

1 Class 1

1.1 Preview 1

$$|c, t\rangle \rightarrow |c, t \oplus c\rangle$$

若 $c=0$, 则对 t 不做操作, 若 $c=1$, 则对 t 逻辑取反
CNOT + 单个量子比特门可以做一切操作

2 Class 2, 3: Simulation

$$|\psi(t)\rangle = e^{-iHt}|\psi(0)\rangle$$

$$|\psi(t)\rangle = U(t)|\psi(0)\rangle$$

$$U = e^{-iK}$$

- input

$$H \quad |\psi(0)\rangle \quad t_f \quad \epsilon$$

- output

$$|\tilde{\psi}(t_f)\rangle \geq s.t.$$

$$|\langle \tilde{\psi}(t_f) | e^{iHt_f} | \psi(0) \rangle| \geq 1 - \epsilon$$

H: 哈密顿量

$$H = \sum_{k=1}^{poly(n)} H_k \quad H_k \text{ 是作用于常数个系统的哈密顿量}$$

$$H = \sum_{k=1}^{n-1} X_k \oplus X_{k+1}$$

$$e^{i(H_1+H_2)} = e^{iH_1} * e^{iH_2} \quad \text{if} \quad [H_1, H_2] = 0$$

$$e^{i(H_1H_2)} = \lim_{n \rightarrow \infty} (e^{i\frac{H_1}{n}} e^{i\frac{H_2}{n}})^n$$