

# Introduction to Computer Science Week 10 – Network Security



# **Lecture Objective**

The objective of this lecture is to understand the conceptual aspects of network security with emphasis on cryptography.



#### **Lecture Outline**

- Introduction to Network Security
- Principles of Cryptography
- Symmetric Key Cryptography
- Public Key Cryptography
- Summary



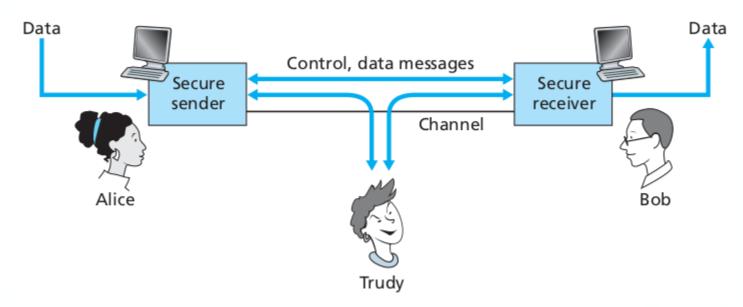
# What is Network Security?

- Confidentiality: only sender, intended receiver should "understand" message contents
  - sender encrypts message
  - receiver decrypts message
- End-point Authentication: sender, receiver want to confirm identity of each other
- Message Integrity: sender, receiver want to ensure message not altered (in transit, or afterwards) without detection
- Access and Availability: services must be accessible and available to users



# Friends and Enemies: Alice, Bob & Trudy

- Well-known in network security world
- Bob, Alice want to communicate "securely"
- Trudy (intruder) may intercept, delete, add messages



# Who might Bob, Alice be?

- ... well, real-life Bobs and Alices!
- Web browser/server for electronic transactions (e.g., on-line purchases)
- On-line banking client/server
- DNS servers
- Routers exchanging routing table updates
- other examples?

## There are Bad Guys (and Girls) Out There!

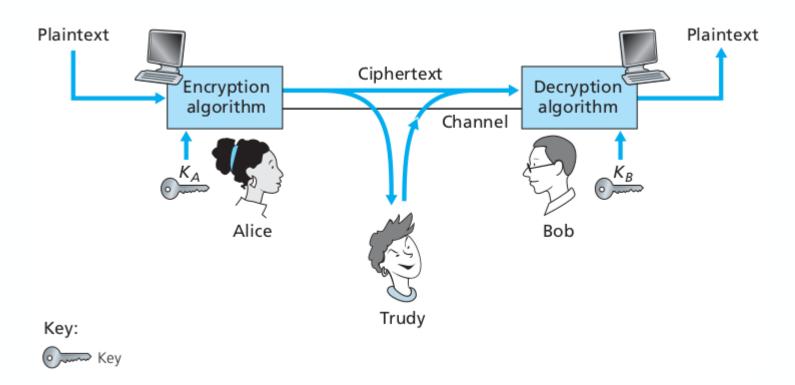
Q: What can a "bad guy" do?

A: A lot!

- Eavesdrop: intercept messages
- Actively insert messages into connection (e.g. man in the middle attack)
- Impersonation: can fake (spoof) source address in packet (or any field in packet)
- Hijacking: "take over" ongoing connection by removing sender or receiver, inserting himself in place
- Denial of Service: prevent service from being used by others (e.g., by overloading resources)



# **Principles of Cryptography**



### m plaintext message

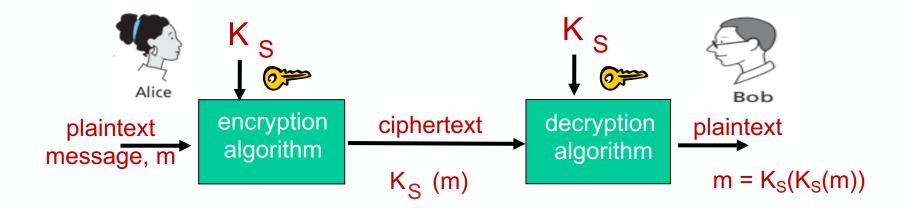
 $K_A(m)$  ciphertext, encrypted with key  $K_A$  $m = K_B(K_A(m))$ 

## **Encryption Schemes**

There are two main types of encryption schemes:

- Symmetric Key Systems: Alice's and Bob's keys are identical and are secret.
- Public Key Systems, a pair of keys is used. One of the keys is known to both Bob and Alice (known to the whole world). The other key is known only by either Bob or Alice (but not both).

# Symmetric Key Cryptography



Symmetric Key cryptography: Bob and Alice share same (symmetric) key: K<sub>s</sub>

- e.g., key is knowing substitution pattern in mono alphabetic substitution cipher
- Q: How do Bob and Alice agree on key value?



# **Simple Encryption Scheme**

Substitution Cipher: substituting one thing for another

monoalphabetic cipher: substitute one letter for another

plaintext: abcdefghijklmnopqrstuvwxyz

ciphertext: mnbvcxzasdfghjklpoiuytrewq

e.g.: Plaintext: bob. i love you. alice ciphertext: nkn. s gktc wky. mgsbc

Encryption key: mapping from set of 26 letters to set of 26 letters



# Symmetric Key Crypto: DES

# **DES: Data Encryption Standard**

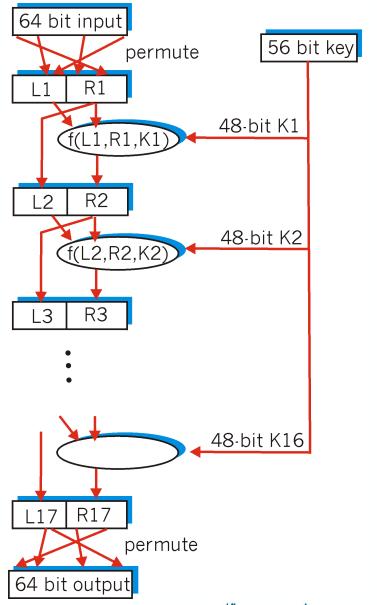
- US encryption standard [NIST 1993]
- ◆ 56-bit symmetric key, 64-bit plaintext input
- Block cipher with cipher block chaining
- How secure is DES?
  - DES Challenge: 56-bit-key-encrypted phrase decrypted (brute force) in less than a day!
  - No known good analytic attack
- Making DES more secure:
  - 3DES: encrypt 3 times with 3 different keys



# Symmetric Key Crypto: DES

#### **DES** Operation

- Initial permutation
- 16 identical "rounds" of function application, each using different 48 bits of key
- Final permutation





# **AES: Advanced Encryption Standard**

- Symmetric-key NIST standard, replaced DES (Nov 2001)
- Processes data in 128 bit blocks
- ◆ 128, 192, or 256 bit keys
- Brute force decryption (try each key) taking 1 second on DES, takes 149 trillion years for AES

# **Public Key Cryptography**

# Symmetric Key Crypto

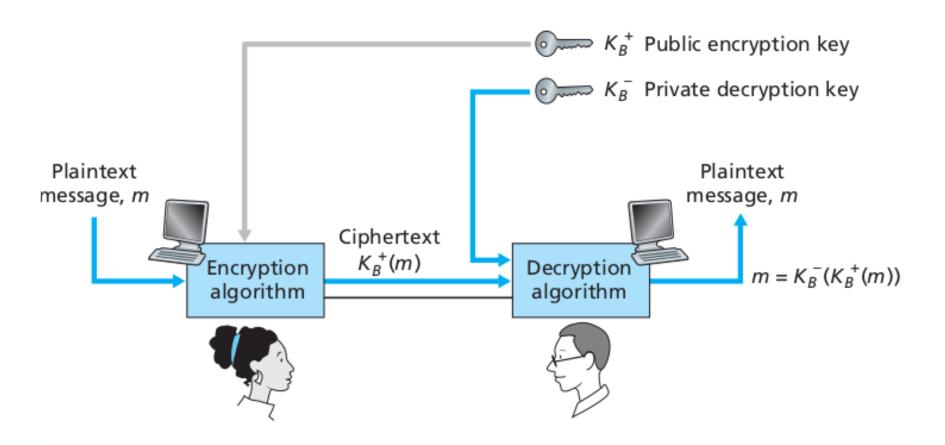
- Requires sender, receiver know shared secret key
- Q: How to agree on key in first place (particularly if never "met")?

# Public Key Crypto

- Radically different approach [Diffie-Hellman76, RSA78]
- Sender, receiver do not share secret key
- Public encryption key known to All
- Private decryption key known only to receiver



## **Public Key Cryptography**



# **Public Key Encryption Algorithms**

# Requirements:

- 1 Need  $K_B^+(\cdot)$  and  $K_B^-(\cdot)$  such that  $K_B^-(K_B^+(m)) = m$
- Given public key K<sub>B</sub><sup>+</sup>, it should be impossible to compute private key K<sub>B</sub>

RSA: Rivest, Shamir, Adelson algorithm



# **Pre-Requisite: Modular Arithmetic**

- x mod n = remainder of x when divided by n
- Facts:

```
[(a mod n) + (b mod n)] mod n = (a+b) mod n

[(a mod n) - (b mod n)] mod n = (a-b) mod n

[(a mod n) * (b mod n)] mod n = (a*b) mod n
```

◆ Thus (from the last fact)

```
(a mod n)<sup>d</sup> mod n = a<sup>d</sup> mod n

Example: a=14, n=10, d=2:

(a mod n)<sup>d</sup> mod n = a<sup>d</sup> mod n

=> (14 \text{ mod } 10)^2 \text{ mod } 10 = 14^2 \text{ mod } 10

=> 16 mod 10 = 196 mod 10 = 6
```



## **RSA: Getting Ready!**

- Message: just a bit pattern
- Bit pattern can be uniquely represented by an integer number
- Thus, encrypting a message is equivalent to encrypting a number.

#### Example:

- → m = 10010001. This message is uniquely represented by the decimal number 145.
- To encrypt m, we encrypt the corresponding number, which gives a new number (the ciphertext).

# **RSA:** Creating Public/Private Key Pair

- 1. choose two large prime numbers p, q. (e.g., 1024 bits each)
- 2. compute n = pq, z = (p-1)(q-1)
- 3. choose e (with e < n) that has no common factors with z (e, z are "relatively prime").
- 4. choose d such that ed 1 is exactly divisible by z. (in other words: ed mod z = 1).
- 5. public key is (n,e). private key is (n,d).



# **RSA:** Encryption/Decryption

- 0. Given (n,e) and (n,d) as computed above
- 1. To encrypt message *m* (<*n*), compute

$$c = m^e \mod n$$

2. To decrypt received bit pattern, c, compute

$$m = c^d \mod n$$

Magic 
$$m = (m^e \mod n)^d \mod n$$
Happens!



# **RSA:** Encryption/Decryption – Example

Bob chooses p=5, q=7. Then n=35, z=24. e=5 (so e, z relatively prime). d=29 (so ed-1 exactly divisible by z).

Plaintext Letter	m: numeric representation	m <sup>e</sup>	Ciphertext $c = m^e \mod n$	
1	12	248832	17	
0	15	759375	15	
V	22	5153632	22	
е	5	3125	10	

**Table 8.2** • Alice's RSA encryption, e = 5, n = 35

Ciphertext c	c <sup>d</sup>	$m = c^d \mod n$	Plaintext Letter
17	4819685721067509150915091411825223071697	12	I
15	127834039403948858939111232757568359375	15	0
22	851643319086537701956194499721106030592	22	٧
10	100000000000000000000000000000000000000	5	е

**Table 8.3** • Bob's RSA decryption, d = 29, n = 35

# Why does RSA Work?

- Must show that cd mod n = m where c = me mod n
- ♦ Fact: for any x and y:  $x^y \mod n = x^{(y \mod z)} \mod n$ 
  - where n= pq and z = (p-1)(q-1)
- ♦ Thus,  $c^d \mod n = (m^e \mod n)^d \mod n$ 
  - = med mod n
  - = m<sup>(ed mod z)</sup> mod n
  - $= m^1 \mod n$
  - = m



## **RSA:** Another Important Property

The following property is *very* useful:

$$K_B(K_B(m)) = m = K_B(K_B(m))$$

use public key first, followed by private key

use private key first, followed by public key

Result is the Same!

Why 
$$K_B(K_B(m)) = m = K_B(K_B(m))$$
?

Follows directly from modular arithmetic:

```
(m^e \mod n)^d \mod n = m^{ed} \mod n
= m^{de} \mod n
= (m^d \mod n)^e \mod n
```



## Why RSA is Secure?

- Suppose you know Bob's public key (n,e). How hard is it to determine d?
- Essentially need to find factors of n without knowing the two factors p and q
  - Fact: factoring a big number is hard!

# **RSA** in Practice: Session Keys

- Exponentiation in RSA is computationally intensive
- ◆ DES is at least 100 times faster than RSA
- Use public key cryptography to establish secure connection, then establish second key – symmetric session key – for encrypting data.

## Session Key, K<sub>S</sub>

- Bob and Alice use RSA to exchange a symmetric key K<sub>S</sub>
- Once both have K<sub>S</sub>, they use symmetric key cryptography

## **Summary**

In this lecture, we have been introduced to

- The basic principles of Network Security
- The principles of Cryptography
- Symmetric and Asymmetric Cryptography including DES, AES and RSA schemes.

## **References / Links**

Chapter #8: Security in Computer Networks, the Computer Networking: A Top-Down Approach (7 edition) by Kurose & Ross