

# **CONTINUOUS RANDOM VARIABLES AND DISTRIBUTIONS**



# DEFINITION

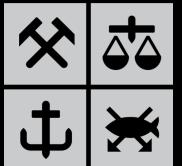
A **continuous random variable** can take all values in some interval of numbers. Thus, it has infinite possible values.

# PROBABILITY DENSITY FUNCTION

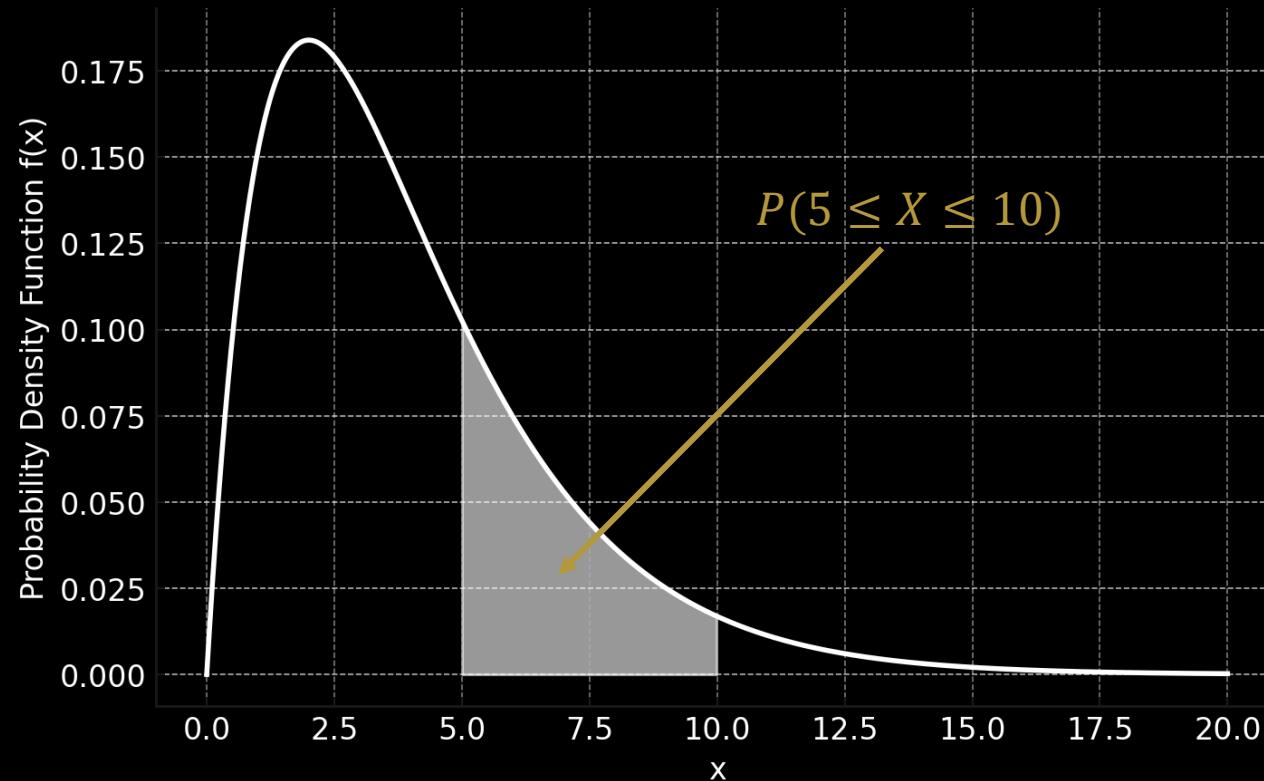
The probability distribution of a continuous variable  $X$  is described by a **probability density function** (pdf)  $f(x)$ .

- $f(x)$  represent the height of the curve at  $x$ .
- The probability of any event  $a \leq X \leq b$  is the area under the pdf between  $a$  and  $b$ :

$$P(a \leq X \leq b) = \int_a^b f(x)dx$$



# PROBABILITIES



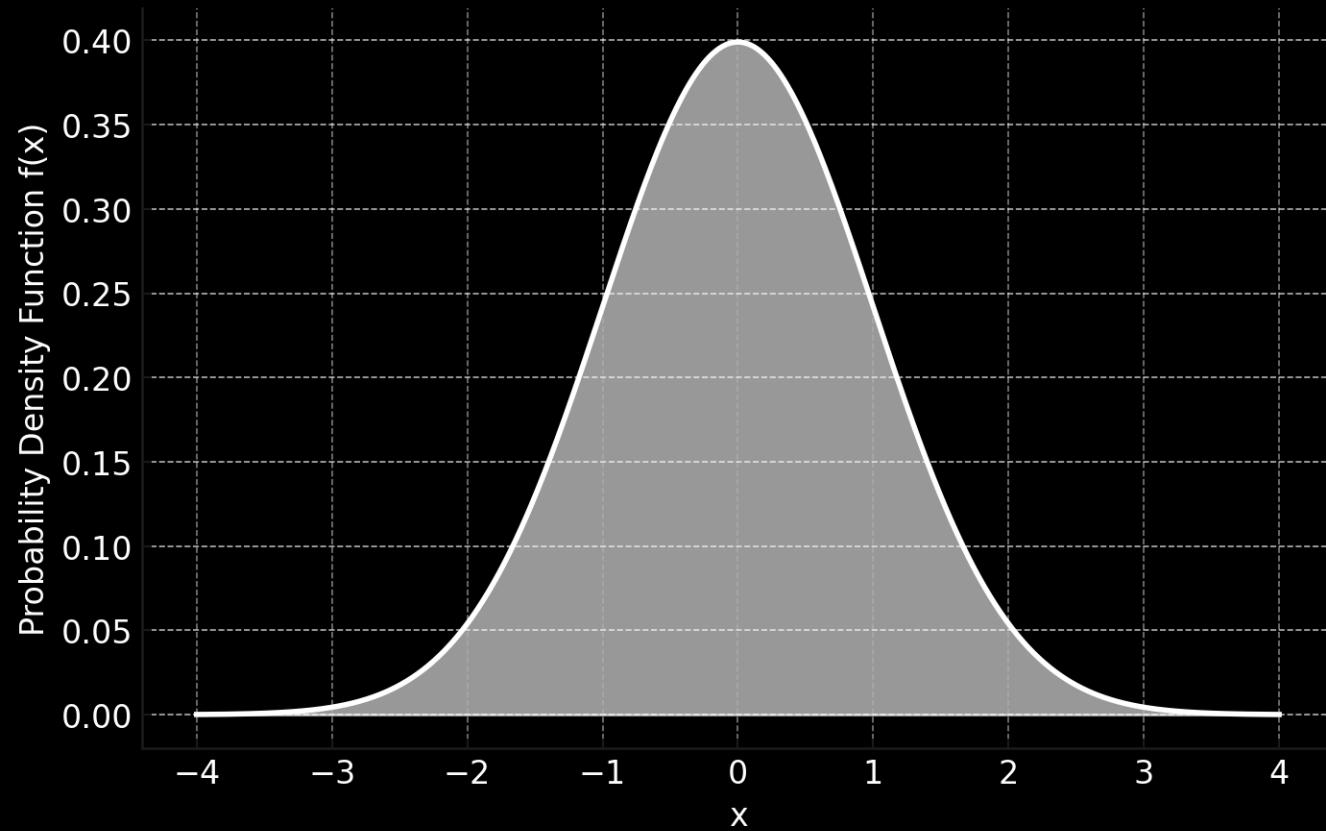
$P(X = a) = 0$  for all values  $a$ .

# PROPERTIES OF A PDF

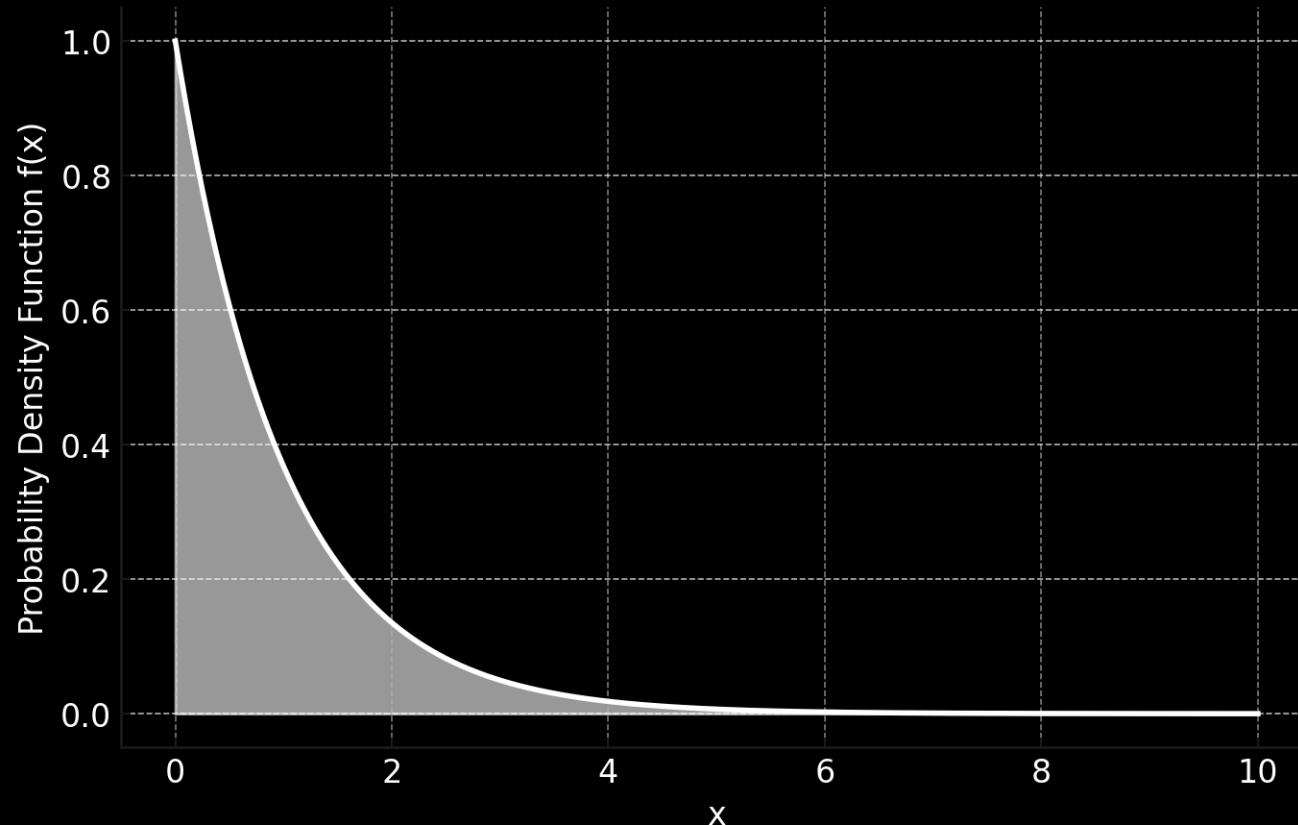
A probability density function must satisfy:

- $f(x) \geq 0$  for all  $x$
- The area under the entire curve is 1:  $\int_{-\infty}^{\infty} f(x)dx = 1$

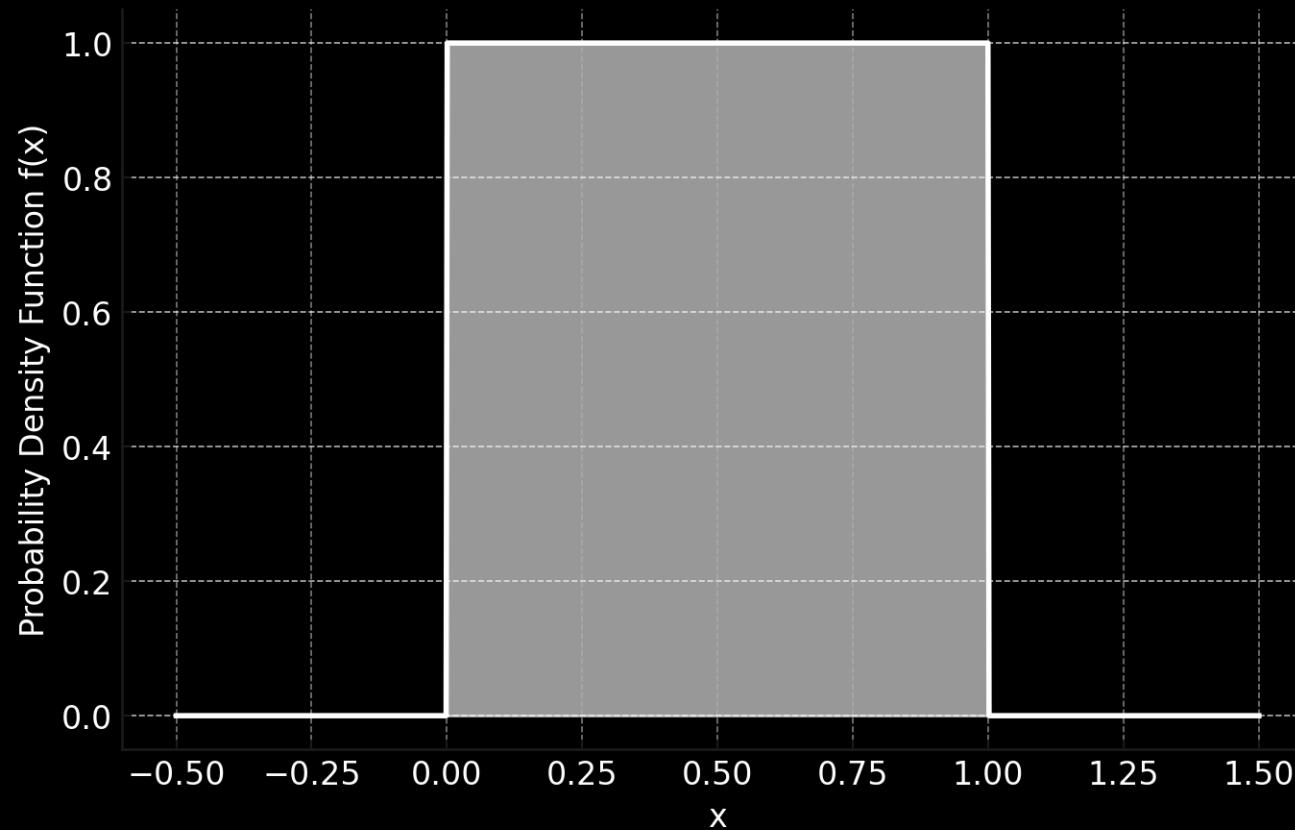
# NORMAL DISTRIBUTION



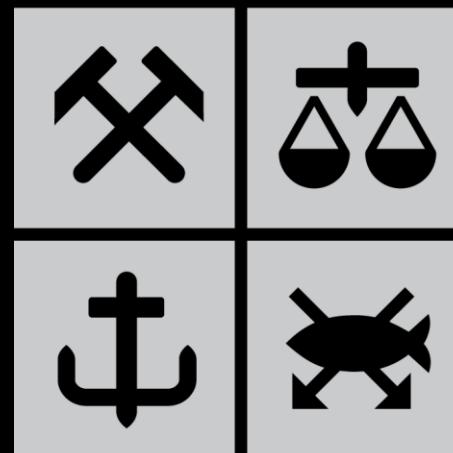
# EXPONENTIAL DISTRIBUTION



# UNIFORM DISTRIBUTION



# NHH TECH3



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