

$$0 < 12$$

Which is true.

∴ Graph of an inequality  $x + 4y \leq 12$  will be towards the origin side.

Put  $(0, 0)$  in

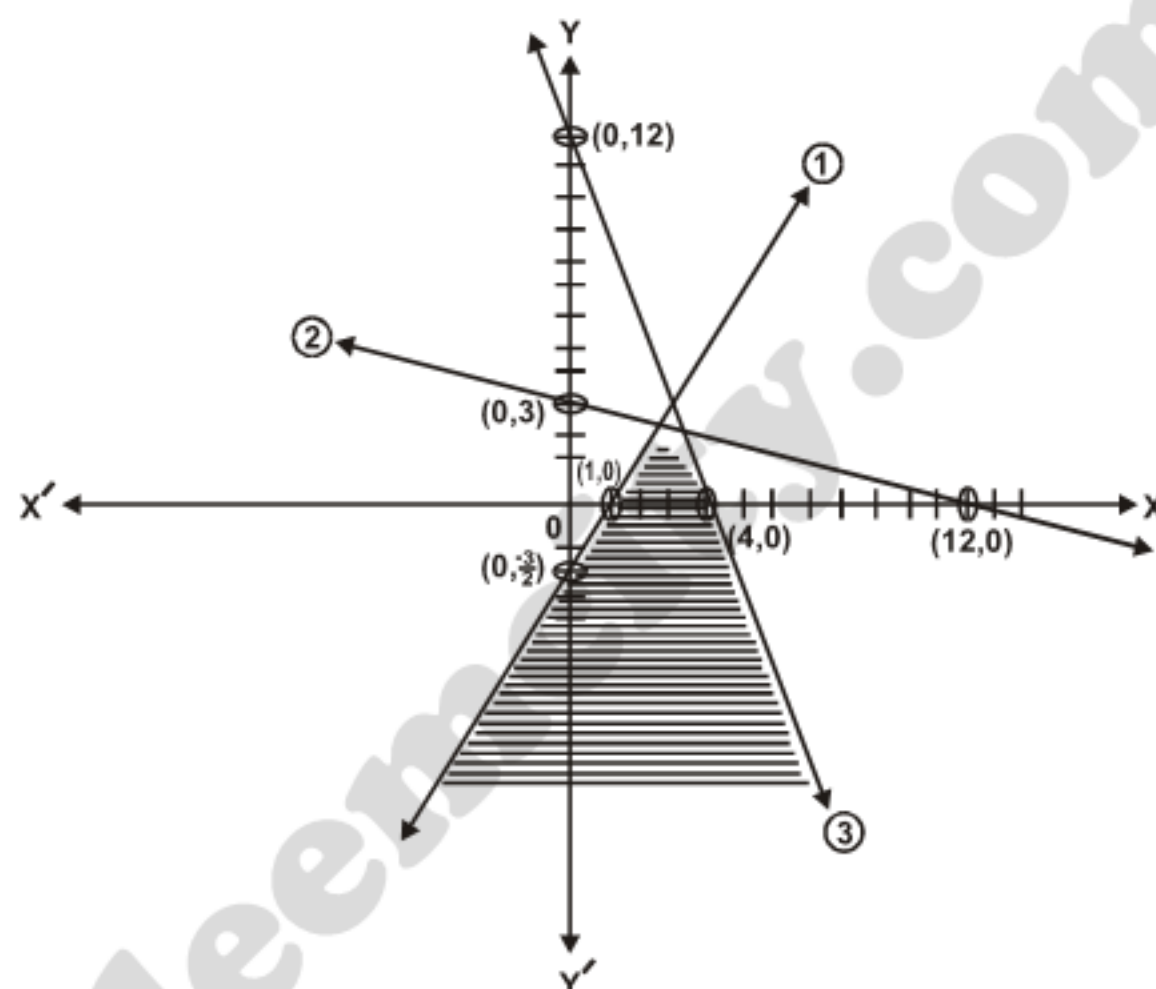
$$3x + y < 12$$

$$3(0) + 0 < 12$$

$$0 < 12$$

Which is true.

∴ Graph of an inequality  $3x + y \leq 12$  will be towards the origin side.



## EXERCISE 5.2

**Q.4:** Graph the feasible region of the following system of linear inequalities and find the corner points in each case.

(i)  $2x - 3y \leq 6$   
 $2x + 3y \leq 12$   
 $x \geq 0, y \geq 0$

(ii)  $x + y \leq 5$   
 $-2x + y \leq 2$   
 $x \geq 0, y \geq 0$

(iii)  $x + y \leq 5$   
 $-2x + y \geq 2$   
 $x \geq 0, y \geq 0$

(iv)  $3x + 7y \leq 21$   
 $x - y \leq 3$   
 $x \geq 0, y \geq 0$

(v)  $3x + 2y \geq 6$   
 $x + y \leq 4$   
 $x \geq 0, y \geq 0$

(vi)  $5x + 7y \leq 35$   
 $x - 2y \leq 4$   
 $x \geq 0, y \geq 0$

**Solution:**

(i)  $2x - 3y \leq 6$  (Lhr. Board 2005)

$$2x + 3y \leq 12$$

$$x \geq 0, y \geq 0$$

The associated equations are

$$2x - 3y = 6 \quad \text{..... (1)}$$

$$2x + 3y = 12 \quad \text{..... (2)}$$

x-intercept

Put  $y = 0$  in eq. (1)

$$2x - 3(0) = 6$$

$$2x = 6$$

$$x = \frac{6}{2} = 3$$

$\therefore$  Point is (3, 0)

y-intercept

Put  $x = 0$  in eq. (1)

$$2(0) - 3y = 6$$

$$-3y = 6$$

$$y = \frac{6}{-3} = -2$$

$\therefore$  Point is (0, -2)

x-intercept

Put  $y = 0$  in eq. (2)

$$2x + 3(0) = 12$$

$$2x = 12$$

$$x = \frac{12}{2} = 6$$

$\therefore$  Point is (6, 0)

y-intercept

Put  $x = 0$  in eq. (2)

$$2(0) + 3y = 12$$

$$3y = 12$$

$$y = \frac{12}{3} = 4$$

∴ Point is (0, 4)

### Test Point

Put (0, 0) in

$$2x - 3y < 6$$

$$2(0) - 3(0) < 6$$

$$0 < 6$$

Which is true.

∴ Graph of an inequality  $2x - 3y \leq 6$  will be towards the origin side.

Put (0, 0) in

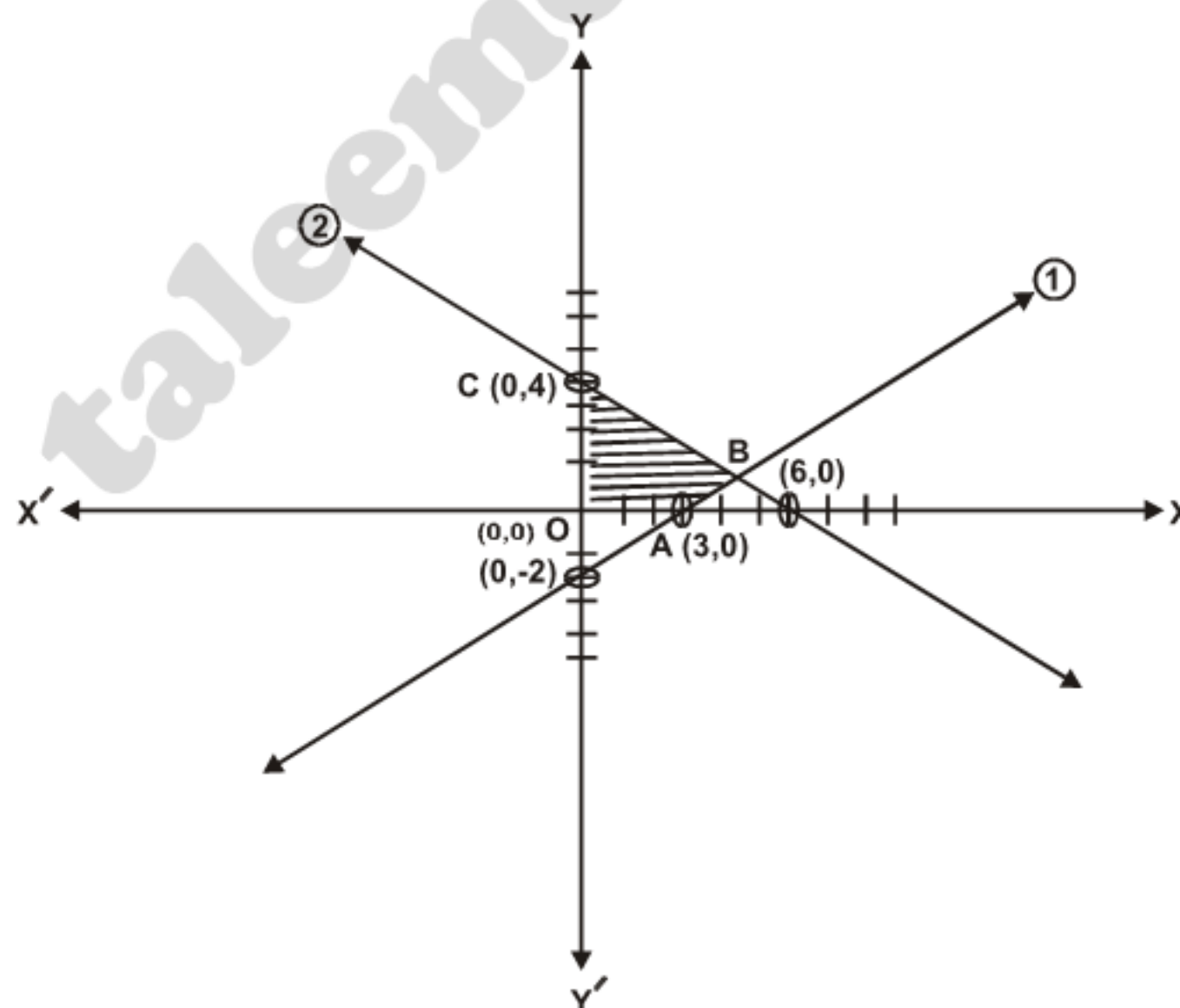
$$2x + 3y < 12$$

$$2(0) + 3(0) < 12$$

$$0 < 12$$

Which is true.

∴ Graph of an inequality  $2x + 3y \leq 12$  will be towards the origin side.



∴ OABC is the feasible solution region so corner points are

$$O(0, 0), \quad A(3, 0), \quad C(0, 4)$$

To find B solving eq. (1) & eq. (2)

Adding eq. (1) & eq. (2)

$$2x - 3y = 6$$

$$\underline{2x + 3y = 12}$$

$$4x = 18$$

$$x = \frac{18}{4} = \frac{9}{2}$$

Put

$$x = \frac{9}{2} \text{ in eq. (1)}$$

$$2\left(\frac{9}{2}\right) - 3y = 6$$

$$9 - 6 = 3y$$

$$y = \frac{3}{3} = 1$$

$$\therefore B\left(\frac{9}{2}, 1\right)$$

(ii)  $x + y \leq 5$

$$-2x + y \leq 2$$

$$x \geq 0, \quad y \geq 0$$

The associated equations are

$$x + y = 5 \quad \text{..... (1)}$$

$$y - 2x = 2 \quad \text{..... (2)}$$

x-intercept

Put  $y = 0$  in eq. (1)

$$x + 0 = 5$$

$$x = 5$$

$\therefore$  Point is (5, 0)

y-intercept

Put  $x = 0$  in eq. (1)

$$0 + y = 5$$

$$y = 5$$

∴ Point is (0, 5)

x-intercept

$$\begin{aligned}\text{Put } y &= 0 \text{ in eq. (2)} \\ 0 - 2x &= 2 \\ x &= \frac{2}{-2} = -1\end{aligned}$$

∴ Point is (-1, 0)

y-intercept

$$\begin{aligned}\text{Put } x &= 0 \text{ in eq. (2)} \\ y - 2(0) &= 2 \\ y &= 2\end{aligned}$$

∴ Point is (0, 2)

Test Point

$$\begin{aligned}\text{Put } (0, 0) &\text{ in} \\ x + y &< 5 \\ 0 + 0 &< 5 \\ 0 &< 5\end{aligned}$$

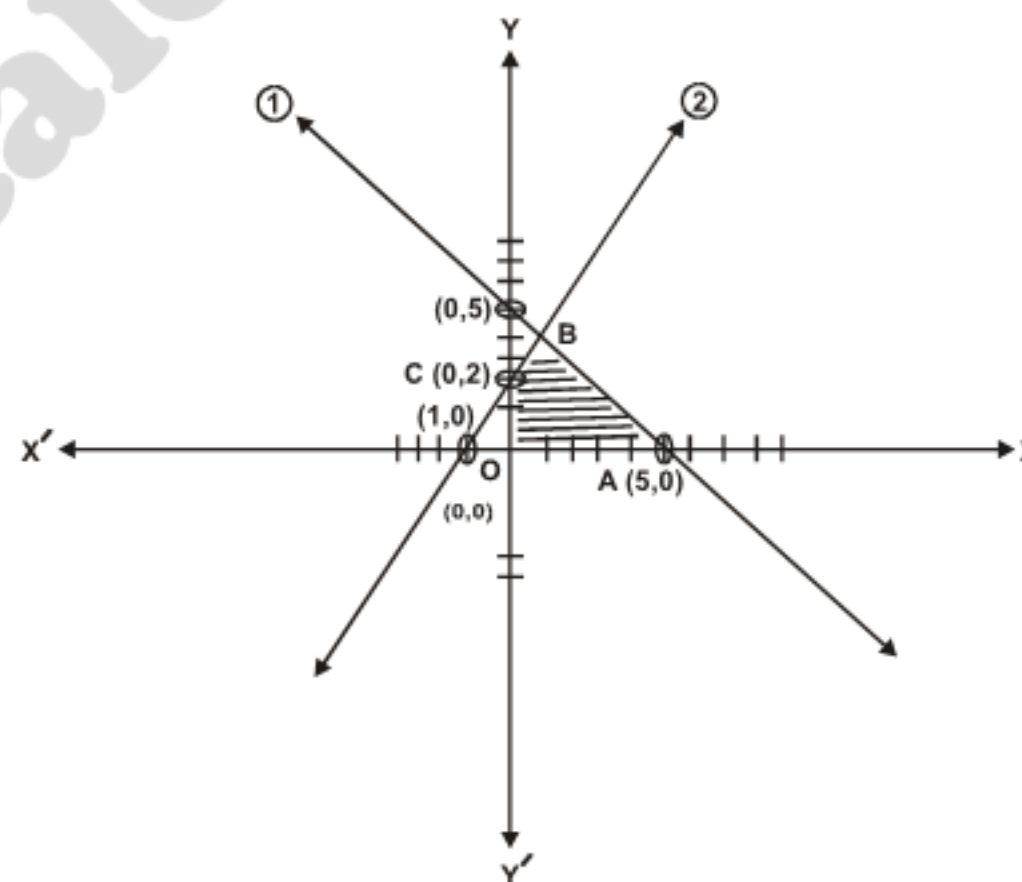
Which is true.

∴ Graph of an inequality  $x + y \leq 5$  will towards the origin side.

$$\begin{aligned}\text{Put } (0, 0) &\text{ in} \\ y - 2x &< 2 \\ 0 - 2(0) &< 2 \\ 0 &< 2\end{aligned}$$

Which is true.

∴ Graph of an inequality  $y - 2x \leq 2$  will towards the origin side.



∴ OABC is the feasible solution region so corner points are

O(0, 0), A(5, 0), C(0, 2)

To find B solving eq. (1) & eq. (2)

Eq. (1) – Eq. (2) we get

$$\begin{array}{r} x + y = 5 \\ -2x + y = -2 \\ \hline \end{array}$$

$$3x = 3$$

$$x = \frac{3}{3} = 1$$

Put

$$x = 1 \text{ in eq. (1)}$$

$$1 + y = 5$$

$$y = 5 - 1 = 4$$

$$\therefore B(1, 4)$$

**(iii)  $x + y \leq 5$**

**$-2x + y \geq 2$**

**$x \geq 0$  ,  $y \geq 0$**

The associated equations are

$$x + y = 5 \quad \dots (1)$$

$$-2x + y = 2 \quad \dots (2)$$

x-intercept

Put  $y = 0$  in eq. (1)

$$x + 0 = 5$$

$$x = 5$$

$\therefore$  Point is (5, 0)

y-intercept

Put  $x = 0$  in eq. (1)

$$0 + y = 5$$

$$y = 5$$

$\therefore$  Point is (0, 5)

x-intercept

Put  $y = 0$  in eq. (2)

$$-2x + 0 = 2$$

$$x = \frac{2}{-2} = -1$$

∴ Point is  $(-1, 0)$

y-intercept

Put  $x = 0$  in eq. (2)

$$-2(0) + y = 2$$

$$y = 2$$

∴ Point is  $(0, 2)$

Test Point

Put  $(0, 0)$  in

$$x + y < 5$$

$$0 + 0 < 5$$

$$0 < 5$$

Which is true.

∴ Graph of an inequality  $x + y \leq 5$  will be towards the origin side.

Put  $(0, 0)$  in

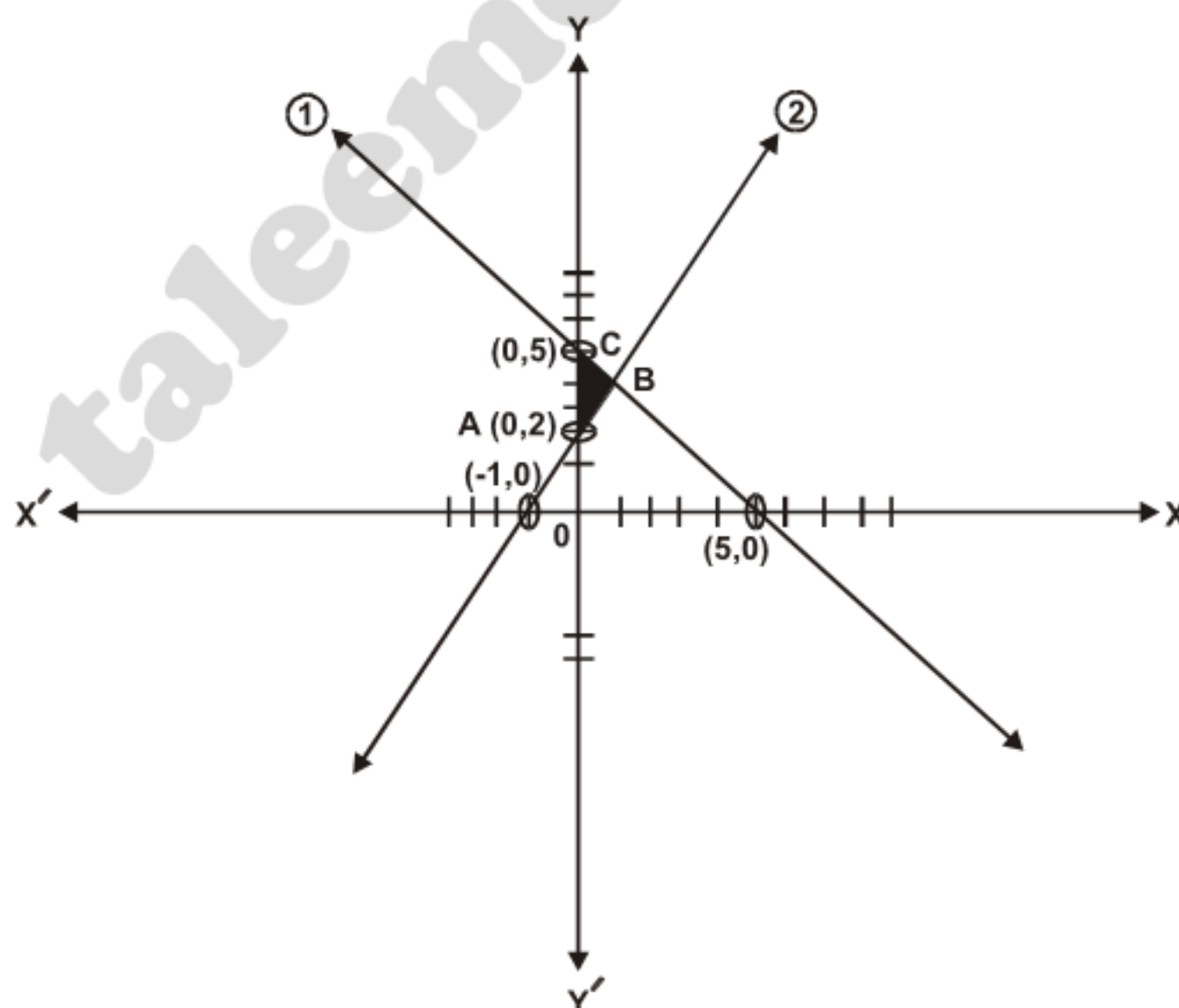
$$-2x + y > 2$$

$$-2(0) + 0 > 2$$

$$0 > 2$$

Which is false.

∴ Graph of an inequality  $-2x + y \geq 2$  will not be towards the origin side.



∴ ABC is the feasible solution region. So corner points are A  $(0, 2)$ , C  $(0, 5)$ . To

find B solving eq. (1) & eq. (2)

Eq. (1) – Eq. (2), we get

$$x + y = 5$$

$$\underline{\mp 2x \pm y = 2}$$

$$3x = 3$$

$$x = \frac{3}{3} = 1$$

Put  $x = 1$  in eq. (1)

$$1 + y = 5$$

$$y = 5 - 1 = 4$$

$\therefore$  B (1, 4)

(iv)  $3x + 7y \leq 21$

$$x - y \leq 3$$

$$x \geq 0, y \geq 0$$

The associated equations are

$$3x + 7y = 21 \quad \text{..... (1)}$$

$$x - y = 3 \quad \text{..... (2)}$$

x-intercept

Put  $y = 0$  in eq. (1)

$$3x + 7(0) = 21$$

$$3x = 21$$

$$x = \frac{21}{3} = 7$$

$\therefore$  Point is (7, 0)

y-intercept

Put  $x = 0$  in eq. (1)

$$3(0) + 7y = 21$$

$$y = \frac{21}{7} = 3$$

$\therefore$  Point is (0, 3)

x-intercept

Put  $y = 0$  in eq. (2)



$$x - 0 = 3$$

$$x = 3$$

∴ Point is (3, 0)

y-intercept

Put  $x = 0$  in eq. (2)

$$0 - y = 3$$

$$y = -3$$

∴ Point is (0, -3)

Test Point

Put (0, 0) in

$$3x + 7y < 21$$

$$3(0) + 7(0) < 21$$

$$0 < 21$$

Which is true.

∴ Graph of an inequality  $3x + 7y \leq 21$  will be towards the origin side.

Put (0, 0) in

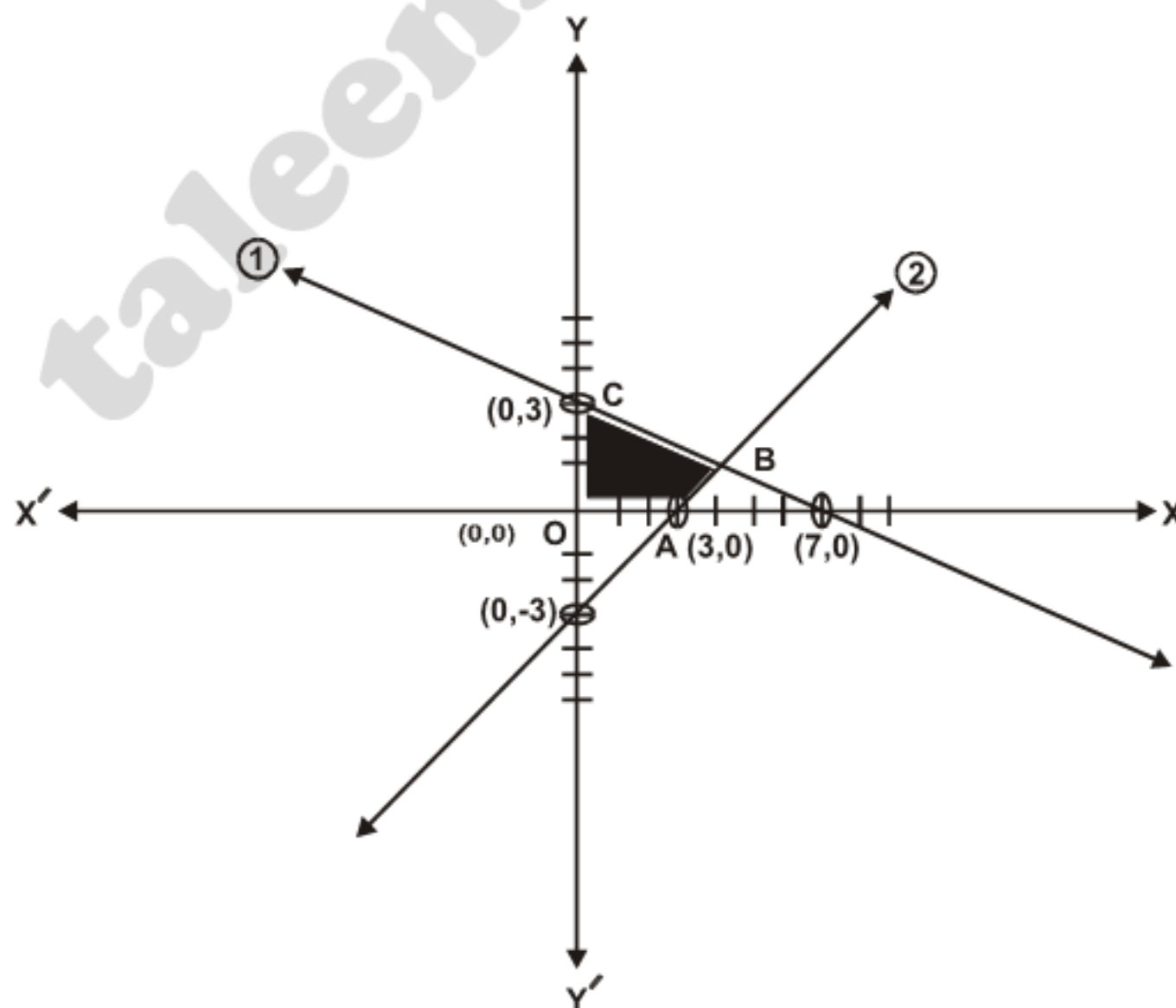
$$x - y < 3$$

$$0 - 0 < 3$$

$$0 < 3$$

Which is true.

∴ Graph of an inequality  $x - y \leq 3$  will be towards the origin side.



∴ OABC is the feasible solution region so corner points are

O(0, 0), A(3, 0), C(0, 3)

To find B solving eq. (1) & eq. (2)

Eq. (1) + Eq. (2) × 7, we get

$$3x + 7y = 21$$

$$\underline{7x - 7y = 21}$$

$$10x = 42$$

$$x = \frac{42}{10} = \frac{21}{5}$$

Put  $x = \frac{21}{5}$  in eq. (2)

$$\frac{21}{5} - y = 3$$

$$\frac{21}{5} - 3 = y$$

$$y = \frac{21 - 15}{5}$$

$$y = \frac{6}{5}$$

∴  $B\left(\frac{21}{5}, \frac{6}{5}\right)$

(v)  $3x + 2y \geq 6$

$$x + y \leq 4$$

$$x \geq 0, y \geq 0$$

The associated equations are

$$3x + 2y = 6 \quad \text{..... (1)}$$

$$x + y = 4 \quad \text{..... (2)}$$

x-intercept

Put  $y = 0$  in eq. (1)

$$3x + 2(0) = 6$$

$$x = \frac{6}{3} = 2$$

∴ Point is (2, 0)

y-intercept

Put  $x = 0$  in eq. (1)

$$3(0) + 2y = 6$$

$$y = \frac{6}{2} = 3$$

∴ Point is (0, 3)

x-intercept

Put  $y = 0$  in eq. (2)

$$x + 0 = 4$$

$$x = 4$$

∴ Point is (4, 0)

y-intercept

Put  $x = 0$  in eq. (2)

$$0 + y = 4$$

$$y = 4$$

∴ Point is (0, 4)

Test Point

Put (0, 0) in

$$3x + 2y > 6$$

$$3(0) + 2(0) > 6$$

$$0 > 6$$

Which is false.

∴ Graph of an inequality  $3x + 2y \geq 6$  will not be towards the origin side.

Put (0, 0) in

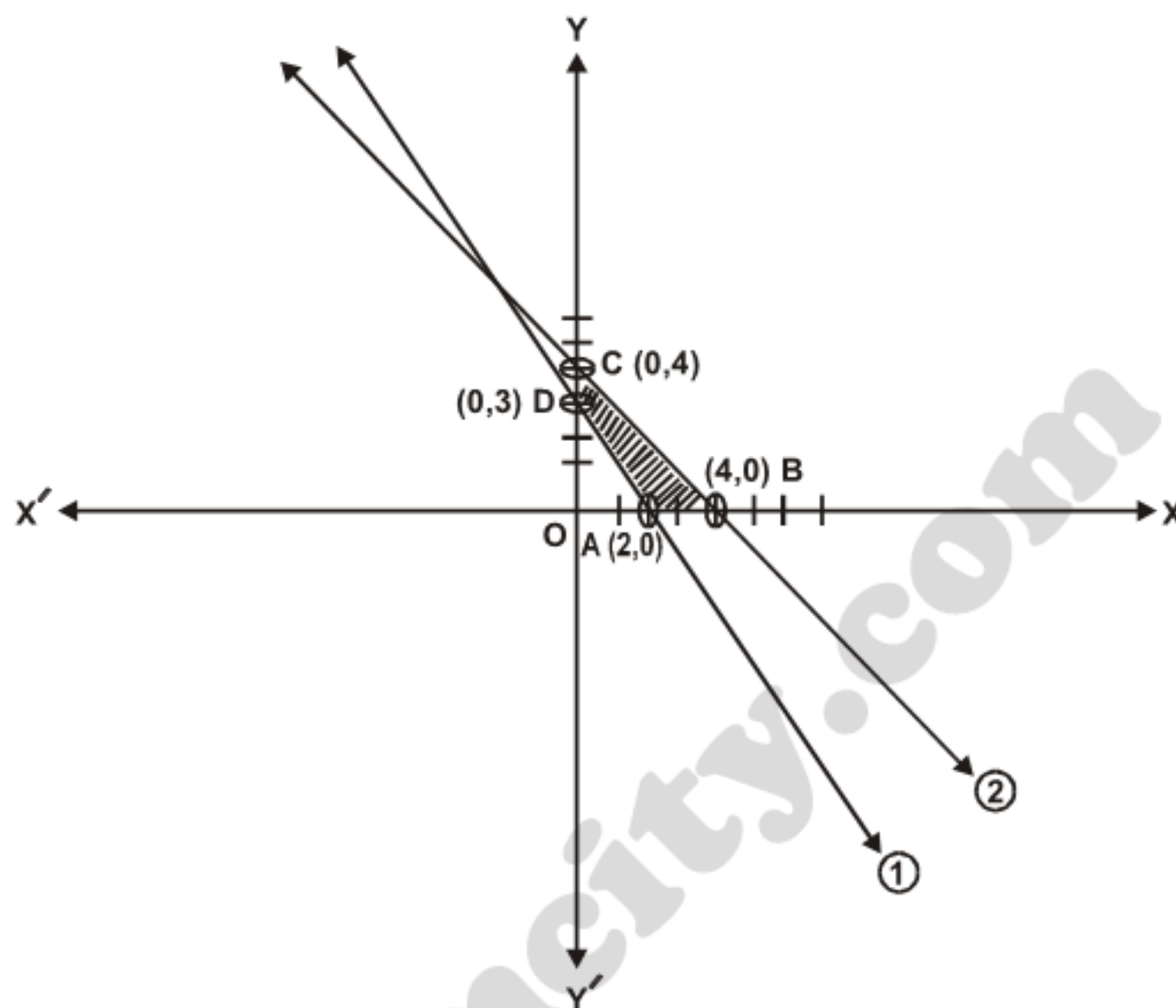
$$x + y < 4$$

$$0 + 0 < 4$$

$$0 < 4$$

Which is true.

∴ Graph of an inequality  $x + y \leq 4$  will be towards the origin side.



∴ ABCD is the feasible solution region so corner points are  
A (2, 0), B (4, 0), C(0, 4), D (0, 3)

(vi)  $5x + 7y \leq 35$

$$x - 2y \leq 4$$

$$x \geq 0, y \geq 0$$

The associated equations are

$$5x + 7y = 35 \quad \text{..... (1)}$$

$$x - 2y = 4 \quad \text{..... (2)}$$

x-intercept

Put  $y = 0$  in eq. (1)

$$5x + 7(0) = 35$$

$$x = \frac{35}{5} = 7$$

∴ Point is (7, 0)

y-intercept

Put  $x = 0$  in eq. (1)

$$5(0) + 7y = 35$$

$$y = \frac{35}{7} = 5$$

$\therefore$  Point is (0, 5)

x-intercept

Put  $y = 0$  in eq. (2)

$$x - 2(0) = 4$$

$$x = 4$$

$\therefore$  Point is (4, 0)

y-intercept

Put  $x = 0$  in eq. (2)

$$0 - 2y = 4$$

$$y = \frac{4}{-2} = -2$$

$\therefore$  Point is (0, -2)

Test Point

Put (0, 0) in

$$5x + 7y < 35$$

$$5(0) + 7(0) < 35$$

$$0 < 35$$

Which is true.

$\therefore$  Graph of an inequality  $5x + 7y \leq 35$  will be towards the origin side.

Put (0, 0) in

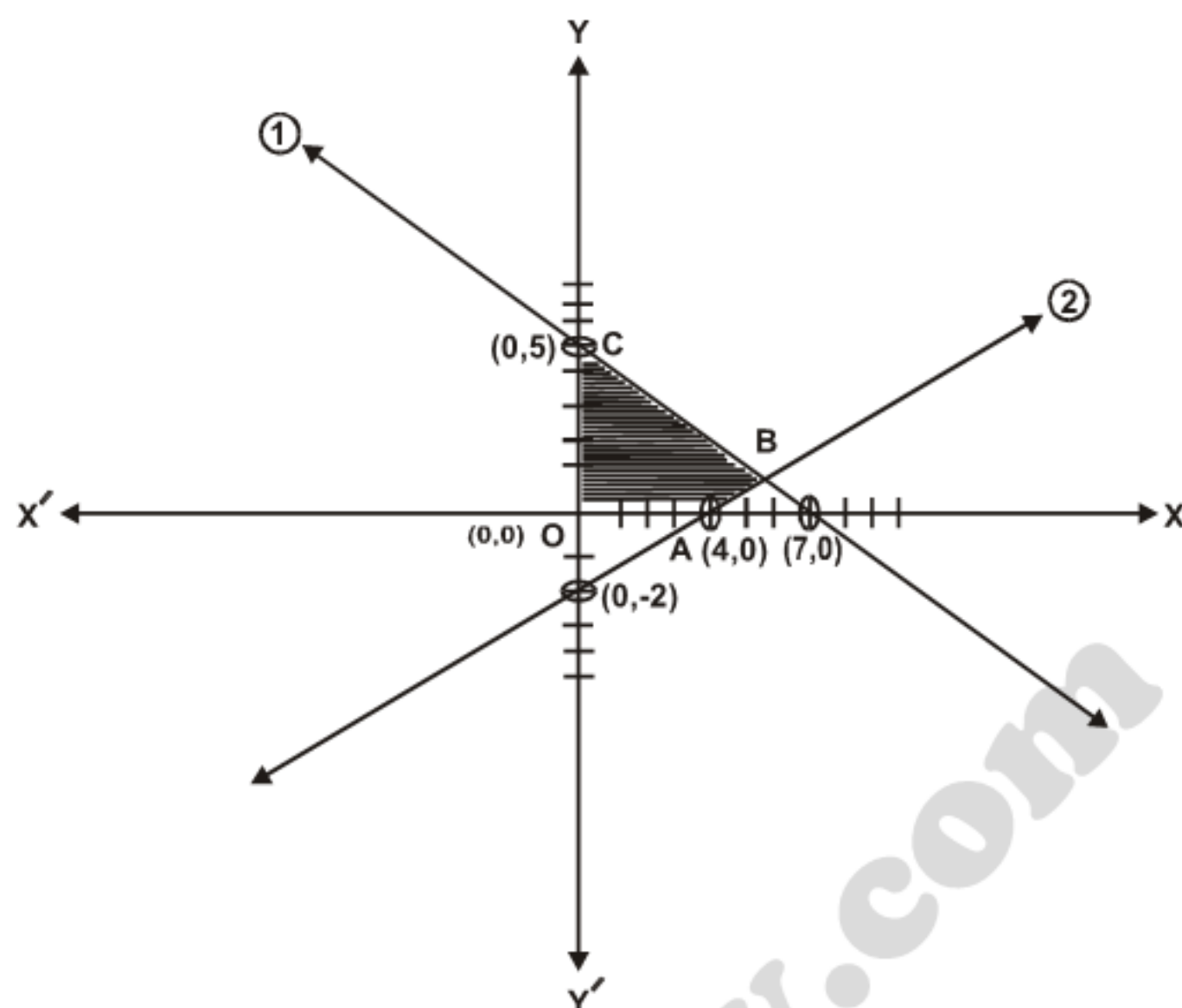
$$x - 2y < 4$$

$$0 - 2(0) < 4$$

$$0 < 4$$

Which is true.

$\therefore$  Graph of an inequality  $x - 2y \leq 4$  will be towards the origin.



∴ OABC is the feasible solution region so corner points are

O (0, 0), A (4, 0), C (0, 5)

To find B solving eq. (1) & eq. (2)

Eq. (1) – Eq. (2) × 5, we get

$$5x + 7y = 35$$

$$- 5x + 10y = -20$$

$$17y = 15$$

$$y = \frac{15}{17}$$

Put  $y = \frac{15}{17}$  in eq. (2)

$$x - 2\left(\frac{15}{17}\right) = 4$$

$$x - \frac{30}{17} = 4$$

$$x = 4 + \frac{30}{17}$$

$$x = \frac{68 + 30}{17}$$

$$x = \frac{98}{17}$$

$$\therefore B = \left( \frac{98}{17}, \frac{15}{17} \right)$$

**Q.2:** Graph the feasible region of the following system of linear inequalities and find the corner points in each case.

(i)  $2x + y \leq 10$

$$x + 4y \leq 12$$

$$x + 2y \leq 10$$

$$x \geq 0, y \geq 0$$

(iii)  $2x + 3y \leq 18$

$$x + 4y \leq 12$$

$$3x + y \leq 12$$

$$x \geq 0, y \geq 0$$

(v)  $x + 3y \leq 15$

$$2x + y \leq 12$$

$$4x + 3y \leq 24$$

$$x \geq 0, y \geq 0$$

(ii)  $2x + 3y \leq 18$

$$2x + y \leq 10$$

$$x + 4y \leq 12$$

$$x \geq 0, y \geq 0$$

(iv)  $x + 2y \leq 14$

$$3x + 4y \leq 36$$

$$2x + y \leq 10$$

$$x \geq 0, y \geq 0$$

(vi)  $2x + y \leq 20$

$$8x + 15y \leq 120$$

$$x + y \leq 11$$

$$x \geq 0, y \geq 0$$

**Solution:**

(i)  $2x + y \leq 10$

$$x + 4y \leq 12$$

$$x + 2y \leq 10$$

$$x \geq 0, y \geq 0$$

The associated eqs. are

$$2x + y = 10 \quad \dots\dots (1)$$

$$x + 4y = 12 \quad \dots\dots (2)$$

$$x + 2y = 10 \quad \dots\dots (3)$$

x-intercept

Put  $y = 0$  in eqs. (1), (2) and (3)

$$2x + 0 = 10$$

$$2x = 10$$

$$x = \frac{10}{2} = 5$$

$\therefore$  Point is (5, 0)

$$x + 4(0) = 12$$

$$x = 12$$

$\therefore$  Point is (12, 0)

$$x + 2(0) = 10$$

$$x = 10$$

$\therefore$  Point is (10, 0)

y-intercept

Put  $x = 0$  in eqs. (1), (2) and (3)

$$2(0) + y = 10$$

$$y = 10$$

$$0 + 4y = 12$$

$$4y = 12$$

$$0 + 2y = 10$$

$$2y = 10$$

∴ Point is (0, 10)

$$y = \frac{12}{4} = 3$$

∴ Point is (0, 3)

$$y = \frac{10}{2} = 5$$

∴ Point is (0, 5)

### Test Point

Put (0, 0)

$$2x + y < 10$$

$$2(0) + 0 < 10$$

$$0 < 10$$

Which is true.

∴ Graph of an inequality  $2x + y \leq 10$  will be towards the origin side.

Put (0, 0) in

$$x + 4y < 12$$

$$0 + 4(0) < 12$$

$$0 < 12$$

Which is true.

∴ Graph of an inequality  $x + 4y \leq 12$  will be towards the origin side.

Put (0, 0) in

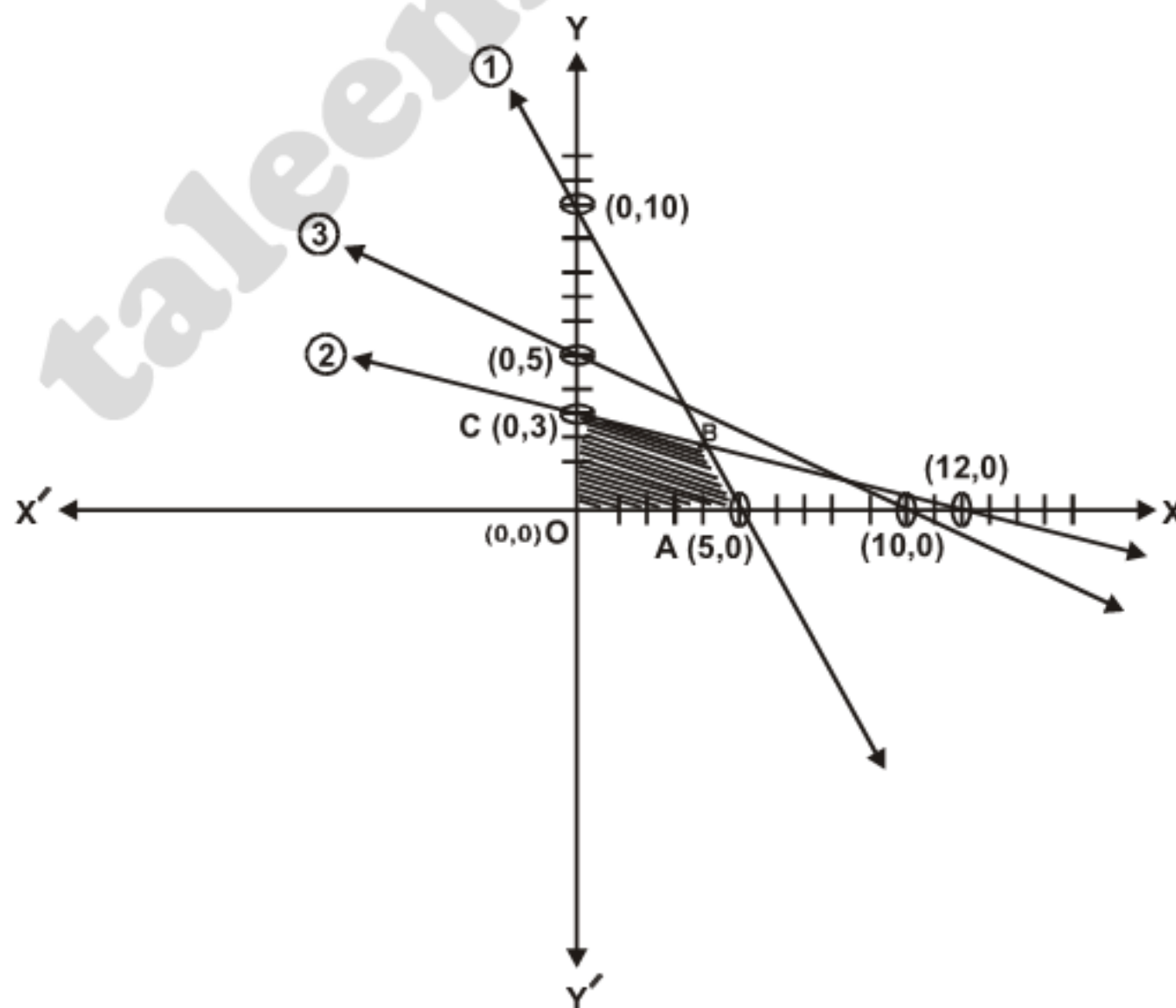
$$x + 2y < 10$$

$$0 + 2(0) < 10$$

$$0 < 10$$

Which is true.

∴ Graph of an inequality  $x + 2y \leq 10$  will be towards the origin side.





∴ OABC is the feasible solution region so the corner points are

O (0, 0), A (5, 0), C (0, 3)

To find B solving eq. (1) & eq. (2)

Eq. (1) – Eq. (2) × 2, we get

$$2x + y = 10$$

$$- \underline{2x + 8y = -24}$$

$$-7y = -14$$

$$y = \frac{14}{7} = 2$$

Put  $y = 2$  in eq. (2)

$$x + 4(2) = 12$$

$$x + 8 = 12$$

$$x = 12 - 8 = 4$$

∴ B = (4, 2)

(ii)  $2x + 3y \leq 18$  (Guj. Board 2005) (Lhr. Board 2008)

$$2x + y \leq 10$$

$$x + 4y \leq 12$$

$$x \geq 0, y \geq 0$$

The associated equations are

$$2x + 3y = 18 \quad \text{..... (1)}$$

$$2x + y = 10 \quad \text{..... (2)}$$

$$x + 4y = 12 \quad \text{..... (3)}$$

x-intercept

Put  $y = 0$  in eqs. (1), (2) and (3)

$$2x + 3(0) = 18$$

$$2x = 18$$

$$x = \frac{18}{2} = 9$$

∴ Point is (9, 0)

$$2x + 0 = 10$$

$$2x = 10$$

$$x = \frac{10}{2} = 5$$

∴ Point is (5, 0)

$$x + 4(0) = 12$$

$$x = 12$$

∴ Point is (12, 0)

y-intercept

Put  $x = 0$  in eqs. (1), (2) and (3)

$$2(0) + 3y = 18$$

$$3y = 18$$

$$y = \frac{18}{3} = 6$$

$\therefore$  Point is (0, 6)

$$2(0) + y = 10$$

$$y = 10$$

$\therefore$  Point is (0, 10)

$$0 + 4y = 12$$

$$4y = 12$$

$$y = \frac{12}{4} = 3$$

$\therefore$  Point is (0, 3)

**Test Point**

Put (0, 0)

$$2x + 3y < 18$$

$$2(0) + 3(0) < 18$$

$$0 < 18$$

Which is true.

$\therefore$  Graph of an inequality  $2x + 3y \leq 18$  will be towards the origin side.

Put (0, 0) in

$$2x + y < 10$$

$$2(0) + 0 < 10$$

$$0 < 10$$

Which is true.

$\therefore$  Graph of an inequality  $2x + y \leq 10$  will be towards the origin side.

Put (0, 0) in

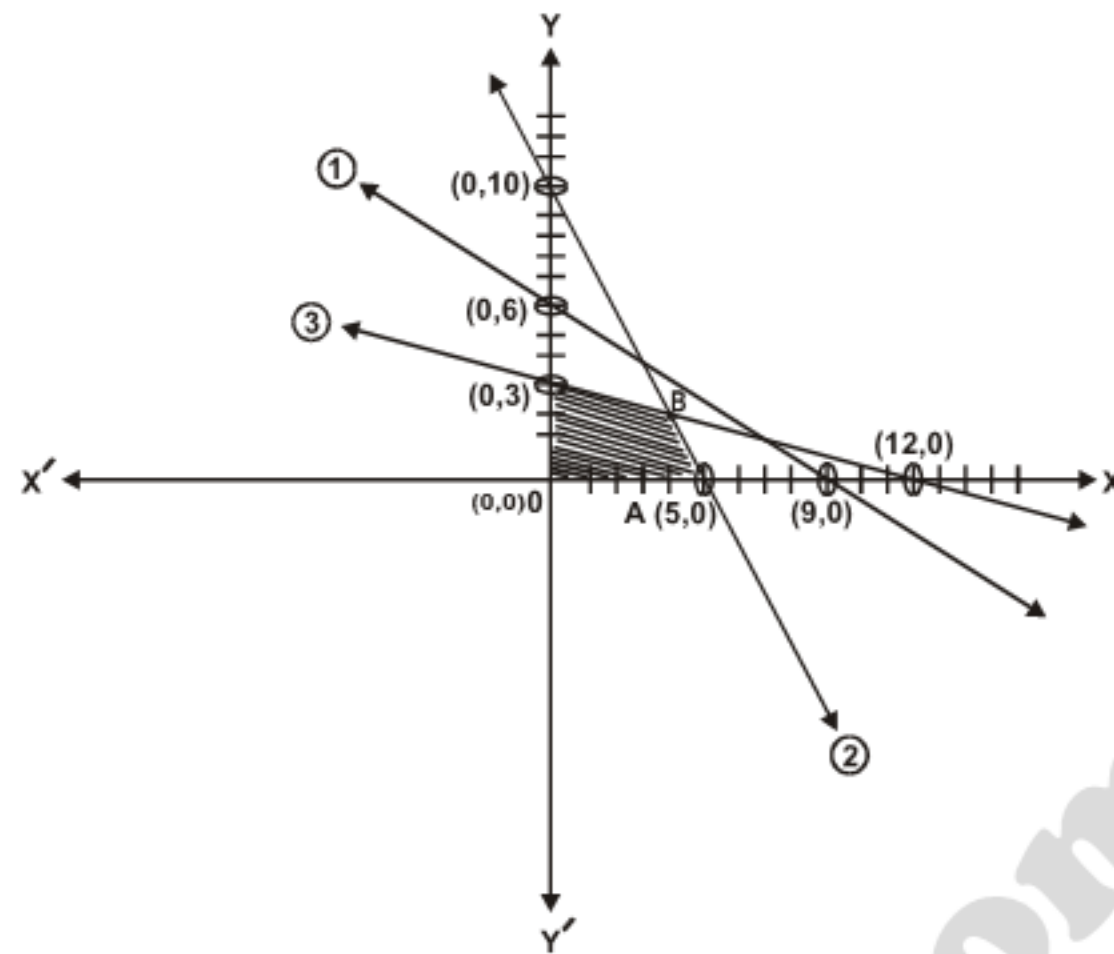
$$x + 4y < 12$$

$$0 + 4(0) < 12$$

$$0 < 12$$

Which is true.

$\therefore$  Graph of an inequality  $x + 4y \leq 12$  will be towards the origin side.



∴ OABC is the feasible solution region so the corner points are

O (0, 0), A (5, 0), C (0, 3)

To find B solving eq. (2) & eq. (3)

Eq. (2) – Eq. (3) × 2, we get

$$\begin{array}{rcl} 2x + y & = & 10 \\ - 2x + 8y & = & -24 \\ \hline -7y & = & -14 \\ y & = & \frac{-14}{-7} = 2 \end{array}$$

Put  $y = 2$  in eq. (3)

$$x + 4(2) = 12$$

$$x + 8 = 12$$

$$x = 12 - 8 = 4$$

∴ B = (4, 2)

(iii)  $2x + 3y \leq 18$

$$x + 4y \leq 12$$

$$3x + y \leq 12$$

$$x \geq 0, \quad y \geq 0$$

The associated equations are

$$2x + 3y = 18 \quad \text{..... (1)}$$

$$x + 4y = 12 \quad \text{..... (2)}$$

$$3x + y = 12 \quad \text{..... (3)}$$

x-interceptPut  $y = 0$  in eqs. (1), (2) and (3)

$$2x + 3(0) = 18$$

$$2x = 18$$

$$x = \frac{18}{2} = 9$$

 $\therefore$  Point is (9, 0)

$$x + 4(0) = 12$$

$$x = 12$$

 $\therefore$  Point is (12, 0)

$$3x + 0 = 12$$

$$3x = 12$$

$$x = \frac{12}{3} = 4$$

 $\therefore$  Point is (4, 0)y-interceptPut  $x = 0$  in eqs. (1), (2) and (3)

$$2(0) + 3y = 18$$

$$3y = 18$$

$$y = \frac{18}{3} = 6$$

 $\therefore$  Point is (0, 6)

$$0 + 4y = 12$$

$$y = \frac{12}{4} = 3$$

 $\therefore$  Point is (0, 3)

$$3(0) + y = 12$$

$$y = 12$$

 $\therefore$  Point is (0, 12)Test Point

Put (0, 0) in

$$2x + 3y < 18$$

$$2(0) + 3(0) < 18$$

$$0 < 18$$

Which is true.

 $\therefore$  Graph of an inequality  $2x + 3y \leq 18$  will be towards the origin side.

Put (0, 0) in

$$x + 4y < 12$$

$$0 + 4(0) < 12$$

$$0 < 12$$

Which is true.

 $\therefore$  Graph of an inequality  $x + 4y \leq 12$  will be towards the origin side.

Put (0, 0) in

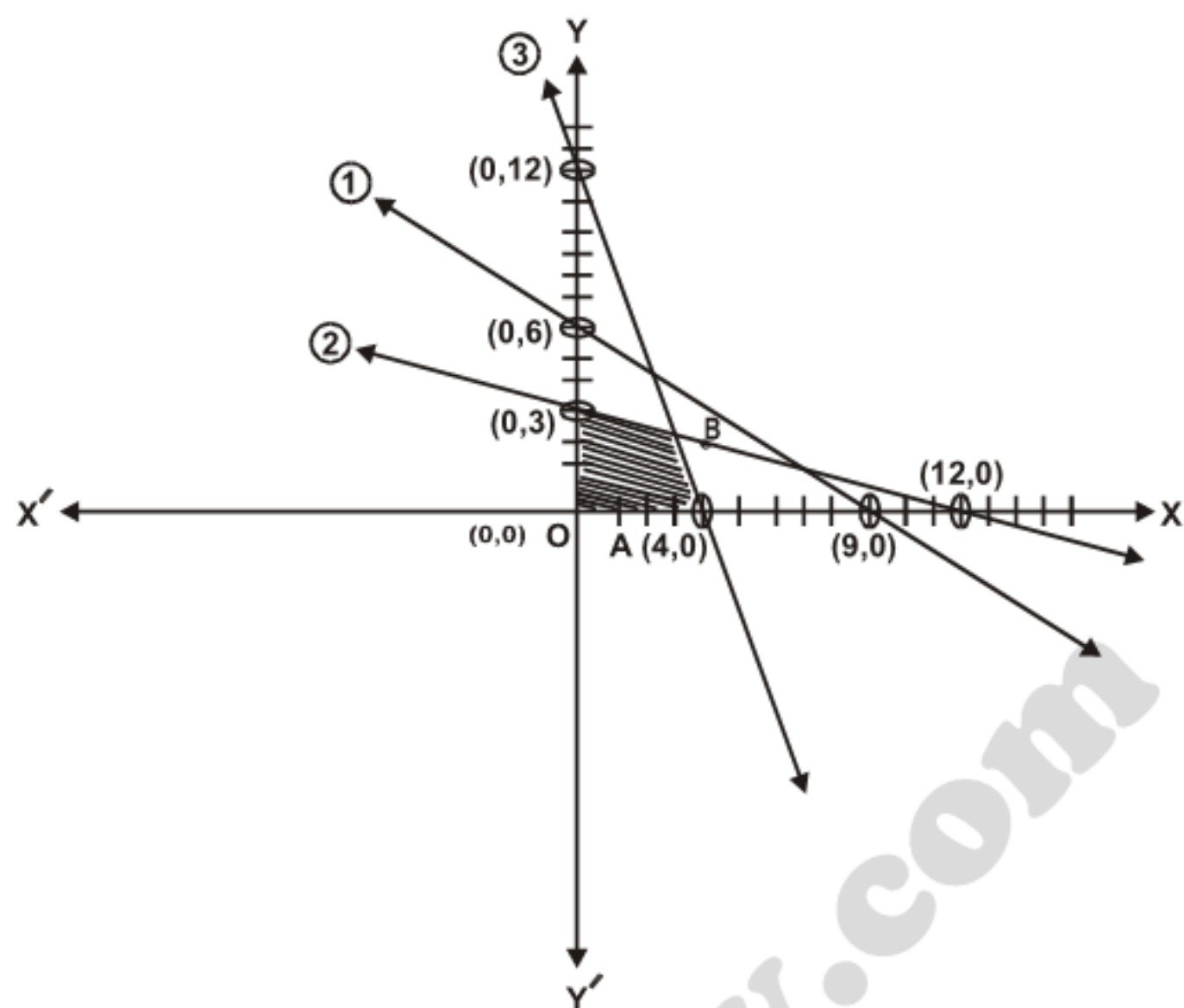
$$3x + y < 12$$

$$3(0) + 0 < 12$$

$$0 < 12$$

Which is true.

 $\therefore$  Graph of an inequality  $3x + y \leq 12$  will be towards the origin side.



∴ OABC is the feasible solution region so the corner points are

O (0, 0), A (4, 0), C (0, 3)

To find B solving eq. (2) & eq. (3)

Eq. (2)  $\times 3$  – Eq. (3), we get

$$\begin{array}{rcl} 3x + 12y & = & 36 \\ - 3x + y & = & -12 \\ \hline 11y & = & 24 \end{array}$$

$$y = \frac{24}{11}$$

Put  $y = \frac{24}{11}$  in eq. (3)

$$3x + \frac{24}{11} = 12$$

$$3x = 12 - \frac{24}{11}$$

$$3x = \frac{132 - 24}{11}$$

$$x = \frac{108}{33} = \frac{36}{11}$$

$$\therefore B\left(\frac{36}{11}, \frac{24}{11}\right)$$

(iv)  $x + 2y \leq 14$

$$3x + 4y \leq 36$$

$$2x + y \leq 10$$

$$x \geq 0, y \geq 0$$

The associated equations are

$$x + 2y = 14 \quad \text{..... (1)}$$

$$3x + 4y = 36 \quad \text{..... (2)}$$

$$2x + y = 10 \quad \text{..... (3)}$$

x-intercept

Put  $y = 0$  in eqs. (1), (2) and (3)

$$x + 2(0) = 14$$

$$x = 14$$

∴ Point is (14, 0)

$$3x + 4(0) = 36$$

$$3x = 36$$

$$x = \frac{36}{3} = 12$$

∴ Point is (12, 0)

$$2x + 0 = 10$$

$$2x = 10$$

$$x = \frac{10}{2} = 5$$

∴ Point is (5, 0)

y-interceptPut  $x = 0$  in eqs. (1), (2) and (3)

$$0 + 2y = 14$$

$$y = \frac{14}{2} = 7$$

 $\therefore$  Point is (0, 7)

$$3(0) + 4y = 36$$

$$4y = 36$$

$$y = \frac{36}{4} = 9$$

 $\therefore$  Point is (0, 9)

$$2(0) + y = 10$$

$$y = 10$$

 $\therefore$  Point is (0, 10)**Test Point**

Put (0, 0) in

$$x + 2y < 14$$

$$0 + 2(0) < 14$$

$$0 < 14$$

Which is true.

 $\therefore$  Graph of an inequality  $x + 2y \leq 14$  will be towards the origin side.

Put (0, 0) in

$$3x + 4y < 36$$

$$3(0) + 4(0) < 36$$

$$0 < 36$$

Which is true.

 $\therefore$  Graph of an inequality  $3x + 4y \leq 36$  will be towards the origin side.

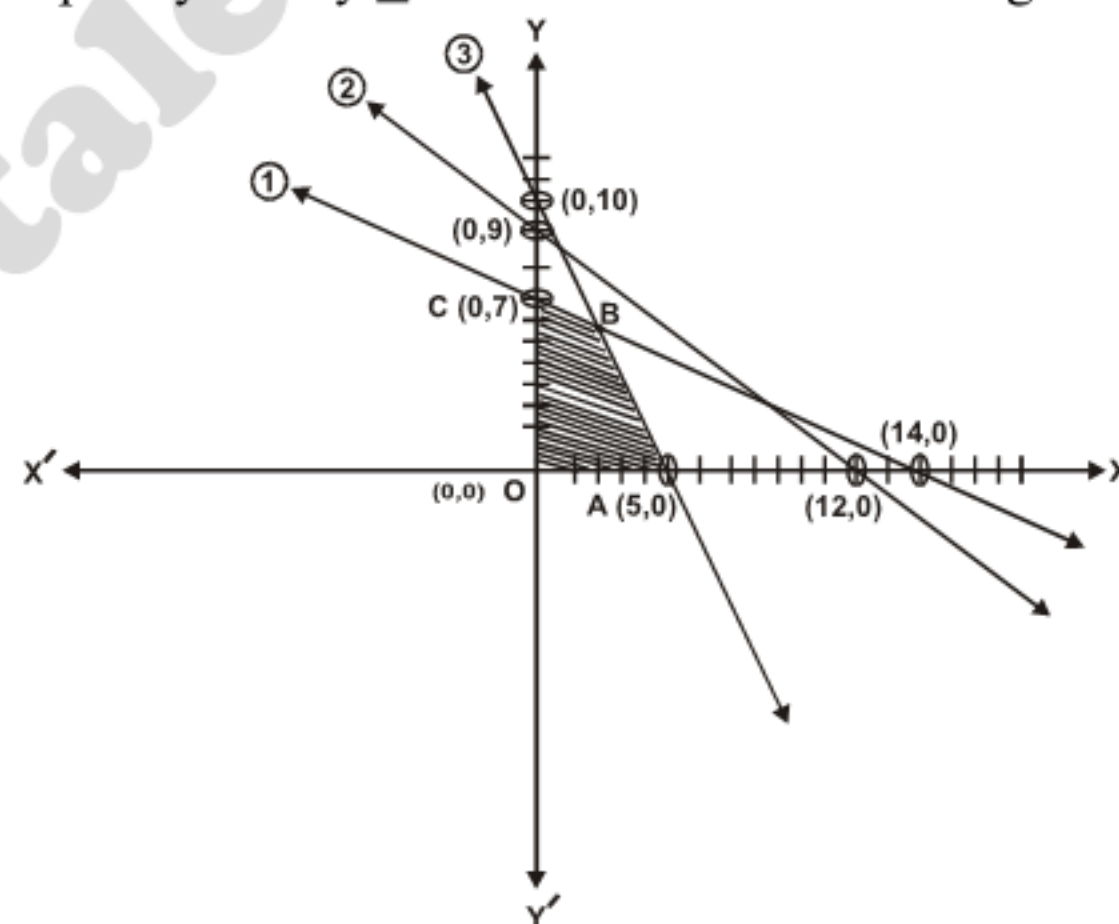
Put (0, 0) in

$$2x + y < 10$$

$$2(0) + 0 < 10$$

$$0 < 10$$

Which is true.

 $\therefore$  Graph of an inequality  $2x + y \leq 10$  will be towards the origin side. $\therefore$  OABC is the feasible solution region so the corner points are

O (0, 0), A (5, 0), C (0, 7)

To find B solving eq. (1) & eq. (3)

Eq. (1)  $\times 2$  – Eq. (3), we get

$$\begin{array}{rcl} 2x + 4y & = & 28 \\ - 2x + y & = & -10 \\ \hline 3y & = & 18 \end{array}$$

$$y = \frac{18}{3} = 6$$

Put  $y = 6$  in eq. (1)

$$x + 2(6) = 14$$

$$x + 12 = 14$$

$$x = 14 - 12$$

$$x = 2$$

$\therefore$  B (2, 6)

(v)  $x + 3y \leq 15$

$$2x + y \leq 12$$

$$4x + 3y \leq 24$$

$$x \geq 0, y \geq 0$$

The associated equations are

$$x + 3y = 15 \quad \text{..... (1)}$$

$$2x + y = 12 \quad \text{..... (2)}$$

$$4x + 3y = 24 \quad \text{..... (3)}$$

x-intercept

Put  $y = 0$  in eqs. (1), (2) and (3)

$$x + 3(0) = 15$$

$$x = 15$$

$\therefore$  Point is (15, 0)

$$2x + 0 = 12$$

$$2x = 12$$

$$x = \frac{12}{2} = 6$$

$\therefore$  Point is (6, 0)

$$4x + 3(0) = 24$$

$$4x = 24$$

$$x = \frac{24}{4} = 6$$

$\therefore$  Point is (6, 0)

y-intercept

Put  $x = 0$  in eqs. (1), (2) and (3)

$$0 + 3y = 15$$

$$y = \frac{15}{3} = 5$$

$\therefore$  Point is (0, 5)

$$2(0) + y = 12$$

$$y = 12$$

$\therefore$  Point is (0, 12)

$$4(0) + 3y = 24$$

$$3y = 24$$

$$y = \frac{24}{3} = 8$$

$\therefore$  Point is (0, 8)



**Test Point**

Put  $(0, 0)$  in

$$x + 3y < 15$$

$$0 + 3(0) < 15$$

$$0 < 15$$

Which is true.

$\therefore$  Graph of an inequality  $x + 3y \leq 15$  will be towards the origin side.

Put  $(0, 0)$  in

$$2x + y < 12$$

$$2(0) + 0 < 12$$

$$0 < 12$$

Which is true.

$\therefore$  Graph of an inequality  $2x + y \leq 12$  will be towards the origin side.

Put  $(0, 0)$  in

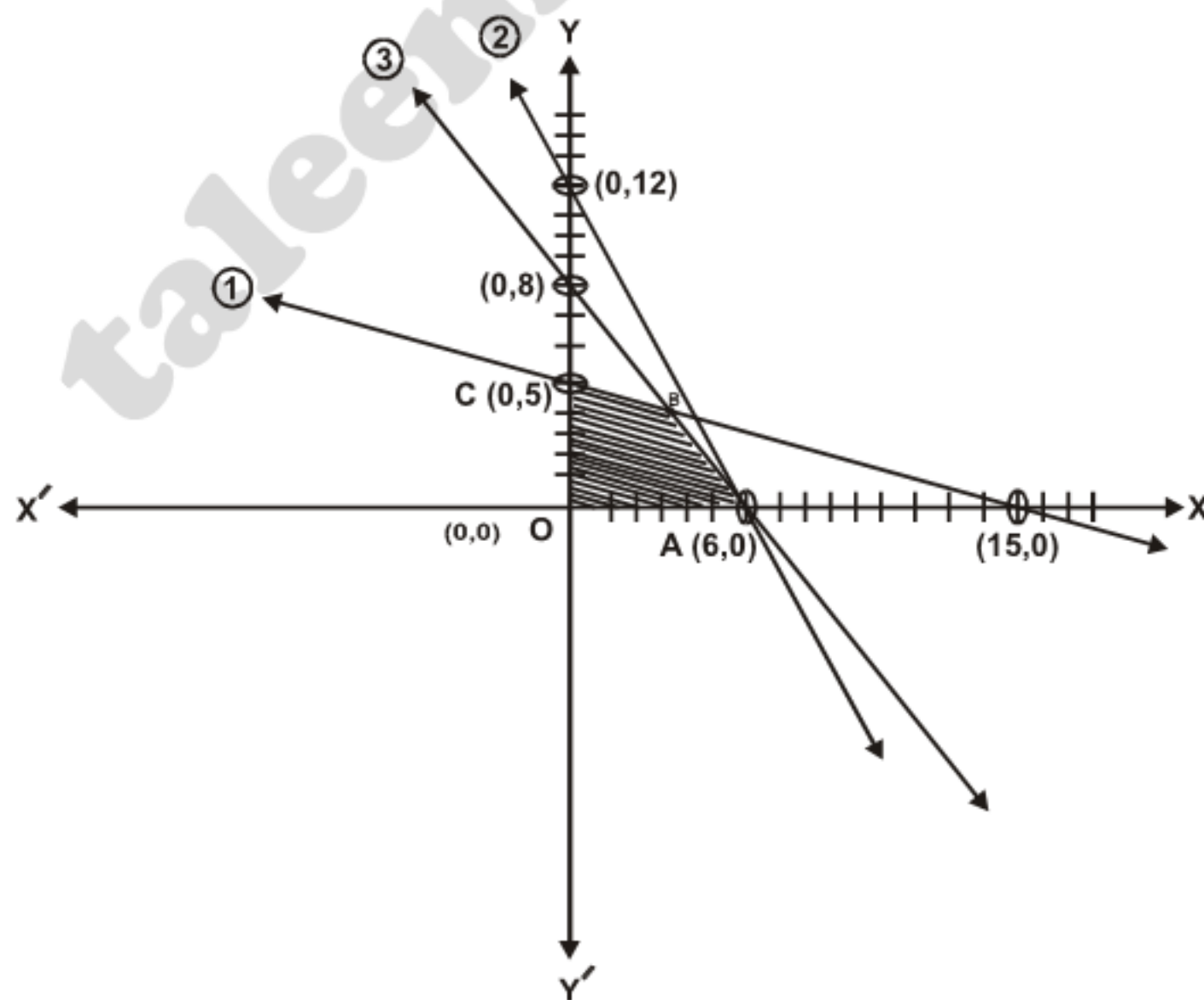
$$4x + 3y < 24$$

$$4(0) + 3(0) < 24$$

$$0 < 24$$

Which is true.

$\therefore$  Graph of an inequality  $4x + 3y \leq 24$  will be towards the origin side.



∴ OABC is the feasible solution region so the corner points are

O (0, 0), A (6, 0), C (0, 5)

To find B solving eq. (1) & eq. (3)

Eq. (1) – Eq. (3), we get

$$\begin{array}{rcl} x + 3y & = & 15 \\ -4x + 3y & = & -24 \\ \hline -3x & = & -9 \\ y & = & \frac{-9}{-3} = 3 \\ \text{Put } x & = & 3 \text{ in eq. (1)} \\ 3 + 3y & = & 15 \\ 3y & = & 15 - 3 \\ 3y & = & 12 \\ y & = & \frac{12}{3} = 4 \end{array}$$

∴ B (3, 4)

(vi)  $2x + y \leq 20$   
 $8x + 15y \leq 120$   
 $x + y \leq 11$   
 $x \geq 0, y \geq 0$

The associated equations are

$$2x + y = 20 \quad \text{..... (1)}$$

$$8x + 15y = 120 \quad \text{..... (2)}$$

$$x + y = 11 \quad \text{..... (3)}$$

x-intercept

Put  $y = 0$  in eqs. (1), (2) and (3)

$$2x + 0 = 20$$

$$2x = 20$$

$$x = \frac{20}{2} = 10$$

∴ Point is (10, 0)

$$8x + 15(0) = 120$$

$$8x = 120$$

$$x = \frac{120}{8} = 15$$

∴ Point is (15, 0)

$$x + 0 = 11$$

$$x = 11$$

∴ Point is (11, 0)

y-intercept

Put  $x = 0$  in eqs. (1), (2) and (3)

$$2(0) + y = 20$$

$$y = 20$$

∴ Point is (0, 20)

$$8(0) + 15y = 120$$

$$15y = 120$$

$$0 + y = 11$$

$$y = 11$$

∴ Point is (0, 11)

$$y = \frac{120}{15} = 8$$

$\therefore$  Point is (0, 8)

### Test Point

Put (0, 0) in

$$2x + y < 20$$

$$2(0) + 0 < 20$$

$$0 < 20$$

Which is true.

$\therefore$  Graph of an inequality  $2x + y \leq 20$  will be towards the origin side.

Put (0, 0) in

$$8x + 15y < 120$$

$$8(0) + 15(0) < 120$$

$$0 < 120$$

Which is true.

$\therefore$  Graph of an inequality  $8x + 15y \leq 120$  will be towards the origin side.

Put (0, 0) in

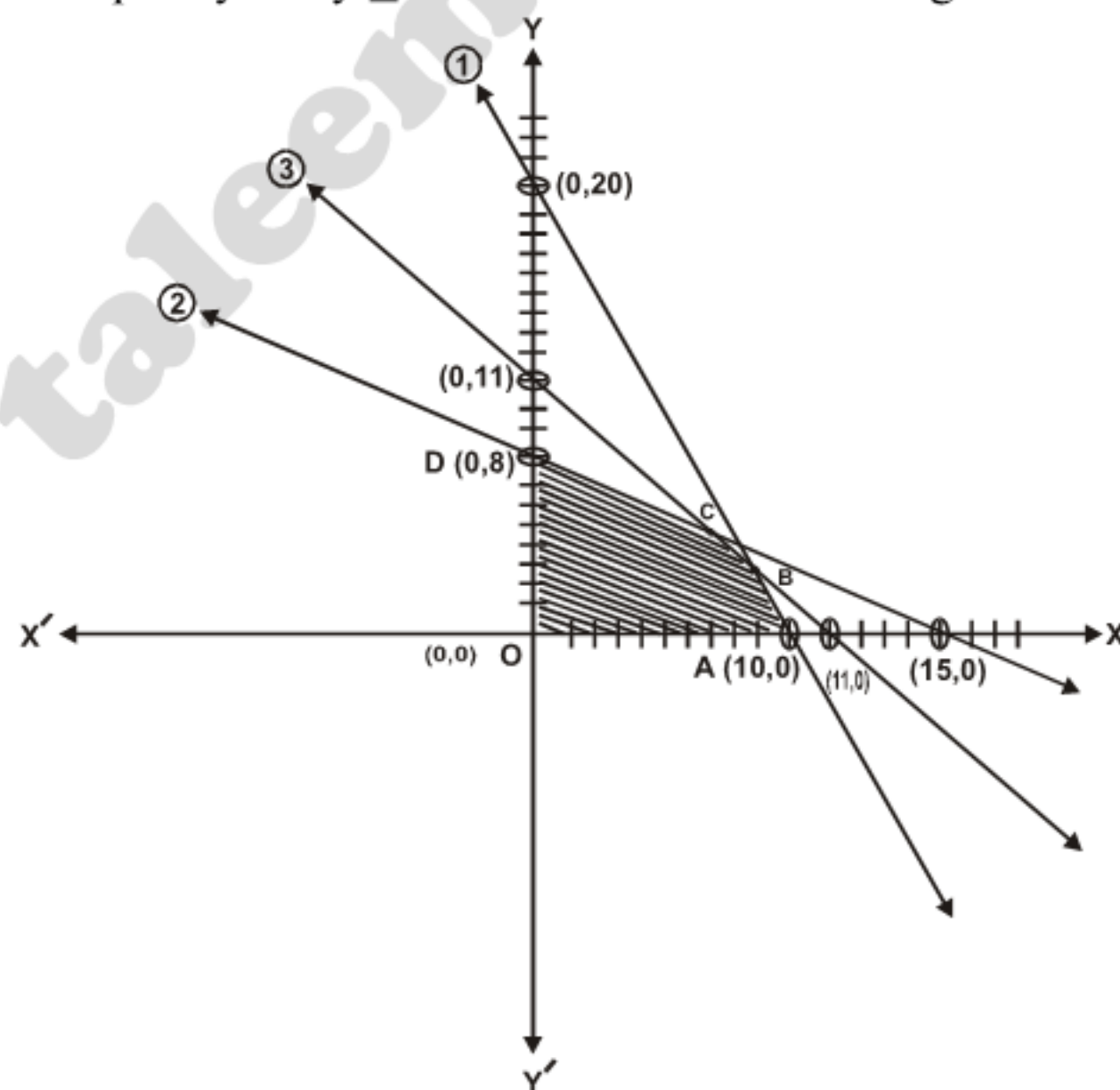
$$x + y < 11$$

$$0 + 0 < 11$$

$$0 < 11$$

Which is true.

$\therefore$  Graph of an inequality  $x + y \leq 11$  will be towards the origin side.



∴ OABCD is the feasible solution region so the corner points are

O (0, 0), A (10, 0), D (0, 8)

To find B solving eq. (1) & eq. (3)

Eq. (1) – Eq. (3), we get

$$\begin{array}{rcl} 2x + y & = & 20 \\ -x + y & = & -11 \\ \hline x & = & 9 \end{array}$$

Put  $x = 9$  in eq. (3)

$$\begin{array}{rcl} 9 + y & = & 11 \\ y & = & 11 - 9 \\ y & = & 2 \end{array}$$

∴ B (9, 2)

To find C solving eq. (2) & eq. (3)

Eq. (2) – Eq. (3) × 8, we get

$$\begin{array}{rcl} 8x + 15y & = & 120 \\ -8x + 8y & = & -88 \\ \hline 23y & = & 32 \\ y & = & \frac{32}{23} \end{array}$$

Put  $y = \frac{32}{23}$  in eq. (3)

$$\begin{array}{rcl} x + \frac{32}{23} & = & 11 \\ x & = & 11 - \frac{32}{23} \\ & = & \frac{253 - 32}{23} \\ & = & \frac{221}{23} \end{array}$$

∴ C  $\left( \frac{221}{23}, \frac{32}{23} \right)$