```
# Graph
                                  BFS/DFS
                                                                         0(m+n)
Connectivity
                                                                         0(m+n)
Bipartiteness
                                  BFS/DFS
Minimum Spanning Tree
                                  Kruskal's
                                                                         O(E \log E) \text{ time } O(E) \text{ space}
Minimum Spanning Tree
                                 Lazy Prim's
                                                                         O(E \log E) \text{ time } O(E) \text{ space}
Minimum Spanning Tree
                                  Red-rule Blue-rule
Single pair shortest path
                                  Dijkstra's shortest path
                                                                      \mid O(E log V) time O(V) space
Single-source shortest paths |
                                  Dijkstra's shortest paths
                                                                         O(E log V) time O(V) space
                                                                         O(E log V) time O(V) space
SS Longest paths in ew DAGs
                                  Dijkstra's shortest path *
* shortest path in this copy is the longest path
# Divide and Conquer
                                                                         O(N log N) time O(log N) space
                                  Mergesort
Sorting
                                  Randomized Quicksort
                                                                         O(N \log N) time O(N) space
Sorting
Integer Multiplication
                                  Grade-school
                                                                         Theta(n^2) time
Integer Multiplication
                                  Karatsuba multiplication
                                                                         0(n^{1.585}) time
Closest pair of points
                                  Kleinberg-Tardos Closest Pair
# Greedy
                                  Cashier's
Coin changing
Interval Scheduling
                                  Earliest-finish-time-first
Interval Partitioning
                                  Earliest-start-time-first
# Dynamic Programming
Weighted Interval Scheduling
                                  top-down
                                                                         O(n log n) time
Subset sums
                                  bottom-up
                                                                         O(nW) or O(n*2^m) time, where m
Knapsack
                                  bottom-up
is the number of bits in W
Sequence alignment
                                  bottom-up
                                                                       | Theta(m n) time
Single pair shortest path
                                  Bellman-Ford
                                                                       \mid O(E V) time O(V) space
# Network Flows
Minimum-cut
                                  Ford-Fulkerson
                                                                       | O(m n C) time
Maximum-flow
                                  Ford-Fulkerson
                                                                      | O(m n C) time
                                  Ford-Fulkerson
                                                                         O(m n C) time
Maximum Matching
                                  Ford-Fulkerson
                                                                         O(m n) time
Bipartite Matching
Largest Bipartite Matching
                                                                         O(N^3) time
                               1
# NP
## Contraint Satisfaction
Circuit-SAT
                                  NP-Complete
3-SAT
                                  NP-Complete
## Packing and Covering
Independent set
                                  NP-Complete
                                  NP-Complete
Vertex cover
Set cover
                                  NP-Complete
                                  NP-Complete
Set packing
## Sequencing
                                  NP-Complete
Directed Hamiltonian cycle
Hamiltonian cycle
                                  NP-Complete
                                  NP-Complete
Hamiltonian path
Longest Path
                                  NP-Hard (decision NP-C exists)
Traveling Salesman Problem
                                  NP-Hard (decision NP-C exists)
## Partitioning
                                  NP-Complete
Graph 3-color
Planar 3-color
                                  NP-Complete
## Numerical
                                  NP-Complete
Subset sums
                                 NP-Complete
Scheduling release/deadline
                               1
---- Integer Factorization (NP and not P and not NP-Hard), Maximum cut, 3D matching, Factoring,
Integer linear programming
```