## Crash Model 1: Finite Markov Chain

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Course Summer Research Project

Assign No. Understand the critical crash number

ABSTRACT: In this note, I will try to understand the effect of crash number in a Markov Chain crash model on MAB algorithm

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1. Critical Crash Number in Crash Model

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## 1. Critical Crash Number in Crash Model

Given a set of fuzzing parameters, the expected number of crashes triggered by active seed will be given in the following.

In a crash model with infinte nodes in Markov chain, which means a seed could potentially trigger infinite unique crashes The length of fuzzing campaign is c (campaignlength), within each campaign, the number of trial is t (trialblock). So the duration d (duration) in fuzzing simulation will be  $d = t \times c$ . If the worker in a pull is w, the total number of testing in a fuzzing is  $m = d \times w$ . In addition, the number of active seeds is a (active). The initial probability of triggering a crash is  $\lambda_0$  (lambdahigh), and the discount factor is  $\gamma$  (exponentialdecay). The the probability of triggering the (n+1)th unique crash will be

$$\lambda_n = \lambda_0 \times \gamma^n$$

Therefore, the expected number of testing in a fuzzing to trigger the nth unique crash by an active seed is

$$s(n) = \frac{1}{\lambda_0} + \frac{1}{\lambda_1} + \ldots + \frac{1}{\lambda_{n-1}} = \frac{1}{\lambda_0} \times \frac{\gamma^n - 1}{\gamma^n - \gamma^{n-1}}$$

Consequently, the expected number of testing in a fuzzing to trigger the nth unique crash by a active seeds will be  $S(n) = a \times s(n)$ .

Matching S(n) with d to estimate the value of n in a fuzzing campaign.

$$\frac{a}{\lambda_0} \times \frac{\gamma^{n+1} - 1}{\gamma^{n+1} - \gamma^n} \approx m = t \times c \times w$$

From above agreba equation, we can solve n.

If 
$$c = 10^3$$
,  $t = 10^2$ ,  $w = 10^3$ ,  $a = 15$ ,  $\lambda_0 = 10^{-4}$ ,  $\gamma = 0.6$ , n will be  $11 \sim 12$ .

Consequently, in a fuzzing campaign with above parameters, in average, an active seed will actually trigger  $11 \sim 12$  unique crashes.

## ${\bf Acknowledgments}$

References