

The background is a deep blue gradient with a starry space texture. Overlaid on the left side are several concentric circular patterns, some solid and some dashed, with small arrows indicating a clockwise direction. A large, semi-circular scale is visible, with numerical markings ranging from 140 to 260 in increments of 10. The text is centered on the right side of the image.

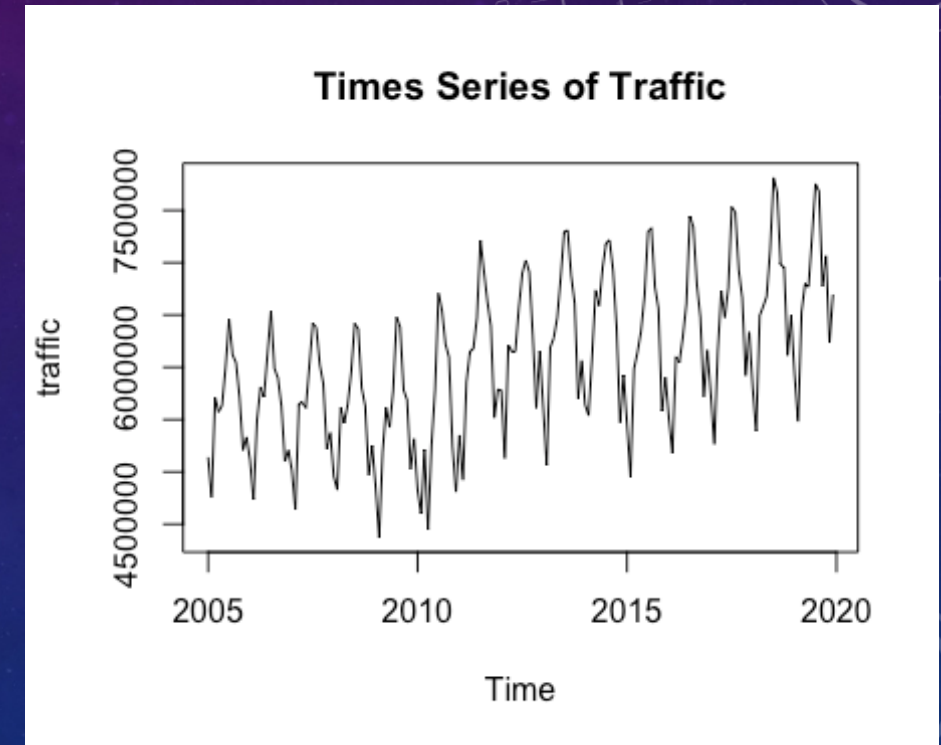
TIME SERIES AND BUSINESS DATA

TIME SERIES PROJECT

FORECAST HEATHROW AIRPORT TRAFFIC TIME SERIES

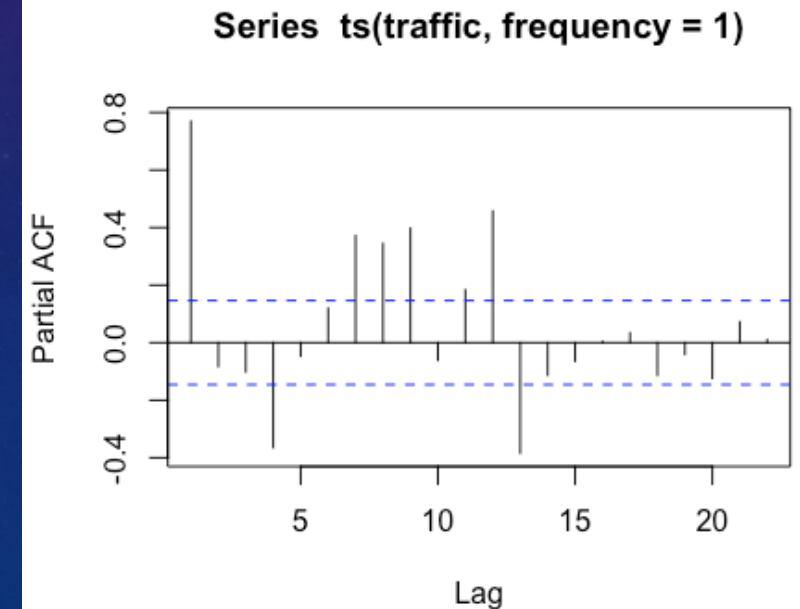
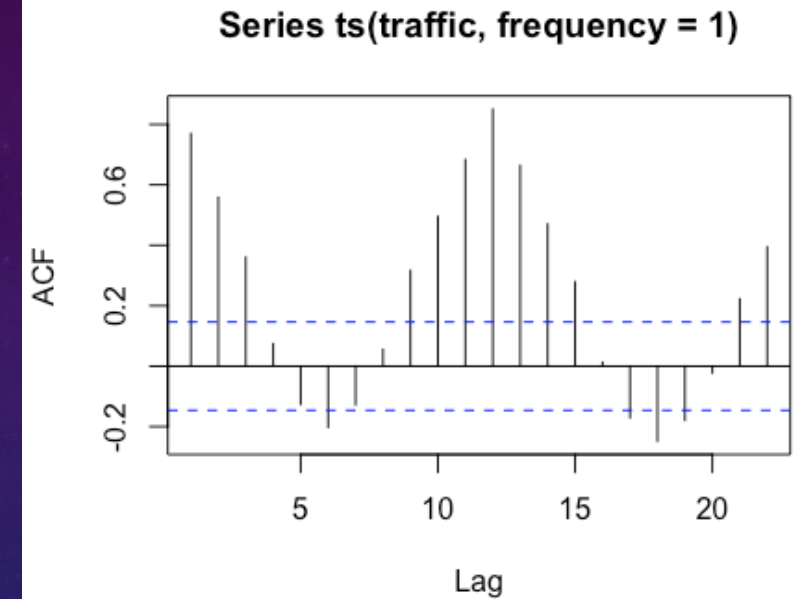
DESCRIPTION OF THE TIME SERIES

- The time series includes the data of monthly traffic of Heathrow Airport, London, The United Kingdom
- From period of January 2005 to December 2019, in total 180 observations
- The data table composes of 3 columns: year, month and traffic of the airport
- The graph of time series shows that it has an increasing trend, changing mean and variance against time
 - Hence the time series is not stationary



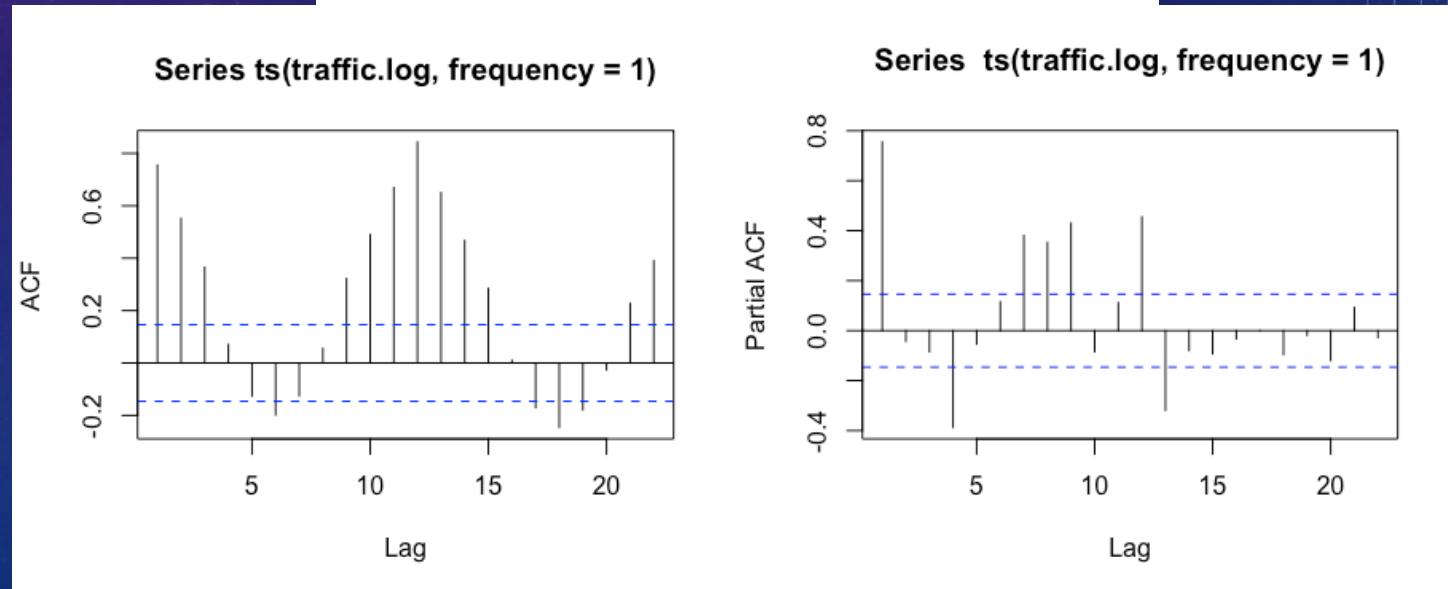
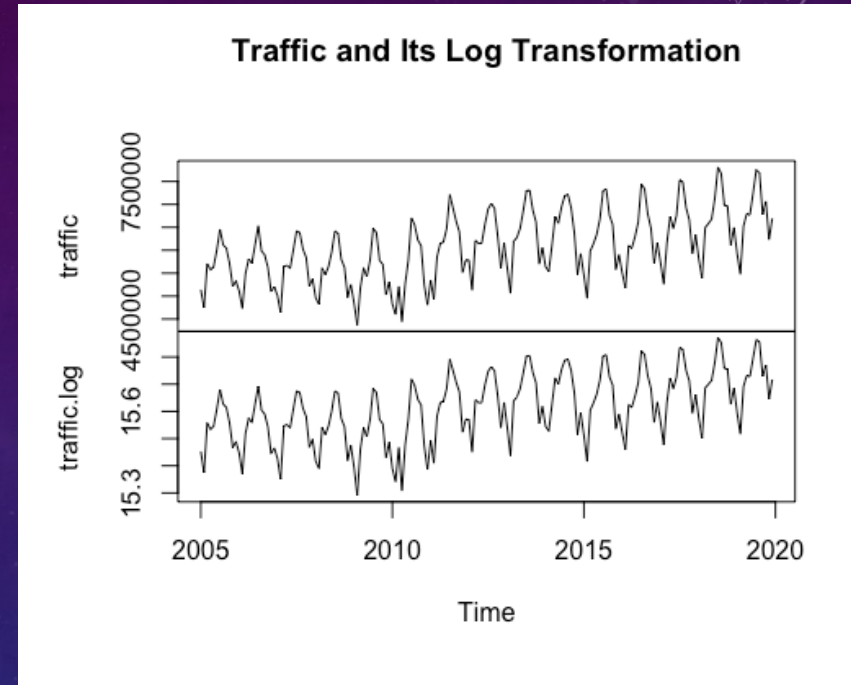
STEP 0: STATIONARIZATION OF DATA

- The upper graph, autocorrelation function (ACF) of original data, shows that the series will not decay to zero
- The lower graph, partial autocorrelation function (PACF) of original data, also shows similar results
- It is necessary to perform a log transformation of the time series to try to reach stationarity



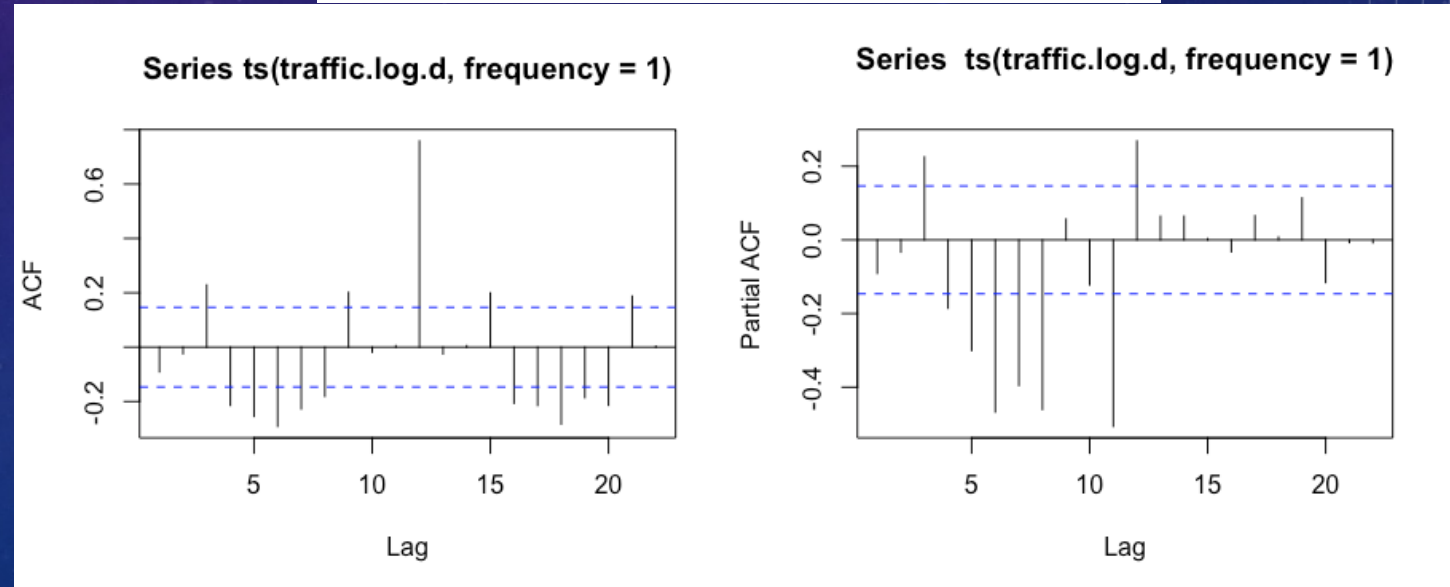
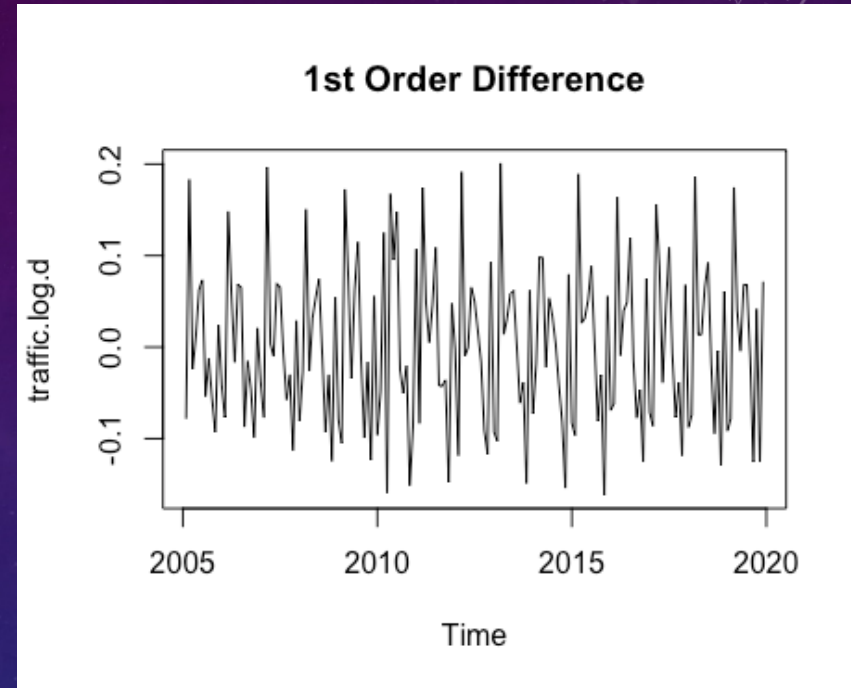
LOG TRANSFORMATION

- The graph of log transformation (upper one) shows that the trend still remains
- The ACF and PACF graphs (below ones) yield similar results
- Need to do further transformations



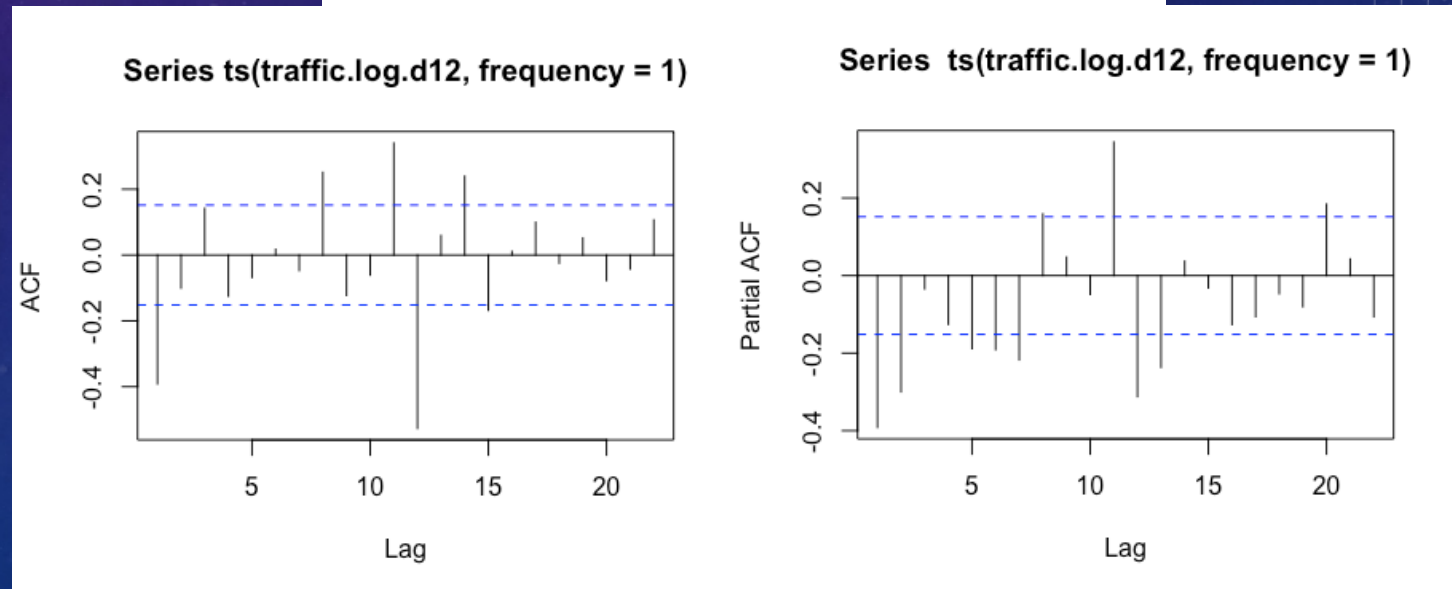
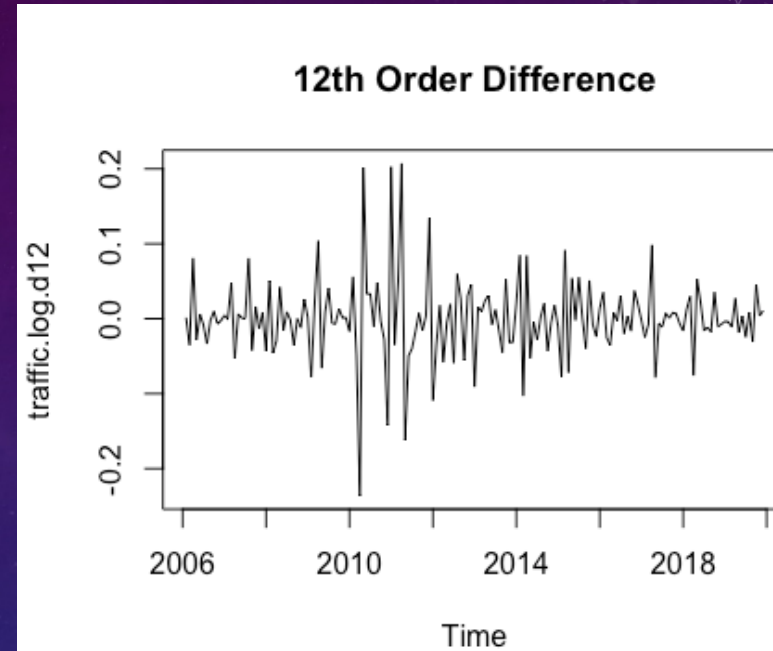
1ST ORDER DIFFERENCE

- 1st order difference is to remove the trend
- The graph of 1st order difference (upper one) indicates that the series is more stationary
- Yet we can clearly see the series is seasonal
- The ACF and PACF graphs (below ones) are more inclined to decay than before transformation.



12TH ORDER DIFFERENCE

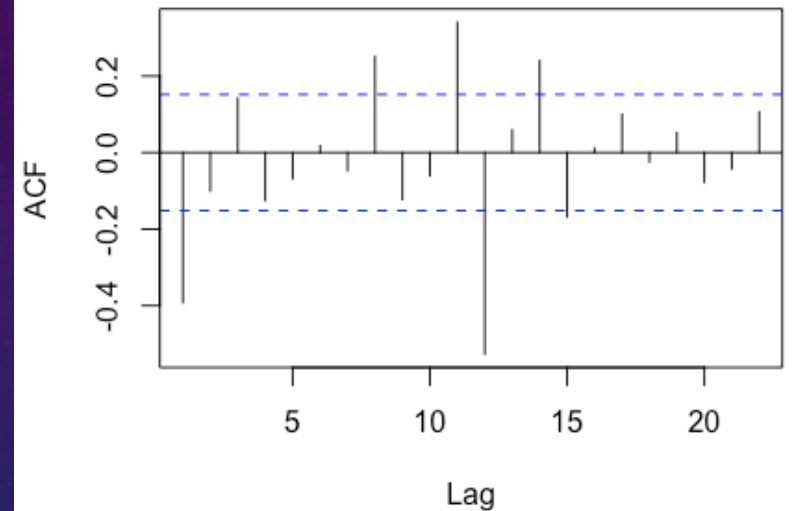
- 12th order difference is to remove the seasonality
- The graph of 12th order difference (upper one) has no seasonality anymore
- The ACF and PACF graphs (below ones) decay to zero faster than before this transformation



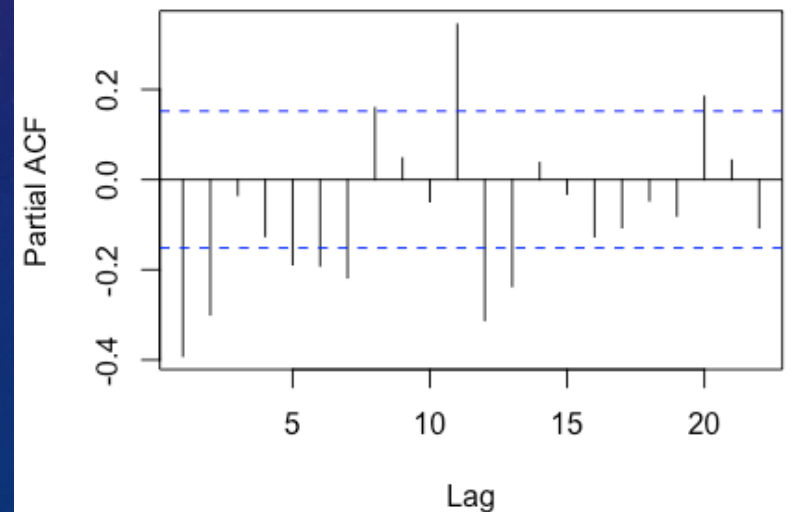
STEP 1: IDENTIFICATION OF ORDERS

- From the graph of ACF (above), we can clearly see that $q = Q = 1$
- From the graph of PACF (below), we can clearly see that $p = P = 2$
- From both graphs, we can deduce $s = 12$

Series ts(traffic.log.d12, frequency = 1)



Series ts(traffic.log.d12, frequency = 1)

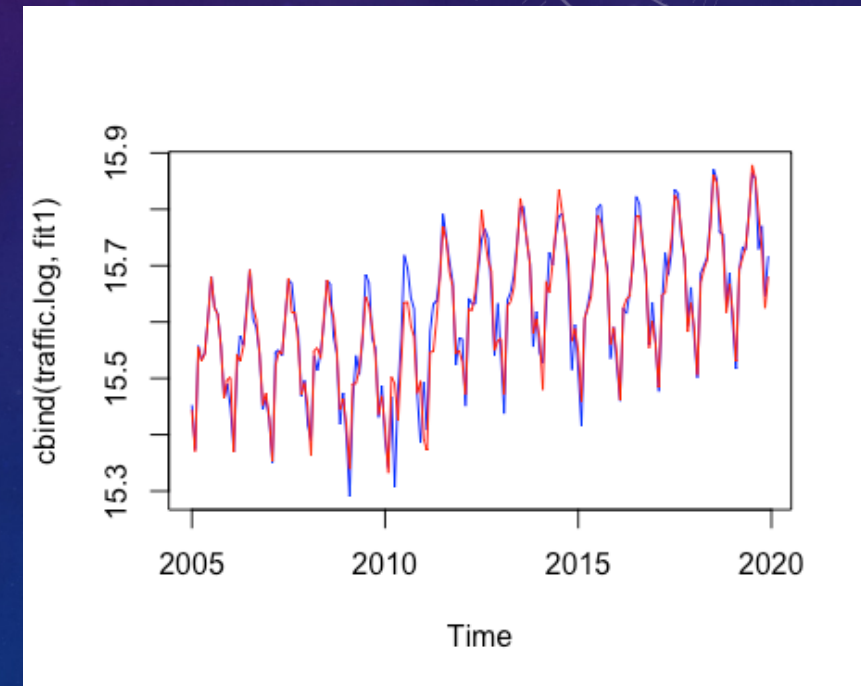


STEP 2: ESTIMATION OF ARMA COEFFICIENTS

- From the orders of the model, we can generate the coefficients of model 1:

ar1	ar2	ma1	sar1	sar2	sma1
0.1929	0.0325	-0.7679	0.0381	0.0594	-0.9999

- A graph of fitted values (in red) is also drawn to predict values and compare with the model



STEP 3: MODEL CHECKING

- Calculate the p values of the coefficients to see whether they are significant

ar1	ar2	ma1	sar1	sar2	sma1
0.068283341	0.714612055	0.000000000	0.636177617	0.449294116	0.003862191

- ar2, sar1 and sar2 are insignificant
- Remove them and re-estimate the model again to generate model 2
- $p = 1, P = 0, q = Q = 1, d = D = 1, s = 12$
- The coefficients would be:

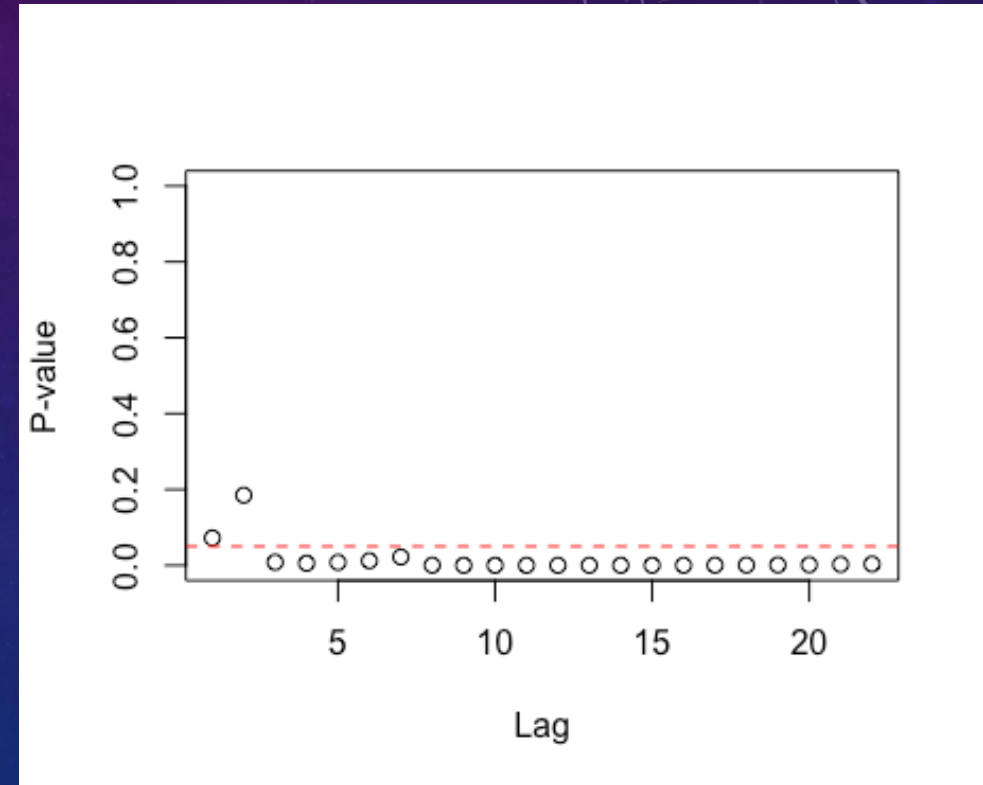
ar1	ma1	sma1
0.1821	-0.7500	-0.9121

STEP 3: MODEL CHECKING

- Check the p values again to see whether they are significant

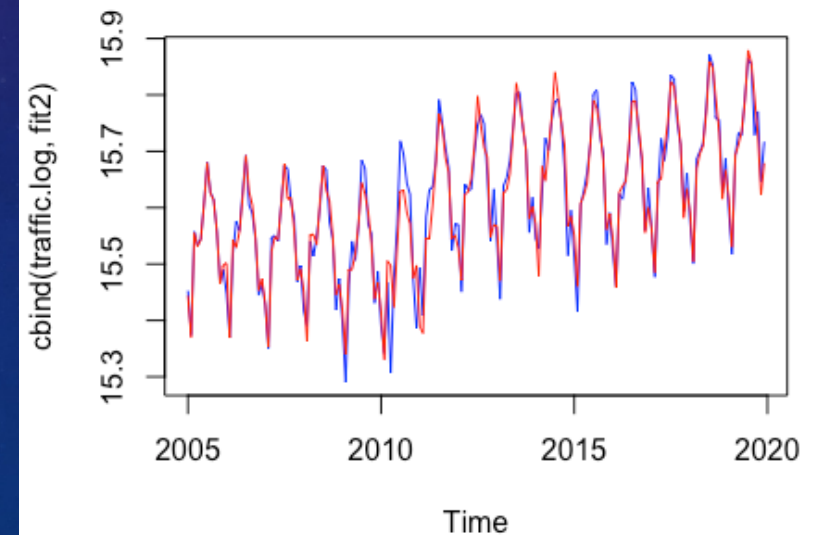
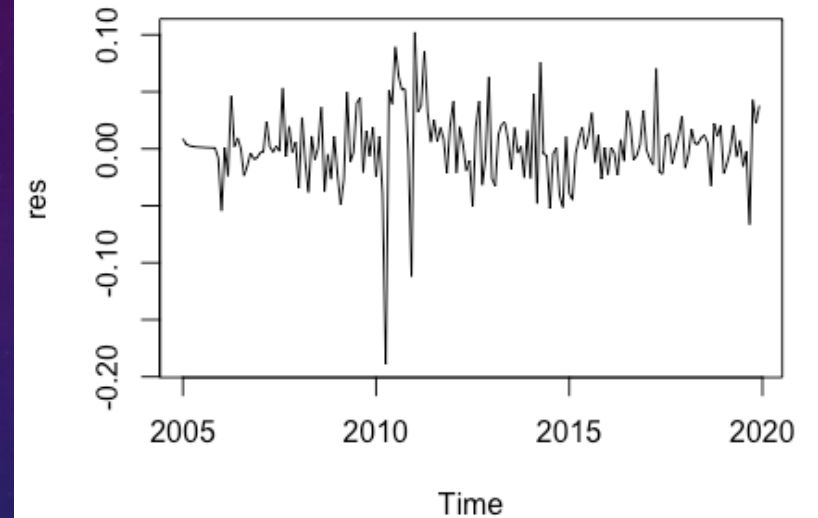
ar1	ma1	sma1
1.090937e-01	0.000000e+00	5.107026e-15

- They are significant
- Perform McLeod Li test to check the model's homoscedasticity
- From the graph, most of the p values are under the red line of 5%
- Reject the null hypothesis, thus the model has heteroscedasticity
- Maybe due to outliers of data



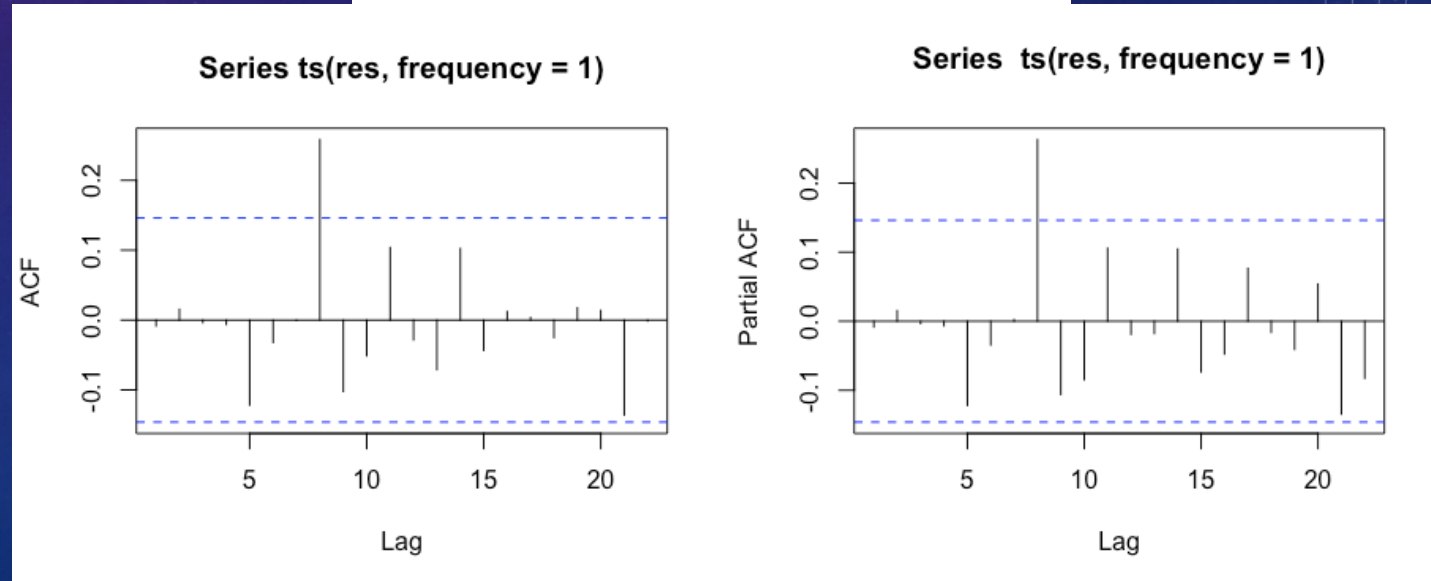
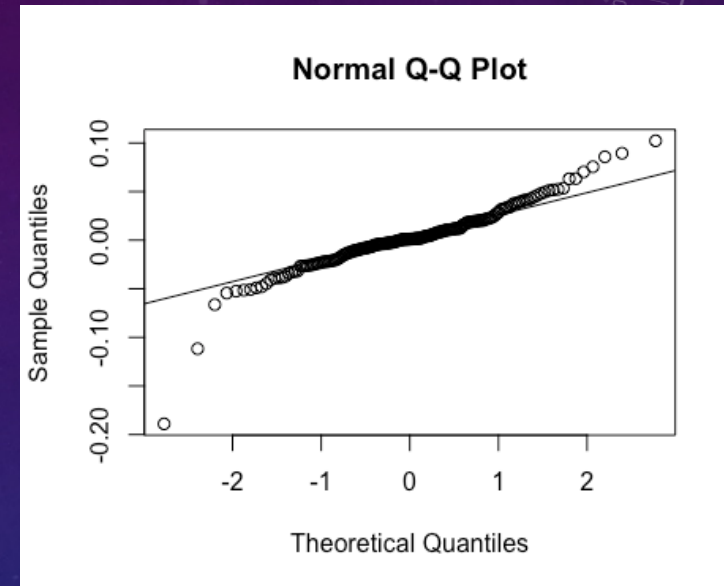
STEP 3: MODEL CHECKING

- Plot the graph of residuals (upper graph)
 - We can clearly see that there are outliers around 2010 and 2011
- Plot its fitted values (lower graph)
 - The line in red is the fitted values
 - It is obvious that the period where outliers are located have caused bigger difference between residuals and fitted values
- Jarque Bera Test obtains p-value $< 2.2e-16$
 - The residuals do not have normal distribution
 - Maybe also due to the outliers



STEP 3: MODEL CHECKING

- From the graph of QQ plot (upper one), we can conclude that the plot is not linear
- The residuals are not normally distributed as there are obvious outliers
- The lower graphs of ACF and PACF of residuals show that there is no autocorrelation as there is no significant coefficient
- The result from Box Ljung test further strengthens the above result:
 - p-value = 0.2335



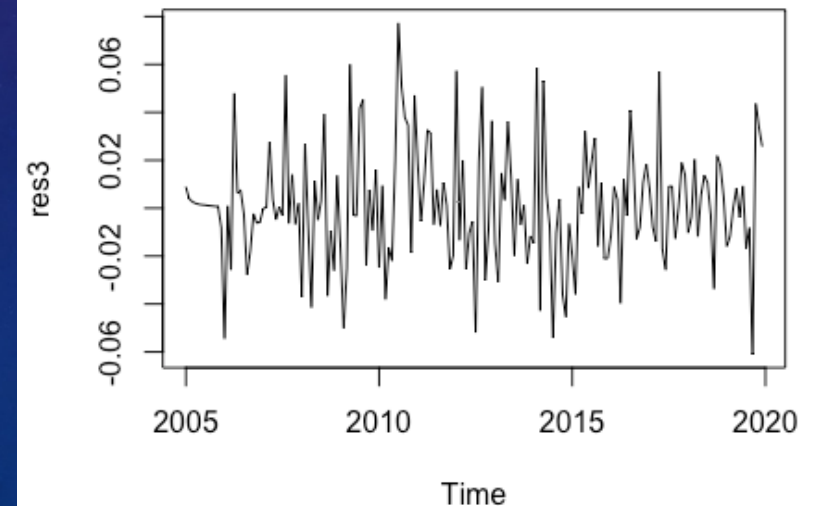
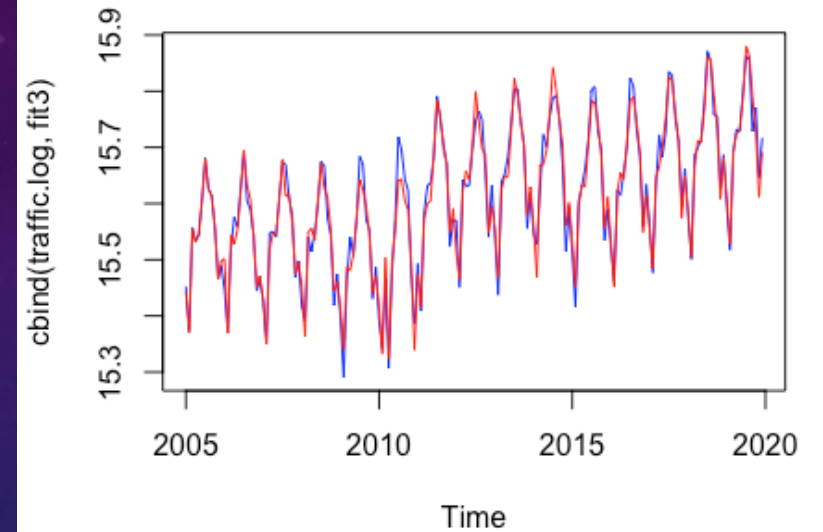
STEP 3: MODEL CHECKING

- The details of outliers:

Date	Value	Traffic
2010.250	-5.650490	4446530
2010.917	-3.339927	4809195

- To deal with the outliers, we assign dummy variables to replace outliers and create model 3 for estimation
- Again we generate the coefficients below, fitted values and residual analysis respectively

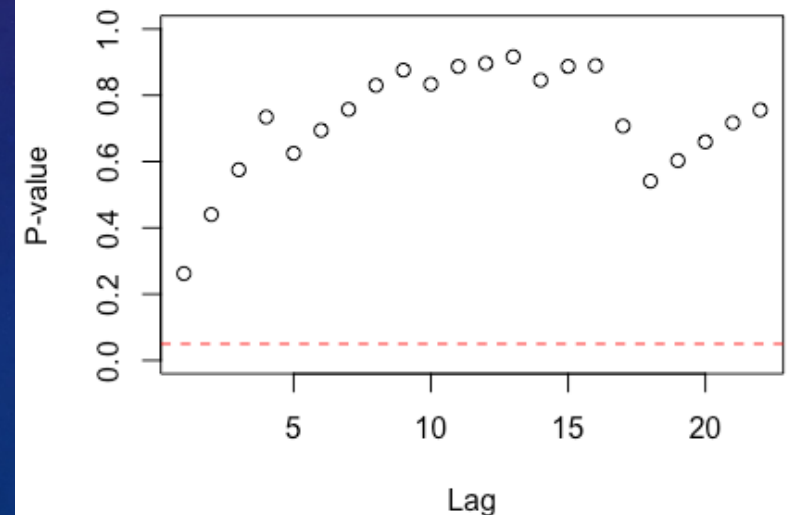
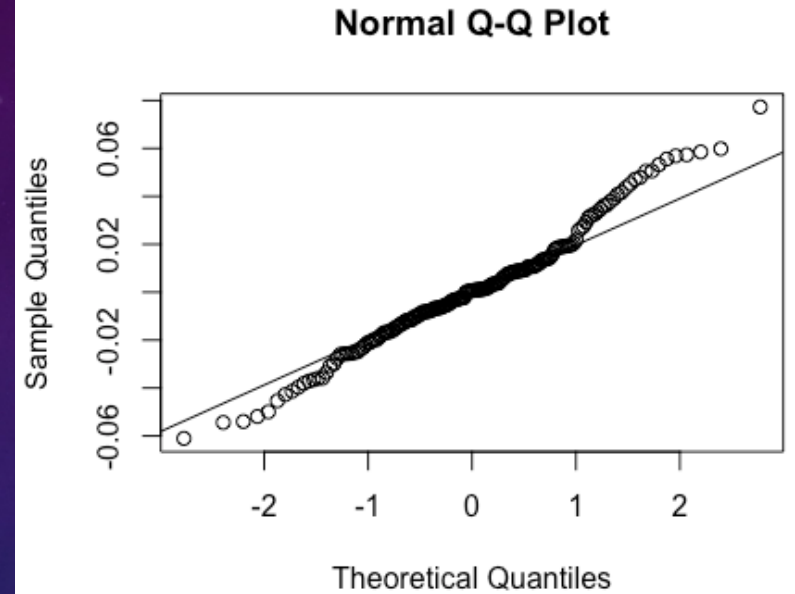
ar1	ma1	sma1	xreg
8.310479e-01	4.703146e-06	0.000000e+00	0.000000e+00



STEP 3: MODEL CHECKING

- Shapiro Test result: p-value = 0.02926
- Jarque Bera Test result: p-value = 0.1637
- Without outliers, the QQ plot of residuals shows that it is linear and normally distributed
 - We can accept that the residuals are normally distributed
- All p values of the graph of McLeod Li test are above 5%
 - Hence the residuals have homoscedasticity
- The AIC and SBC of all models show that model 2 is the best fit
 - It has the lowest values of both AIC and SBC

Model	AIC	SBC
Model 1	-626.2883	-604.4624
Model 2	-631.7395	-619.2676
Model 3 (with dummy values)	-731.0842	-715.4942



STEP 4: PREDICTION

- In-sample and out-of-sample analysis:

In-sample data	Out-of-sample data
Jan 2005 – Jan 2015	Feb 2015 – Dec 2019

- Accuracy:

	ME	RMSE	MAE	MPE	MAPE	ACF1
Test set	0.01729778	0.03286758	0.02643252	0.1096912	0.1682953	0.376278

- ME, RMSE, MAE are relatively small, showing that the model is at least 96.8% accurate which is a good model
- MPE and MAPE are higher but still the majority of the model is accurate
- ACF at lag 1 has the correlation between first and next point is around 0.37, showing that there is an exponential decrease

STEP 4: PREDICTION

- Plot the graph of quality of fit for examination
- Calculate the proportion of points in the confidence bound to see how good the fit is: 86.11%
- The fit is good
- The predicted values for 3 months are shown in red
- The dotted lines show the upper and lower confidence level

