Examples for kinetic evaluations using mkin

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Key words: Kinetics, FOCUS, nonlinear optimisation

1 Kinetic evaluations for parent compounds

These examples are also evaluated in a parallel vignette of the **kinfit** package (?). The datasets are from Appendix 3, of the FOCUS kinetics report (??).

1.1 Laboratory Data L1

The following code defines example dataset L1 from the FOCUS kinetics report, p. 284

The next step is to set up the models used for the kinetic analysis. Note that the model definitions contain the names of the observed variables in the data. In this case, there is only one variable called parent.

```
R> SF0 <- mkinmod(parent = list(type = "SF0"))
R> FOMC <- mkinmod(parent = list(type = "FOMC"))
R> DF0P <- mkinmod(parent = list(type = "DF0P"))</pre>
```

The three models cover the first assumption of simple first order (SFO), the case of declining rate constant over time (FOMC) and the case of two different phases of the kinetics (DFOP). For a more detailed discussion of the models, please see the FOCUS kinetics report.

The following two lines fit the model and produce the summary report of the model fit. This covers the numerical analysis given in the FOCUS report.

```
R> m.L1.SF0 <- mkinfit(SF0, F0CUS_2006_L1_mkin, quiet=TRUE)
R> summary(m.L1.SF0)
mkin version:
              0.9.23
R version:
               3.0.1
Date of fit: Wed Nov 6 08:28:45 2013
Date of summary: Wed Nov 6 08:28:45 2013
Equations:
[1] d_parent = - k_parent_sink * parent
Method used for solution of differential equation system:
analytical
Weighting: none
Starting values for optimised parameters:
           value type transformed
           100.0 state 100.000000
parent_0
Fixed parameter values:
None
Optimised, transformed parameters:
           Estimate Std. Error Lower Upper
parent_0
             92.470 1.36800 89.570 95.370
k_parent_sink -2.347 0.04057 -2.433 -2.261
Backtransformed parameters:
           Estimate
                      Lower
                               Upper
parent_0
           92.47000 89.57000 95.3700
k_parent_sink 0.09561 0.08773 0.1042
Residual standard error: 2.948 on 16 degrees of freedom
Chi2 error levels in percent:
       err.min n.optim df
All data 3.424 2 7
                    2 7
        3.424
parent
Estimated disappearance times:
       DT50 DT90
parent 7.249 24.08
```

Estimated formation fractions:

```
ff parent_sink 1
```

Parameter correlation:

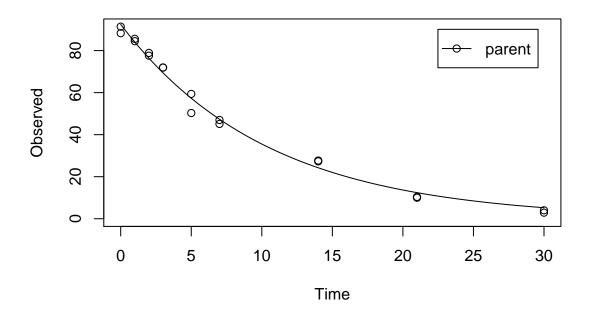
		parent_0	k_parent_	_sink
parent_0		1.0000	0.	. 6248
k parent.	sink	0.6248	1.	.0000

Data:

time	variable	observed	predicted	residual
0	parent	88.3	92.471	-4.1710
0	parent	91.4	92.471	-1.0710
1	parent	85.6	84.039	1.5610
1	parent	84.5	84.039	0.4610
2	parent	78.9	76.376	2.5241
2	parent	77.6	76.376	1.2241
3	parent	72.0	69.412	2.5884
3	parent	71.9	69.412	2.4884
5	parent	50.3	57.330	-7.0301
5	parent	59.4	57.330	2.0699
7	parent	47.0	47.352	-0.3515
7	parent	45.1	47.352	-2.2515
14	parent	27.7	24.247	3.4527
14	parent	27.3	24.247	3.0527
21	parent	10.0	12.416	-2.4163
21	parent	10.4	12.416	-2.0163
30	parent	2.9	5.251	-2.3513
30	parent	4.0	5.251	-1.2513

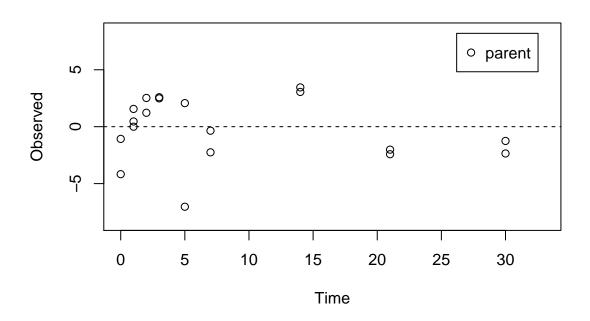
A plot of the fit is obtained with the plot function for mkinfit objects.

R> plot(m.L1.SF0)



The residual plot can be easily obtained by

R> mkinresplot(m.L1.SFO, ylab = "Observed", xlab = "Time")



For comparison, the FOMC model is fitted as well, and the χ^2 error level is checked.

R> m.L1.FOMC <- mkinfit(FOMC, FOCUS_2006_L1_mkin, quiet=TRUE) R> summary(m.L1.FOMC)

mkin version: 0.9.23
R version: 3.0.1

Date of fit: Wed Nov 6 08:28:45 2013
Date of summary: Wed Nov 6 08:28:45 2013

Equations:

[1] $d_{parent} = - (alpha/beta) * ((time/beta) + 1)^{-1} * parent$

Method used for solution of differential equation system: analytical

Weighting: none

Starting values for optimised parameters:

 value
 type transformed

 parent_0
 100 state
 100.000000

 alpha
 1 deparm
 0.000000

 beta
 10 deparm
 2.302585

Fixed parameter values:

None

Optimised, transformed parameters:

Backtransformed parameters:

Estimate Lower Upper

Residual standard error: 3.045 on 15 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df

All data 3.619 3 6 parent 3.619 3 6

Estimated disappearance times:

DT50 DT90

parent 7.249 24.08

Estimated formation fractions:

ff

parent_sink 1

Parameter correlation:

Could not estimate covariance matrix; singular system:

Data:

time variable observed predicted residual 0 parent 88.3 92.471 -4.1711 92.471 -1.0711 parent 91.4 0 85.6 84.038 1.5618 1 parent 84.5 84.038 0.4618 1 parent 78.9 76.377 2 2.5233 parent 2 77.6 76.377 1.2233 parent 3 parent 72.0 69.412 2.5884 3 parent 71.9 69.412 2.4884 50.3 57.331 -7.0306 5 parent 59.4 57.331 2.0694 parent 7 47.0 47.351 -0.3510 parent 7 parent 45.1 47.351 -2.2510 14 27.7 24.247 3.4526 parent 27.3 24.247 3.0526 14 parent 21 parent 10.0 12.416 -2.4162 parent 21 10.4 12.416 -2.0162

```
30 parent 2.9 5.251 -2.3513
30 parent 4.0 5.251 -1.2513
```

Due to the higher number of parameters, and the lower number of degrees of freedom of the fit, the χ^2 error level is actually higher for the FOMC model (3.6%) than for the SFO model (3.4%). Additionally, the covariance matrix can not be obtained, indicating overparameterisation of the model.

The χ^2 error levels reported in Appendix 3 and Appendix 7 to the FOCUS kinetics report are rounded to integer percentages and partly deviate by one percentage point from the results calculated by mkin. The reason for this is not known. However, mkin gives the same χ^2 error levels as the kinfit package. Furthermore, the calculation routines of the kinfit package have been extensively compared to the results obtained by the KinGUI software, as documented in the kinfit package vignette. KinGUI is a widely used standard package in this field. Therefore, the reason for the difference was not investigated further.

1.2 Laboratory Data L2

The following code defines example dataset L2 from the FOCUS kinetics report, p. 287

```
R> FOCUS_2006_L2 = data.frame(
    t = rep(c(0, 1, 3, 7, 14, 28), each = 2),
    parent = c(96.1, 91.8, 41.4, 38.7,
+
               19.3, 22.3, 4.6, 4.6,
               2.6, 1.2, 0.3, 0.6))
R> FOCUS_2006_L2_mkin <- mkin_wide_to_long(FOCUS_2006_L2)
Again, the SFO model is fitted and a summary is obtained.
R> m.L2.SFO <- mkinfit(SFO, FOCUS_2006_L2_mkin, quiet=TRUE)
R> summary(m.L2.SF0)
                 0.9.23
mkin version:
R version:
                 3.0.1
Date of fit:
                 Wed Nov
                          6 08:28:46 2013
Date of summary: Wed Nov
                          6 08:28:46 2013
Equations:
[1] d_parent = - k_parent_sink * parent
Method used for solution of differential equation system:
analytical
Weighting: none
Starting values for optimised parameters:
```

value type transformed

100.0000000 state 100.000000 parent_0 k_parent_sink 0.1000009 deparm -2.302576

Fixed parameter values:

None

Optimised, transformed parameters:

Estimate Std. Error Lower Upper

91.4700 3.8070 82.9800 99.9500 parent_0

k_parent_sink -0.4112 0.1074 -0.6505 -0.1719

Backtransformed parameters:

Estimate Lower Upper

91.4700 82.9800 99.9500 parent_0

k_parent_sink 0.6629 0.5218 0.8421

Residual standard error: 5.51 on 10 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df

2 4 All data 14.38

14.38 2 4 parent

Estimated disappearance times:

DT50 DT90

parent 1.046 3.474

Estimated formation fractions:

ff

parent_sink 1

Parameter correlation:

parent_0 k_parent_sink

1.0000 0.4295 parent_0

k_parent_sink 0.4295 1.0000

Data:

time variable observed predicted residual

0 parent 96.1 9.147e+01 4.6344

0 parent 91.8 9.147e+01 0.3344

1 parent 41.4 4.714e+01 -5.7395

parent 38.7 4.714e+01 -8.4395

3 19.3 1.252e+01 6.7790 parent

3 parent 22.3 1.252e+01 9.7790

parent 4.6 8.834e-01 3.7166

7 4.6 8.834e-01 3.7166 parent

14 parent 2.6 8.532e-03 2.5915 14 parent 1.2 8.532e-03 1.1915

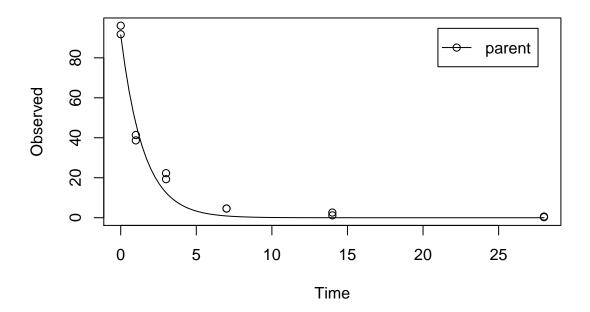
```
28 parent 0.3 7.958e-07 0.3000
28 parent 0.6 7.958e-07 0.6000
```

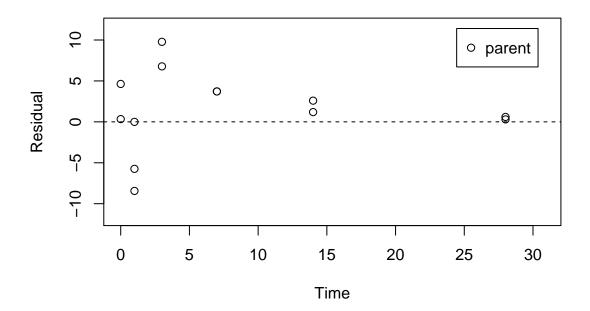
The χ^2 error level of 14% suggests that the model does not fit very well. This is also obvious from the plots of the fit and the residuals.

```
R > par(mfrow = c(2, 1))
```

R> plot(m.L2.SF0)

R> mkinresplot(m.L2.SF0)





In the FOCUS kinetics report, it is stated that there is no apparent systematic error observed from the residual plot up to the measured DT90 (approximately at day 5), and

there is an underestimation beyond that point.

We may add that it is difficult to judge the random nature of the residuals just from the three samplings at days 0, 1 and 3. Also, it is not clear *a priori* why a consistent underestimation after the approximate DT90 should be irrelevant. However, this can be rationalised by the fact that the FOCUS fate models generally only implement SFO kinetics.

For comparison, the FOMC model is fitted as well, and the χ^2 error level is checked.

```
R> m.L2.FOMC <- mkinfit(FOMC, FOCUS_2006_L2_mkin, quiet = TRUE)</pre>
R > par(mfrow = c(2, 1))
R> plot(m.L2.FOMC)
R> mkinresplot(m.L2.FOMC)
R> summary(m.L2.FOMC, data = FALSE)
mkin version:
               0.9.23
R version:
               3.0.1
              Wed Nov 6 08:28:46 2013
Date of fit:
Date of summary: Wed Nov 6 08:28:46 2013
Equations:
[1] d_parent = -(alpha/beta) * ((time/beta) + 1)^{-1} * parent
Method used for solution of differential equation system:
analytical
Weighting: none
Starting values for optimised parameters:
       value type transformed
parent_0 100 state 100.000000
alpha
           1 deparm 0.000000
          10 deparm 2.302585
beta
Fixed parameter values:
None
Optimised, transformed parameters:
       Estimate Std. Error Lower Upper
parent 0 93.7700 1.8560 89.5700 97.9700
        0.3180
                   0.1867 -0.1044 0.7405
alpha
          0.2102
                    0.2943 -0.4556 0.8759
beta
Backtransformed parameters:
    Estimate Lower Upper
parent_0 93.770 89.5700 97.970
alpha 1.374 0.9009 2.097
beta
          1.234 0.6341 2.401
```

Residual standard error: 2.628 on 9 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df

All data 6.205 3 3 parent 6.205 3 3

Estimated disappearance times:

DT50 DT90

parent 0.8092 5.356

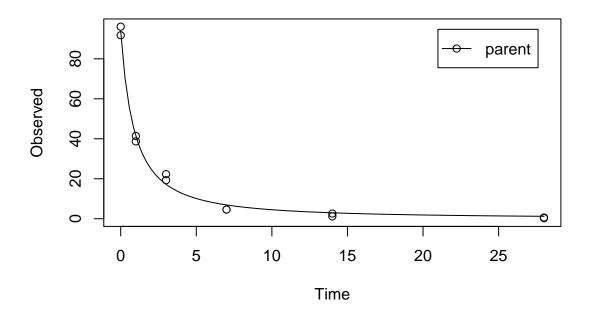
Estimated formation fractions:

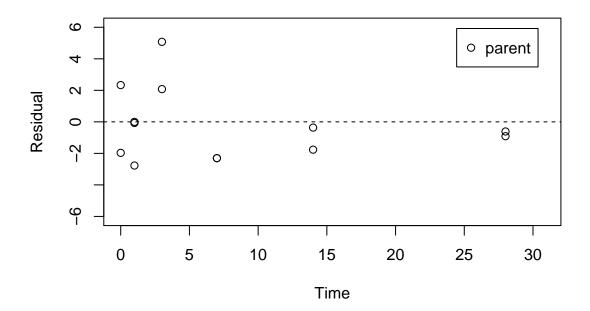
ff

parent_sink 1

Parameter correlation:

parent_0 alpha beta parent_0 1.00000 -0.09553 -0.1863 alpha -0.09553 1.00000 0.9757 beta -0.18628 0.97568 1.0000

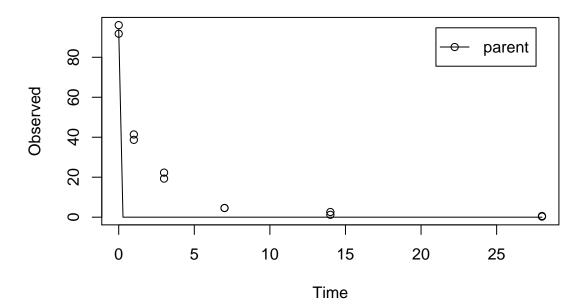




The error level at which the χ^2 test passes is much lower in this case. Therefore, the FOMC model provides a better description of the data, as less experimental error has to

be assumed in order to explain the data.

Fitting the four parameter DFOP model further reduces the χ^2 error level.



Here, the default starting parameters for the DFOP model obviously do not lead to a reasonable solution. Therefore the fit is repeated with different starting parameters.

Equations:

[1] $d_{parent} = -((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 * time)) / (g * exp(-k2 * time$

Method used for solution of differential equation system:

analytical

Weighting: none

Starting values for optimised parameters:

 value
 type
 transformed

 parent_0
 1e+02
 state
 100.0000000

 k1
 1e+00
 deparm
 0.0000000

 k2
 1e-02
 deparm
 -4.6051702

 g
 8e-01
 deparm
 0.9802581

Fixed parameter values:

None

Optimised, transformed parameters:

Backtransformed parameters:

Estimate Lower Upper parent_0 93.9500 NA NA k1 142.4000 NA NA k2 0.3369 NA NA q 0.4016 NA NA

Residual standard error: 1.732 on 8 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df All data 2.53 4 2

All data 2.53 4 2 parent 2.53 4 2

Estimated disappearance times:

DT50 DT90

parent NA NA

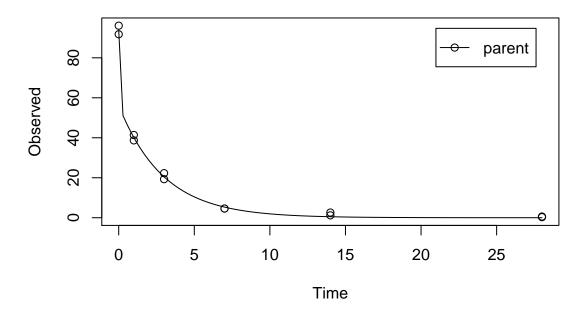
Estimated formation fractions:

ff

parent_sink 1

Parameter correlation:

Could not estimate covariance matrix; singular system:



Here, the DFOP model is clearly the best-fit model for dataset L2 based on the χ^2 error level criterion. However, the failure to calculate the covariance matrix indicates that the parameter estimates correlate excessively. Therefore, the FOMC model may be preferred for this dataset.

1.3 Laboratory Data L3

The following code defines example dataset L3 from the FOCUS kinetics report, p. 290.

Date of summary: Wed Nov 6 08:28:47 2013

Equations:

[1] d_parent = - k_parent_sink * parent

Method used for solution of differential equation system: analytical

Weighting: none

Starting values for optimised parameters:

Fixed parameter values:

None

Optimised, transformed parameters:

Estimate Std. Error Lower Upper parent_0 74.870 8.4580 54.180 95.57 k_parent_sink -3.678 0.3261 -4.476 -2.88

Backtransformed parameters:

Estimate Lower Upper parent_0 74.87000 54.18000 95.57000 k_parent_sink 0.02527 0.01138 0.05612

Residual standard error: 12.91 on 6 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df All data 21.24 2 6 parent 21.24 2 6

Estimated disappearance times:

DT50 DT90 parent 27.43 91.12

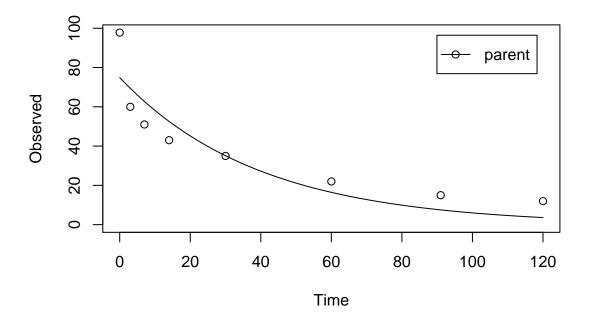
Estimated formation fractions:

 $\begin{array}{cc} & \textit{ff} \\ \textit{parent_sink} & 1 \\ \end{array}$

Parameter correlation:

Data:

```
time variable observed predicted
                                     residual
                   97.8
                            74.873
   0
       parent
                                     22.92734
   3
       parent
                   60.0
                            69.407
                                     -9.40654
   7
                   51.0
                            62.734 -11.73403
       parent
  14
       parent
                   43.0
                            52.563
                                     -9.56336
  30
                   35.0
                            35.083
                                     -0.08281
       parent
                   22.0
                            16.439
                                      5.56137
  60
       parent
  91
       parent
                   15.0
                             7.510
                                      7.48961
                   12.0
 120
                             3.609
                                      8.39083
       parent
```



The χ^2 error level of 22% as well as the plot suggest that the model does not fit very well. The FOMC model performs better:

```
R> m.L3.FOMC <- mkinfit(FOMC, FOCUS_2006_L3_mkin, quiet = TRUE)
R> plot(m.L3.FOMC)
R> summary(m.L3.FOMC, data = FALSE)
```

mkin version: 0.9.23
R version: 3.0.1

Date of fit: Wed Nov 6 08:28:47 2013
Date of summary: Wed Nov 6 08:28:47 2013

Equations:

[1] $d_parent = -(alpha/beta) * ((time/beta) + 1)^{-1} * parent$

Method used for solution of differential equation system: analytical

Weighting: none

Starting values for optimised parameters:

 value
 type
 transformed

 parent_0
 100
 state
 100.000000

 alpha
 1
 deparm
 0.000000

 beta
 10
 deparm
 2.302585

Fixed parameter values:

None

Optimised, transformed parameters:

 Estimate Std. Error Lower Upper

 parent_0
 96.9700
 4.5500
 85.2800
 108.7000

 alpha
 -0.8619
 0.1704
 -1.3000
 -0.4237

 beta
 0.6193
 0.4744
 -0.6003
 1.8390

Backtransformed parameters:

Estimate Lower Upper parent_0 96.9700 85.2800 108.7000 alpha 0.4224 0.2725 0.6546 beta 1.8580 0.5487 6.2890

Residual standard error: 4.572 on 5 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df
All data 7.32 3 5
parent 7.32 3 5

Estimated disappearance times:

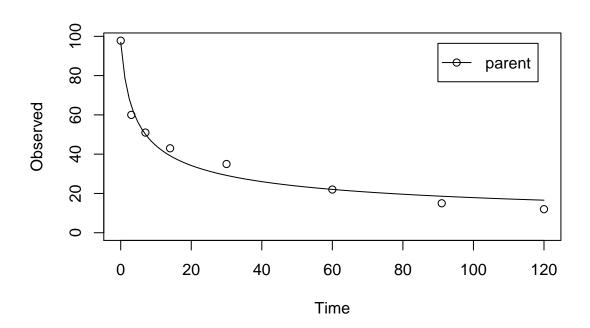
DT50 DT90 parent 7.729 431.2

Estimated formation fractions:

ff parent_sink 1

Parameter correlation:

parent_0 alpha beta parent_0 1.0000 -0.1512 -0.4271 alpha -0.1512 1.0000 0.9110 beta -0.4271 0.9110 1.0000



The error level at which the χ^2 test passes is 7% in this case.

Fitting the four parameter DFOP model further reduces the χ^2 error level considerably:

```
R> m.L3.DFOP <- mkinfit(DFOP, FOCUS_2006_L3_mkin, quiet = TRUE)
R> plot(m.L3.DFOP)
```

R> summary(m.L3.DFOP, data = FALSE)

mkin version: 0.9.23
R version: 3.0.1

Date of fit: Wed Nov 6 08:28:47 2013
Date of summary: Wed Nov 6 08:28:47 2013

Equations:

```
[1] d_{parent} = -((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 * time)) / (g * exp(-k2 * time
```

 $\begin{tabular}{ll} \it Method used for solution of differential equation system: \\ \it analytical \\ \end{tabular}$

Weighting: none

Starting values for optimised parameters:

 g 5e-01 deparm 0.000000

Fixed parameter values: None

Optimised, transformed parameters:

Estimate Std. Error Lower Upper parent_0 97.7500 1.43800 93.7500 101.70000 k1 -0.6612 0.13340 -1.0310 -0.29100 k2 -4.2860 0.05902 -4.4500 -4.12200 g -0.1229 0.05121 -0.2651 0.01925

Backtransformed parameters:

Estimate Lower Upper parent_0 97.75000 93.75000 101.70000 k1 0.51620 0.35650 0.74750 k2 0.01376 0.01168 0.01621 g 0.45660 0.40730 0.50680

Residual standard error: 1.439 on 4 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df

All data 2.225 4 4 parent 2.225 4 4

Estimated disappearance times:

DT50 DT90

parent 7.464 123

Estimated formation fractions:

ff

parent_sink 1

Parameter correlation:

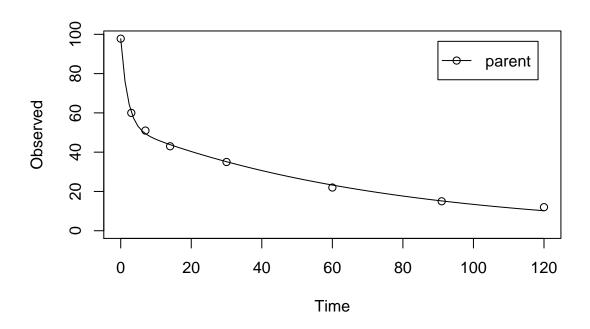
 parent_0
 k1
 k2
 g

 parent_0
 1.00000
 0.1640
 0.01315
 0.4253

 k1
 0.16399
 1.0000
 0.46477
 -0.5526

 k2
 0.01315
 0.4648
 1.00000
 -0.6631

 g
 0.42526
 -0.5526
 -0.66310
 1.0000



Here, a look to the model plot, the confidence intervals of the parameters and the correlation matrix suggest that the parameter estimates are reliable, and the DFOP model can be used as the best-fit model based on the χ^2 error level criterion for laboratory data L3.

1.4 Laboratory Data L4

The following code defines example dataset L4 from the FOCUS kinetics report, p. 293

mkin version: 0.9.23
R version: 3.0.1

Date of fit: Wed Nov 6 08:28:48 2013
Date of summary: Wed Nov 6 08:28:48 2013

Equations:

[1] d_parent = - k_parent_sink * parent

Method used for solution of differential equation system: analytical

Weighting: none

Starting values for optimised parameters:

value type transformed

Fixed parameter values:

None

Optimised, transformed parameters:

Estimate Std. Error Lower Upper

parent_0 96.44 1.94900 91.670 101.200 k_parent_sink -5.03 0.07999 -5.225 -4.834

Backtransformed parameters:

Estimate Lower Upper

parent_0 96.440000 91.670000 1.012e+02

k_parent_sink 0.006541 0.005378 7.955e-03

Residual standard error: 3.651 on 6 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df

All data 3.287 2 6 parent 3.287 2 6

Estimated disappearance times:

DT50 DT90

parent 106 352

Estimated formation fractions:

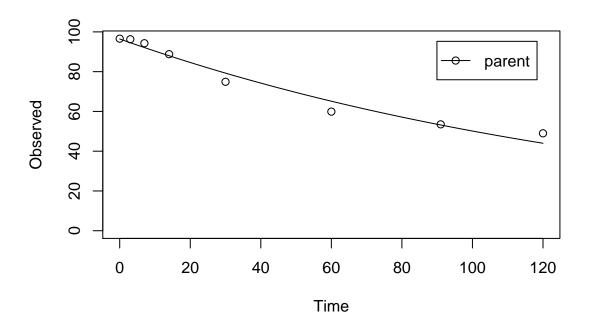
ff

parent_sink 1

Parameter correlation:

parent_0 k_parent_sink

parent_0 1.0000 0.5865 k_parent_sink 0.5865 1.0000



The χ^2 error level of 3.3% as well as the plot suggest that the model fits very well.

The FOMC model for comparison

```
R> m.L4.FOMC <- mkinfit(FOMC, FOCUS_2006_L4_mkin, quiet = TRUE)
R> plot(m.L4.FOMC)
```

R> summary(m.L4.FOMC, data = FALSE)

mkin version: 0.9.23
R version: 3.0.1

Date of fit: Wed Nov 6 08:28:48 2013
Date of summary: Wed Nov 6 08:28:48 2013

Equations:

[1] $d_{parent} = - (alpha/beta) * ((time/beta) + 1)^{-1} * parent$

Method used for solution of differential equation system: analytical

Weighting: none

Starting values for optimised parameters:

 value
 type
 transformed

 parent_0
 100
 state
 100.000000

 alpha
 1
 deparm
 0.000000

 beta
 10
 deparm
 2.302585

Fixed parameter values:

None

Optimised, transformed parameters:

 Estimate
 Std. Error
 Lower
 Upper

 parent_0
 99.1400
 1.6800
 94.820
 103.5000

 alpha
 -0.3506
 0.3725
 -1.308
 0.6068

 beta
 4.1740
 0.5635
 2.725
 5.6230

Backtransformed parameters:

Estimate Lower Upper parent_0 99.1400 94.8200 103.500 alpha 0.7042 0.2703 1.835 beta 64.9800 15.2600 276.600

Residual standard error: 2.315 on 5 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df
All data 2.029 3 5
parent 2.029 3 5

Estimated disappearance times:

DT50 DT90

parent 108.9 1644

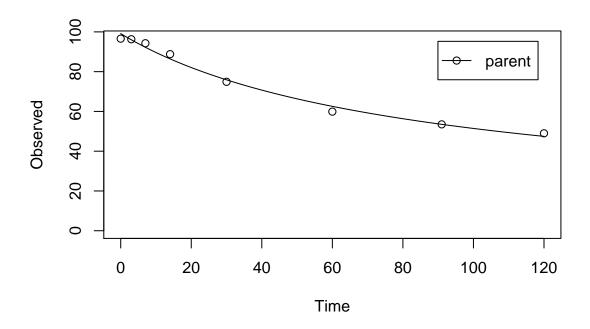
Estimated formation fractions:

ff

parent_sink 1

Parameter correlation:

parent_0 alpha beta parent_0 1.0000 -0.5365 -0.6083 alpha -0.5365 1.0000 0.9913 heta -0.6083 0.9913 1.0000



The error level at which the χ^2 test passes is slightly lower for the FOMC model. However, the difference appears negligible.

2 Kinetic evaluations for parent and metabolites

2.1 Laboratory Data for example compound Z

The following code defines the example dataset from Appendix 7 to the FOCUS kinetics report, p.350

```
+ Z3 = c(0, NA, NA, NA, NA, 0.5 * LOD, 9.2, 13.1, 22.3, 28.4, 32.5,

+ 25.2, 17.2, 4.8, 4.5, 2.8, 4.4))

R> FOCUS_2006_Z_mkin <- mkin_wide_to_long(FOCUS_2006_Z)
```

The next step is to set up the models used for the kinetic analysis. As the simultaneous fit of parent and the first metabolite is usually straightforward, Step 1 (SFO for parent only) is skipped here. We start with the model 2a, with formation and decline of metabolite Z1 and the pathway from parent directly to sink included (default in mkin).

```
R > Z.2a \leftarrow mkinmod(ZO = list(type = "SFO", to = "Z1"),
                  Z1 = list(type = "SFO"))
R> m.Z.2a <- mkinfit(Z.2a, FOCUS_2006_Z_mkin, quiet = TRUE)
R> plot(m.Z.2a)
R> summary(m.Z.2a, data = FALSE)
                 0.9.23
mkin version:
R version:
                 3.0.1
Date of fit:
               Wed Nov 6 08:28:49 2013
Date of summary: Wed Nov 6 08:28:49 2013
Equations:
[1] d_20 = -k_20_{sink} * 20 - k_20_{21} * 20
[2] d_Z1 = + k_Z0_Z1 * Z0 - k_Z1_sink * Z1
Method used for solution of differential equation system:
eigen
```

Weighting: none

Starting values for optimised parameters:

Fixed parameter values:

value type Z1_0 0 state

Optimised, transformed parameters:

	Estimate	Std.	Error	Lower	Upper
Z0_0	97.0100		NA	NA	NA
k_Z0_sink	-36.2900		NA	NA	NA
k_Z0_Z1	0.8047		NA	NA	NA
k_Z1_sink	-0.7296		NA	NA	NA

Backtransformed parameters:

Estimate Lower Upper

Z0_0	9.701e+01	NA	NA
k_Z0_sink	1.733e-16	NA	NA
k_Z0_Z1	2.236e+00	NA	NA
k_Z1_sink	4.821e-01	NA	NA

Residual standard error: 5.064 on 27 degrees of freedom

Chi2 error levels in percent:

		err.min	n.optim	df
A11	data	17.89	4	26
Z0		18.04	3	14
Z1		15.08	1	12

Estimated disappearance times:

DT50 DT90 Z0 0.310 1.030 Z1 1.438 4.776

Estimated formation fractions:

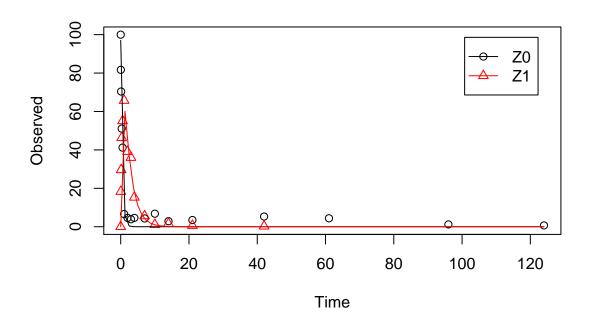
ff

Z0_sink 7.75e-17 Z0_Z1 1.00e+00

Z1_sink 1.00e+00

Parameter correlation:

Could not estimate covariance matrix; singular system:



As obvious from the summary, the kinetic rate constant from parent compound Z to sink is negligible. Accordingly, the exact magnitude of the fitted parameter log k_Z_sink is ill-defined and the covariance matrix is not returned. This suggests, in agreement with the analysis in the FOCUS kinetics report, to simplify the model by removing the pathway to sink.

A similar result can be obtained when formation fractions are used in the model formulation:

```
R > Z.2a.ff <- mkinmod(ZO = list(type = "SFO", to = "Z1"),
                  Z1 = list(type = "SFO"), use_of_ff = "max")
R> m.Z.2a.ff <- mkinfit(Z.2a.ff, FOCUS_2006_Z_mkin, quiet = TRUE)
R> plot(m.Z.2a.ff)
R> summary(m.Z.2a.ff, data = FALSE)
mkin version:
                 0.9.23
R version:
                 3.0.1
                 Wed Nov
                          6 08:28:49 2013
Date of fit:
Date of summary: Wed Nov
                          6 08:28:50 2013
Equations:
[1] d_Z0 = -k_Z0 * Z0
[2] d_Z1 = + f_Z0_to_Z1 * k_Z0 * Z0 - k_Z1 * Z1
```

Method used for solution of differential equation system: eigen

Weighting: none

Starting values for optimised parameters:

Fixed parameter values:

value type Z1_0 0 state

Optimised, transformed parameters:

Backtransformed parameters:

Residual standard error: 5.064 on 27 degrees of freedom

Chi2 error levels in percent:

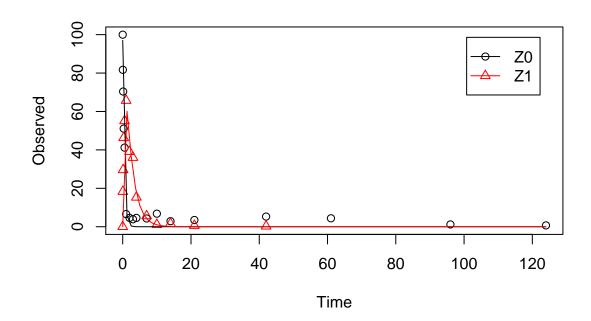
err.min n.optim df All data 17.89 4 26 Z0 17.56 2 15 Z1 15.59 2 11

Estimated disappearance times:

DT50 DT90 Z0 0.310 1.030 Z1 1.438 4.776

Parameter correlation:

Could not estimate covariance matrix; singular system:



Here, the ilr transformed formation fraction fitted in the model takes a very large value, and the backtransformed formation fraction from parent Z to Z1 is practically unity. Again, the covariance matrix is not returned as the model is overparameterised.

The simplified model is obtained by setting the list component sink to FALSE. This model definition is not supported when formation fractions are used.

```
R > Z.3 \leftarrow mkinmod(ZO = list(type = "SFO", to = "Z1", sink = FALSE),
                  Z1 = list(type = "SFO"))
R > m.Z.3 \leftarrow mkinfit(Z.3, FOCUS_2006_Z_mkin, parms.ini = c(k_Z0_Z1 = 0.5),
                   quiet = TRUE)
R> #m.Z.3 <- mkinfit(Z.3, FOCUS_2006_Z_mkin, solution_type = "deSolve")
R > plot(m.Z.3)
R> summary(m.Z.3, data = FALSE)
                 0.9.23
mkin version:
R version:
                 3.0.1
Date of fit:
                 Wed Nov
                           6 08:28:50 2013
Date of summary: Wed Nov
                           6 08:28:50 2013
Equations:
[1] d_{Z0} = -0 - k_{Z0}Z1 * Z0
[2] d_Z1 = + k_Z0_Z1 * Z0 - k_Z1_sink * Z1
```

Method used for solution of differential equation system: eigen

Weighting: none

Starting values for optimised parameters:

value type transformed

100.0000000 state 100.0000000 ZO 0

k_Z0_Z1 0.5000000 deparm -0.6931472

 k_{Z1} sink 0.1000004 deparm -2.3025810

Fixed parameter values:

value type

Z1 0 0 state

Optimised, transformed parameters:

Estimate Std. Error Lower Upper

 Z0_0
 97.0100
 2.68200
 91.5200
 102.5000

 k_Z0_Z1
 0.8047
 0.06568
 0.6702
 0.9392

k_Z1_sink -0.7296 0.08854 -0.9109 -0.5482

Backtransformed parameters:

Estimate Lower Upper

Z0_0 97.0100 91.5200 102.500

k_Z0_Z1 2.2360 1.9550 2.558

k_Z1_sink 0.4821 0.4022 0.578

Residual standard error: 4.973 on 28 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df

All data 17.61 3 27

Z0 17.56 2 15

15.08 1 12

Estimated disappearance times:

DT50 DT90

Z0 0.310 1.030

Z1 1.438 4.776

Estimated formation fractions:

ff

Z0_sink 1

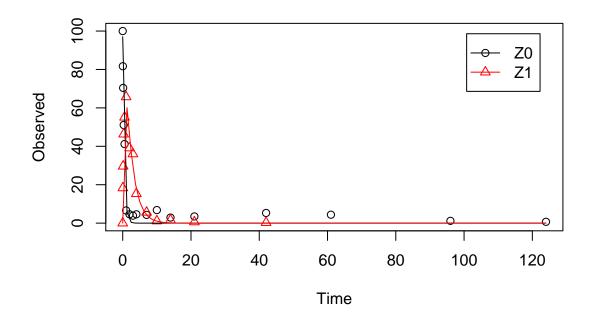
Z0_Z1 1

Z1_sink 1

Parameter correlation:

Z0_0 k_Z0_Z1 k_Z1_sink

ZO 0 1.0000 0.10629 0.41038



The first attempt to fit the model failed, as the default solution type chosen by mkinfit is based on eigenvalues, and the system defined by the starting parameters is identified as being singular to the solver. This is caused by the fact that the rate constants for both state variables are the same using the default starting parameters. Setting a different starting value for one of the parameters overcomes this. Alternatively, the **deSolve** based model solution can be chosen, at the cost of a bit more computing time.

```
R> Z.4a <- mkinmod(ZO = list(type = "SFO", to = "Z1", sink = FALSE),
+
                  Z1 = list(type = "SFO", to = "Z2"),
+
                  Z2 = list(type = "SFO"))
R > m.Z.4a < -mkinfit(Z.4a, FOCUS_2006_Z_mkin, parms.ini = c(k_Z0_Z1 = 0.5),
                    quiet = TRUE)
R> plot(m.Z.4a)
R> summary(m.Z.4a, data = FALSE)
                 0.9.23
mkin version:
R version:
                 3.0.1
Date of fit:
                 Wed Nov
                          6 08:28:51 2013
Date of summary: Wed Nov
                          6 08:28:51 2013
```

Equations:

```
[1] d_Z0 = -0 - k_Z0_Z1 * Z0
```

$$[2] d_Z1 = + k_Z0_Z1 * Z0 - k_Z1_sink * Z1 - k_Z1_Z2 * Z1$$

 $[3] d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2$

Method used for solution of differential equation system: eigen

Weighting: none

Starting values for optimised parameters:

k_Z2_sink 0.1000003 deparm -2.3025823

Fixed parameter values:

value type
Z1_0 0 state
Z2 0 0 state

Optimised, transformed parameters:

Backtransformed parameters:

Residual standard error: 4.54 on 39 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df
All data 19.31 5 37
Z0 17.47 2 15
Z1 15.71 2 11
Z2 19.54 1 11

Estimated disappearance times: DT50 DT90

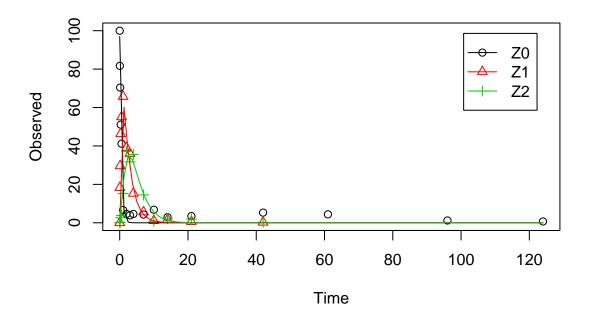
```
Z0 0.3124 1.038
Z1 1.4410 4.787
Z2 1.6072 5.339
```

Estimated formation fractions:

ff
Z0_sink 1.0000
Z0_Z1 1.0000
Z1_sink 0.0343
Z1_Z2 0.9657
Z2_sink 1.0000

Parameter correlation:

	Z0_0	k_Z0_Z1	k_Z1_sink	k_Z1_Z2	k_Z2_sink
Z0_0	1.0000	0.1064	0.3492	-0.1769	-0.1534
k_Z0_Z1	0.1064	1.0000	0.1479	-0.1501	-0.1226
k_Z1_sink	0.3492	0.1479	1.0000	-0.8745	-0.8656
k_Z1_Z2	-0.1769	-0.1501	-0.8745	1.0000	0.8190
k_Z2_sink	-0.1534	-0.1226	-0.8656	0.8190	1.0000



As suggested in the FOCUS report, the pathway to sink was removed for metabolite Z1 as well in the next step. While this step appears questionable on the basis of the above results, it is followed here for the purpose of comparison. Also, in the FOCUS report, it is assumed that there is additional empirical evidence that Z1 quickly and exclusively hydrolyses to Z2. Again, in order to avoid a singular system when using default starting

```
parameters, the starting parameter for the pathway without sink term has to be adapted.
```

```
R > Z.5 \leftarrow mkinmod(ZO = list(type = "SFO", to = "Z1", sink = FALSE),
                   Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
                  Z2 = list(type = "SFO"))
+
R> m.Z.5 <- mkinfit(Z.5, FOCUS_2006_Z_mkin,
                     parms.ini = c(k_{Z0}Z1 = 0.5, k_{Z1}Z2 = 0.2), quiet = TRUE)
R > plot(m.Z.5)
R> summary(m.Z.5, data = FALSE)
mkin version:
                 0.9.23
R version:
                 3.0.1
Date of fit:
                Wed Nov 6 08:28:52 2013
Date of summary: Wed Nov 6 08:28:52 2013
Equations:
[1] d_{Z0} = -0 - k_{Z0}Z1 * Z0
[2] d_Z1 = + k_Z0_Z1 * Z0 - 0 - k_Z1_Z2 * Z1
[3] d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2
Method used for solution of differential equation system:
eigen
```

Weighting: none

```
Starting values for optimised parameters:
```

Fixed parameter values:

value type $Z1_0$ 0 state $Z2_0$ 0 state

Optimised, transformed parameters:

Estimate Std. Error Lower Upper Z0_0 96.7700 2.26600 92.1900 101.3000 k_Z0_Z1 0.7948 0.05843 0.6767 0.9129 k_Z1_Z2 -0.7410 0.06821 -0.8789 -0.6032 k_Z2_sink -0.8027 0.11090 -1.0270 -0.5785

Backtransformed parameters:

Estimate Lower Upper Z0_0 96.7700 92.1900 101.3000 k_Z0_Z1 2.2140 1.9670 2.4920

Residual standard error: 4.486 on 40 degrees of freedom

Chi2 error levels in percent:

		err.min	n.optim	df
All	data	19.10	4	38
Z0		17.43	2	15
Z1		15.27	1	12
Z2		19.57	1	11

Estimated disappearance times:

DT50 DT90

Z0 0.3131 1.040

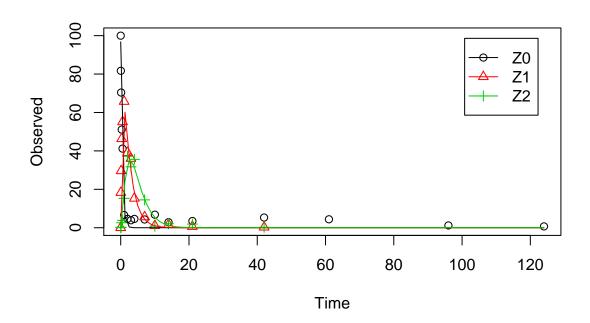
Z1 1.4543 4.831

Z2 1.5468 5.138

Estimated formation fractions:

Z2_sink 1

Parameter correlation:



Finally, metabolite Z3 is added to the model.

```
R> Z.FOCUS <- mkinmod(ZO = list(type = "SFO", to = "Z1", sink = FALSE),
+
                   Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
                   Z2 = list(type = "SFO", to = "Z3"),
+
                   Z3 = list(type = "SFO"))
R> m.Z.FOCUS <- mkinfit(Z.FOCUS, FOCUS_2006_Z_mkin,
+
                     parms.ini = c(k_20_21 = 0.5, k_21_22 = 0.2, k_22_3 = 0.3),
                     quiet = TRUE)
R> plot(m.Z.FOCUS)
R> summary(m.Z.FOCUS, data = FALSE)
                 0.9.23
mkin version:
R version:
                 3.0.1
                 Wed Nov
                          6 08:28:53 2013
Date of fit:
                          6 08:28:53 2013
Date of summary: Wed Nov
Equations:
[1] d_{Z0} = -0 - k_{Z0}Z1 * Z0
[2] d_{Z1} = + k_{Z0}Z1 * Z0 - 0 - k_{Z1}Z2 * Z1
[3] d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3 * Z2
[4] d_Z3 = + k_Z2_Z3 * Z2 - k_Z3_sink * Z3
```

Method used for solution of differential equation system:

eigen

Weighting: none

Starting values for optimised parameters:

	value	type	transformed
Z0_0	100.0000000	state	100.0000000
k_Z0_Z1	0.5000000	deparm	-0.6931472
k_Z1_Z2	0.2000000	deparm	-1.6094379
k_Z2_Z3	0.3000000	deparm	-1.2039728
k_Z2_sink	0.1000001	deparm	-2.3025843
k_Z3_sink	0.1000009	deparm	-2.3025758

Fixed parameter values:

 $\begin{array}{cccc} & value & type \\ Z1_0 & 0 & state \\ Z2_0 & 0 & state \\ Z3_0 & 0 & state \\ \end{array}$

Optimised, transformed parameters:

	Estimate	Std. Error	Lower	Upper
Z0_0	96.8400	2.05900	92.7100	101.0000
k_Z0_Z1	0.7954	0.05332	0.6884	0.9025
k_Z1_Z2	-0.7375	0.06123	-0.8604	-0.6146
k_Z2_Z3	-1.5470	0.12250	-1.7930	-1.3010
k_Z2_sink	-1.4330	0.17160	-1.7770	-1.0880
k Z3 sink	-2.8350	0.24360	-3.3240	-2.3470

Backtransformed parameters:

	Estimate	Lower	Upper
Z0_0	96.84000	92.71000	101.0000
k_Z0_Z1	2.21500	1.99100	2.4660
k_Z1_Z2	0.47830	0.42300	0.5409
k_Z2_Z3	0.21290	0.16650	0.2723
k_Z2_sink	0.23870	0.16910	0.3368
k_Z3_sink	0.05869	0.03599	0.0957

Residual standard error: 4.1 on 51 degrees of freedom

Chi2 error levels in percent:

		err.min	n.optim	df
All	data	19.23	6	48
Z0		17.45	2	15
Z1		15.24	1	12
Z2		20.32	2	10
Z3		11.89	1	11

Estimated disappearance times: DT50 DT90

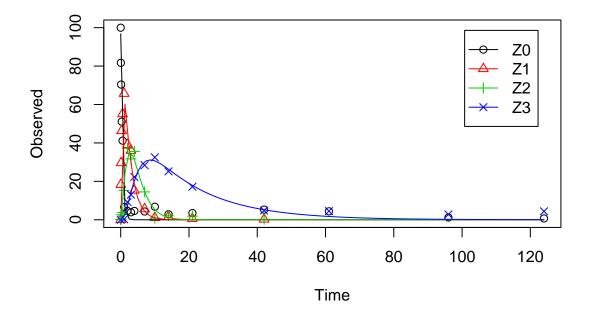
```
Z0  0.3129  1.039
Z1  1.4492  4.814
Z2  1.5348  5.099
Z3  11.8101  39.232
```

Estimated formation fractions:

ff
Z0_sink 1.0000
Z0_Z1 1.0000
Z1_sink 1.0000
Z1_Z2 1.0000
Z2_sink 0.5285
Z2_Z3 0.4715
Z3 sink 1.0000

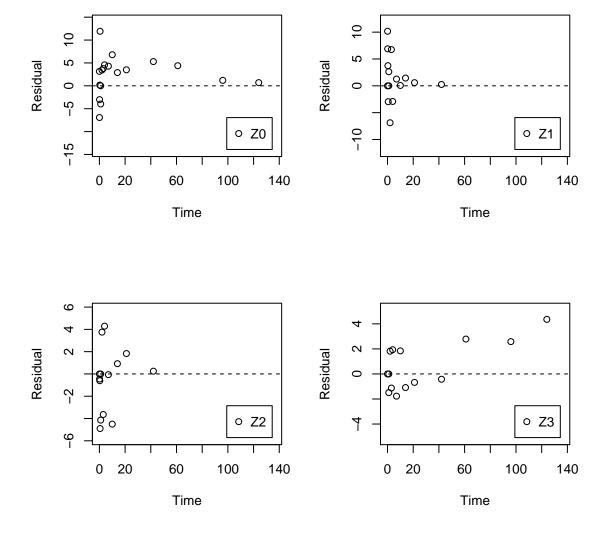
Parameter correlation:

 $Z0_0$ k_Z0_Z1 k_Z1_Z2 k_Z2_Z3 k_Z2_sink k_Z3_sink Z0_0 1.00000 0.05387 0.2727 -0.07296 0.37006 -0.11348k_Z0_Z1 0.05387 1.00000 -0.0521 -0.03581 0.02442 -0.02521 k_Z1_Z2 0.27275 -0.05210 1.0000 -0.12132 0.29384 -0.19144k_Z2_Z3 -0.07296 -0.03581 -0.1213 1.00000 -0.18887 0.55155 k_Z2_sink 0.37006 0.02442 0.2938 -0.18887 1.00000 -0.64293 k_Z3_sink -0.11348 -0.02521 -0.1914 0.55155 -0.64293 1.00000



This is the fit corresponding to the final result chosen in Appendix 7 of the FOCUS report. The residual plots can be obtained by

```
R> par(mfrow = c(2, 2))
R> mkinresplot(m.Z.FOCUS, "ZO", lpos = "bottomright")
R> mkinresplot(m.Z.FOCUS, "Z1", lpos = "bottomright")
R> mkinresplot(m.Z.FOCUS, "Z2", lpos = "bottomright")
R> mkinresplot(m.Z.FOCUS, "Z3", lpos = "bottomright")
```



As the FOCUS report states, there is a certain tailing of the time course of metabolite Z3. Also, the time course of the parent compound is not fitted very well using the SFO model, as residues at a certain low level remain.

Therefore, an additional model is offered here, using the single first-order reversible binding (SFORB) model for metabolite Z3. As expected, the χ^2 error level is lower for metabolite Z3 using this model and the graphical fit for Z3 is improved. However, the covariance matrix is not returned.

```
R> Z.mkin.1 <- mkinmod(ZO = list(type = "SFO", to = "Z1", sink = FALSE),
                                                       Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
                                                        Z2 = list(type = "SFO", to = "Z3"),
                                                        Z3 = list(type = "SFORB"))
R> m.Z.mkin.1 <- mkinfit(Z.mkin.1, FOCUS_2006_Z_mkin,
                                                              parms.ini = c(k_Z0_Z1 = 0.5, k_Z1_Z2 = 0.3),
+
                                                              quiet = TRUE)
R> plot(m.Z.mkin.1)
R> summary(m.Z.mkin.1, data = FALSE)
                                                  0.9.23
mkin version:
R version:
                                                   3.0.1
Date of fit:
                                                  Wed Nov 6 08:29:00 2013
Date of summary: Wed Nov 6 08:29:00 2013
Equations:
[1] d_Z0 = -0 - k_Z0_Z1 * Z0
[2] d_{Z1} = + k_{Z0}Z1 * Z0 - 0 - k_{Z1}Z2 * Z1
[4] \ d_Z3\_free = + \ k_Z2\_Z3\_free * Z2 - k_Z3\_free\_sink * Z3\_free - k_Z3\_free\_bound * Z3\_free\_sink * Z3\_free\_bound * Z3\_free\_sink * Z3\_free\_bound * Z3\_free\_sink * Z3\_free\_bound * Z3\_free\_sink * Z3\_f
[5] d_Z3_bound = + k_Z3_free_bound * Z3_free - k_Z3_bound_free * Z3_bound
Method used for solution of differential equation system:
eigen
Weighting: none
Starting values for optimised parameters:
                                                                 value type transformed
Z0_0
                                               100.0000000 state 100.0000000
k Z0 Z1
                                                   0.5000000 deparm -0.6931472
k_Z1_Z2
                                                     0.3000000 deparm -1.2039728
k_Z2_sink
                                                     0.1000010 deparm -2.3025755
```

Fixed parameter values:

k_Z2_Z3_free

```
value type
Z1_0 0 state
Z2_0 0 state
```

0.1000003 deparm -2.3025819

 $k_Z3_free_sink$ 0.1000008 deparm -2.3025767 $k_Z3_free_bound$ 0.1000000 deparm -2.3025851 $k_Z3_bound_free$ 0.0200000 deparm -3.9120230

Optimised, transformed parameters:

	Estimate	Std.	Error	Lower	Upper
ZO_0	96.7400		NA	NA	NA
k_Z0_Z1	0.7947		NA	NA	NA
k_Z1_Z2	-0.7426		NA	NA	NA
k_Z2_sink	-1.4950		NA	NA	NA
k_Z2_Z3_free	-1.5040		NA	NA	NA
k_Z3_free_sink	-2.6540		NA	NA	NA
$k_Z3_free_bound$	-5.2440		NA	NA	NA
$k_Z3_bound_free$	-27.3300		NA	NA	NA

Backtransformed parameters:

	Estimate	Lower	Upper
ZO_0	9.674e+01	NA	NA
k_Z0_Z1	2.214e+00	NA	NA
k_Z1_Z2	4.759e-01	NA	NA
k_Z2_sink	2.243e-01	NA	NA
k_Z2_Z3_free	2.222e-01	NA	NA
k_Z3_free_sink	7.034e-02	NA	NA
$k_Z3_free_bound$	5.279e-03	NA	NA
k_Z3_bound_free	1.345e-12	NA	NA

Residual standard error: 4.107 on 49 degrees of freedom

Chi2 error levels in percent:

		err.min	n.optim	df
All	data	19.230	8	46
Z0		17.429	2	15
Z1		15.275	1	12
Z2		20.279	2	10
Z3		8.222	3	9

Estimated disappearance times:

DT50 DT90

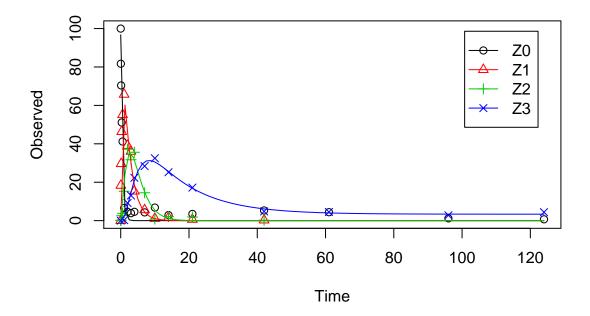
Z0 0.3131 1.040

Z1 1.4566 4.839

Z2 1.5523 5.157

Z3 10.1978 45.329

Estimated formation fractions:



Therefore, a further stepwise model building is performed starting from the stage of parent and one metabolite, starting from the assumption that the model fit for the parent compound can be improved by using the SFORB model.

Equations:

- $[1] \ d_Z0_free = -\ 0 \ -\ k_Z0_free_bound \ *\ Z0_free \ +\ k_Z0_bound_free \ *\ Z0_bound \ -\ k_Z0_free_bound \ -\ k_Z0_free_bound$
- [2] $d_Z0_bound = + k_Z0_free_bound * Z0_free k_Z0_bound_free * Z0_bound$
- [3] $d_Z1 = + k_Z0_free_Z1 * Z0_free k_Z1_sink * Z1$

Method used for solution of differential equation system: eigen

Weighting: none

Starting values for optimised parameters:

Fixed parameter values:

Optimised, transformed parameters:

Backtransformed parameters:

Residual standard error: 4.438 on 26 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df All data 15.63 5 25 Z0 14.74 4 13 Z1 14.31 1 12

Estimated disappearance times: DT50 DT90

```
Z0 0.302 1.190
Z1 1.532 5.091
```

Estimated formation fractions:

 ### Contraction
 ### Contraction

 ### Zong free _ Zink
 1

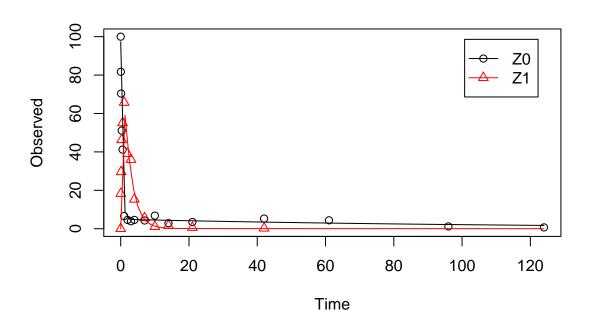
 ### Zing ink
 1

Estimated Eigenvalues of SFORB model(s):

Z0_b1 Z0_b2 2.476314 0.008461

Parameter correlation:

	Z0_free_0 k_	Z0_free_bound	k_Z0_bound_free
Z0_free_0	1.000000	0.006494	0.03324
$k_Z0_free_bound$	0.006494	1.000000	0.54647
$k_Z0_bound_free$	0.033238	0.546465	1.00000
k_Z0_free_Z1	0.111819	0.413926	0.15837
k_Z1_sink	0.391553	-0.291911	-0.12597
	k_Z0_free_Z1	k_Z1_sink	
Z0_free_0	0.11182	0.39155	
$k_Z0_free_bound$	0.41393	-0.29191	
$k_Z0_bound_free$	0.15837	-0.12597	
k_Z0_free_Z1	1.00000	-0.04188	
k_Z1_sink	-0.04188	1.00000	



When metabolite Z2 is added, the additional sink for Z1 is turned off again, for the same reasons as in the original analysis.

```
R> Z.mkin.3 <- mkinmod(ZO = list(type = "SFORB", to = "Z1", sink = FALSE),
                  Z1 = list(type = "SFO", to = "Z2"),
+
                  Z2 = list(type = "SFO"))
R> m.Z.mkin.3 <- mkinfit(Z.mkin.3, FOCUS_2006_Z_mkin, quiet = TRUE)
R> plot(m.Z.mkin.3)
R> summary(m.Z.mkin.3, data = FALSE)
mkin version:
                 0.9.23
                 3.0.1
R version:
Date of fit:
                 Wed Nov
                          6 08:29:04 2013
Date of summary: Wed Nov
                          6 08:29:04 2013
```

Equations:

```
[1] d_20_free = -0 - k_20_free_bound * Z0_free + k_20_bound_free * Z0_bound - k_20_free_bound * Z0_free - k_20_bound_free * Z0_bound = + k_20_free_bound * Z0_free - k_20_bound_free * Z0_bound = + k_20_free_Z1 * Z0_free - k_21_sink * Z1 - k_21_Z2 * Z1  
[4] <math>d_22 = + k_21_22 * Z1 - k_22_sink * Z2
```

Method used for solution of differential equation system: eigen

Weighting: none

Starting values for optimised parameters:

	value	type	transformed
Z0_free_0	100.0000000	state	100.000000
$k_Z0_free_bound$	0.1000000	deparm	-2.302585
$k_Z0_bound_free$	0.0200000	deparm	-3.912023
k_Z0_free_Z1	0.1000009	deparm	-2.302576
k_Z1_sink	0.1000003	deparm	-2.302582
k_Z1_Z2	0.1000006	deparm	-2.302579
k_Z2_sink	0.1000004	deparm	-2.302581

Fixed parameter values:

 $\begin{array}{cccc} & value & type \\ Z0_bound_0 & 0 & state \\ Z1_0 & 0 & state \\ Z2_0 & 0 & state \\ \end{array}$

Optimised, transformed parameters:

	Estimate	Std. Error	Lower	Upper
Z0_free_0	97.4400	2.312e+00	9.275e+01	1.021e+02
$k_Z0_free_bound$	-2.1490	4.126e-01	-2.985e+00	-1.313e+00
$k_Z0_bound_free$	-4.8380	1.637e+00	-8.155e+00	-1.521e+00
k_Z0_free_Z1	0.8457	5.956e-02	7.250e-01	9.664e-01
k_Z1_sink	-17.6300	2.506e+06	-5.078e+06	5.078e+06
k_Z1_Z2	-0.7812	1.059e-01	-9.957e-01	-5.667e-01
k_Z2_sink	-0.8606	1.707e-01	-1.206e+00	-5.149e-01

Backtransformed parameters:

	Estimate	Lower	Upper
Z0_free_0	9.744e+01	9.275e+01	102.1000
$k_Z0_free_bound$	1.166e-01	5.055e-02	0.2691
$k_Z0_bound_free$	7.920e-03	2.872e-04	0.2184
k_Z0_free_Z1	2.330e+00	2.065e+00	2.6280
k_Z1_sink	2.200e-08	0.000e+00	Inf
k_Z1_Z2	4.579e-01	3.695e-01	0.5674
k_Z2_sink	4.229e-01	2.993e-01	0.5976

Residual standard error: 4.136 on 37 degrees of freedom

Chi2 error levels in percent:

err.min n.optim df
All data 17.54 7 35
Z0 14.67 4 13
Z1 14.90 2 11
Z2 20.29 1 11

Estimated disappearance times:

DT50 DT90 Z0 0.3043 1.185

Z1 1.5138 5.029Z2 1.6391 5.445

Estimated formation fractions:

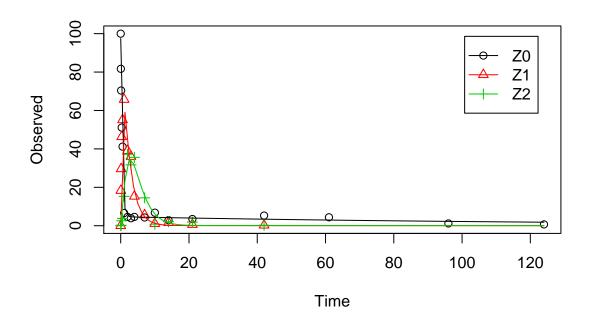
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${\it Estimated \ Eigenvalues \ of \ SFORB \ model(s):}$

Z0_b1 Z0_b2 2.446638 0.007542

Parameter correlation:

	Z0_free_0 k	Z0_free_bound	k_Z0_bound_free
Z0_free_0	1.00000	0.01518	0.033545
k_Z0_free_bound	0.01518	1.00000	0.545959
k_Z0_bound_free	0.03354	0.54596	1.000000
k_Z0_free_Z1	0.13432	0.40225	0.152314
k_Z1_sink	0.41954	-0.12487	-0.072828
k_Z1_Z2	-0.18395	-0.04229	0.003678
k_Z2_sink	-0.16196	-0.03394	0.007076
	$k_Z0_free_Z1$	k_Z1_sink	k_Z1_Z2
Z0_free_0	0.1343	0.41954 -0	.183953 -0.161962
k_Z0_free_bound	0.4022	-0.12487 -0	.042291 -0.033937
$k_Z0_bound_free$	0.1523	-0.07283 0	.003678 0.007076
k_Z0_free_Z1	1.0000	0.12526 -0	.160310 -0.128025
k_Z1_sink	0.1253	1.00000 -0	.783932 -0.778334
k_Z1_Z2	-0.1603	-0.78393 1	.000000 0.716491
k_Z2_sink	-0.1280	-0.77833 0	.716491 1.000000



This results in a much better representation of the behaviour of the parent compound Z0.

Finally, Z3 is added as well. This model appears overparameterised (no covariance matrix returned) if the sink for Z1 is left in the model.

```
R> Z.mkin.4 <- mkinmod(ZO = list(type = "SFORB", to = "Z1", sink = FALSE),
                                                                   Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
                                                                    Z2 = list(type = "SFO", to = "Z3"),
                                                                   Z3 = list(type = "SFO"))
R> m.Z.mkin.4 <- mkinfit(Z.mkin.4, FOCUS_2006_Z_mkin,
              parms.ini = c(k_Z1_Z2 = 0.05), quiet = TRUE)
R> plot(m.Z.mkin.4)
R> summary(m.Z.mkin.4, data = FALSE)
                                                              0.9.23
mkin version:
R version:
                                                               3.0.1
                                                                                                6 08:29:09 2013
Date of fit:
                                                              Wed Nov
Date of summary: Wed Nov
                                                                                                6 08:29:09 2013
Equations:
[1] d_20_free = -0 - k_20_free_bound * 20_free + k_20_bound_free * 20_bound - k_20_free_bound + k_20
[2] d_Z0_bound = + k_Z0_free_bound * Z0_free - k_Z0_bound_free * Z0_bound
[3] d_Z1 = + k_Z0_free_Z1 * Z0_free - 0 - k_Z1_Z2 * Z1
[4] d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3 * Z2
```

```
[5] d_Z3 = + k_Z2_Z3 * Z2 - k_Z3_sink * Z3
```

Method used for solution of differential equation system: eigen

Weighting: none

Starting values for optimised parameters:

	value	type	transformed
Z0_free_0	100.0000000	state	100.000000
k_Z1_Z2	0.0500000	deparm	-2.995732
$k_Z0_free_bound$	0.1000000	deparm	-2.302585
$k_Z0_bound_free$	0.0200000	deparm	-3.912023
k_Z0_free_Z1	0.1000002	deparm	-2.302583
k_Z2_sink	0.1000007	deparm	-2.302579
k_Z2_Z3	0.1000006	deparm	-2.302579
k_Z3_sink	0.1000003	deparm	-2.302582

Fixed parameter values:

	value	type
Z0_bound_0	0	state
Z1_0	0	state
Z2_0	0	state
Z3_0	0	state

Optimised, transformed parameters:

	Estimate	Std. Error	Lower	Upper
Z0_free_0	97.5300	1.88700	93.7400	101.3000
k_Z1_Z2	-0.7769	0.05834	-0.8942	-0.6597
$k_Z0_free_bound$	-2.1360	0.36810	-2.8760	-1.3960
$k_Z0_bound_free$	-4.7650	1.41700	-7.6130	-1.9170
k_Z0_free_Z1	0.8470	0.05339	0.7398	0.9543
k_Z2_sink	-1.5610	0.18260	-1.9280	-1.1940
k_Z2_Z3	-1.5280	0.11350	-1.7560	-1.2990
k_Z3_sink	-2.7690	0.22460	-3.2200	-2.3180

Backtransformed parameters:

	Estimate	Lower	Upper
Z0_free_0	97.53000	9.374e+01	101.3000
k_Z1_Z2	0.45980	4.089e-01	0.5170
$k_Z0_free_bound$	0.11810	5.636e-02	0.2475
$k_Z0_bound_free$	0.00852	4.938e-04	0.1470
k_Z0_free_Z1	2.33300	2.095e+00	2.5970
k_Z2_sink	0.20990	1.455e-01	0.3030
k_Z2_Z3	0.21700	1.728e-01	0.2727
k_Z3_sink	0.06272	3.994e-02	0.0985

Residual standard error: 3.737 on 49 degrees of freedom

```
Chi2 error levels in percent:
```

err.min n.optim df
All data 17.50 8 46
Z0 14.69 4 13
Z1 14.39 1 12
Z2 21.05 2 10
Z3 11.76 1 11

Estimated disappearance times:

DT50 DT90

Z0 0.304 1.186

Z1 1.507 5.008

Z2 1.623 5.393

Z3 11.051 36.712

Estimated formation fractions:

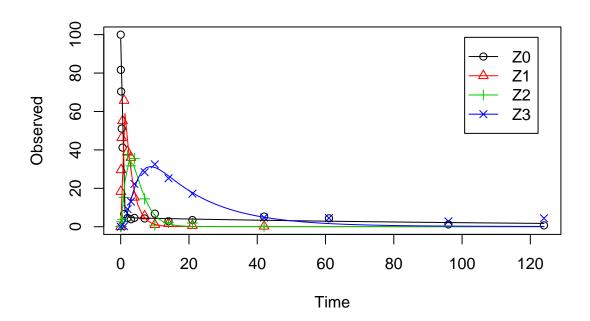
ff
Z0_free_sink 1.0000
Z0_free_Z1 1.0000
Z1_sink 1.0000
Z1_Z2 1.0000
Z2_sink 0.4917
Z2_Z3 0.5083
Z3_sink 1.0000

Estimated Eigenvalues of SFORB model(s):

Z0_b1 Z0_b2 2.451259 0.008108

Parameter correlation:

	Z0_free_0 }	k_ <i>Z1</i> _ <i>Z2</i> k_ <i>Z</i>	0_free_bou	and k_{20} bo	ound_free
Z0_free_0	1.00000	0.24238	0.078	323	0.06921
k_Z1_Z2	0.24238	1.00000	-0.227	42	-0.08934
k_Z0_free_bound	0.07823 -0	0.22742	1.000	000	0.53976
$k_Z0_bound_free$	0.06921 -0	0.08934	0.539	76	1.00000
k_Z0_free_Z1	0.08883 -0	0.10841	0.427	66	0.16281
k_Z2_sink	0.32993	0.34052	-0.263	31	-0.12743
k_Z2_Z3	-0.07494 -0	0.14885	0.066	598	0.06082
k_Z3_sink	-0.10456 -0	0.22486	0.138	845	0.12526
	k_Z0_free_Z	1 k_Z2_sink	k_Z2_Z3	k_Z3_sink	
Z0_free_0	0.08883	3 0.3299	-0.07494	-0.10456	
k_Z1_Z2	-0.10842	1 0.3405	-0.14885	-0.22486	
k_Z0_free_bound	0.4276	6 -0.2633	0.06698	0.13845	
$k_Z0_bound_free$	0.16283	1 -0.1274	0.06082	0.12526	
k_Z0_free_Z1	1.00000	0 -0.0531	-0.01281	0.01858	
k_Z2_sink	-0.05310	1.0000	-0.25473	-0.68321	
k_Z2_Z3	-0.01282	1 -0.2547	1.00000	0.56390	
k_Z3_sink	0.01858	8 -0.6832	0.56390	1.00000	



The error level of the fit, but especially of metabolite Z3, can be improved if the SFORB model is chosen for this metabolite, as this model is capable of representing the tailing of the metabolite decline phase.

Using the SFORB additionally for Z1 or Z2 did not further improve the result.

```
R> Z.mkin.5 <- mkinmod(ZO = list(type = "SFORB", to = "Z1", sink = FALSE),
                                                                       Z1 = list(type = "SFO", to = "Z2", sink = FALSE),
+
                                                                       Z2 = list(type = "SFO", to = "Z3"),
+
                                                                       Z3 = list(type = "SFORB"))
R> m.Z.mkin.5 <- mkinfit(Z.mkin.5, FOCUS_2006_Z_mkin,
               parms.ini = c(k_Z1_Z2 = 0.2), quiet = TRUE)
R> plot(m.Z.mkin.5)
R> summary(m.Z.mkin.5, data = FALSE)
mkin version:
                                                                  0.9.23
                                                                  3.0.1
R version:
                                                                  Wed Nov
Date of fit:
                                                                                                     6 08:29:26 2013
Date of summary: Wed Nov
                                                                                                     6 08:29:26 2013
Equations:
[1] d_20_free = -0 - k_20_free_bound * Z0_free + k_20_bound_free * Z0_bound - k_20_free_bound + k_20
[2] d_Z0_bound = + k_Z0_free_bound * Z0_free - k_Z0_bound_free * Z0_bound
[3] d_Z1 = + k_Z0_free_Z1 * Z0_free - 0 - k_Z1_Z2 * Z1
```

```
[4] d_Z2 = + k_Z1_Z2 * Z1 - k_Z2_sink * Z2 - k_Z2_Z3_free * Z2
```

[5] $d_Z3_free = + k_Z2_Z3_free * Z2 - k_Z3_free_sink * Z3_free - k_Z3_free_bound * Z3_free_sink * Z3_free_bound * Z3_free_sink * Z3_free_bound * Z3_free_sink * Z3_free_bound * Z3_free_sink * Z3_free_bound * Z3_free_b$

[6] $d_Z3_bound = + k_Z3_free_bound * Z3_free - k_Z3_bound_free * Z3_bound$

Method used for solution of differential equation system: eigen

Weighting: none

Starting values for optimised parameters:

	value	type	transformed
Z0_free_0	100.0000000	state	100.000000
k_Z1_Z2	0.2000000	deparm	-1.609438
$k_Z0_free_bound$	0.1000000	deparm	-2.302585
$k_Z0_bound_free$	0.0200000	deparm	-3.912023
k_Z0_free_Z1	0.1000002	deparm	-2.302583
k_Z2_sink	0.1000008	deparm	-2.302577
k_Z2_Z3_free	0.1000000	deparm	-2.302585
k_Z3_free_sink	0.1000006	deparm	-2.302579
$k_Z3_free_bound$	0.1000000	deparm	-2.302585
k_Z3_bound_free	0.0200000	deparm	-3.912023

Fixed parameter values:

	value	type
Z0_bound_0	0	state
Z1_0	0	state
Z2_0	0	state
<i>Z3_free_0</i>	0	state
Z3 bound 0	0	state

Optimised, transformed parameters:

	Estimate	Std. Error	Lower	Upper
Z0_free_0	97.4200	1.88200	93.6400	101.2000
k_Z1_Z2	-0.7823	0.05861	-0.9002	-0.6644
$k_Z0_free_bound$	-2.1400	0.36300	-2.8700	-1.4100
$k_Z0_bound_free$	-4.8390	1.41700	-7.6900	-1.9890
k_Z0_free_Z1	0.8464	0.05312	0.7395	0.9533
k_Z2_sink	-1.6340	0.22360	-2.0840	-1.1840
k_Z2_Z3_free	-1.4860	0.17810	-1.8440	-1.1270
k_Z3_free_sink	-2.5930	0.37420	-3.3460	-1.8410
$k_Z3_free_bound$	-5.2610	1.00200	-7.2760	-3.2460
k_Z3_bound_free	-17.0500	20.03000	-57.3500	23.2500

Backtransformed parameters:

	Estimate	Lower	Upper
Z0_free_0	9.742e+01	9.364e+01	1.012e+02
k_Z1_Z2	4.573e-01	4.065e-01	5.146e-01
$k_Z0_free_bound$	1.177e-01	5.668e-02	2.443e-01
$k_Z0_bound_free$	7.912e-03	4.575e-04	1.368e-01

Residual standard error: 3.73 on 47 degrees of freedom

Chi2 error levels in percent:

		err.min	n.optim	df
All	data	17.434	10	44
ZO		14.669	4	13
Z1		14.404	1	12
Z2		21.054	2	10
Z3		8.095	3	9

Estimated disappearance times:

DT50 DT90
Z0 0.3042 1.186
Z1 1.5156 5.035
Z2 1.6444 5.462
Z3 9.5687 41.058

Estimated formation fractions:

ff
Z0_free_sink 1.000
Z0_free_Z1 1.000
Z1_sink 1.000
Z1_Z2 1.000
Z2_sink 0.463
Z2_Z3_free 0.537
Z3_free_sink 1.000

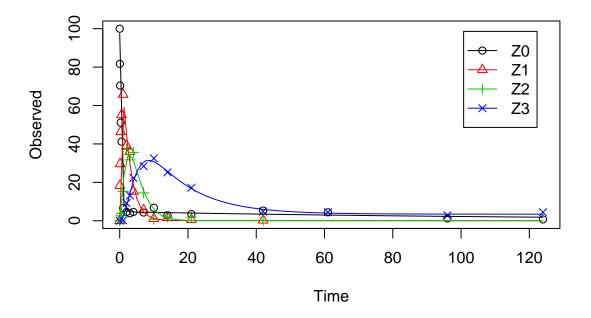
Estimated Eigenvalues of SFORB model(s):

Z0_b1 Z0_b2 Z3_b1 Z3_b2 2.449e+00 7.531e-03 7.996e-02 3.686e-08

Parameter correlation:

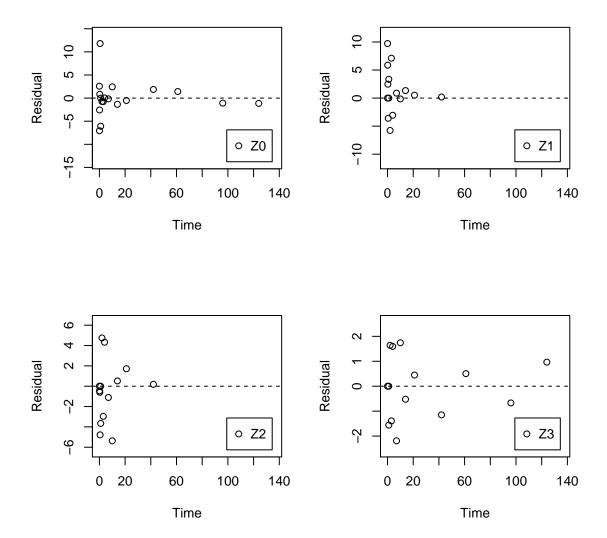
I di dinocol ocilo:				
	<i>Z0_free_0</i>	k_Z1_Z2	$k_Z0_free_bound$	$k_Z0_bound_free$
Z0_free_0	1.000000	0.246104	0.06614	0.05361
k_Z1_Z2	0.246104	1.000000	-0.24410	-0.11439
k_Z0_free_bound	0.066139	-0.244103	1.00000	0.52970
k_Z0_bound_free	0.053612	-0.114386	0.52970	1.00000
k_Z0_free_Z1	0.083075	-0.113942	0.42018	0.14740
k_Z2_sink	0.335105	0.358733	-0.15876	0.02971
k_Z2_Z3_free	-0.065530	-0.086307	-0.08455	-0.13972
k_Z3_free_sink	-0.095118	-0.227130	0.22917	0.27312
k_Z3_free_bound	-0.057690	0.009601	-0.38337	-0.58579

k_Z3_bound_free	-0.002904 0.04	8227	-0.05110	0.17308
	k_Z0_free_Z1 k_	Z2_sink k_	<i>Z2_Z3</i> _free	k_Z3_free_sink
Z0_free_0	0.083075	0.33510	-0.06553	-0.09512
k_Z1_Z2	-0.113942	0.35873	-0.08631	-0.22713
k_Z0_free_bound	0.420182 -	0.15876	-0.08455	0.22917
k_Z0_bound_free	0.147397	0.02971	-0.13972	0.27312
k_Z0_free_Z1	1.000000 -	0.01045	-0.07643	0.06862
k_Z2_sink	-0.010446	1.00000	0.08789	-0.68327
k_Z2_Z3_free	-0.076428	0.08789	1.00000	-0.07674
k_Z3_free_sink	0.068615 -	0.68327	-0.07674	1.00000
k_Z3_free_bound	-0.175464	0.17434	0.53068	-0.27450
k_Z3_bound_free	0.007372 -	0.27929	-0.76653	0.50567
k_Z3_free_bound k_Z3_bound_free				
Z0_free_0	-0.057690	-0.	002904	
k_Z1_Z2	0.009601	0.	048227	
k_Z0_free_bound	-0.383372	-0.	051097	
k_Z0_bound_free	-0.585788	0.	173081	
k_Z0_free_Z1	-0.175464	0.	007372	
k_Z2_sink	0.174338	-0.	279286	
k_Z2_Z3_free	0.530682	-0.	766526	
k_Z3_free_sink	-0.274495	0.	505672	
k_Z3_free_bound	1.000000	-0.	545333	
k_Z3_bound_free	-0.545333	1.	000000	



Looking at the confidence intervals of the SFORB model parameters of Z3, it is clear that nothing can be said about the degradation rate of Z3 towards the end of the experiment. However, this appears to be a feature of the data.

```
R> par(mfrow = c(2, 2))
R> mkinresplot(m.Z.mkin.5, "ZO", lpos = "bottomright")
R> mkinresplot(m.Z.mkin.5, "Z1", lpos = "bottomright")
R> mkinresplot(m.Z.mkin.5, "Z2", lpos = "bottomright")
R> mkinresplot(m.Z.mkin.5, "Z3", lpos = "bottomright")
```



As expected, the residual plots are much more random than in the case of the all SFO model for which they were shown above. In conclusion, the model Z.mkin.5 is proposed as the best-fit model for the dataset from Appendix 7 of the FOCUS report.