# Example evaluation of FOCUS dataset Z

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Key words: Kinetics, FOCUS, nonlinear optimisation		

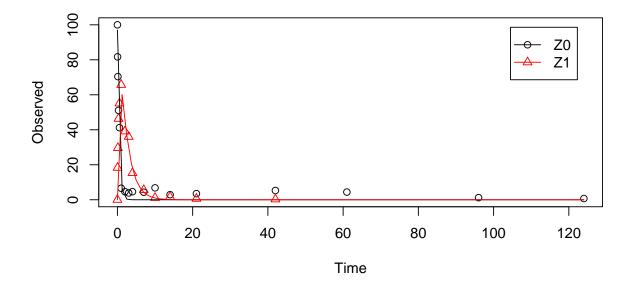
#### 1 The data

The following code defines the example dataset from Appendix 7 to the FOCUS kinetics report (FOCUS Work Group on Degradation Kinetics, 2011), p.350.

```
require(mkin)
## Loading required package:
                               mkin
## Loading required package:
                               minpack.lm
## Loading required package:
                               rootSolve
## Loading required package:
                               inline
## Loading required package:
                               methods
## Loading required package:
                               parallel
LOD = 0.5
FOCUS_2006_Z = data.frame(
  t = c(0, 0.04, 0.125, 0.29, 0.54, 1, 2, 3, 4, 7, 10, 14, 21,
        42, 61, 96, 124),
  Z0 = c(100, 81.7, 70.4, 51.1, 41.2, 6.6, 4.6, 3.9, 4.6, 4.3, 6.8,
         2.9, 3.5, 5.3, 4.4, 1.2, 0.7),
  Z1 = c(0, 18.3, 29.6, 46.3, 55.1, 65.7, 39.1, 36, 15.3, 5.6, 1.1,
         1.6, 0.6, 0.5 * LOD, NA, NA, NA),
  Z2 = c(0, NA, 0.5 * LOD, 2.6, 3.8, 15.3, 37.2, 31.7, 35.6, 14.5,
         0.8, 2.1, 1.9, 0.5 * LOD, NA, NA, NA),
  Z3 = c(0, NA, NA, NA, NA, NA, 0.5 * LOD, 9.2, 13.1, 22.3, 28.4, 32.5,
         25.2, 17.2, 4.8, 4.5, 2.8, 4.4))
FOCUS_2006_Z_mkin <- mkin_wide_to_long(FOCUS_2006_Z)
```

## 2 Parent compound and one metabolite

The next step is to set up the models used for the kinetic analysis. As the simultaneous fit of parent and the first metabolite is usually straightforward, Step 1 (SFO for parent only) is skipped here. We start with the model 2a, with formation and decline of metabolite Z1 and the pathway from parent directly to sink included (default in mkin).



```
## Model predictions using solution type deSolve
## Fitted with method Port using 340 model solutions performed in 1.372 s
## Weighting: none
##
## Starting values for parameters to be optimised:
               value
                       type
## ZO_0
            100.0000 state
## k_Z0_sink 0.1000 deparm
## k_Z0_Z1
              0.1001 deparm
## k_Z1_sink 0.1002 deparm
## Starting values for the transformed parameters actually optimised:
##
                     value lower upper
## ZO_0
                100.000000 -Inf
                                   Inf
## log_k_Z0_sink -2.302585 -Inf
                                   Inf
## log_k_Z0_Z1
                 -2.301586 -Inf
                                   Inf
## log_k_Z1_sink -2.300587 -Inf
                                 Inf
##
## Fixed parameter values:
       value type
## Z1_0
           0 state
## Optimised, transformed parameters with symmetric confidence intervals:
##
                Estimate Std. Error
                                         Lower
                                                    Upper
## ZO_0
                 97.0100 2.734e+00 9.141e+01 1.026e+02
## log_k_Z0_sink -25.0800 3.244e+05 -6.657e+05 6.656e+05
## log_k_Z0_Z1
                  0.8047 9.448e-02 6.108e-01 9.985e-01
## log_k_Z1_sink -0.7296 9.030e-02 -9.148e-01 -5.443e-01
##
## Parameter correlation:
##
                   ZO_O log_k_ZO_sink log_k_ZO_Z1 log_k_Z1_sink
## ZO_0
                 1.0000
                             -0.04450 0.106603
                                                      0.406943
## log_k_Z0_sink -0.0445
                             1.00000
                                      -0.706243
                                                      0.054352
## log_k_Z0_Z1
                             -0.70624
                                      1.000000
                                                     -0.007661
                0.1066
## log_k_Z1_sink 0.4069
                             0.05435
                                      -0.007661
                                                       1.000000
##
## Residual standard error: 5.064 on 27 degrees of freedom
## Backtransformed parameters:
```

```
Confidence intervals for internally transformed parameters are asymmetric.
##
     t-test (unrealistically) based on the assumption of normal distribution
##
     for estimators of untransformed parameters.
##
              Estimate
                         t value
                                    Pr(>t)
                                                       Upper
## ZO_0
             9.701e+01 2.730e+01 1.679e-21 91.4100 102.6000
## k_Z0_sink 1.281e-11 5.647e-11 5.000e-01 0.0000
                                                         Inf
             2.236e+00 1.355e+01 7.397e-14 1.8420
## k_Z0_Z1
                                                      2.7140
## k_Z1_sink 4.821e-01 7.321e+00 3.552e-08 0.4006
                                                      0.5803
##
## Chi2 error levels in percent:
            err.min n.optim df
              17.89
## All data
                          4 26
## Z0
              18.04
                          3 14
              15.08
## Z1
                          1 12
##
## Resulting formation fractions:
##
                  ff
## Z0_sink 5.731e-12
## ZO_Z1
           1.000e+00
## Z1_sink 1.000e+00
##
## Estimated disappearance times:
       DT50 DT90
## Z0 0.310 1.030
## Z1 1.438 4.776
```

As obvious from the summary, the kinetic rate constant from parent compound Z to sink is negligible. Accordingly, the exact magnitude of the fitted parameter log k\_Z\_sink is ill-defined and the covariance matrix is not returned. This suggests, in agreement with the analysis in the FOCUS kinetics report, to simplify the model by removing the pathway to sink.

A similar result can be obtained when formation fractions are used in the model formulation:

```
summary(m.Z.2a.ff, data = FALSE)
## mkin version:
                    0.9.39
## R version:
                    3.2.1
                    Fri Jun 26 14:41:50 2015
## Date of fit:
## Date of summary: Fri Jun 26 14:41:50 2015
##
## Equations:
## d_Z0 = - k_Z0 * Z0
## d_Z1 = + f_Z0_to_Z1 * k_Z0 * Z0 - k_Z1 * Z1
##
## Model predictions using solution type deSolve
##
## Fitted with method Port using 329 model solutions performed in 1.317 s
##
## Weighting: none
##
## Starting values for parameters to be optimised:
                 value
                         type
## ZO_0
              100.0000 state
## k_Z0
                0.1000 deparm
## k_Z1
                0.1001 deparm
## f_Z0_to_Z1
                0.5000 deparm
##
```

```
## Starting values for the transformed parameters actually optimised:
##
                  value lower upper
## ZO_0
             100.000000 -Inf
## log_k_Z0
             -2.302585 -Inf
                                Inf
## log_k_Z1
              -2.301586 -Inf
                                Inf
## f_Z0_ilr_1 0.000000 -Inf
                                Inf
## Fixed parameter values:
       value type
## Z1_0
           0 state
## Optimised, transformed parameters with symmetric confidence intervals:
             Estimate Std. Error
                                      Lower
                                                 Upper
## Z0_0
             97.0100 2.771e+00 9.133e+01
                                            1.027e+02
## log_k_Z0
              0.8047 1.043e-01 5.907e-01 1.019e+00
              -0.7296 9.140e-02 -9.171e-01 -5.420e-01
## log_k_Z1
## f_Z0_ilr_1 15.8900 5.756e+05 -1.181e+06 1.181e+06
##
## Parameter correlation:
                 Z0_0 log_k_Z0 log_k_Z1 f_Z0_ilr_1
## ZO_0
                                          -0.1698
              1.00000 -0.06309 0.42676
## log_k_Z0
            -0.06309 1.00000 -0.09811
                                           0.7672
                                           -0.1637
## log_k_Z1 0.42676 -0.09811 1.00000
## f_Z0_ilr_1 -0.16981 0.76721 -0.16372
                                            1.0000
## Residual standard error: 5.064 on 27 degrees of freedom
## Backtransformed parameters:
    Confidence intervals for internally transformed parameters are asymmetric.
    t-test (unrealistically) based on the assumption of normal distribution
##
    for estimators of untransformed parameters.
##
             Estimate t value
                                 Pr(>t)
                                                   Upper
              97.0100 27.300 1.679e-21 91.3300 102.7000
## ZO_0
## k Z0
               2.2360 10.310 3.662e-11 1.8050
                                                  2.7690
## k_Z1
               0.4821 7.321 3.552e-08 0.3997
                                                  0.5816
## f_Z0_to_Z1
             1.0000 9.855 9.707e-11 0.0000
                                                1.0000
## Chi2 error levels in percent:
           err.min n.optim df
## All data
             17.89
                         4 26
             17.56
## Z0
                         2 15
## Z1
             15.59
                         2 11
```

Here, the ilr transformed formation fraction fitted in the model takes a very large value, and the backtransformed formation fraction from parent Z to Z1 is practically unity. Again, the covariance matrix is not returned as the model is overparameterised.

The simplified model is obtained by setting the list component sink to FALSE.



```
summary(m.Z.3, data = FALSE)
## mkin version:
                  0.9.39
## R version:
                   3.2.1
                  Fri Jun 26 14:41:50 2015
## Date of fit:
## Date of summary: Fri Jun 26 14:41:50 2015
##
## Equations:
\#\# d_Z0 = - k_Z0 * Z0
\#\# d_Z1 = + k_Z0 * Z0 - k_Z1 * Z1
## Model predictions using solution type deSolve
## Fitted with method Port using 100 model solutions performed in 0.428 s
##
## Weighting: none
## Starting values for parameters to be optimised:
          value
                  type
## Z0_0 100.0000 state
## k_Z0
        0.1000 deparm
## k_Z1
        0.1001 deparm
## Starting values for the transformed parameters actually optimised:
##
                value lower upper
        100.000000 -Inf
## ZO_0
                              Inf
## log_k_Z0 -2.302585 -Inf
                              Tnf
## log_k_Z1 -2.301586 -Inf
                              Inf
##
## Fixed parameter values:
       value type
## Z1_0 0 state
##
## Optimised, transformed parameters with symmetric confidence intervals:
          Estimate Std. Error Lower
                                         Upper
## ZO_0
           97.0100
                      2.68200 91.5200 102.5000
## log_k_Z0 0.8047
                      0.06568 0.6702
                                       0.9392
                     0.08854 -0.9109 -0.5482
## log_k_Z1 -0.7296
##
## Parameter correlation:
            Z0_0 log_k_Z0 log_k_Z1
## Z0_0 1.0000 0.10629 0.41038
```

```
## log_k_Z0 0.1063 1.00000
                              0.04346
## log_k_Z1 0.4104
                    0.04346
                              1.00000
##
## Residual standard error: 4.973 on 28 degrees of freedom
## Backtransformed parameters:
##
     Confidence intervals for internally transformed parameters are asymmetric.
##
     t-test (unrealistically) based on the assumption of normal distribution
     for estimators of untransformed parameters.
##
##
        Estimate t value
                             Pr(>t)
                                      Lower
                                              Upper
         97.0100
                   36.18 2.364e-25 91.5200 102.500
## ZO_0
## k Z0
                   15.23 2.247e-15
          2.2360
                                    1.9550
                                              2.558
## k Z1
          0.4821
                   11.29 3.069e-12 0.4022
                                              0.578
##
## Chi2 error levels in percent:
            err.min n.optim df
              17.61
## All data
                           3 27
## Z0
              17.56
                           2 15
## 7.1
              15.08
                           1 12
##
## Estimated disappearance times:
       DT50 DT90
## Z0 0.310 1.030
## Z1 1.438 4.776
```

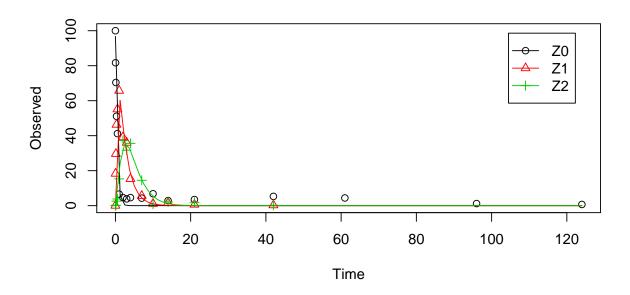
As there is only one transformation product for Z0 and no pathway to sink, the formation fraction is internally fixed to unity.

## 3 Including metabolites Z2 and Z3

As suggested in the FOCUS report, the pathway to sink was removed for metabolite Z1 as well in the next step. While this step appears questionable on the basis of the above results, it is followed here for the purpose of comparison. Also, in the FOCUS report, it is assumed that there is additional empirical evidence that Z1 quickly and exclusively hydrolyses to Z2.

## Successfully compiled differential equation model from auto-generated C code.

```
m.Z.5 <- mkinfit(Z.5, FOCUS_2006_Z_mkin, quiet = TRUE)
plot(m.Z.5)</pre>
```



```
summary(m.Z.5, data = FALSE)
## mkin version:
                    0.9.39
## R version:
                    3.2.1
## Date of fit:
                    Fri Jun 26 14:41:52 2015
## Date of summary: Fri Jun 26 14:41:52 2015
##
## Equations:
\#\# d_Z0 = -0 - k_Z0_Z1 * Z0
## d_Z1 = + k_Z0_Z1 * Z0 - 0 - k_Z1_Z2 * Z1
## d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2
##
## Model predictions using solution type deSolve
## Fitted with method Port using 199 model solutions performed in 1.126 s
## Weighting: none
## Starting values for parameters to be optimised:
##
                value
                        type
## Z0_0 100.0000 state
```

```
## k_Z0_Z1 0.1000 deparm
## k_Z1_Z2
              0.1001 deparm
## k_Z2_sink
             0.1002 deparm
##
## Starting values for the transformed parameters actually optimised:
                     value lower upper
## ZO_0
                100.000000 -Inf
## log_k_Z0_Z1
                -2.302585 -Inf
                                   Inf
## log_k_Z1_Z2
                 -2.301586 -Inf
                                   Tnf
## log_k_Z2_sink -2.300587 -Inf
                                   Inf
## Fixed parameter values:
       value type
           0 state
## Z1_0
## Z2_0
           0 state
##
## Optimised, transformed parameters with symmetric confidence intervals:
##
                Estimate Std. Error
                                      Lower
                                               Upper
## ZO_0
                 96.7700
                            2.26600 92.1900 101.3000
                 0.7948
                            0.05843 0.6767
## log_k_Z0_Z1
                                            0.9129
## log_k_Z1_Z2
                 -0.7410 0.06821 -0.8789
                                            -0.6032
## log_k_Z2_sink -0.8027
                           0.11090 -1.0270 -0.5785
##
## Parameter correlation:
##
                   Z0_0 log_k_Z0_Z1 log_k_Z1_Z2 log_k_Z2_sink
## ZO_0
                1.00000
                           0.05782
                                       0.28748
                                                      0.31786
## log_k_Z0_Z1
                0.05782
                                       -0.04361
                            1.00000
                                                      0.01213
## log_k_Z1_Z2
                0.28748
                           -0.04361
                                        1.00000
                                                      0.24019
## log_k_Z2_sink 0.31786
                                        0.24019
                           0.01213
                                                      1.00000
##
## Residual standard error: 4.486 on 40 degrees of freedom
## Backtransformed parameters:
    Confidence intervals for internally transformed parameters are asymmetric.
##
    t-test (unrealistically) based on the assumption of normal distribution
##
    for estimators of untransformed parameters.
##
            Estimate t value
                                Pr(>t)
                                        Lower
                                                  Upper
## ZO_0
             96.7700 42.710 2.717e-35 92.1900 101.3000
## k_Z0_Z1
              2.2140 17.120 2.615e-20 1.9670
                                                 2.4920
## k_Z1_Z2
              0.4766 14.660 5.572e-18 0.4152
                                                 0.5471
## k_Z2_sink 0.4481
                     9.016 1.754e-11 0.3581
                                                 0.5607
##
```

```
## Chi2 error levels in percent:
           err.min n.optim df
## All data
            19.10
                        4 38
## Z0
             17.43
                          2 15
             15.27
## Z1
                          1 12
## Z2
             19.57
                         1 11
##
## Resulting formation fractions:
         ff
## Z0_Z1
           1
## Z1_Z2
           1
## Z2_sink 1
##
## Estimated disappearance times:
      DT50 DT90
## Z0 0.3131 1.040
## Z1 1.4543 4.831
## Z2 1.5468 5.138
```

Finally, metabolite Z3 is added to the model. The fit is accellerated by using the starting parameters from the previous fit.

```
Z0
                                                                                       Z1
                                                                                       Z2
Observed
     9
                                                                                       Z3
     4
     20
             0
                         20
                                      40
                                                  60
                                                               80
                                                                           100
                                                                                       120
                                                  Time
```

```
summary(m.Z.FOCUS, data = FALSE)
## mkin version:
                    0.9.39
## R version:
                    3.2.1
## Date of fit:
                    Fri Jun 26 14:41:55 2015
## Date of summary: Fri Jun 26 14:41:56 2015
##
## Equations:
\#\# d_Z0 = -0 - k_Z0_Z1 * Z0
## d_Z1 = + k_Z0_Z1 * Z0 - 0 - k_Z1_Z2 * Z1
## d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3 * Z2
## d_Z3 = + k_Z2_Z3 * Z2 - k_Z3_sink * Z3
##
## Model predictions using solution type deSolve
## Fitted with method Port using 465 model solutions performed in 3.376 s
##
## Weighting: none
## Starting values for parameters to be optimised:
##
                value
                        type
## ZO_0
             100.0000
                      state
## k_Z0_Z1
               0.1000 deparm
## k_Z1_Z2
             0.1001 deparm
```

```
## k_Z2_sink 0.1002 deparm
## k_Z2_Z3
              0.1003 deparm
## k_Z3_sink
              0.1004 deparm
##
## Starting values for the transformed parameters actually optimised:
                     value lower upper
## ZO_0
                100.000000 -Inf
## log_k_Z0_Z1
                -2.302585 -Inf
                                   Inf
## log_k_Z1_Z2
                 -2.301586 -Inf
                                   Inf
## log_k_Z2_sink -2.300587 -Inf
                                   Inf
## log_k_Z2_Z3
                 -2.299590 -Inf
                                   Inf
## log_k_Z3_sink -2.298593 -Inf
                                   Inf
##
## Fixed parameter values:
      value type
## Z1_0
           0 state
## Z2_0
           0 state
## Z3_0
            0 state
## Optimised, transformed parameters with symmetric confidence intervals:
##
                Estimate Std. Error
                                      Lower
                                               Upper
## ZO_0
                 96.8400
                            2.05900 92.7100 101.0000
## log_k_Z0_Z1
                  0.7954
                            0.05332 0.6884
                                            0.9025
## log_k_Z1_Z2 -0.7375 0.06117 -0.8603 -0.6147
## log_k_Z2_sink -1.4330 0.17150 -1.7770 -1.0880
                 -1.5470
## log_k_Z2_Z3
                            0.12250 -1.7930 -1.3010
## log_k_Z3_sink -2.8350 0.24350 -3.3240 -2.3470
## Parameter correlation:
##
                    Z0_0 log_k_Z0_Z1 log_k_Z1_Z2 log_k_Z2_sink
## Z0_0
                  1.00000
                             0.05396
                                         0.27244
                                                       0.36977
## log_k_Z0_Z1
                 0.05396
                             1.00000
                                        -0.05186
                                                       0.02481
## log_k_Z1_Z2
                 0.27244
                            -0.05186
                                         1.00000
                                                       0.29261
## log_k_Z2_sink 0.36977
                            0.02481
                                         0.29261
                                                       1.00000
## log_k_Z2_Z3
                -0.07264
                            -0.03613
                                        -0.12025
                                                      -0.18859
## log_k_Z3_sink -0.11291
                            -0.02580
                                        -0.18947
                                                      -0.64263
##
                log_k_Z2_Z3 log_k_Z3_sink
## ZO_0
                   -0.07264
                                  -0.1129
## log_k_Z0_Z1
                   -0.03613
                                  -0.0258
## log_k_Z1_Z2
                   -0.12025
                                  -0.1895
## log_k_Z2_sink
                   -0.18859
                                  -0.6426
## log_k_Z2_Z3
                    1.00000
                                   0.5514
```

```
## log_k_Z3_sink
                     0.55142
                                     1.0000
##
## Residual standard error: 4.1 on 51 degrees of freedom
##
## Backtransformed parameters:
     Confidence intervals for internally transformed parameters are asymmetric.
     t-test (unrealistically) based on the assumption of normal distribution
##
##
     for estimators of untransformed parameters.
##
             Estimate t value
                                  Pr(>t)
                                           Lower
                                                      Upper
                       47.040 5.580e-44 92.7100 101.00000
## Z0_0
             96.84000
## k_Z0_Z1
              2.21500
                       18.750 7.735e-25
                                          1.9910
                                                    2.46600
## k_Z1_Z2
              0.47830
                      16.330 3.337e-22
                                          0.4230
                                                    0.54080
## k_Z2_sink
              0.23870
                       5.827 1.912e-07 0.1691
                                                    0.33680
## k_Z2_Z3
              0.21290
                        8.160 4.089e-11 0.1665
                                                    0.27230
## k_Z3_sink
              0.05869
                        4.106 7.288e-05 0.0360
                                                    0.09569
##
## Chi2 error levels in percent:
            err.min n.optim df
## All data
              19.23
                           6 48
## Z0
              17.45
                           2 15
## Z1
              15.24
                           1 12
## Z2
              20.32
                           2 10
              11.89
## Z3
                           1 11
##
## Resulting formation fractions:
               ff
## ZO_Z1
           1.0000
## Z1_Z2
           1.0000
## Z2_sink 0.5285
## Z2_Z3
           0.4715
## Z3_sink 1.0000
##
## Estimated disappearance times:
##
         DT50
                DT90
## Z0
       0.3129
               1.039
       1.4492
## Z1
               4.814
               5.099
## Z2
       1.5348
## Z3 11.8096 39.231
```

This is the fit corresponding to the final result chosen in Appendix 7 of the FOCUS report. The residual plots can be obtained by

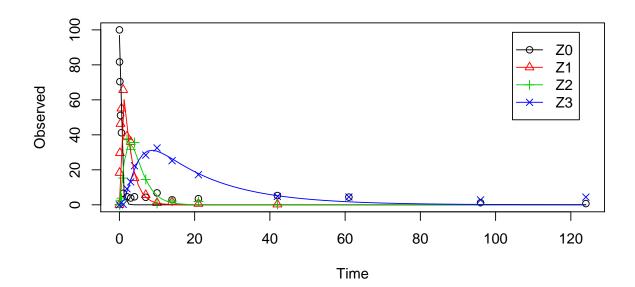
```
par(mfrow = c(2, 2))
mkinresplot(m.Z.FOCUS, "ZO", lpos = "bottomright")
mkinresplot(m.Z.FOCUS, "Z1", lpos = "bottomright")
mkinresplot(m.Z.FOCUS, "Z2", lpos = "bottomright")
mkinresplot(m.Z.FOCUS, "Z3", lpos = "bottomright")
```



We can also investigate the confidence interval for the formation fraction from Z2 to Z3 by specifying the model using formation fractions.

m.Z.FOCUS.ff <- mkinfit(Z.FOCUS.ff, FOCUS\_2006\_Z\_mkin, quiet = TRUE)</pre>

plot(m.Z.FOCUS.ff)



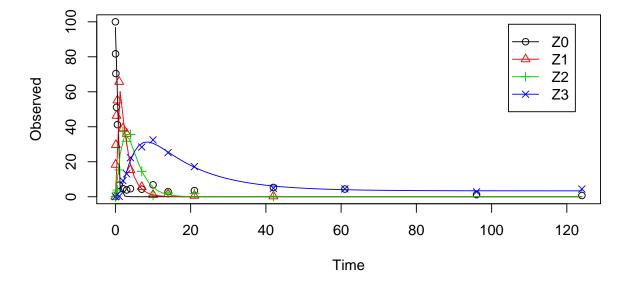
```
## Model predictions using solution type deSolve
## Fitted with method Port using 423 model solutions performed in 3.091 s
## Weighting: none
## Starting values for parameters to be optimised:
##
               value
                       type
## Z0_0
            100.0000 state
## k_Z0
              0.1000 deparm
## k_Z1
              0.1001 deparm
## k Z2
              0.1002 deparm
## k_Z3
             0.1003 deparm
## f_Z2_to_Z3 0.5000 deparm
##
## Starting values for the transformed parameters actually optimised:
##
                 value lower upper
## Z0_0
           100.000000 -Inf
                              Inf
## log_k_Z0
            -2.302585 -Inf
                              Inf
## log_k_Z1 -2.301586 -Inf Inf
## log_k_Z2
             -2.300587 -Inf
                              Inf
## log_k_Z3
            -2.299590 -Inf Inf
## f_Z2_ilr_1 0.000000 -Inf Inf
##
## Fixed parameter values:
      value type
## Z1_0
         0 state
## Z2_0
           0 state
## Z3_0
           0 state
## Optimised, transformed parameters with symmetric confidence intervals:
            Estimate Std. Error Lower
                                         Upper
## ZO_0
            96.84000
                       2.05900 92.7100 101.0000
## log_k_Z0 0.79540
                      0.05331 0.6884 0.9025
## log_k_Z1
            -0.73750 0.06116 -0.8603 -0.6147
            -0.79490
## log_k_Z2
                      0.09789 -0.9914 -0.5984
## log_k_Z3 -2.83500
                      0.24350 -3.3240 -2.3470
0.2442
##
## Parameter correlation:
##
               Z0_0 log_k_Z0 log_k_Z1 log_k_Z2 log_k_Z3 f_Z2_ilr_1
## ZO_0
            1.00000 0.054230 0.27243 0.299610 -0.11299 -0.31613
```

```
## log_k_Z0 0.05423 1.000000 -0.05099 0.001953 -0.02648 -0.03857
## log_k_Z1 0.27243 -0.050994 1.00000 0.199986 -0.18938
                                                             -0.28365
## log_k_Z2 0.29961 0.001953 0.19999 1.000000 -0.26974
                                                             -0.38832
## log_k_Z3 -0.11299 -0.026480 -0.18938 -0.269738 1.00000
                                                              0.77699
## f_Z2_ilr_1 -0.31613 -0.038565 -0.28365 -0.388324 0.77699
                                                              1.00000
## Residual standard error: 4.1 on 51 degrees of freedom
## Backtransformed parameters:
    Confidence intervals for internally transformed parameters are asymmetric.
    t-test (unrealistically) based on the assumption of normal distribution
    for estimators of untransformed parameters.
             Estimate t value
                                 Pr(>t)
                                                   Upper
                                         Lower
## Z0_0
             96.84000 47.040 5.582e-44 92.7100 101.00000
## k_Z0
              2.21500 18.760 7.693e-25 1.9910
                                                 2.46600
## k_Z1
              0.47830 16.330 3.330e-22 0.4230 0.54080
## k_Z2
              0.45160 10.210 3.110e-14 0.3710 0.54970
## k_Z3
              0.05869 4.106 7.285e-05 0.0360 0.09569
## f_Z2_to_Z3 0.47150 8.265 2.809e-11 0.3604 0.58550
## Chi2 error levels in percent:
           err.min n.optim df
## All data 19.23
                         6 48
             17.45
## Z0
                         2 15
## Z1
             15.24
                        1 12
## Z2
             19.61
                         1 11
## Z3
             12.32
                         2 10
## Resulting formation fractions:
##
              ff
## Z2_Z3
         0.4715
## Z2_sink 0.5285
## Estimated disappearance times:
        DT50
              DT90
## Z0 0.3129 1.039
## Z1 1.4492 4.814
## Z2 1.5348 5.099
## Z3 11.8096 39.231
```

### 4 Using the SFORB model for parent and metabolites

As the FOCUS report states, there is a certain tailing of the time course of metabolite Z3. Also, the time course of the parent compound is not fitted very well using the SFO model, as residues at a certain low level remain.

Therefore, an additional model is offered here, using the single first-order reversible binding (SFORB) model for metabolite Z3. As expected, the  $\chi^2$  error level is lower for metabolite Z3 using this model and the graphical fit for Z3 is improved. However, the covariance matrix is not returned.



```
summary(m.Z.mkin.1, data = FALSE)
## mkin version: 0.9.39
## R version: 3.2.1
```

```
## Date of fit: Fri Jun 26 14:42:06 2015
## Date of summary: Fri Jun 26 14:42:06 2015
##
## Equations:
## d_Z0 = - 0 - k_Z0_Z1 * Z0
## d_Z1 = + k_Z0_Z1 * Z0 - 0 - k_Z1_Z2 * Z1
\#\# d_Z2 = \# k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3_free * Z2
## d_Z3_free = + k_Z2_Z3_free * Z2 - k_Z3_free_sink * Z3_free -
              k_Z3_free_bound * Z3_free + k_Z3_bound_free *
##
              Z3_bound
## d_Z3_bound = + k_Z3_free_bound * Z3_free - k_Z3_bound_free *
              Z3 bound
##
## Model predictions using solution type deSolve
## Fitted with method Port using 829 model solutions performed in 6.139 s
##
## Weighting: none
## Starting values for parameters to be optimised:
##
                      value
                              type
## ZO_0
                   100.0000 state
## k_Z0_Z1
                     0.1000 deparm
## k_Z1_Z2
                     0.1001 deparm
## k_Z2_sink
                     0.1002 deparm
## k_Z2_Z3_free
                   0.1003 deparm
## k_Z3_free_sink     0.1004 deparm
## k_Z3_free_bound 0.1000 deparm
## k_Z3_bound_free 0.0200 deparm
##
## Starting values for the transformed parameters actually optimised:
##
                            value lower upper
## ZO_0
                       100.000000
                                  -Inf
                                          Inf
## log_k_Z0_Z1
                        -2.302585
                                  -Tnf
                                          Tnf
                        -2.301586
                                   -Inf
                                          Inf
## log_k_Z1_Z2
## log_k_Z2_sink
                        -2.300587
                                   -Inf
                                        Inf
                                  -Inf
## log_k_Z2_Z3_free
                        -2.299590
                                        Inf
## log_k_Z3_free_sink
                        -2.298593
                                   -Inf
                                          Inf
## log_k_Z3_free_bound -2.302585
                                   -Inf
                                          Inf
## log_k_Z3_bound_free -3.912023 -Inf
                                          Inf
##
## Fixed parameter values:
```

```
##
              value type
## Z1_0
                  0 state
## Z2_0
                  0 state
## Z3_free_0
                  0 state
## Z3_bound_0
                  0 state
## Optimised, transformed parameters with symmetric confidence intervals:
##
                       Estimate Std. Error Lower Upper
## ZO_0
                        96.7400
                                         NA
                                                NΑ
                                                      NΑ
## log_k_Z0_Z1
                         0.7947
                                         NA
                                               NA
                                                      NA
## log_k_Z1_Z2
                        -0.7426
                                         NA
                                                NA
                                                      NA
## log_k_Z2_sink
                        -1.4950
                                         NA
                                                NA
                                                      NA
## log_k_Z2_Z3_free
                                         NA
                                               NA
                                                      NA
                        -1.5040
## log_k_Z3_free_sink
                        -2.6540
                                         NA
                                               NA
                                                      NA
## log_k_Z3_free_bound -5.2440
                                         NA
                                               NA
                                                      NA
## log_k_Z3_bound_free -22.0900
                                         NA
                                               NA
                                                      NA
##
## Parameter correlation:
## Could not estimate covariance matrix; singular system:
## Residual standard error: 4.107 on 49 degrees of freedom
## Backtransformed parameters:
     Confidence intervals for internally transformed parameters are asymmetric.
     t-test (unrealistically) based on the assumption of normal distribution
     for estimators of untransformed parameters.
##
                    Estimate
                                t value
                                           Pr(>t) Lower Upper
                   9.674e+01 4.683e+01 1.197e-42
## ZO_0
                                                      NΑ
                                                            NΑ
## k_Z0_Z1
                   2.214e+00 1.871e+01 2.944e-24
                                                            NA
                                                      NA
## k_Z1_Z2
                   4.759e-01 1.619e+01 1.328e-21
                                                            NA
                                                      NA
## k_Z2_sink
                   2.243e-01 4.747e+00 9.147e-06
                                                            NA
                                                      NA
## k_Z2_Z3_free
                   2.222e-01 7.134e+00 2.059e-09
                                                            NA
## k_Z3_free_sink 7.034e-02 2.743e+00 4.243e-03
                                                            NA
                                                      NA
## k_Z3_free_bound 5.279e-03 4.513e-01 3.269e-01
                                                      NΑ
                                                            NΑ
## k_Z3_bound_free 2.562e-10 8.607e-09 5.000e-01
                                                      NA
                                                            NΑ
##
## Chi2 error levels in percent:
            err.min n.optim df
## All data 19.406
                           8 47
## Z0
             17.429
                           2 15
## Z1
             15.275
                           1 12
## Z2
             20.279
                           2 10
```

```
## Z3
               8.562
                            3 10
##
## Estimated Eigenvalues of SFORB model(s):
##
       Z3_b1
                  Z3_b2
## 7.562e-02 2.383e-10
##
## Resulting formation fractions:
##
                     ff
## ZO_Z1
                 1.0000
## Z1_Z2
                 1.0000
## Z2_sink
                 0.5024
## Z2_Z3_free
                 0.4976
## Z3_free_sink 1.0000
##
## Estimated disappearance times:
                 DT90 DT50_Z3_b1 DT50_Z3_b2
##
         DT50
                               NA
## Z0
       0.3131
                1.040
                                           NA
## Z1
       1.4566
                4.839
                               NA
                                           NA
## Z2
       1.5523
                5.157
                               NA
                                           NA
## Z3 10.1978 45.329
                            9.166
                                   2.909e+09
```

Therefore, a further stepwise model building is performed starting from the stage of parent and one metabolite, starting from the assumption that the model fit for the parent compound can be improved by using the SFORB model.

```
Operado

Ope
```

```
summary(m.Z.mkin.2, data = FALSE)
## mkin version:
                    0.9.39
## R version:
                    3.2.1
## Date of fit:
                    Fri Jun 26 14:42:07 2015
## Date of summary: Fri Jun 26 14:42:07 2015
##
## Equations:
## d_Z0_free = - 0 - k_Z0_free_bound * Z0_free + k_Z0_bound_free
              * Z0_bound - k_Z0_free_Z1 * Z0_free
## d_Z0_bound = + k_Z0_free_bound * Z0_free - k_Z0_bound_free *
              Z0_bound
## d_Z1 = + k_Z0_free_Z1 * Z0_free - k_Z1_sink * Z1
##
## Model predictions using solution type deSolve
## Fitted with method Port using 176 model solutions performed in 0.724 s
## Weighting: none
##
## Starting values for parameters to be optimised:
                      value
                              type
## Z0_free_0
                   100.0000 state
## k_Z0_free_bound
                   0.1000 deparm
```

```
## k_Z0_bound_free 0.0200 deparm
## k_Z0_free_Z1
                     0.1002 deparm
## k_Z1_sink
                     0.1003 deparm
##
## Starting values for the transformed parameters actually optimised:
                            value lower upper
## Z0_free_0
                       100.000000
                                   -Inf
                                          Inf
## log_k_Z0_free_bound -2.302585
                                   -Inf
                                          Inf
## log_k_Z0_bound_free -3.912023
                                          Tnf
                                   -Inf
## log_k_Z0_free_Z1
                        -2.300587
                                   -Inf
                                          Inf
## log_k_Z1_sink
                        -2.299590
                                   -Inf
                                          Inf
##
## Fixed parameter values:
              value type
## Z0_bound_0
                  0 state
## Z1_0
                  0 state
##
## Optimised, transformed parameters with symmetric confidence intervals:
##
                       Estimate Std. Error
                                             Lower
                                                       Upper
## Z0_free_0
                                   2.39500 92.3600 102.2000
                        97.2900
## log_k_Z0_free_bound -2.0820
                                   0.43260 -2.9710 -1.1930
## log_k_Z0_bound_free -4.7200
                                   1.60000 -8.0090 -1.4310
## log_k_Z0_free_Z1
                                   0.06431 0.7227
                        0.8549
                                                    0.9871
## log_k_Z1_sink
                        -0.7934
                                   0.08507 -0.9682 -0.6185
##
## Parameter correlation:
##
                       Z0_free_0 log_k_Z0_free_bound log_k_Z0_bound_free
## Z0_free_0
                         1.00000
                                               0.0066
                                                                  0.03334
                         0.00660
                                               1.0000
## log_k_Z0_free_bound
                                                                  0.54771
## log_k_Z0_bound_free
                                              0.5477
                                                                  1.00000
                         0.03334
## log_k_Z0_free_Z1
                                                                  0.15887
                         0.11184
                                              0.4141
## log_k_Z1_sink
                         0.39149
                                             -0.2922
                                                                 -0.12655
##
                       log_k_Z0_free_Z1 log_k_Z1_sink
## Z0_free_0
                                0.11184
                                              0.39149
## log_k_Z0_free_bound
                                0.41406
                                             -0.29216
## log_k_Z0_bound_free
                                0.15887
                                             -0.12655
                                             -0.04204
## log_k_Z0_free_Z1
                                1.00000
## log_k_Z1_sink
                               -0.04204
                                               1.00000
##
## Residual standard error: 4.438 on 26 degrees of freedom
##
## Backtransformed parameters:
```

```
Confidence intervals for internally transformed parameters are asymmetric.
    t-test (unrealistically) based on the assumption of normal distribution
    for estimators of untransformed parameters.
##
                    Estimate t value
##
                                        Pr(>t)
                                                             Upper
                                                    Lower
## Z0_free_0
                   97.290000 40.6100 2.364e-25 9.236e+01 102.2000
## k_Z0_free_bound 0.124700 2.3140 1.443e-02 5.123e-02
                                                            0.3034
## k_Z0_bound_free 0.008912 0.6231 2.693e-01 3.324e-04
                                                            0.2390
## k_Z0_free_Z1
                    2.351000 15.5500 5.521e-15 2.060e+00
                                                            2.6830
## k_Z1_sink
                    0.452300 11.7600 3.299e-12 3.797e-01
                                                            0.5387
##
## Chi2 error levels in percent:
            err.min n.optim df
## All data
             15.63
                          5 25
              14.74
## Z0
                          4 13
## Z1
              14.31
                          1 12
##
## Estimated Eigenvalues of SFORB model(s):
      Z0_b1
               Z0_b2
## 2.476315 0.008462
## Resulting formation fractions:
              ff
## Z0_free_Z1 1
## Z1_sink
               1
##
## Estimated disappearance times:
      DT50 DT90 DT50_Z0_b1 DT50_Z0_b2
## Z0 0.302 1.190
                      0.2799
                                  81.92
## Z1 1.532 5.091
                                     NA
                          NA
```

When metabolite Z2 is added, the additional sink for Z1 is turned off again, for the same reasons as in the original analysis.

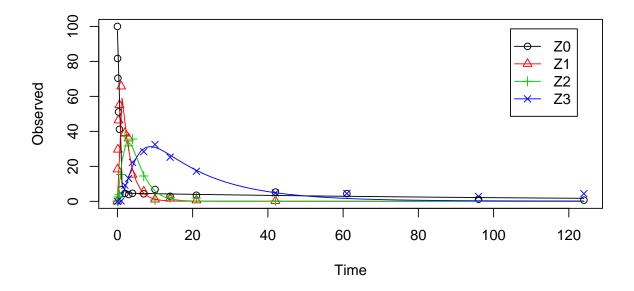
```
summary(m.Z.mkin.3, data = FALSE)
## mkin version:
                    0.9.39
## R version:
                    3.2.1
                    Fri Jun 26 14:42:09 2015
## Date of fit:
## Date of summary: Fri Jun 26 14:42:09 2015
##
## Equations:
## d_Z0_free = - 0 - k_Z0_free_bound * Z0_free + k_Z0_bound_free
              * Z0_bound - k_Z0_free_Z1 * Z0_free
## d_Z0_bound = + k_Z0_free_bound * Z0_free - k_Z0_bound_free *
##
              Z0_bound
## d_Z1 = + k_Z0_free_Z1 * Z0_free - 0 - k_Z1_Z2 * Z1
\#\# d_Z2 = \# k_Z1_Z2 * Z1 - k_Z2_sink * Z2
## Model predictions using solution type deSolve
##
## Fitted with method Port using 347 model solutions performed in 1.937 s
## Weighting: none
##
## Starting values for parameters to be optimised:
##
                      value
                              type
## Z0_free_0
                   100.0000 state
```

```
## k_ZO_free_bound 0.1000 deparm
## k_Z0_bound_free
                     0.0200 deparm
## k_Z0_free_Z1
                     0.1002 deparm
## k_Z1_Z2
                     0.1003 deparm
## k_Z2_sink
                     0.1004 deparm
##
## Starting values for the transformed parameters actually optimised:
##
                            value lower upper
## Z0_free_0
                                   -Inf
                       100.000000
                                           Inf
## log_k_Z0_free_bound -2.302585
                                   -Inf
                                           Inf
## log_k_Z0_bound_free -3.912023
                                   -Inf
                                           Inf
## log_k_Z0_free_Z1
                        -2.300587
                                   -Inf
                                           Inf
## log_k_Z1_Z2
                        -2.299590
                                   -Inf
                                          Inf
## log_k_Z2_sink
                        -2.298593
                                   -Inf
                                           Inf
##
## Fixed parameter values:
##
              value type
## Z0 bound 0
                  0 state
## Z1 0
                  0 state
## Z2_0
                  0 state
##
## Optimised, transformed parameters with symmetric confidence intervals:
                       Estimate Std. Error
                                              Lower
                                                       Upper
## Z0_free_0
                        97.4400
                                   2.07100 93.2400 101.6000
## log_k_Z0_free_bound -2.1490
                                   0.40310 -2.9650 -1.3330
## log_k_Z0_bound_free -4.8380
                                   1.57800 -8.0320 -1.6450
## log_k_Z0_free_Z1
                                   0.05831 0.7277 0.9638
                        0.8457
## log_k_Z1_Z2
                        -0.7812
                                   0.06484 -0.9124 -0.6499
## log_k_Z2_sink
                        -0.8606
                                   0.10570 -1.0750 -0.6466
##
## Parameter correlation:
##
                       Z0_free_0 log_k_Z0_free_bound log_k_Z0_bound_free
## Z0_free_0
                         1.00000
                                              0.07538
                                                                  0.07232
## log_k_Z0_free_bound
                         0.07538
                                              1.00000
                                                                  0.54571
## log_k_Z0_bound_free
                         0.07232
                                              0.54571
                                                                  1.00000
## log_k_Z0_free_Z1
                         0.09094
                                              0.42470
                                                                  0.16631
## log_k_Z1_Z2
                         0.25720
                                             -0.22703
                                                                 -0.08737
## log_k_Z2_sink
                                             -0.21014
                                                                 -0.08015
                         0.28877
##
                       log_k_Z0_free_Z1 log_k_Z1_Z2 log_k_Z2_sink
## Z0_free_0
                                0.09094
                                            0.25720
                                                           0.28877
## log_k_Z0_free_bound
                                0.42470
                                            -0.22703
                                                          -0.21014
## log_k_Z0_bound_free
                                0.16631
                                            -0.08737
                                                          -0.08015
```

```
## log_k_Z0_free_Z1
                                 1.00000
                                            -0.10056
                                                           -0.04878
## log_k_Z1_Z2
                                -0.10056
                                             1.00000
                                                            0.27259
## log_k_Z2_sink
                                -0.04878
                                             0.27259
                                                            1.00000
##
## Residual standard error: 4.081 on 38 degrees of freedom
## Backtransformed parameters:
##
     Confidence intervals for internally transformed parameters are asymmetric.
     t-test (unrealistically) based on the assumption of normal distribution
##
     for estimators of untransformed parameters.
##
##
                   Estimate t value
                                        Pr(>t)
                                                   Lower
                                                             Upper
                   97.44000 47.0500 1.353e-35 9.324e+01 101.6000
## Z0_free_0
## k_ZO_free_bound 0.11660 2.4730 8.993e-03 5.157e-02
                                                            0.2638
## k_Z0_bound_free 0.00792
                             0.6198 2.695e-01 3.248e-04
                                                            0.1931
## k_Z0_free_Z1
                    2.33000 17.1400 8.899e-20 2.070e+00
                                                            2.6220
## k_Z1_Z2
                    0.45790 15.4200 3.057e-18 4.015e-01
                                                            0.5221
## k_Z2_sink
                    0.42290 9.4580 7.842e-12 3.414e-01
                                                            0.5238
##
## Chi2 error levels in percent:
            err.min n.optim df
## All data
              17.33
                           6 36
## Z0
              14.67
                           4 13
                          1 12
## Z1
              14.41
## Z2
              20.29
                           1 11
##
## Estimated Eigenvalues of SFORB model(s):
      Z0_b1
               Z0_b2
##
## 2.446636 0.007541
##
## Resulting formation fractions:
##
              ff
## Z0_free_Z1
               1
## Z1_Z2
               1
## Z2_sink
               1
##
## Estimated disappearance times:
        DT50 DT90 DT50_Z0_b1 DT50_Z0_b2
## Z0 0.3043 1.185
                       0.2833
                                    91.91
## Z1 1.5138 5.029
                            NA
                                       NA
## Z2 1.6391 5.445
                           NA
                                       NA
```

This results in a much better representation of the behaviour of the parent compound Z0.

Finally, Z3 is added as well. These models appear overparameterised (no covariance matrix returned) if the sink for Z1 is left in the models.



```
##
              Z0_bound
## d_Z1 = + k_Z0_free_Z1 * Z0_free - 0 - k_Z1_Z2 * Z1
\#\# d_Z2 = \# k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3 * Z2
## d_Z3 = + k_Z2_Z3 * Z2 - k_Z3_sink * Z3
## Model predictions using solution type deSolve
## Fitted with method Port using 607 model solutions performed in 4.407 s
## Weighting: none
## Starting values for parameters to be optimised:
                      value
##
                             type
## Z0_free_0
                   100.0000 state
## k_ZO_free_bound 0.1000 deparm
## k_Z0_bound_free 0.0200 deparm
## k_Z0_free_Z1
                   0.1002 deparm
## k_Z1_Z2
                    0.1003 deparm
## k_Z2_sink
                    0.1004 deparm
## k_Z2_Z3
                     0.1005 deparm
## k_Z3_sink
                     0.1006 deparm
## Starting values for the transformed parameters actually optimised:
##
                            value lower upper
## Z0_free_0
                       100.000000
                                  -Inf
                                          Inf
## log_k_Z0_free_bound -2.302585
                                  -Inf
                                          Inf
## log_k_Z0_bound_free -3.912023
                                  -Inf
                                          Inf
## log_k_Z0_free_Z1
                        -2.300587
                                  -Inf
                                          Tnf
                       -2.299590 -Inf Inf
## log_k_Z1_Z2
                       -2.298593 -Inf
                                       Inf
## log_k_Z2_sink
## log_k_Z2_Z3
                        -2.297598
                                  -Inf
                                          Inf
## log_k_Z3_sink
                        -2.296603 -Inf
                                          Inf
## Fixed parameter values:
             value type
## Z0_bound_0
                 0 state
## Z1_0
                  0 state
## Z2_0
                  0 state
## Z3_0
                  0 state
## Optimised, transformed parameters with symmetric confidence intervals:
##
                       Estimate Std. Error Lower Upper
```

```
## Z0_free_0
                        97.5300
                                   1.88700 93.7400 101.3000
## log_k_Z0_free_bound -2.1360
                                   0.36820 -2.8760 -1.3960
## log_k_Z0_bound_free
                        -4.7650
                                   1.41800 -7.6140 -1.9160
## log_k_Z0_free_Z1
                                   0.05339 0.7398 0.9543
                         0.8470
## log_k_Z1_Z2
                        -0.7769
                                   0.05834 -0.8942 -0.6597
## log_k_Z2_sink
                                   0.18260 -1.9280 -1.1940
                        -1.5610
## log_k_Z2_Z3
                        -1.5280 0.11350 -1.7560 -1.2990
## log_k_Z3_sink
                        -2.7690
                                   0.22460 -3.2200 -2.3180
##
## Parameter correlation:
##
                       Z0_free_0 log_k_Z0_free_bound log_k_Z0_bound_free
## Z0_free_0
                         1.00000
                                             0.07822
                                                                  0.06921
## log_k_Z0_free_bound
                         0.07822
                                             1.00000
                                                                  0.53978
## log_k_Z0_bound_free
                         0.06921
                                             0.53978
                                                                  1.00000
## log_k_Z0_free_Z1
                         0.08882
                                             0.42766
                                                                  0.16282
## log_k_Z1_Z2
                         0.24238
                                                                 -0.08936
                                            -0.22742
## log_k_Z2_sink
                         0.32993
                                            -0.26331
                                                                 -0.12744
## log_k_Z2_Z3
                        -0.07494
                                             0.06698
                                                                  0.06082
                                             0.13844
## log_k_Z3_sink
                        -0.10456
                                                                  0.12525
##
                       log_k_Z0_free_Z1 log_k_Z1_Z2 log_k_Z2_sink
## Z0_free_0
                                0.08882
                                           0.24238
                                                           0.32993
## log_k_Z0_free_bound
                                           -0.22742
                                0.42766
                                                         -0.26331
## log_k_Z0_bound_free
                                0.16282
                                           -0.08936
                                                         -0.12744
## log_k_Z0_free_Z1
                                           -0.10841
                                1.00000
                                                         -0.05309
## log_k_Z1_Z2
                               -0.10841
                                           1.00000
                                                          0.34052
## log_k_Z2_sink
                               -0.05309
                                            0.34052
                                                          1.00000
## log_k_Z2_Z3
                               -0.01281
                                           -0.14885
                                                         -0.25473
## log_k_Z3_sink
                                0.01858
                                           -0.22486
                                                          -0.68320
##
                       log_k_Z2_Z3 log_k_Z3_sink
## Z0_free_0
                          -0.07494
                                        -0.10456
## log_k_Z0_free_bound
                                         0.13844
                           0.06698
## log_k_Z0_bound_free
                          0.06082
                                         0.12525
## log_k_Z0_free_Z1
                                         0.01858
                          -0.01281
## log_k_Z1_Z2
                          -0.14885
                                        -0.22486
## log_k_Z2_sink
                                        -0.68320
                          -0.25473
## log_k_Z2_Z3
                           1.00000
                                         0.56390
## log_k_Z3_sink
                           0.56390
                                         1.00000
##
## Residual standard error: 3.737 on 49 degrees of freedom
## Backtransformed parameters:
     Confidence intervals for internally transformed parameters are asymmetric.
```

```
##
     t-test (unrealistically) based on the assumption of normal distribution
##
     for estimators of untransformed parameters.
##
                     Estimate t value
                                          Pr(>t)
                                                               Upper
                                                     Lower
## Z0_free_0
                    97.530000 51.7000 1.033e-44 9.374e+01 101.3000
## k_Z0_free_bound
                    0.118100 2.7160 4.548e-03 5.636e-02
                                                              0.2475
## k_Z0_bound_free
                    0.008522 0.7054 2.419e-01 4.936e-04
                                                              0.1471
## k_Z0_free_Z1
                     2.333000 18.7300 2.790e-24 2.095e+00
                                                              2.5970
## k_Z1_Z2
                     0.459800 17.1400 1.223e-22 4.089e-01
                                                              0.5170
## k_Z2_sink
                     0.209900
                               5.4770 7.394e-07 1.455e-01
                                                              0.3030
## k_Z2_Z3
                     0.217000
                               8.8070 5.733e-12 1.728e-01
                                                              0.2727
## k_Z3_sink
                     0.062720
                               4.4520 2.459e-05 3.994e-02
                                                              0.0985
##
## Chi2 error levels in percent:
            err.min n.optim df
## All data
              17.50
                           8 46
## Z0
              14.69
                           4 13
## Z1
              14.39
                           1 12
## Z2
              21.05
                           2.10
## Z3
              11.76
                           1 11
##
## Estimated Eigenvalues of SFORB model(s):
             Z0_b2
##
     Z0_b1
## 2.45126 0.00811
##
## Resulting formation fractions:
                   ff
## Z0_free_Z1 1.0000
## Z1_Z2
              1.0000
## Z2_sink
              0.4917
## Z2_Z3
              0.5083
## Z3_sink
              1.0000
##
## Estimated disappearance times:
##
        DT50
               DT90 DT50_Z0_b1 DT50_Z0_b2
                                      85.47
## Z0
       0.304
              1.186
                         0.2828
## Z1
       1.507
              5.008
                             NA
                                         NA
## Z2
       1.623
              5.393
                             NA
                                         NA
## Z3 11.051 36.712
                             NA
                                         NA
```

The error level of the fit, but especially of metabolite Z3, can be improved if the SFORB model is chosen for this metabolite, as this model is capable of representing the tailing of the metabolite decline phase.



```
summary(m.Z.mkin.5, data = FALSE)$bpar
##
                       Estimate se_notrans
                                                 t value
## Z0_free_0
                   9.742496e+01 1.88615829 5.165259e+01 2.327739e-43
## k_Z0_free_bound 1.167582e-01 0.04302217 2.713909e+00 4.633395e-03
## k_Z0_bound_free 7.890260e-03 0.01162028 6.790077e-01 2.502316e-01
                   2.330002e+00 0.12411426 1.877304e+01 8.893667e-24
## k_Z0_free_Z1
## k_Z1_Z2
                   4.575901e-01 0.02681895 1.706219e+01 4.516643e-22
## k_Z2_sink
                   1.957097e-01 0.04395612 4.452388e+00 2.605224e-05
## k_Z2_Z3_free
                   2.265848e-01 0.02922696 7.752595e+00 2.987495e-10
## k_Z3_free_sink 7.478914e-02 0.02433843 3.072882e+00 1.761201e-03
## k_Z3_free_bound 5.217939e-03 0.01034277 5.045013e-01 3.081332e-01
## k_Z3_bound_free 4.406164e-10 0.02663898 1.654029e-08 5.000000e-01
##
                   Lower Upper
```

```
## Z0_free_0
                        NA
                              NA
## k_Z0_free_bound
                        NA
                              NA
## k_Z0_bound_free
                              NA
                        NA
## k_Z0_free_Z1
                        NA
                              NA
## k_Z1_Z2
                        NA
                              NA
## k_Z2_sink
                        NA
                              NA
## k_Z2_Z3_free
                        NA
                              NA
## k_Z3_free_sink
                              NA
                        NA
## k_Z3_free_bound
                              NA
                        NA
## k_Z3_bound_free
                        NA
                              NA
```

The summary view of the backtransformed parameters shows that we get no confidence intervals due to overparameterisation. As the optimized k\_Z3\_bound\_free is excessively small, it seems reasonable to fix it to zero.

```
m.Z.mkin.5a <- mkinfit(Z.mkin.5, FOCUS_2006_Z_mkin,
                       parms.ini = c(k_Z3_bound_free = 0),
                       fixed_parms = "k_Z3_bound_free",
                       quiet = TRUE)
summary(m.Z.mkin.5a, data = FALSE)$bpar
##
                                                             Pr(>t)
                       Estimate
                                 se_notrans
                                               t value
## Z0_free_0
                   97.424978857 1.864396799 52.255496 2.880619e-44
## k_Z0_free_bound 0.116757939 0.042567928
                                              2.742862 4.268192e-03
## k_Z0_bound_free 0.007890184 0.011498777
                                              0.686176 2.479517e-01
## k_Z0_free_Z1
                    2.329999746 0.122793940 18.974876 2.997958e-24
## k_Z1_Z2
                    0.457590280 0.026468268 17.288260 1.494011e-22
## k_Z2_sink
                    0.195709803 0.041590057
                                             4.705687 1.089697e-05
## k_Z2_Z3_free
                    0.226584724 0.027560331
                                              8.221408 5.106652e-11
## k_Z3_free_sink
                    0.074789042 0.020202690
                                              3.701935 2.757338e-04
## k_Z3_free_bound
                    0.005217923 0.004074066
                                              1.280765 1.032150e-01
##
                          Lower
                                      Upper
## Z0_free_0
                   9.367767e+01 101.1722896
## k_Z0_free_bound 5.619674e-02
                                  0.2425838
## k_Z0_bound_free 4.354112e-04
                                  0.1429798
## k_Z0_free_Z1
                   2.095795e+00
                                  2.5903768
## k_Z1_Z2
                   4.073348e-01
                                  0.5140461
## k_Z2_sink
                   1.277075e-01
                                  0.2999224
## k_Z2_Z3_free
                   1.775320e-01
                                  0.2891908
## k_Z3_free_sink
                   4.353436e-02
                                  0.1284825
## k_Z3_free_bound 1.098317e-03
                                  0.0247895
```

A graphical representation of the confidence intervals can finally be obtained.

#### mkinparplot(m.Z.mkin.5a)



The endpoints obtained with this model are

```
Z0_b1
                      Z0_b2
                                  Z3_b1
                                               Z3_b2
## 2.447135360 0.007512509 0.080006965 0.000000000
##
## $distimes
##
           DT50
                      DT90 DT50_Z0_b1 DT50_Z0_b2 DT50_Z3_b1 DT50_Z3_b2
## Z0 0.3043059
                            0.2832484
                                         92.26573
                                                           NA
                 1.184812
                                                                       NA
## Z1 1.5147769
                 5.031980
                                                                      NA
                                   NA
                                               NA
                                                           NA
## Z2 1.6413833
                 5.452557
                                   NA
                                               NA
                                                           NA
                                                                      NA
## Z3 9.5675326 41.136701
                                   NA
                                               NA
                                                    8.663585
                                                                     Inf
```

It is clear the degradation rate of Z3 towards the end of the experiment is very low as DT50\_Z3\_b2 is reported to be infinity. However, this appears to be a feature of the data.

```
par(mfrow = c(2, 2))
mkinresplot(m.Z.mkin.5, "Z0", lpos = "bottomright")
mkinresplot(m.Z.mkin.5, "Z1", lpos = "bottomright")
mkinresplot(m.Z.mkin.5, "Z2", lpos = "bottomright")
mkinresplot(m.Z.mkin.5, "Z3", lpos = "bottomright")
```



As expected, the residual plots are much more random than in the case of the all SFO model for which they were shown above. In conclusion, the model Z.mkin.5 is proposed as the best-fit model for the dataset from Appendix 7 of the FOCUS report.

#### References

FOCUS Work Group on Degradation Kinetics. Generic guidance for estimating persistence and degradation kinetics from environmental fate studies on pesticides in EU registration, 1.0 edition, November 2011. URL http://focus.jrc.ec.europa.eu/dk.