

### Tarea Unidad 3

Pols → 3.6

The atomic lines for a star are observed to be shifted relative to their normal positions. This is due to a radial velocity of the star (i.e. the component of the star's velocity along the line of sight). If the shift of the H  $\beta$  line is  $\Delta \lambda = +0.4 \text{ \AA}$ , what is the value and the direction of the radial velocity of the star?

Calculate the equivalent width of a rectangular line with a  $4 \text{ \AA}$  width and with a flux in its interior that is  $2/3$  of that of its value in the continuum.

Consider a photosphere composed of pure neutral hydrogen. At what temperature will the density of atoms in the  $n=2$  excited state and in the  $n=1$  ground state are equal ( $N_2/N_1 = 1$ )? And for  $n=3$ ?

Calculate the electronic density ( $n_e$ ) in a gas at  $T = 14\,000 \text{ K}$  composed of pure hydrogen where 70 % of the atoms are ionised (assume  $U_I = 2$ ).

Assume our photosphere has a constant electron pressure of  $P_e = 2 \text{ Pa}$  ( $2 \text{ N/m}^2$ ). Use the Saha equation to find the temperature at which the ionized and neutral fractions are equal  $N_{II}/N_I = 1$ .

Consider our photosphere of pure hydrogen again. Combine the Boltzmann and Saha equations to estimate the fraction  $N_2/N$  of hydrogen atoms in the  $n=2$  state of H I to the total number density of atoms  $N = N_I + N_{II}$ , for stars with temperatures of  $T=6000 \text{ K}$  (type G0),  $T = 7200 \text{ K}$  (F0),  $T = 10400 \text{ K}$  (A0), and  $T = 27000 \text{ K}$  (B0). Again set  $P_e = 2 \text{ Pa}$ . Compare your estimates to Figure 8-13 of the book. Which spectral type should have the strongest Balmer lines, and why?