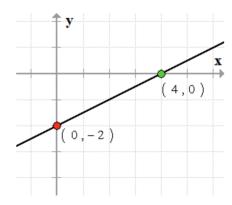
## Math 102 Precalculus - Problem Set 1: Lines, Circles, Distance and Midpoint Formula, Functions and Domains

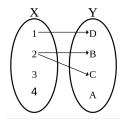
- (1) Consider the points (-1,2) and (0,-2).
  - (a) Plot and label these points in the x-y plane.
  - (b) Find the slope of the line connecting these points.
  - (c) Write the equation of the line that goes through these points in point-slope form.
  - (d) Write the equation of the line that goes through these points in slope—intercept form.
  - (e) Sketch the line and label the y-intercept.
- (2) Repeat the steps above for the points  $(\frac{2}{3}, -1)$  an  $(-\frac{1}{3}, -2)$ .
- (3) Consider the line y = -2x + 5.
  - (a) Determine whether the point (2, 1) lies on the graph of the line. Approach this problem two ways— use the equation and also use your graph by plotting the point.
  - (b) Determine whether the point (3, -1) lies on the graph of the line.
  - (c) Determine whether the point (3, -2) lies on the graph of the line.
- (4) Consider the equation -3x + 6y 2 = 0.
  - (a) Rewrite this equation in slope-intercept form.
  - (b) What is the slope of this line?
  - (c) What is the y-intercept (give as a point)?
  - (d) What is the x-intercept (give as a point)? Hint: to find an x-intercept, set y = 0 and solve for x.
  - (e) Sketch the line.
  - (f) What observations can you make about the general form of the equation of a line? For example, what are the powers of x and y terms for equations of lines?
- (5) Consider the following graph. Write the equation of the line in slope-intercept form.



- (6) Consider the line x = 5.
  - (a) List any two points which lie on this line.
  - (b) In general, if a point is on this line, what is its x-coordinate?

- (c) What is the slope of this line?
- (d) We have defined slope to be "rise over run." For the two points you selected, what is the rise? What is the run?
- (e) Write a short explanation for why a number divided by zero is undefined. Hint: Feel free to use google. Both Wikipedia and Khan Academy have explanations.
- (f) Sketch the line.
- (7) Consider the line  $y = -\frac{1}{3}x 1$ .
  - (a) Write the equation of the line parallel to the given line and passing through the point (3, 2). Give your equation in slope-intercept form.
  - (b) Sketch both lines.
  - (c) What is the only difference between the equations for each line?
- (8) Consider the line y = 2x 1.
  - (a) Write the equation of the line perpendicular to the given line and passing through the point (-2,1). Give your equation in slope-intercept form.
  - (b) Sketch both lines.
  - (c) Where do the lines intersect? Hint: set the equations equal to each other and solve for x. Then use this x value to solve for y.
- (9) Consider a line, y = 2x + 1.
  - (a) If the line is reflected across the y-axis, find its equation. Sketch both lines. How did the y intercept change with the reflection? How did the slope change with the reflection?
  - (b) If the line is reflected across the x-axis, find its equation. Sketch both lines. How did the y intercept change with the reflection? How did the slope change with the reflection?
  - (c) Can you make any generalizations about a line of the form y = mx + b and the equations of the reflections above? Hint: it might help to do a few more concrete examples.
- (10) A line with slope -3 passes through the points (-8, p) and (2, 3p).
  - (a) Find p.
  - (b) Write the equation of this line in slope-intercept form.
  - (c) Sketch this line.
- (11) Graph a family of lines of the form y = 3x + c on the same x-y plane where c is any real number. Describe the pattern of the graph. How does changing c change the graphs of the lines? Hint: choose a few values of c and graph those lines. For example, you might sketch y = 3x + 1, y = 3x + 2, y = 3x 10.
- (12) Graph a family of lines of the form y = dx + 1 on the same x-y plane where d is any real number. Describe the pattern of the graph. How does changing d change the graphs of the lines? Now check your intuition using this Desmos application which has a slider for the parameters m and b for lines of the form y = mx + b: https://www.desmos.com/calculator/wuxkicjcre
- (13) Consider the points (2,3) and (0,6).
  - (a) Plot and label these points in the x-y plane.
  - (b) Find the slope of the line connecting these points.

- (c) Find the distance between the points.
- (d) Find the midpoint of the line segment connecting these points. Label the midpoint on your sketch.
- (14) Find a point of the form (2a, a) in the third quadrant such that the distance from this point to (1,3) is 5. Hint: You might start by writing the distance formula for the two points and setting it equal to 5.
- (15) Consider the circle with equation  $x^2 + y^2 + 8x 6y + 16 = 0$ .
  - (a) Complete the square to put this equation in standard form  $((x-h)^2+(y-k)^2=r^2)$ .
  - (b) What is the center?
  - (c) What is the radius?
  - (d) Sketch the circle.
  - (e) Is this a function?
- (16) Consider the following mapping. Is it a function? Why or why not?



(17) Let  $f(x) = 8 - x^2$ . Fill out the following table by evaluating the function.

_		
x	f(x)	
-2		
-1		
0		
1		
2		
apple		
2 + h	i	

- (18) Consider f(x) = 2x + 1.
  - (a) Fill out the following table (I did the first row as an example):

	(		1 /
x	f(x)	f(x+2)	f(x) + 3
1	2(1) + 1 = 3	2(1+2) + 1 = 7	2(1) + 1 + 3 = 6
2			
3			
4			

- (b) Sketch f(x). Label the four points in your table on the graph.
- (c) Sketch f(x+2). Label the four points in your table on the graph. How does this sketch relate to the sketch of f(x)?

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- (d) Sketch f(x) + 3. Label the four points in your table on the graph. How does this sketch relate to the sketch of f(x)?
- (e) Can you make a guess about how the addition of constants inside and outside the function alters the graph? For example, f(x+a) does what to a graph? And f(x) + b does what?
- (19) Sketch the domain of each function on the real number line. Give the domain in **interval** notation of the following functions.
  - (a)  $f(x) = \sqrt{x-7}$
  - (b)  $f(x) = \frac{1}{x-4}$
  - (c)  $f(x) = \frac{2x-3}{3x+5}$
  - (d)  $f(x) = \sqrt{x-5} + \frac{x+1}{x-10}$  Hint: you might consider the domain of each term separately, then look for the intersection.
- (20) REFLECTION AND CONSOLIDATION (Hint: this will form part of a study guide for your first exam!)
  - (a) Summarize the main ideas/formulas you used for this problem set. You can list formulas, bullet-out phrases, write a paragraph, draw sketches, or answer this question in any way that makes sense to you.
  - (b) What three problems were the most challenging for you? After deciding, look at your solutions carefully, and write a short explanation of what you found challenging and how you overcame this challenge in your problem solving. For example, did you find a simpler problem about the same topic? Did you guess and check? Did you graph with technology?
  - (c) Write three potential test questions on the topics covered in this problem set.