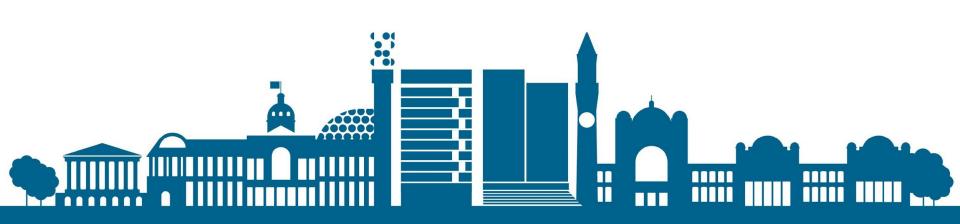


Computer Systems Subroutines and Stacks



Lecture Objectives

To introduce the fundamentals concepts of subroutines and how they are implemented using stacks.

Lecture Outline

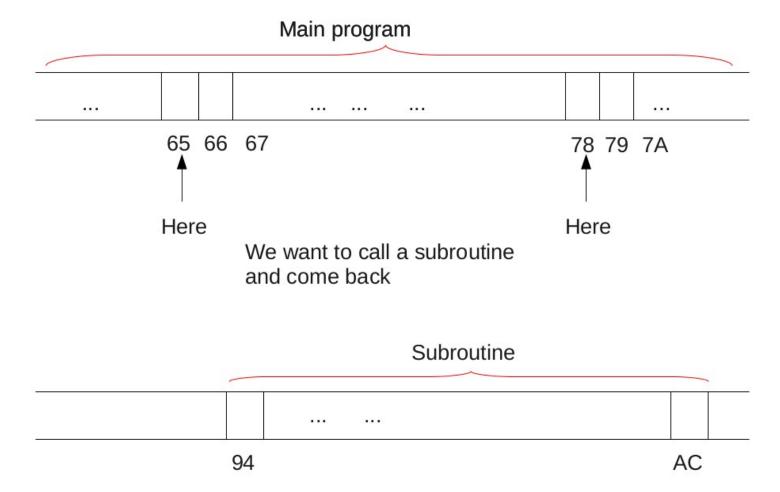
- How a Subroutine Works?
 - Call / Return Instructions
- Introduction to Stacks
 - Saving Registers
 - Stacks for Calculation
- Reverse Polish Notation
- Bitwise Boolean Operations
- Conditional & Unconditional Jumps
- Summary



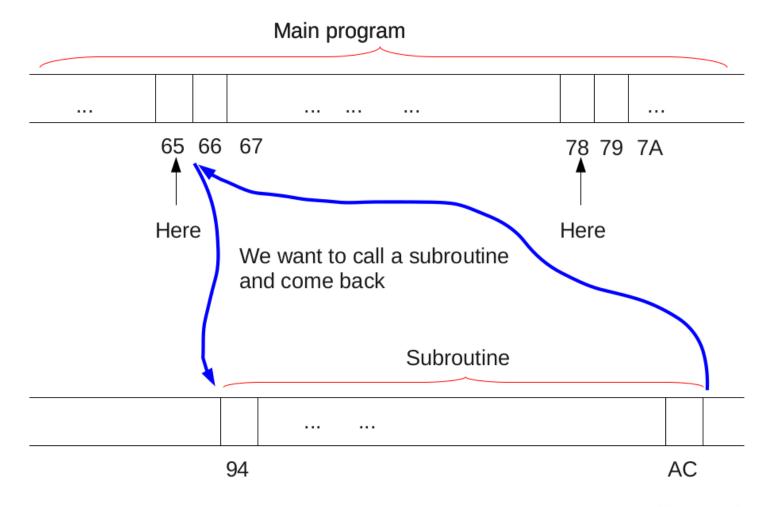
Subroutines (Methods) - Example

```
class Main {
    public static void main(String[] args) {
   myFunction(); -----
    private static void myFunction() { <</pre>
        // function body
```

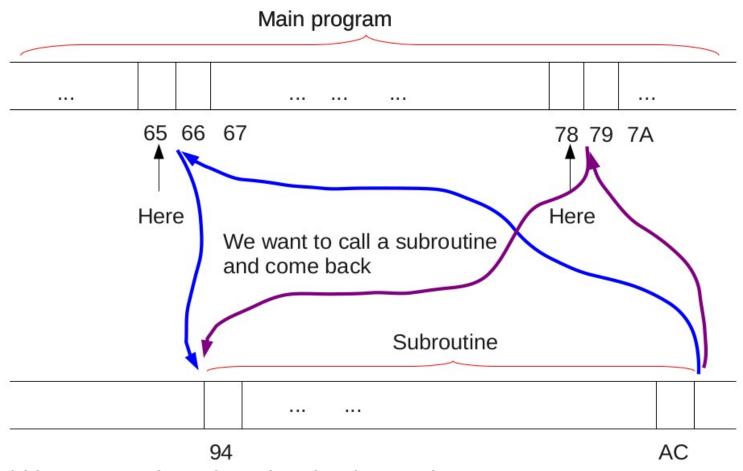
Subroutines (Methods)



Subroutines (Methods)



Subroutines (Methods)



Could jump to 94 for subroutine, but how to know where to jump back afterwards?

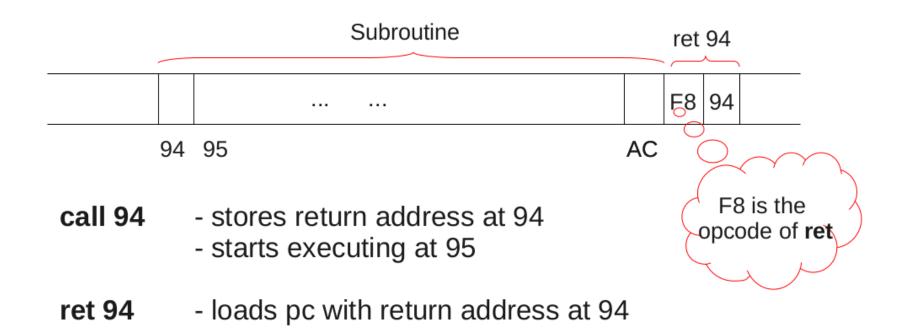
Must store the return address somewhere.

Call / Return Instructions

- Two new operations:
 - **call** operand : Like jump, but stores current PC value (the return address) somewhere suitable.
 - ret : Read return address from where it was stored, and load it into PC.

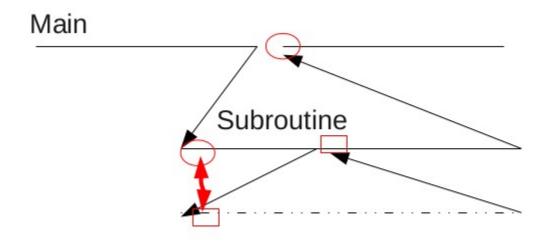
Storing the Return Address

Idea #1: In each subroutine, its first byte is used to store the return address



Disadvantage of Idea #1

- Can only store one return address
- Consequence: subroutine cannot call itself
 - If it were to call itself it would need to store 2 return addresses



Main calls subroutine

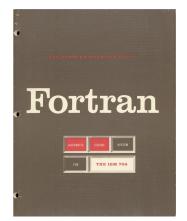
Subroutine calls itself

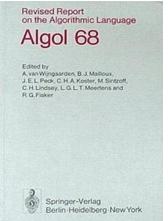
Dotted line = the same subroutine



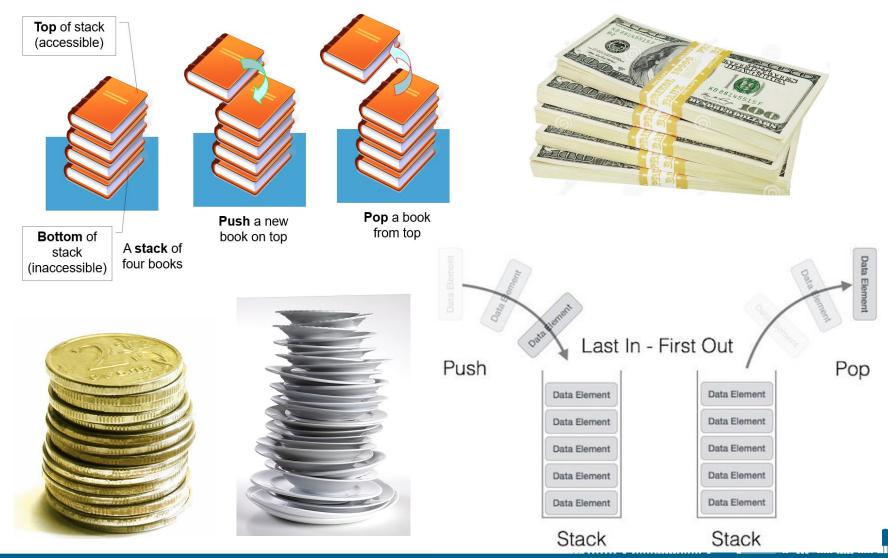
History: 2 Early Programming Languages

- FORTRAN ("FORmula TRANslation")
 - Used jumps (GOTO), conditional jumps
 - Banned recursion (i.e. for a method to call itself) to allow idea 1.
- Algol ("Algorithmic language")
 - structured programming (if .. then .. else, etc.)
 - Allowed recursion
- Initially, FORTRAN was more successful, but modern languages (e.g. C, Java) took forward the ideas from Algol.



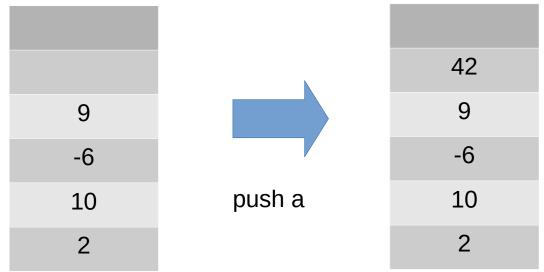


What is a Stack?



- A stack can flexibly store a variable number of bytes
- LIFO = Last In, First Out (aka FILO)

a	b	С	d
42	54	13	27



- A stack can flexibly store a variable number of bytes
- LIFO = Last In, First Out (aka FILO)

a

-6

10

b

42	54	13	27
			13
42			42
9			9

push c

C

d

-6

10

2

- A stack can flexibly store a variable number of bytes
- LIFO = Last In, First Out (aka FILO)

	()		
42	13	13	27
	_		
13			
42			42
9			9
-6			-6
10	pop	b	10
2			2

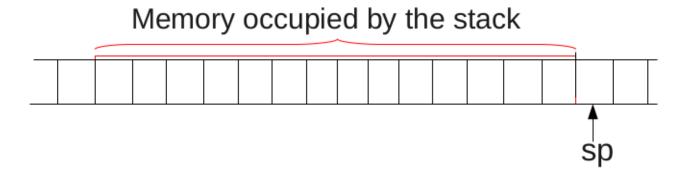
- A stack can flexibly store a variable number of bytes
- LIFO = Last In, First Out (aka FILO)

b

42	13	13	42
42			
9			9
-6	_		-6
10	рор	d	10
2			2

In Memory

- Give CPU another register
 - sp (stack pointer) shows where top is



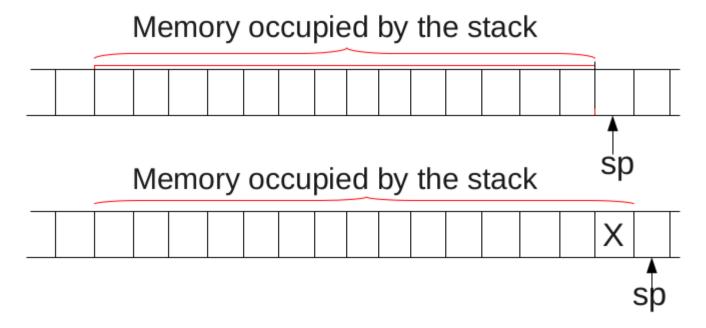
- Don't need to know where bottom is!
 - Provided that we are careful: only pop when you know you've pushed

In Memory

- To push a value X:
 - Write the value to memory at address sp
 - Add 1 to sp
- To pop a value:
 - Subtract 1 from sp
 - Read value from memory at address sp

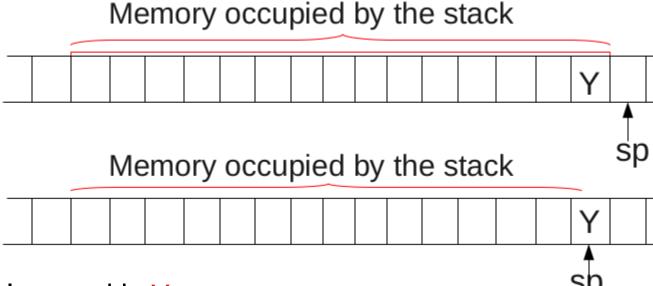
In Memory - Push a Value

- To push a value X:
 - Write the value to memory at address sp
 - Add 1 to sp



In Memory - Pop a Value

- To pop a value:
 - Subtract 1 from sp
 - Read value from memory at address sp



The value read is Y.

Still in memory but will be overwritten by a later push operation.

Storing the Return Address

Idea #2: Store the return address on a stack.

```
call N works as if:

push pc // push program counter
ld pc N // jump to N

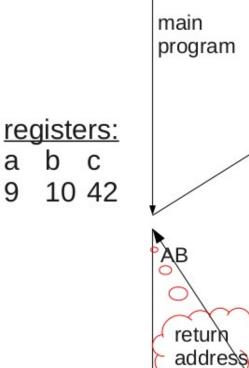
ret works as if:

pop pc // pop return address
// & jump to it
(none of these are actual operations)
```

Why should we Save Registers?

- Subroutine may need to use registers for its calculations.
 - But previous register values are needed on return!
- Common pattern for subroutines:
 - Start by pushing all registers
 - Pop them back before return
- Return address & saved registers = <u>stack frame</u>
 Java method-calls develop this idea.

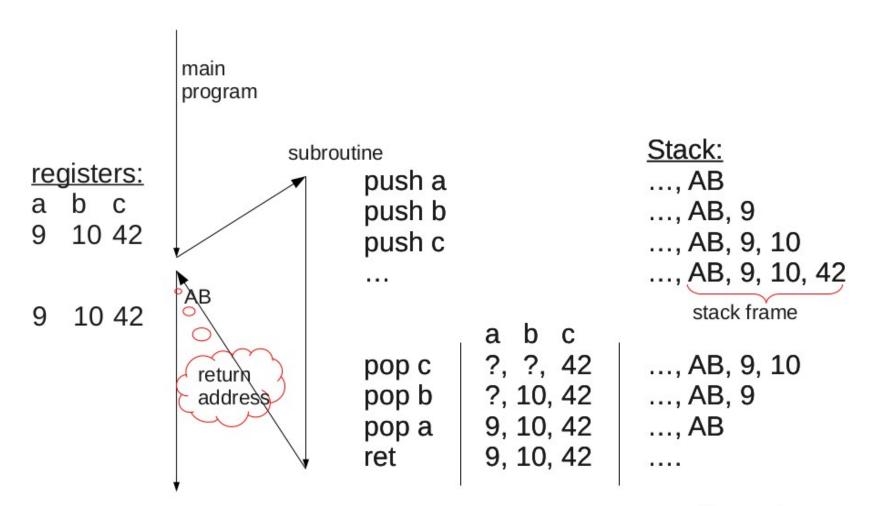
Saving Registers - Stack Frame



subroutine
push a
push b
push c

Stack:
..., AB
..., AB, 9
..., AB, 9, 10
..., AB, 9, 10, 42
stack frame

Saving Registers - Stack Frame



Stacks for Calculation

Example:

$$(5+2)*\sqrt{x*x+y*y}+8$$

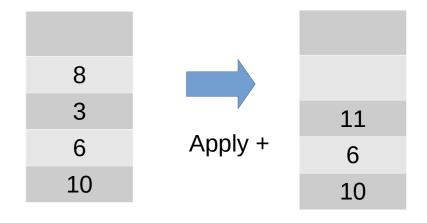
What order are operations applied in?

$$(5+2)*\sqrt{x*x+y*y}+8$$

means "square root of" (SQRT) e.g. SQRT(
$$x*x + y*y$$
)

Reverse Polish Notation (RPN)

- Order of operations is as written
- No brackets needed
- Powerful use of stack (= operand stack) to store intermediate results
- ◆ If its a Number or Variable: push it on the stack
- If its an Operation: apply to the top elements on stack
 & push result back on the stack





RPN for the Example

$$(5+2)*\sqrt{x*x+y*y}+8$$

Reverse Polish: push operands, then operate.

We get:

$$5 \quad 2 \quad + \quad x \quad x \quad * \quad y \quad y \quad * \quad + \quad \sqrt{} \quad * \quad 8 \quad + \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7$$



How to use RPN along with a Stack?

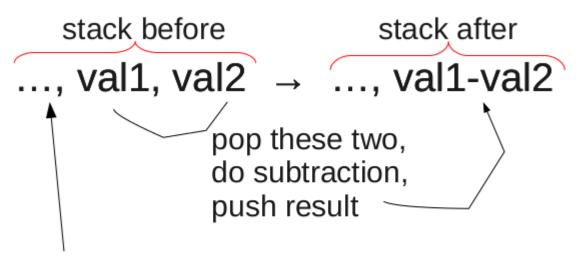
- Suppose that x has value3, and y has value 4
- Now, evaluate the expression. (Top of stack is on right.)

Operation	<u>Stack</u>
	empty
5	5
2	5,2
+	7
X	7,3
Χ	7,3,3
*	7,9
у	7,9,4
У	7,9,4,4
*	7,9,16
+	7,25
SQRT	7,5
*	35
8	35,8
+	43



Notation for Operand Stack

- To show what an operation does to the stack:
- e.g. subtraction



the rest is unchanged

More on Reverse Polish Notation

- Any expression can be converted to Reverse Polish Notation and then its easy to execute with a stack.
- Applications
 - Humans use reverse Polish directly (See <u>Details</u>)
 - e.g. some pocket calculators HP in 1970s (HP-41C)

https://www.theregister.co.uk/Print/2014/01/03/ten_classic_calcutors/

- Forth programming language has two stacks:
 - Operand stacks for calculations
 - Return stack for module calls More details:

https://en.wikipedia.org/wiki/Forth_(programming_language)



Applications of Reverse Polish Notation

- Compile to a reverse Polish form that is then executed.
 - e.g. Postscript format, for printable files
 - executed by printers
 - e.g. Java byte code
 - uses operand stacks for calculations
- In Java, each method call has its own operand stack.

Stack instead of Registers (Stack Machines)

- Use 2 stacks
 - return stack for subroutine return
 - operand stack for Reverse Polish calculations
- Don't need a,b,c registers
 - Advantages
 - More space for calculations
 - Opcodes don't need to specify registers
 - Disadvantages
 - Harder to know where things are on the stack

What is an Operand?

- Underlying meaning:
 - Whatever an operator operates on?
- Two meanings here (don't confuse them):
 - 1) Extra bytes after the instruction opcode in memory, e.g. ld a 42
 - 2) Entries in the operand stack.

Machine Instructions as Stack Operators

Arithmetic:

```
e.g. add - adds top 2 stack entries ..., val1, val2 → ..., val1+val2
e.g. sub - subtracts top 2 stack entries ..., val1, val2 → ..., val1-val2
e.g. neg - negates top stack entry ..., val → ..., -val
```

Similarity: mul, div, rem

remainder

Example of a Stack Machine (JVM mnemonics)

	push 5
	push 2
	add
	load x
	load x
	mul
	load y
	load y
	mul
more	add
next week	call √
	mul
	push 8
	add

5	2	+	X	X	*	y	y	*	+	$\sqrt{}$	*	8	+
---	---	---	---	---	---	---	---	---	---	-----------	---	---	---

<u>Operation</u>	<u>Stack</u>	
1.5	empty	
5	5	
5 2	5,2	
+	7	
X	7,3	
X	7,3,3	
*	7,9	
У	7,9,4	
y *	7,9,4,4	
*	7,9,16	
+	7,25	
SQRT	7,5	
*	35	
8	35,8	
+	43	



Bitwise Boolean Operations

 Boolean operations on one bit 0=false, 1=true

"eXclusive OR"
7

OR	0	1
0	0	1
1	1	1

AND	0	1
0	0	0
1	0	1

XOR	0	1	
0	0	1	
1	1	0	

Can do these bit-wise on binary values. Example for XOR:

0011101111......011001000 0001001001.....111101100 ------0010100110......100100100

XOR: done on top 2 stack entries (similar to: or, and): ..., val1, val2 → ..., val1 XOR val2



Jumps

- Unconditional jumps
 - Operand stack is not used!
- Conditional jumps



Conditional Jumps with Other Comparisons

jump if
$$val = 0$$
 eq lt le le ne gt ge

6 operators: ifeq, iflt, ifle, etc. also: if_cmpeq, if_cmplt, etc.

Summary

We have now seen:

- What is a subroutine and how it is implemented.
- What is a stack and how it is used for implementing subroutines.
- What is the importance of saving registers and how these can be used to perform computations.
- What is reverse polish notation and how it is used to to do calculations using an operand stack.
- What is a stack machine and how it operates using a stack instead of registers.
- What are Bitwise Boolean operations and Jump instructions.

Notes on Exercises

- You will need to use an algorithm to convert math expressions from the usual "infix" notation to reverse-Polish. This algo is called Dijkstra's Shunting-Yard Algorithm.
- You can also read the Wikipedia page on this algo https://en.wikipedia.org/wiki/Shunting-yard_algorithm