

1 Class 1

1.1 相位因子估计

$$X = HZH$$

$$X|0\rangle = |1\rangle$$

$$X|1\rangle = |0\rangle$$

$$X\left(\frac{|0\rangle + |1\rangle}{\sqrt{2}}\right) = 1 * \frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

$$X\left(\frac{|0\rangle - |1\rangle}{\sqrt{2}}\right) = (-1) * \frac{|0\rangle - |1\rangle}{\sqrt{2}}$$

在 n 维空间里

$$X|n\rangle = |n+1\rangle$$

$$X^N = I$$

$$\omega_N = \exp\left(\frac{2\pi i}{N}\right)$$

$$\omega_0, \omega_1, \dots, \omega_{N-1}$$

$$X = FZF^+$$

$$F|k\rangle = \frac{1}{\sqrt{N}} \sum_{j=0}^{N-1} \omega^{kj} |j\rangle$$

$$F = \left(\frac{1}{\sqrt{N}} \omega^{kj}\right)_{N \times N} \quad \omega = e^{\frac{2\pi i}{N}} \quad N = 2^n$$

$$|\hat{k}\rangle = F|k\rangle = \frac{1}{\sqrt{2^n}} \sum_{j=0}^{2^n-1} \omega^{kj} |j\rangle$$