

8. (1) 若 $b \rightarrow c$ 为绝热过程, 则 $a \rightarrow b$ 升温吸热增压 (Q_1)

$c \rightarrow a$ 降温压缩放热 (Q_2)

$$\begin{aligned} \text{有 } \eta &= \frac{Q_1 - Q_2}{Q_1} = \frac{C_{v,m}(P_2 V_1 - P_1 V_1) - C_{p,m} P_1 (V_2 - V_1)}{C_{v,m}(P_2 V_1 - P_1 V_1)} \\ &= \frac{P_2 V_1 - P_1 V_1 - (\ln(\frac{P_1}{P_2}) / \ln(\frac{V_1}{V_2})) P_1 (V_2 - V_1)}{P_2 V_1 - P_1 V_1} \end{aligned}$$

(2) 若 $b \rightarrow c$ 为等温过程, 则

$$\begin{aligned} \eta &= \frac{W}{Q_{ab}} = \frac{\gamma R T \ln \frac{V_2}{V_1}}{\gamma R T \ln \frac{V_2}{V_1} + C_{p,m} \frac{(P_2 - P_1) V_1}{\rho}} \\ &= \frac{(\gamma - 1) \gamma R T \ln \frac{V_2}{V_1}}{(\gamma - 1) \gamma R T \ln \frac{V_2}{V_1} + \gamma (P_2 - P_1) V_1} \end{aligned}$$

13. 声速有 $v^2 = \left(\frac{\partial P}{\partial \rho}\right)_s$, 由绝热过程 (单位质量)

$$\frac{dP}{\rho} + \gamma \frac{dV}{V} = 0 \quad \text{而 } dP = -\frac{dV}{V^2}$$

$$\text{有 } \frac{dP}{\rho} - \gamma V d\rho = 0$$

$$\text{故而 } v^2 = \frac{\partial P}{\partial \rho} = \gamma P V$$

$$\text{而 } u = \frac{i}{2} \frac{RT}{m_0} + u_0 \quad \text{而 } \gamma = \frac{i+2}{i}$$

$$\begin{aligned} \text{故而 } u &= \frac{v^2}{\gamma(\gamma-1)} + u_0 = \frac{\gamma RT}{m_0} \frac{i}{2} \cdot \frac{1}{\gamma} + u_0 \\ &= \frac{i}{2} \frac{RT}{m_0} + u_0 \end{aligned}$$

$$\bar{h} = u + pV = u + \frac{RT}{m_0} = \frac{v^2}{\gamma(\gamma-1)} + \frac{v^2}{\gamma} + h_0$$

$$h = \frac{v^2 + (\gamma-1)v^2}{\gamma(\gamma-1)} + h_0 = \frac{v^2}{\gamma-1} + h_0$$

14. 解:

$$\eta = 1 - \frac{Q_0}{Q_2} = 1 - \frac{(1-\eta_1)(1-\eta_2)Q_2}{Q_2}$$

$$= 1 - 1 + \eta_1 + \eta_2 - \eta_1\eta_2$$

$$= \eta_1 + \eta_2 - \eta_1\eta_2$$