Same thing with the  $mod\ 9=0$  block but with 0 as the remainder. The design of  $mod\ 9=0$  &  $mod\ 9=4$  are shown in figure 5 and figure 6, respectively.

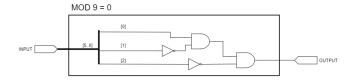


Figure 5: Circuit of mod 9 = 0 block

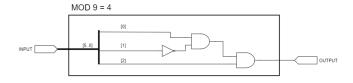


Figure 6: Circuit of mod 9 = 4 block

All the words will have been generated after sixty-one clock cycles. The counter will shut itself and the *ready* signal is set indicating all round keys have been generated. After done generating and the *ready* signal is set, round keys can be accessed by inputting the appropriate address through *Key Address* input, which have the value range from 0 to 14

## 3.2 AES-256 Encryption

Figure 7 shows the design of AES Encryption circuit. This circuit takes 128-bit data in and a set of round keys to perform AES encrytion on the inputted data.

A reset signal must be inputted in order for the circuit to work properly. A counter will keep track of which round and round key the encryption process is currently at. In the first clock cycle, inputted data will be stored in a register and added with the first round key and saved in another register that acts as the State, completing the initial round. In the next thirteen clock cycles, the circuit performs thirteen rounds comprising SubBytes, ShiftRows, MixColumns, and AddRoundKey transformations in each round on the State. In the last round, the MixColumns transformation is optted out. The encryption process will be completed after fifteen clock cycles and the done signal will be pulled high.

Details on smaller circuits in this AES Encryption circuit like *SubBytes*, *ShiftRows*, *MixColumns*, etc. are represented in the following sub-sections.

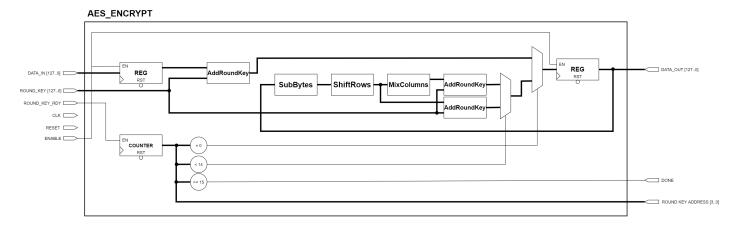


Figure 7: Diagram of AES Encryption Circuit.

#### 3.2.1 Bytes Substitution

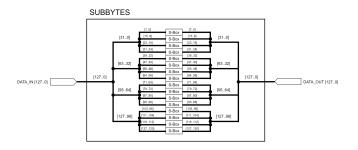


Figure 8: SubBytes circuit diagram.

The design for SubBytes block is shown in figure 8. The SBox used in this circuit is implemented as LUT and is the same as SBox from figure 1 and SubWord in  $Key\ Expansion$  routine.

This ciruit takes 128-bit data and splits into words and then into individual bytes. Each byte will be fed into SBox and the corresponding byte will be outputted. The outputted bytes will then be combined into words and eventually into 128-bit output data.

# 3.2.2 Shift Rows

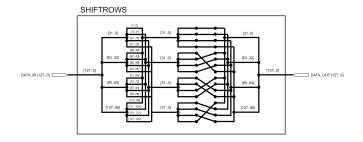


Figure 9: ShiftRows circuit diagram.

The circuit diagram for *ShiftRows* is shown in figure 9. This circuit takes 128-bit data in, performs shifting and outputs 128-bit data.

The inputted data will first be split into 32-bit words, note that each word corresponds to a column in the *State*. The first row is formed by taking the first byte in each word, and the second byte in each word for the second row and so

on for the third and fourth rows. After dividing the input into rows, the shifting operation is done by wiring each row with the corresponding offsets which discussed in section 2.2.2.

Finally, all the rows will be split and combined into correct columns and rows format of the *State*.

#### 3.2.3 Mix Columns

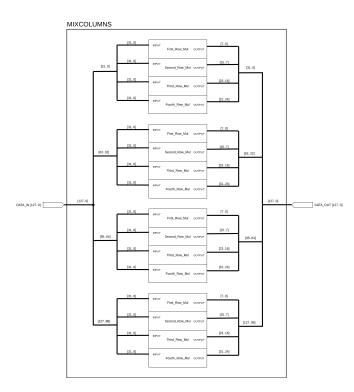


Figure 10: MixColumns circuit diagram.

In figure 10 is the circuit design for MixColumns transformation. The 128-bit data input fed into the circuit is divided into four words. Each word is fed into  $First\_Row\_Mul$ ,  $Second\_Row\_Mul$ ,  $Third\_Row\_Mul$ , and  $Fourth\_Row\_Mul$  blocks, which is basically multiplying that word using the multiplication in  $GF(2^8)$  with first, second, third, and fourth rows of the matrix (4) from section 2.2.3. Each of the four blocks will output a new byte after the multiplication. Four bytes will be combined into a word. And the 128-bit output is formed by combining four words.

The implementation of the  $First\_Row\_Mul$ ,  $Second\_Row\_Mul$ ,  $Third\_Row\_Mul$ , and  $Fourth\_Row\_Mul$  blocks is shown in figure 11, 12, 13, and 14, respectively. Note that all the addition operations (the plus symbol) in these circuits are all XOR operations.

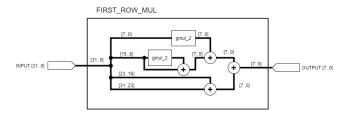


Figure 11: First\_Row\_Mul.

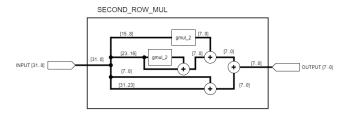


Figure 12: Second\_Row\_Mul.

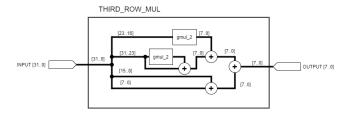


Figure 13: Third\_Row\_Mul.

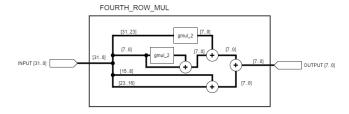


Figure 14: Fourth\_Row\_Mul.

The implementation of the multiplication by 2 in  $GF(2^8)$ , which is denoted as  $gmul_-2$ , is shown in figure 15. This multiplication operation is performed at byte level as shift operation one bit to the left followed by a conditional XOR operation with the number 1B in hexadecimal.

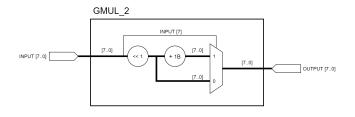


Figure 15: gmul\_2.

# 3.3 AES-256 Decryption

#### 3.3.1 Inverse Byte Substitution

Text here.

#### 3.3.2 Inverse Shift Rows

Text here.

#### 3.3.3 Inverse Mix Columns

Text here.

# 3.4 Add Round Keys

AddRoundKeys can simply be performed by the XOR operation with the State and a round key, which both have the length of 128 bits. The output is 128-bit.

# 4 RESULTS

# 4.1 Key Expansion

Figure 16 shows simulation waveform result using *ModelSim*. As can be seen in the figure, after 61 clock cycles since the last *reset* signal, the textitready signal is set indicating round keys have been generated. Therefore, they can be retrieved correctly, which is the part circled in the figure.

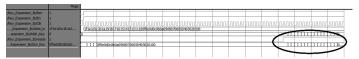


Figure 16: Key Expansion simulation result in *ModelSim*.

The circuit is tested with different keys from the example section in [1] and the web-based tool https://www.cryptool.org/en/cto/aes-step-by-step. The results produced by the circuit are the same with the expected results in each test case.

## 4.2 AES-256 Encryption

Text here.

# 4.3 AES-256 Decryption

Text here.

# 5 CONCLUSION

(N/A)

# References

- [1] Federal Information Processing Standard (FIPS) 197. Advanced Encryption Standard (AES) 26 November 2001.
- [2] Sam Trenholme. Rijndael's key schedule. https://samiam.org/key-schedule.html.
- [3] Sam Trenholme. Rijndael's mix column stage. https://samiam.org/mix-column.html.

- $[4] \mbox{ Sam Trenholme. } AES' \mbox{ Galois field.} \\ \mbox{ } https://samiam.org/galois.html.$
- $[5] \ \ {\rm Sam} \ \ {\rm Trenholme}. \ \textit{Rijndael's S-Box}.$

- https://samiam.org/s-box.html.
- [6] Kit Choy Xintong. Understanding AES Mix-Columns Transformation Calculation.