

## E The description of the main functions for numerical evaluation

The main function is `fmbeta` which implement the optimization using `spg` function in R.

Argument: `data`, `bb`, `A`, `a`, `bg`, `br`

- `data`: the data set for the analysis. the first column is the censoring indicator, the second column is the survival time, the rest of the columns are covariates
- `bb`: initial value of the parameters  $\beta$
- `A`: the R matrix in the manuscript
- `a`: the b matrix in the manuscript
- `bg`: the vector  $\gamma$  in the paper
- `br`: the vector  $r$  in the paper

Values:

- a vector of result, the first element is the vector of estimator for  $\beta$ , the second element is the convergence code from `spg` function in R.