

We are given the following layer partition, for which we request page 3:

a) **layer partition**

layers	L ₀	L ₁	L ₂	L ₃	L ₄	L ₅
pages	1,2	3,4	5,6	7,8	9,10	11,12
created at time t	—	30	40	50	60	70

b) request(3)
yields:

layers	L ₀	L ₁	L ₂	L ₃	L ₄	L ₅
pages	1,2,4	5,6	7,8	9,10	∅	11,12,3
created at time t	—	40	50	60	—	70

The contents of layers L₁ \ {3}, L₂, L₃ and L₄ all have to move **one position to the left**.

Let us see how this is implemented by TStamp:

TStamp

a) **birth array**

		L ₁	L ₂	L ₃	L ₄	L ₅
		↓	↓	↓	↓	↓
array index	0	1	2	3	4	
t	30	40	50	60	70	
v	1	1	1	1	1	
prefix sum of v	1	2	3	4	5	

b) request(3)

array index	0	1	2	3	4	
t	X	40	50	60	70	
v	X	1	1	1	1	
prefix sum of v	X	2	3	4	5	

← Column 0 is deleted (indicated by X).

request(3)
yields:

array index	0	1	2	3	4	
t	40	50	60	70	—	
v	1	1	1	2	—	
prefix sum of v	1	2	3	5	—	

Columns 1 to 4 are moved **one position to the left** (this becomes obvious if we look at the t values).

← v is **updated** to indicate the insertion of an empty set, and the prefix sum is recomputed.

L₁ L₂ L₃ L₅

We can convince ourselves that this reflects the structure of the layer partition.

Recall that the birth array has a maximum length of k. In such a case k-1 columns have to be shifted to the left which is expensive.