

Notes

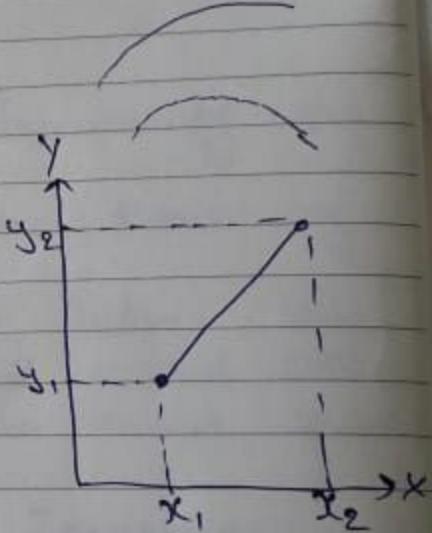
- Output Primitives →  
 Points and lines →  
 → Point is the fundamental element of picture representation.  
 → It is the position in the plane defined as either the pair or triplet of numbers depending upon the dimension.  
 → Two points represent line or edge & 3 or more points a Polygon.  
 → Curved lines are represented by short straight lines.

\* Line drawing Algorithms →

→ Slope - Intercept Equation  
 $y = mx + b$

→ Slope →  
 $m = \frac{y_2 - y_1}{x_2 - x_1}$

→ Intercept →  
 $b = y_1 - mx_1$



→ Interval Calculation →

$$\Delta y = m \Delta x \quad \Delta x = \frac{\Delta y}{m}$$

→ The process of 'turning on' the pixels of a line segment is called as vector generation or line generation & the algorithms for them are known as vector generation algorithm or line generation algorithm or drawing.

Notes

- Des
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- Line
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- bright
- length
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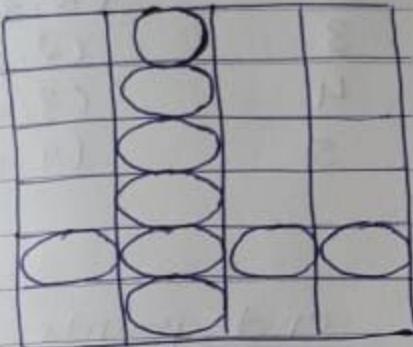
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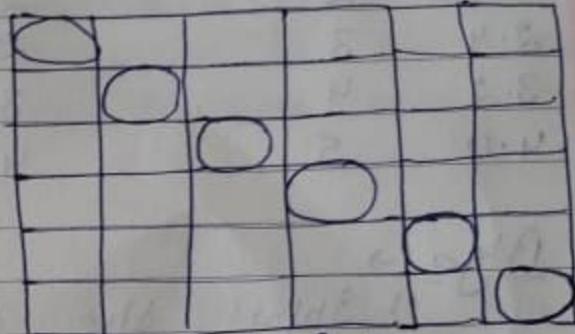
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## Notes

- Desired characteristics of a line →
  - o The line should appear as a straight line & it should start and end accurately.
  - o The line should be displayed with constant brightness along its length, independent of its length and orientation.
  - o The line should be drawn rapidly.



Vertical & Horizontal lines



45° line.

- DDA Algorithm → (Digital differential Analyzer)
  - o Sample the line at unit intervals in one coordinate.
- Determine the corresponding integer values nearest the line path in another coordinate.

$$\text{Slope} \Rightarrow m = \frac{y_{k+1} - y_k}{x_{k+1} - x_k} = \frac{\Delta y}{\Delta x}$$

$$|m| < 1$$

$$\rightarrow \Delta y < \Delta x$$

$$\rightarrow x_{k+1} = x_k + 1$$

$$\rightarrow y_{k+1} = y_k + m$$

$$|m| > 1$$

$$\rightarrow \Delta y > \Delta x$$

$$\rightarrow y_{k+1} = y_k + 1$$

$$\rightarrow x_{k+1} = x_k + \frac{1}{m}$$

$$|m| = 1$$

$$\Delta y = \Delta x$$

$$\rightarrow y_{k+1} = y_k + 1$$

$$\rightarrow x_{k+1} = x_k + 1$$

Notes

Example → Draw a line b/w  $(0,0)$  to  $(4,5)$   
Sol:  $m = \frac{5-0}{4-0} > 1$   $\frac{1}{m} = \frac{4}{5} \Rightarrow 0.8$

X	Y	$X_{Plot}$	$Y_{Plot}$	$(X, Y)$
0	0	0	0	$(0, 0)$
0.8	1	1	1	$(1, 1)$
1.6	2	2	2	$(2, 2)$
2.4	3	2	3	$(2, 3)$
3.2	4	3	4	$(3, 4)$
4.0	5	4	5	$(4, 5)$

Alg: →

- 1) Input the two line end points & store the left endpoint in  $(x_0, y_0)$ .
- 2) Plot the first point  $(x_0, y_0)$ .
- 3) Calculate constants  $\Delta x$  &  $\Delta y$ .
- 4) If  $|\Delta x| > |\Delta y|$  steps =  $\Delta x$  else steps =  $\Delta y$
- 5) Calculate  $x_{inc} = |\Delta x| / \text{steps}$  &

$$y_{inc} = |\Delta y| / \text{steps}$$

- 6) At each  $x_k$  along the line, starting at  $k=0$ , plot the next pixel at  $(x_k + x_{inc}, y_k + y_{inc})$ .

- 7) Repeat step 6 several times.

Example 2 draw a line b/w  $(10, 15)$  &  $(15, 30)$ .

## Notes

### Advantages of DDA Algorithm :-

- 1) It is the simplest algorithm & it does not require special skills for implementation.
- 2) It is faster method for calculating pixel positions than the direct use of Equation  $y=mx+b$ . It eliminates the multiplication in the equation by making use ofoller Characteristics, so that appropriate increment are applied in the x or y directions to find the pixel position along the line path.

### Disadvantages :-

- 1) Floating point arithmetic in DDA is still time consuming.
- 2) The algorithm is orientation dependent. So the end point accuracy is poor.

### Code :-

```
#include <graphics.h>
#include <stdio.h>
#include <math.h>
#include <dos.h>
```

```
void main()
```

```
{ float x, y, x1, y1, x2, y2, dx, dy, step;
int i, gd = DETECT, gm;
```

```
initgraph(&gd, &gm, "C:\turboc3\bg1");
```

```
printf("Enter the value of x1 & y1");
```

## Notes

### \* Bresenham's Algorithm :-

→ Uses only incremental integer calculations.  
 → For  $|m| < 1$

o Start from left end point  $(x_0, y_0)$  Step to each successive column (x samples) & plot the pixel whose scan line y value is closest to the line path.

→ After  $(x_k, y_k)$  the choice could be  $(x_{k+1}, y_k)$  or  $(x_k, y_{k+1})$ .

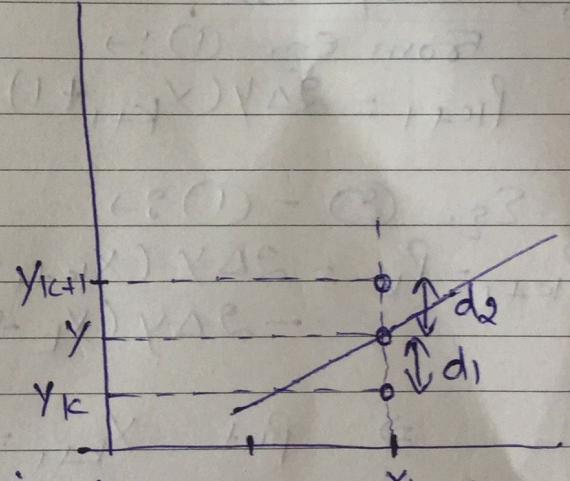
$$y = m(x_{k+1}) + c$$

$$d_1 = y - y_k$$

$$d_1 = m(x_{k+1}) + c - y_k$$

$$d_2 = y_{k+1} - y$$

$$d_2 = y_{k+1} - m(x_{k+1}) - c$$



Difference b/w separation :-

$$d_1 - d_2 = m(x_{k+1}) + c - y_k - y_{k+1} + m(x_{k+1}) + c$$

$$d_1 - d_2 = 2m(x_{k+1}) - 2y_k + 2c - 1$$

Defining Decision Parameter :-

$$P_k = \Delta x (d_1 - d_2)$$

Putting the value of  $(d_1 - d_2)$  :-

$$P_k = \Delta x [2m(x_{k+1}) - 2y_k + 2c - 1]$$

$$\Rightarrow \Delta x [2 \frac{\Delta y}{\Delta x} (x_{k+1}) - 2y_k + 2c - 1]$$

$$\Rightarrow 2\Delta y (x_{k+1}) - 2\Delta x y_k + 2\Delta x c - \Delta x$$

$$\Rightarrow 2\Delta y (x_{k+1}) - 2\Delta x y_k + \Delta x (2c - 1) - ①$$

Notes

$$\text{As, } y = mx_k + c$$

$$c = y_k - mx_k$$

$$c = y_k - \frac{\Delta y}{\Delta x} \cdot x_k$$

Put the value of  $c \Rightarrow$

$$\Rightarrow 2\Delta y(x_{k+1}) - 2\Delta x y_k + \Delta x(2y - 2x \frac{\Delta y}{\Delta x} - 1)$$

$$\Rightarrow 2\Delta y(x_{k+1}) - 2\Delta x y_k + 2\Delta x y_k - 2x_k \Delta y - \Delta x$$

$$\Rightarrow 2\Delta y x_{k+1} + 2\Delta y - 2\Delta x y_k + 2\Delta x y_k - 2x_k \Delta y - \Delta x$$

$$P_0 \Rightarrow 2\Delta y - \Delta x$$

From eq. (1) :-

$$P_{k+1} = 2\Delta y(x_{k+1} + 1) - 2\Delta x y_{k+1} + \Delta x(2c - 1) - \textcircled{2}$$

$$\Sigma_2, \textcircled{2} - \textcircled{1} \Rightarrow$$

$$P_{k+1} - P_k = 2\Delta y(x_{k+1} + 1) - 2\Delta x y_{k+1} + \Delta x(2c - 1) \\ - 2\Delta y(x_k + 1) + 2\Delta x y_k - \Delta x(2c - 1)$$

$$\Rightarrow \text{Put } x_{k+1} = x_k + 1$$

$$\Rightarrow 2\Delta y(x_k + 2) - 2\Delta x y_{k+1} + \Delta x(2c - 1) \\ - 2\Delta y(x_k + 1) + 2\Delta x y_k - \Delta x(2c - 1)$$

$$\Rightarrow 2\Delta y x_k + 4\Delta y - 2\Delta x y_{k+1} \\ - 2\Delta x x_k - 2\Delta y + 2\Delta x y_k$$

$$\Rightarrow 2\Delta y - 2\Delta x(y_{k+1} - y_k)$$

$$P_{k+1} = P_k + 2\Delta y - 2\Delta x(y_{k+1} - y_k)$$

$$\text{If } P_0 \geq 0$$

$$\left[ \begin{array}{l} P_{k+1} = P_k + 2\Delta y - 2\Delta x \\ \because y_{k+1} - y_k = 1 \end{array} \right]$$

$$\text{If } P_0 < 0, \left[ \begin{array}{l} P_{k+1} = P_k + 2\Delta y \\ \because y_{k+1} - y_k = 0 \end{array} \right]$$

# Notes

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3

Algorithm :-

- 1) Input the two line end points & store the left end point in  $(x_0, y_0)$ .
- 2) Plot first point  $(x_0, y_0)$ .
- 3) Calculate constants  $\Delta x$ ,  $\Delta y$ ,  $2\Delta y - 2\Delta x$  & Obtain  $P_0 = 2\Delta y - \Delta x$ .
- 4) At each  $x_k$  along the line, starting at  $k=0$  perform the following test:  
If  $P_k < 0$ , the next point plot is  $(x_{k+1}, y_k)$   
&  $P_{k+1} = P_k + 2\Delta y$
- Otherwise, the next point to plot is  $(x_{k+1}, y_{k+1})$   
 $P_{k+1} = P_k + 2\Delta y - 2\Delta x$

5) Repeat step 4  $\Delta x$  times.

Example :- Endpoints :-  $(20, 10)$  &  $(30, 18)$

Sol:- Slope :-  $\frac{18-10}{30-20} = \frac{8}{10} = 0.8 < 1$

$$\Delta x = 30 - 20 = 10 \quad P_0 = 2 \times 8 - 10 = 6$$

$$\Delta y = 18 - 10 = 8 \quad 2\Delta y - 2\Delta x = -4$$

Plot  $(x_0, y_0) = (20, 10)$

K	$P_k$	$(x_{k+1}, y_{k+1})$
0	6	$(21, 11)$
1	2	$(22, 12)$
2	-2	$(23, 12)$
3	14	$(24, 13)$
4	10	$(25, 14)$
5	6	$(26, 15)$
6	2	$(27, 16)$
7	-2	$(28, 16)$
8	14	$(29, 17)$
9	10	$(30, 18)$

Example 2

$(15, 18)$  to  $(10, 15)$

## Notes

Advantage :- Involves only the calculation of constants  $\Delta x, \Delta y, 2\Delta y, 2\Delta y - 2\Delta x$  once & integer addition & subtraction in each step.

### \* Circle Generating Algorithm :-

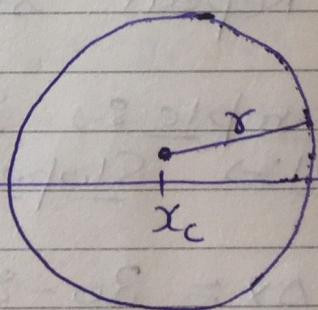
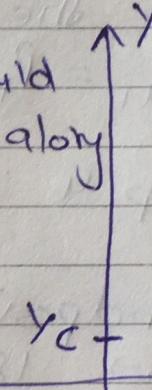
#### Basic foundation :-

circle Equation  $\Rightarrow$

$$(x - x_c)^2 + (y - y_c)^2 = r^2$$

Point along circumference could be calculated by stepping along x-axis  $\Rightarrow$

$$y = y_c \pm \sqrt{r^2 - (x_c - x)^2}$$



#### Problem in above method :-

$\rightarrow$  Computational Complexity.

$\rightarrow$  Spacing: Non uniform spacing of plotted pixels

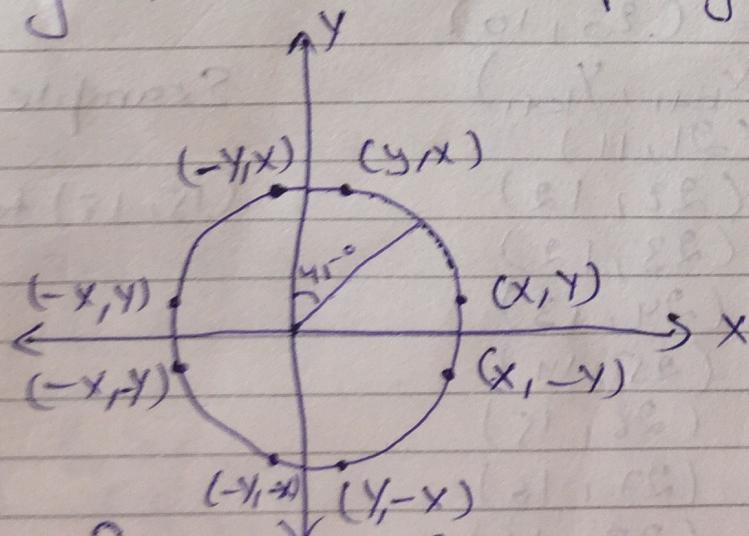


Fig. circle symmetry.

NotesMid-Point circle Algorithm :-

→ Circle function defined as  $f_{\text{circle}}(x, y) = x^2 + y^2 - r^2$

→ Any point  $(x, y)$  satisfy the following conditions :-

$$f_{\text{circle}}(x, y) \begin{cases} < 0 & \text{if } (x, y) \text{ is inside the circle boundary} \\ = 0 & \text{if } (x, y) \text{ is on the circle boundary} \\ > 0 & \text{if } (x, y) \text{ is outside the circle boundary.} \end{cases}$$

→ Decision parameter in the circle functions

$x$ - unit intervals.

$y_k$  or  $y_{k-1}$

So the plotting points will be either  $(x_{k+1}, y_k)$  or  $(x_{k+1}, y_{k-1})$ .

$$\text{Mid point} \Rightarrow \left( \frac{x_k + 1 + x_{k+1}}{2}, \frac{y_k + y_{k-1}}{2} \right)$$

$$\Rightarrow \left( x_k + \frac{1}{2}, y_k - \frac{1}{2} \right)$$

$$\Rightarrow x^2 + y^2 = r^2$$

$$P_k = x^2 + y^2 - r^2$$

put the values of  $x$  &  $y$  :-

Notes

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$$P_{lc} = (x_{lc} + 1)^2 + (y_{lc} - \frac{1}{2})^2 - \gamma^2$$

$$P_{k+1} = (x_{k+1} + 1)^2 + (y_{k+1} - \frac{1}{2})^2 - \gamma^2$$

$$\Rightarrow ((x_k + 1) + 1)^2 + (y_{k+1} - \frac{1}{2})^2 - \gamma^2$$

$$P_{k+1} - P_{lc} \Rightarrow ((x_{lc} + 1) + 1)^2 + (y_{k+1} - \frac{1}{2})^2 - \gamma^2 - (x_{lc} + 1)^2 - (y_{lc} - \frac{1}{2})^2 + \gamma^2$$

$$\Rightarrow (x_{lc} + 1)^2 + 1 + 2(x_k + 1) - (x_{lc} + 1)^2 - (y_{lc} - \frac{1}{2})^2$$

$$\Rightarrow 2(x_k + 1) + y_{k+1}^2 + \cancel{y_{lc}^2} - y_{k+1}^2 - \cancel{y_k^2} - \cancel{x_{lc}^2} + y_k + 1$$

$$\Rightarrow 2(x_k + 1) + (y_{k+1}^2 - y_k^2) - (y_{k+1} - y_k) + 1$$

$$P_{lc+1} = P_{lc} + 2(x_k + 1) + (y_{k+1}^2 - y_k^2) - (y_{k+1} - y_k) + 1$$

Initial decision parameter is

$$x_{lc} = 0, y_k = \gamma$$

$$P_0 = (0 + 1)^2 + (\gamma - \frac{1}{2})^2 - \gamma^2$$

$$= 1 + \gamma^2 + \frac{1}{4} - 2 \cdot \frac{\gamma}{2} - \gamma^2$$

$$\Rightarrow \frac{5}{4} - \gamma$$

$$\boxed{P_0 \Rightarrow 1 - \gamma}$$

$$P_{lc} \geq 0$$

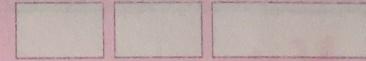
$$y_{k+1} = y_k - 1$$

$$(x_{lc+1}, y_{lc-1})$$

$$P_k < 0$$

$$y_{k+1} = y_k$$

$$(x_{k+1}, y_k)$$



# Notes

Example: Plot a circle of radius 8 cm using midpoint algorithm.

Sol:  $\rightarrow r = 8$

$$P_0 = 1 - r$$

$$P_{k+1} = P_k + 2(x_{k+1}) + (y_{k+1}^2 - y_k^2) - (y_{k+1} - y_k) + 1$$

K	$(x_k, y_k)$	$P_k$	$(x_{k+1}, y_{k+1})$
0	$(0, 8)$	-7	$(1, 8)$
1	$(1, 8)$	-4	$(2, 8)$
2	$(2, 8)$	+1	$(3, 7)$
3	$(3, 7)$	-6	$(4, 7)$
4	$(4, 7)$	+2	$(5, 6)$
5	$(5, 6)$	+1	$(6, 5)$ $\rightarrow (x_7, y)$ <u>STOP</u>

$(x, y)$	$(-x, y)$	$(x, -y)$	$(-x, -y)$
$(0, 8)$	$(0, 8)$	$(0, -8)$	$(0, -8)$
$(1, 8)$	$(-1, 8)$	$(1, -8)$	$(-1, -8)$
$(2, 8)$	$(-2, 8)$	$(-2, -8)$	$(2, -8)$
$(3, 7)$	$(-3, 7)$	$(3, -7)$	$(-3, -7)$
$(4, 7)$	$(-4, 7)$	$(4, -7)$	$(-4, -7)$
$(5, 6)$	$(-5, 6)$	$(5, -6)$	$(-5, -6)$
$(6, 5)$	$(-6, 5)$	$(6, -5)$	$(-6, -5)$
$(7, 4)$	$(-7, 4)$	$(7, -4)$	$(-7, -4)$
$(7, 3)$	$(-7, 3)$	$(7, -3)$	$(-7, -3)$
$(8, 2)$	$(-8, 2)$	$(8, -2)$	$(-8, -2)$
$(8, 1)$	$(-8, 1)$	$(8, -1)$	$(-8, -1)$
$(8, 0)$	$(-8, 0)$	$(8, 0)$	$(-8, 0)$

Example 32  
 $r = 10$

Note If  $P_k < 0$   
 $y_{k+1} = y_k$

If  $P_k \geq 0$   
 $y_{k+1} = y_k - 1$

$$P_{k+1} = P_k + 2(x_{k+1}) + 1$$

$$P_{k+1} = P_k + 2(x_{k+1}) + 1 - 2y_{k+1}$$

# Notes

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Algorithm :-

1) Input radius  $r$  and circle center  $(x_0, y_0)$  and obtain the first point of the circumference of circle centered on the origin as  $\frac{r}{2}$ .  
 $(x_0, y_0) = (0, r)$

2) Calculate the initial value of the decision parameter as  $\frac{r}{4}$ .

$$P_0 = \frac{5}{4} - r$$

3) At each  $x_k$  position, starting at  $k=0$ , perform the following test :-  
if  $P_k < 0$ , the next point along the circle centered at  $(0, 0)$  is  $(x_{k+1}, y_{k+1})$  &

$$P_{k+1} = P_k + 2(x_k + 1) + 1$$

Otherwise, the next point along the circle centered at  $(0, 0)$  is  $(x_{k+1}, y_{k+1})$ . &

$$P_{k+1} = P_k + 2(x_k + 1) - 2y_{k+1} + 1$$

4) Determine the symmetry points in the other seven octants.

5) Move each calculated pixel position  $(x, y)$  on to the circular path

$$X = x + x_0 \quad Y = y + y_0$$

6) Repeat step 3 through 5 until  $x \geq y$ .

# Notes

## Inside Outside Test

→ Odd Even Rule  
→ Odd Edge means interior

→ Non zero winding Number rule  
→ Non zero winding number means interior.

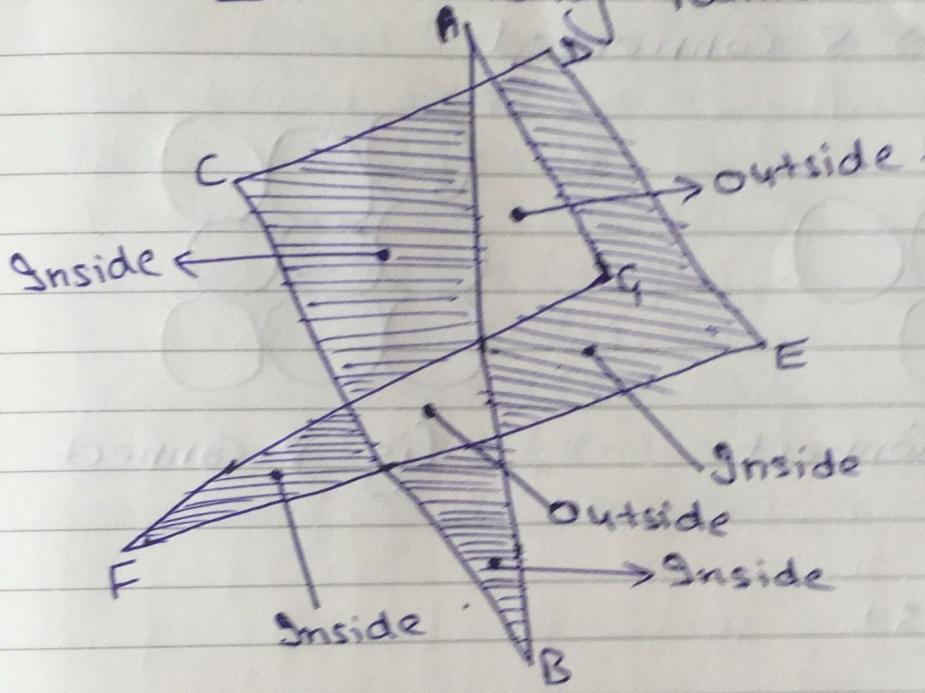
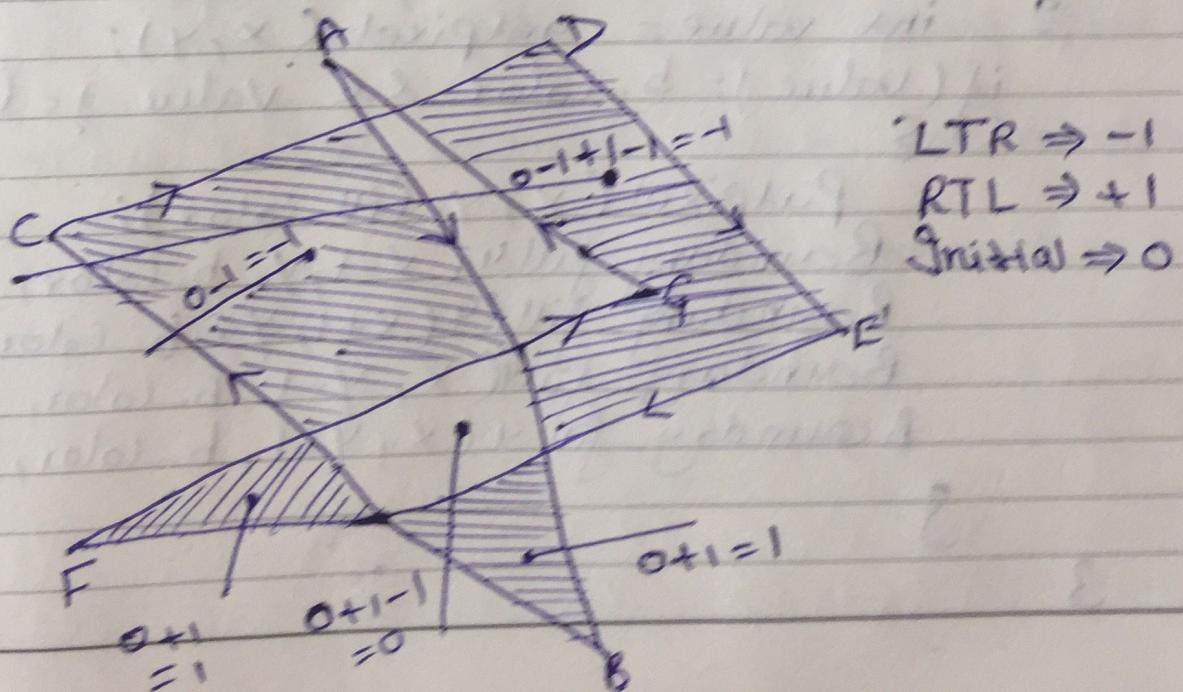


Fig. Filling using Odd Even Rule.



## \* Boundary Fill Algorithm

- Fill the region starting from the interior point until the appropriate color boundary is reached.
- Two ways:
  - 4 Connected
  - 8 Connected

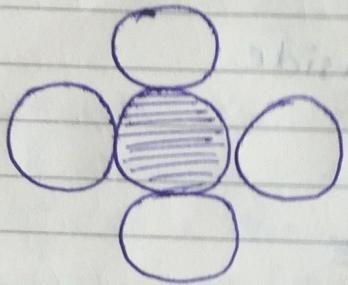


Fig. 4 Connect

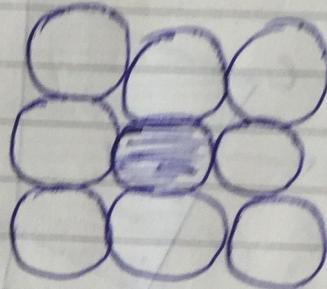


fig 8. Connect

### 4 Connected :-

```
Void Boundary fill4 (int x, int y, int  
b_color, int fill_color)  
{  
    int value = getpixel (x, y);  
    if (value != b_color && value != fill_color)  
    {  
        Putpixel (x, y, fill_color);  
        Boundary - fill4 (x-1, y, b_color, fill_color);  
        Boundary - fill4 (x+1, y, b_color, fill_color);  
        Boundary - fill4 (x, y-1, b_color, fill_color);  
        Boundary - fill4 (x, y+1, b_color, fill_color);  
    }  
}
```

3

# Notes

## 8 Connected :-

void Boundary\_fill8(int x, int y, int b\_color, int fill\_color)  
 { int current = getpixel(x, y);  
 if (current != b\_color && current != fill\_color)  
 {

```
        putpixel(x, y, fill_color);
        Boundary_fill8(x-1, y, b_color, fill_color);
        Boundary_fill8(x+1, y, b_color, fill_color);
        Boundary_fill8(x, y-1, b_color, fill_color);
        Boundary_fill8(x, y+1, b_color, fill_color);
        Boundary_fill8(x-1, y-1, b_color, fill_color);
        Boundary_fill8(x+1, y-1, b_color, fill_color);
        Boundary_fill8(x-1, y+1, b_color, fill_color);
        Boundary_fill8(x+1, y+1, b_color, fill_color);
    }
```

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## Drawbacks :-

- 1) If any interior pixel is already colored with the fill color then the region may not be colored properly.
- 2) It makes lot of use of stack so memory inefficient.
- 3) For some figures 4-connected method may not work fine.

# Notes

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## \* Flood fill Algo :-

### Drawback of Boundary fill Algo :-

→ If the boundary is of more than one color then region may not be colored properly.

→ Flood fill Algo works based on the previous color of the pixels in the region we want to fill color.

#### Algo :-

1) Get a pixel inside the region we want to color.

    current = getPixel(x, y);

2) Check if the color of the pixel (Current) is old color. Then if fill the pixel with fill color.

3) Using 4 Connected / 8 Connected find the neighbours of the current pixel & repeat step 2 for every pixel.

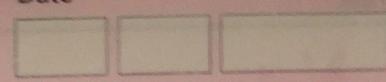
void flood\_fill\_4 (int x, int y, int old\_color,  
                      int fill\_color)

```
    int current = get_pixel(x, y);
    if (current == old_color)
        
```

        putpixel(x, y, fill\_color);

        Flood\_fill\_4(x-1, y, fill\_color, old\_color);

        Flood\_fill\_4(x+1, y, fill\_color, old\_color);



# Notes

Flood-Fill4(x, y-1, fill\_color, old\_color);  
 Flood-Fill4(x, y+1, fill\_color, old\_color);

3  
3

Drawbacks :-

1) If an inside pixel is in some other color then the fill terminates & the polygon remains unfilled.

\* Cell Arrays :-

→ A computer graphics output primitive defined by a rectangular grid of equal size rectangular cells each having a single color.

\* Character Generation :-

→ A computer graphics character can be generated using software.

→ In hardware implementation of character generation limited faces of character can be generated.

→ A wide variety of faces of character can be generated with software implementation.

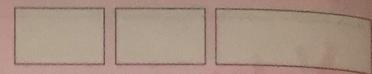
→ Three methods :- 1) Stroke method  
 2) Vector method / Bitmap method  
 3) Star bust method.

→ Stroke method :-

→ In this method we use a sequence of line drawing function & arc function to generate characters.

# Notes

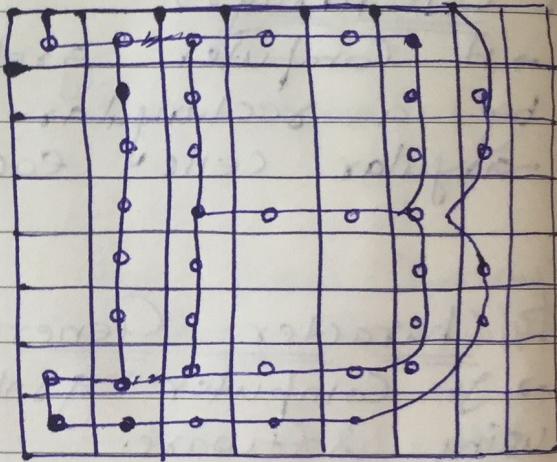
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- we can generate a sequence of characters by assigning starting and end point of line or arc.
- By using this method various faces of character can be generated by changing the values in line & Arc function.
- The main disadvantage of this method is when we draw a diagonal line it produce aliased character.

## ⇒ Bitmap Method :-

1	1	1	1	1	1	1	0	0
0	1	1	0	0	1	1	0	
0	1	1	0	0	1	1	0	
0	1	1	1	1	1	0	0	
0	1	1	0	0	1	1	0	
0	1	1	0	0	1	1	0	
1	1	1	1	1	1	0	0	
0	0	0	0	0	0	0	0	



- This method is suitable for producing various character.
- font size of character can be increased by increasing the size of array.
- The main drawback of this method is that this method produce aliased character.

## ⇒ Starburst Method :-

- In this method a fixed pattern of line is used to generate the character.
- In this method we use a segment

# Notes

- Combination of 24 bit line segments.
- In 24 bit line segment code each bit represent a single line.
  - To highlight a line we put corresponding bit 1 in 24 bit line segment code & 0 otherwise.

## Drawbacks:-

- 1) 24 bit segment code is required to put in memory for generating character. Hence extra memory is required in the method.
- 2) Character quality is poor due to limited faces.

