

## **MODULE-4**

### **Three Phase Induction Motor** **and** **Three Phase Synchronous Generators**

#### **THREE PHASE INDUCTION MOTOR**

##### **Introduction:**

A three-phase induction motor is a three phase ac motor which convert electrical energy in AC form into mechanical energy. These motors are widely used for many industrial applications.

The first induction motor was invented by the famed Nikola Tesla in 1887 at his workshop on 89 Liberty Street, New York

They work on the principle of electromagnetic induction. The advantages of induction motor are:

- (1) Construction is simple, rugged, unbreakable.
- (2) Low cost and highly reliable.
- (3) It has high efficiency.
- (4) It works with good power factor at rated load.
- (5) Less maintenance
- (6) Small IM are self starting and large motors starting arrangement is simple.

##### **Disadvantages:**

1. It's a constant speed motor, hence speed cannot be varied easily.
2. Its starting torque is less, compared to dc shunt motor.

**Construction:** A 3 $\Phi$  IM has mainly two parts. **Stator and Rotor.**

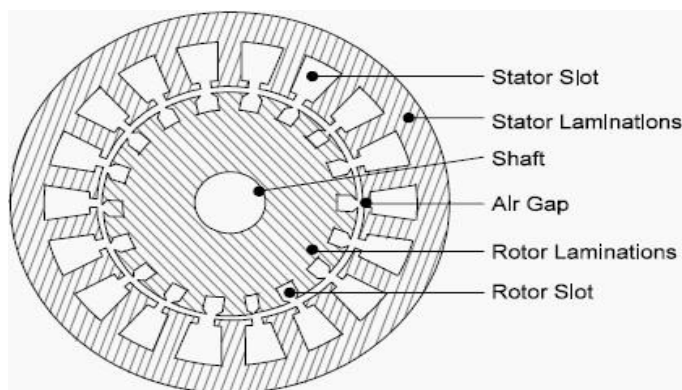


Fig. 4.1 Stator of three phase IM

## STATOR

1. The stator is enclosed in steel frame which has hollow cylindrical core made up of thin laminations of silicon steel to reduce eddy current loss and hysteresis loss.
2. The stator conductors are placed in the slots which are insulated from one another and from the slots.
3. Conductors are connected as a balanced three phase star or delta winding.
4. Windings are wound for a definite number of poles and speed.

$$N_s = 120f/P$$

$N_s$  = Synchronous speed

$f$  = frequency

$P$  = number of poles.

5. When  $3\Phi$  supply is applied to stator winding a magnetic field of constant magnitude rotating at synchronous speed is produced.
6. Rotating magnetic field is responsible for producing torque in the rotor.

**Rotor:** It is the rotating part of IM, which is mounted on the shaft to which the mechanical load is connected. There are two types are rotor: Squirrel cage rotor and Phase wound rotor.

Types – squirrel cage and wound rotor,

Squirrel cage rotor:

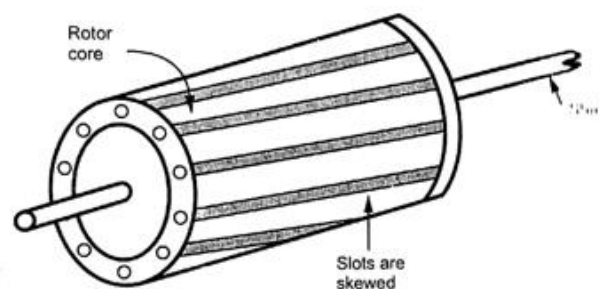


Fig 4.2(a): Squirrel cage induction motor

Almost 90% of IM are squirrel cage type, as their construction is simple and rugged. Its consists of cylindrical laminated core with slots for carrying rotor windings is shown in Fig 4.2(a). The rotor windings are heavy bars of copper or aluminum. Each slot has one bar of copper placed in it. All the bars are welded at both the ends of the end rings, thereby short circuiting both ends of the rotor. Slots are skewed to reduce the noise due to magnetic hum and to make the rotor run quietly. It also reduces the locking tendency between rotor and stator.

#### Advantages:

- 1.Simple and rugged construction and can withstand rough handling.
- 2.Low cost of maintenance and repair.
3. Good efficiency and power factor.
4. Simple star-delta starter is sufficient for starting.

#### Disadvantages:

1. Size of slip ring IM of same capacity is more than squirrel cage IM.
2. Costlier as the construction is complicated.
3. High maintenance cost and repair.

#### Applications:

Used for loads which require high starting torque such hoists, cranes, etc

Phase wound rotor:

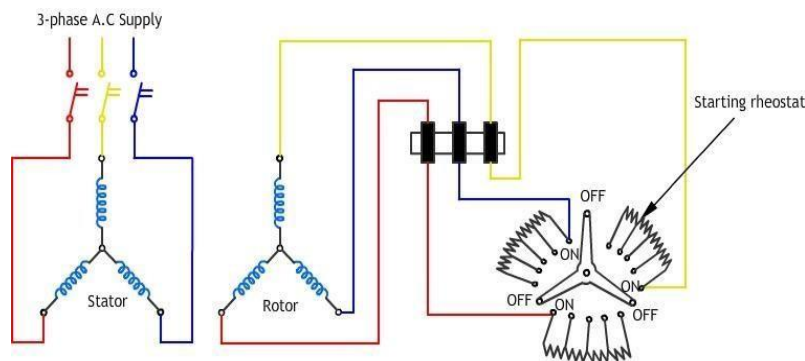


Fig 4.2(b): Phase wound rotor

The rotor is laminated, cylindrical having uniform slots on its outer periphery. A 3 phase which is star connected is placed in these slots is shown in Fig 4.2(b). The open end of star winding is brought out and connected to 3 insulated slip rings, mounted on the shaft with carbon brushes resting on them. Three brushes are externally connected to 3 phase star connected rheostat which is used as starter. When running under normal conditions the slip rings are automatically short circuited by means of metal collar, which is pushed along the shaft that connects all the rings. Brushes are lifted from slip rings to reduce frictional losses and wear and tear.

**Advantages:**

- 1.Has external resistance in the rotor circuit which is used to start.
- 2.Has high starting torque and low starting current.
3. Smooth running motor
4. Slip ring IM of very high capacity can be built.
5. Explosion proof due to absence of slip ring and brush.

**Disadvantages:**

1. Low starting torque, hence pf is also low.
2. Starting current is high, no smooth running

## Applications

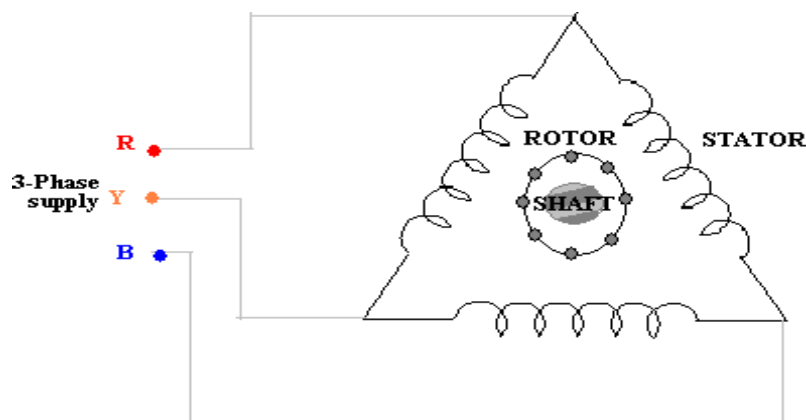
Used for loads which require normal starting torque such as lathes, etc.

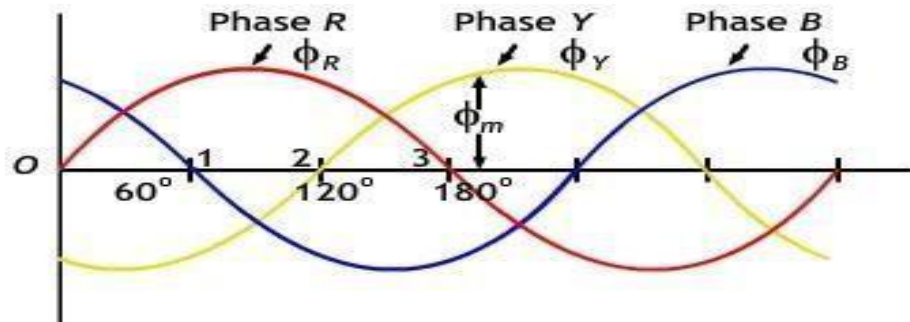
### Comparison between Phase wound Rotor and Squirrel cage rotor:

Sr. No.	Wound or slip ring rotor	Squirrel cage rotor
1	Rotor consists of a three phase winding similar to the stator winding.	Rotor consists of bars which are shorted at the ends with the help of end rings.
2	Construction is complicated.	Construction is very simple.
3	Resistance can be added externally.	As permanently shorted, external resistance cannot be added.
4	Slip rings and brushes are present to add external resistance.	Slip rings and brushes are absent.
5	The construction is delicate and due to brushes, frequent maintenance is necessary.	The construction is robust and maintenance free.
6	The rotors are very costly.	Due to simple construction, the rotors are cheap.
7	Only 5% of induction motors in industry use slip ring rotor.	Very common and almost 95% induction motors use this type of rotor.
8	High starting torque can be obtained.	Moderate starting torque which cannot be controlled.
9	Rotor resistance starter can be used.	Rotor resistance starter cannot be used.
10	Rotor must be wound for the same number of poles as that of stator.	The rotor automatically adjusts itself for the same number of poles as that of stator.
11	Speed control by rotor resistance is possible.	Speed control by rotor resistance is not possible.
12	Rotor copper losses are high hence efficiency is less.	Rotor copper losses are less hence have higher efficiency.
13	Used for lifts, hoists, cranes, elevators, compressors etc.	Used for lathes, drilling machines, fans, blowers, water pumps, grinders, printing machines etc.

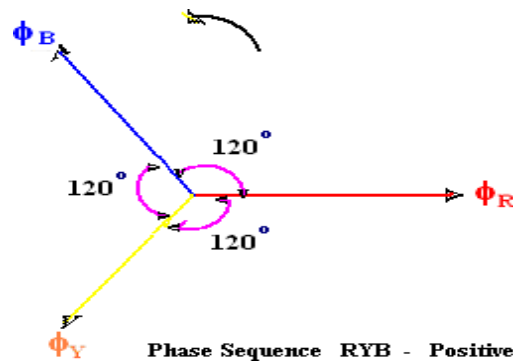
### Concept of rotating magnetic field:

Consider a 3- phase induction motor whose stator windings mutually displaced from each other by  $120^\circ$  are connected in delta and energized by a 3- phase supply.





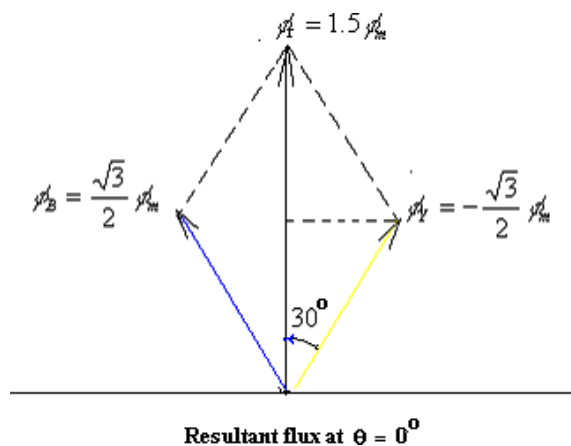
Three phase waveform



The resultant flux at any instant is given by the vector sum of the flux in each of the phases.

(i) When  $\theta = 0^\circ$ , from the flux waveform diagram, we have

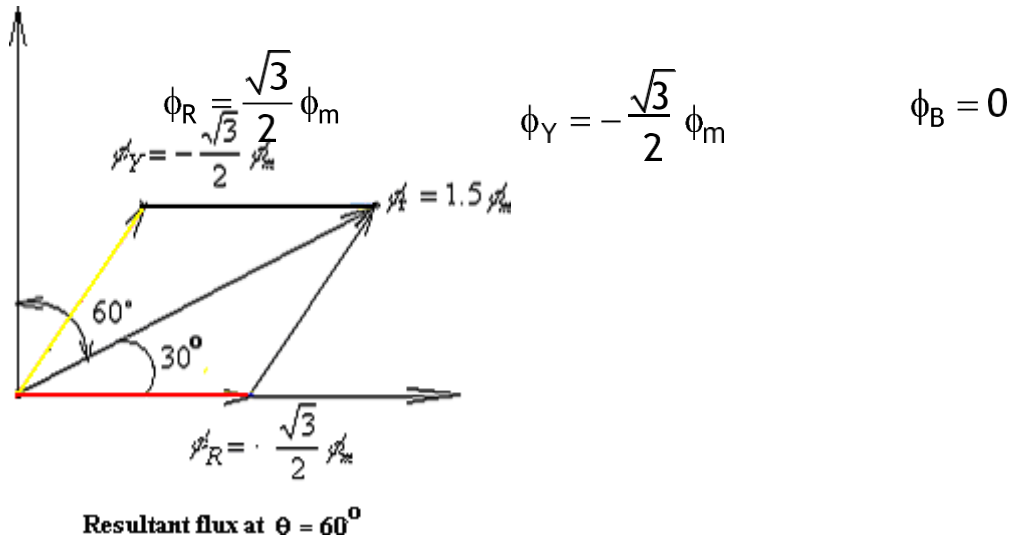
This corresponds to point O in the Fig of waveforms of phases R, Y and B.



$$\phi_R = 0, \phi_Y = -\frac{\sqrt{3}}{2} \phi_m, \phi_B = \frac{\sqrt{3}}{2} \phi_m$$

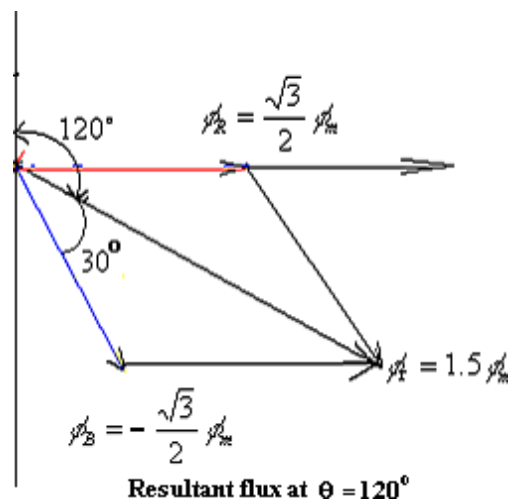
$$\therefore \phi_T = 2 \times \frac{\sqrt{3}}{2} \phi_m \cos \frac{60^\circ}{2} = \sqrt{3} \times \frac{\sqrt{3}}{2} \phi_m = \frac{3}{2} \phi_m$$

ii) At  $\theta = 60^\circ$ , corresponding to point 1 in the Fig 5.4(c) of waveforms of phases R, Y and B.



$$\therefore \phi_T = 2 \times \frac{\sqrt{3}}{2} \phi_m \cos 30^\circ = \frac{3}{2} \phi_m$$

iii) The resultant flux is again  $3/2 \Phi_m$ , but has rotated clockwise through an angle of  $60^\circ$  at  $\theta = 120^\circ$  i.e. corresponds to point 2 in the Fig of waveforms of phases R, Y and B



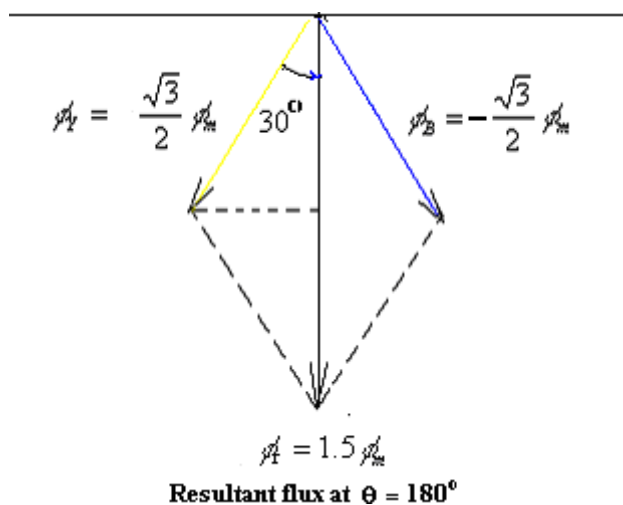
$$\phi_R = \frac{\sqrt{3}}{2} \phi_m, \quad \phi_Y = 0, \quad \phi_B = -\frac{\sqrt{3}}{2} \phi_m$$

$$\phi_T = \frac{\sqrt{3}}{2} \phi_m$$

Thus, once again the resultant has the same value, but has further rotated clockwise through an angle of 60

VI) At  $\theta = 180^\circ$ , i.e. relating to point 3 in the Fig of waveforms of phases R, Y and B

$$\phi_R = 0, \quad \phi_Y = \frac{\sqrt{3}}{2} \phi_m, \quad \phi_B = -\frac{\sqrt{3}}{2} \phi_m$$



The resultant is  $\frac{3}{2} \Phi_m$ , and has rotated clockwise through an additional angle of 60 or through an angle of 180 from the beginning. Thus, we come to the following conclusions

1. The resultant flux is of constant value  $= \frac{3}{2} \Phi_m$ , i.e. 1.5 times the maximum value of the flux due to any phase.
2. The resultant flux rotates around the stator at synchronous speed  $N_s = \frac{120f}{p}$  by where P = number of stator poles and f = supply frequency in Hz.

Working principle:



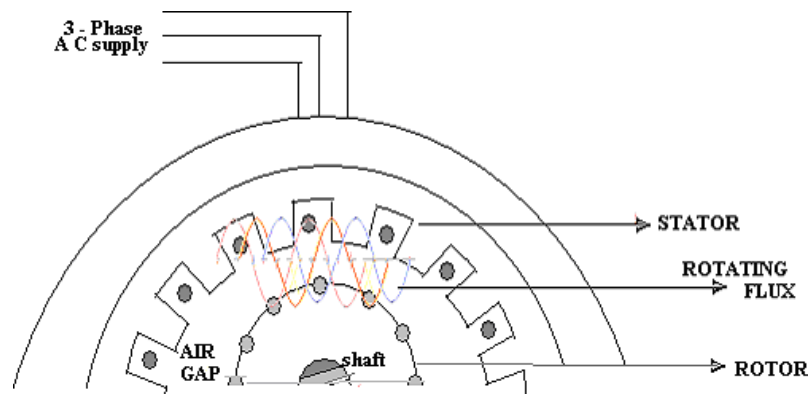


Fig: 4.4 Working principle of Induction motor

- When the stator of a 3-phase induction motor is connected to a 3-phase a.c supply, a rotating magnetic field is established which rotates at synchronous speed.
- The magnetic flux of constant amplitude, rotating at synchronous speed, passes through the air-gap and cuts the rotor conductors which are stationary.
- Due to the relative speed between the rotating flux and the stationary conductors an e.m.f is induced in the latter as per Faraday's Laws of Electromagnetic Induction.
- The frequency of the induced e.m.f is the same as the supply frequency. Its magnitude is proportional to the relative velocity between the flux and the conductors, and its direction is given by Fleming's Right-Hand Rule.
- Since the rotor conductors form a closed circuit, rotor current is produced, whose direction in terms of Lenz's Law is such as to oppose the very cause producing it.
- According to Lenz's law, the direction of rotor current will be such that they tend to oppose the cause producing it.
- The cause producing the rotor current is the relative speed between the rotating field and the stationary rotor.
- Hence, to reduce this relative speed, the rotor starts running in the same direction as that of stator field and tries to catch it.
- In practice the rotor can never reach the speed of the rotating magnetic field produced by the stator.
- This is because if rotor speed equals the synchronous speed, then there is no relative speed between the rotating magnetic field and the rotor.
- This makes the rotor current zero and hence no torque is produced and the rotor will tend to remain stationary.
- In practice, windage and friction losses cause the rotor to slow down. Hence, the rotor speed ( $N$ ) is always less than the stator field speed ( $N_s$ ).

- Thus the induction motor cannot run with ZERO SLIP. The frequency of the rotor current  $f_r = sf$ .
- The difference between the synchronous speed ( $N_s$ ) of the rotating stator field and the actual rotor speed ( $N$ ) is called the **slip speed**.
- Slip speed =  $N_s - N$  depends upon the load on the motor

$$N_s - N$$

$$\% \text{ Slip (s)} = \frac{N_s - N}{N_s} * 100$$

$$N_s$$

**Note:** In an induction motor the slip value ranges from 2% to 4%

### Concept of Slip:

#### Slip:

- The difference between the synchronous speed  $N_s$  and the actual speed  $N$  of the rotor is called slip speed. (The quantity  $N_s - N$  is sometimes called the slip-speed.)
- It is usually expressed as a percentage of synchronous speed.
- It is apparent that the rotor (or motor) speed is  $N = N_s(1-S)$ . –
- In an induction motor, the change in slip from no-load to full-load is hardly 3 - 6%, so that the induction motor is essentially a constant speed motor

### Slip Significance

So slip of the induction motor is defined as the difference between the synchronous speed ( $N_s$ ) and actual speed of rotor i.e. motor ( $N$ ) expressed as a fraction of the synchronous speed ( $N_s$ ). This is also called absolute slip or fractional slip and is denoted as 's'.

Thus 
$$s = \frac{N_s - N}{N_s} \quad \dots \text{ (absolute slip)}$$

The percentage slip is expressed as,

$$\% s = \frac{N_s - N}{N_s} \times 100 \quad \dots \text{ (percentage slip)}$$

In terms of slip, the actual speed of motor ( $N$ ) can be expressed as,

$$N = N_s (1 - s) \quad \dots \text{ (from the expression of slip)}$$

At start, motor is at rest and hence its speed  $N$  is zero.

$$s = 1 \text{ at start}$$

This is maximum value of slip  $s$  possible for induction motor which occurs at start. While  $s = 0$  gives us  $N = N_s$ , which is not possible for an induction motor. So slip of induction motor cannot be zero under any circumstances.

#### Frequency of Rotor Current:

- When the rotor is at standstill, the frequency of rotor current is the same as the supply frequency.
- When there is relative speed between the rotor and the stator field, the frequency of the induced voltage, and hence the current, in the rotor varies with the rotor speed i.e., slip
- Let at any speed  $N$  of the rotor, the frequency of the rotor current be  $f'$ .
- Hence, the frequency of rotor current (or e.m.f) may be obtained by multiplying the supply frequency by fractional slip.

#### APPLICATIONS OF INDUCTION MOTORS:

##### Squirrel cage induction motor

- Squirrel cage induction motors are simple and rugged in construction, are relatively cheap and require little maintenance.
- Hence, squirrel cage induction motors are preferred in most of the industrial applications such as in

- i) Lathes
- ii) Drilling machines
- iii) Agricultural and industrial pumps
- iv) Industrial drives.

### **Slip ring induction motors**

Slip ring induction motors when compared to squirrel cage motors have high starting torque, smooth acceleration under heavy loads, adjustable speed and good running characteristics.

They are used in

- i) Lifts
- ii) Cranes
- iii) Conveyors , etc.,

#### **Problems:**

The frequency of the emf in the stator of a 4-pole induction motor is 50 Hz and in the rotor is 1.5 Hz. What is the slip and at what speed is the motor running?

#### **Solution:**

Synchronous speed,

$$f' = sf$$

$$1.5 = s \times 50$$

$$S = 0.03 \text{ Or } 3\%$$

$$N_s = \frac{120f}{P} = \frac{120 \times 50}{4} = 1500 \text{ rpm}$$

$$\text{Rotor speed, } N = N_s(1-s)$$

$$= 1500(1-0.03) = 1455 \text{ rpm}$$

### Exercise Problems

1. A 12 pole , 3 phase alternator is coupled to an engine running at 500r.p.m It supplies an IM, which has full load speed of 1440r.p.m Find the percentage slip and the number of poles the motor.
2. A 3-phase, 6 pole, 50Hz IM has a slip of 1% at no-load, and 3% at full load. Determine:  
i) Synchronous speed; ii) no-load speed; iii) full-load speed; iv) frequency of the rotor current at stand still ; v) frequency of the rotor current at full load.
3. A 3-phase, 8 pole, 50Hz IM has a slip of 1% at no-load, and 3% at full load. Determine;  
i) synchronous speed, ii) No-load speed, iii) Full load speed, iv) Frequency of rotor at stand still
4. The rotor induced voltage of a 3-phase, 4 –pole squirrel cage induction motor fed by a salient pole alternator is observed to make 1.5 alterations per second. The star connected alternator with 592, full pitched armature conductors in series per phase with distribution factor of 0.966 develops a line voltage of 6600 volts when the flux per pole is 60mWb. Determine the speed of the IM.
5. The frequency of the emf in the stator of a 4 pole induction motor is 50 Hz, & that in the rotor is 1.5 Hz. What is its slip, & at what speed is the motor running?
6. A 4 pole, 3 phase, 50 Hz induction motor runs at a speed of 1470 rpm. Find the frequency of the induced emf in the rotor under this condition
7. A 10 pole induction motor is supplied by a 6 pole alternator which is driven at 1200 rpm. If the motor runs with a slip of 3% , what is its speed?
8. A 3-phase, 6 pole, 50 Hz induction motor has a slip of 1% at no load, & 3% at full load. Determine synchronous speed, no-load speed, full-load speed, frequency of rotor current at stand still & frequency of rotor current at full load.
9. An 8 pole alternator runs at 750 rpm & supplies power to a 6 pole, 3 phase induction motor which runs at 970 rpm. What is the slip of induction motor?
10. If the electromotive force in the stator of an 8 pole induction motor has a frequency of 50Hz & that in the rotor 1.5 Hz, at what speed is the motor running & what is the slip?
11. A 6 pole, 3 phase, star connected alternator has an armature with 90 slots & 10 conductors/slot. It revolves at 1000 rpm. The flux/pole is 0.05 Wb. Calculate the emf generated/phase, if the winding factor is 0.97 & all conductors in each phase are in series.
12. A 6 pole induction motor supplied from a 3 phase, 50 Hz supply has a rotor frequency of 2.3 Hz. Calculate the %slip & the speed of the motor.

## **THREE PHASE SYNCHRONOUS GENERATORS**

### **Introduction:**

The machines generating ac emf are called as alternators. These work at specific constant speed called synchronous speed and hence in general called synchronous generators. The main difference b/w DC generators and alternators is that in alternators the field is rotating while armature is stationary and the commutator absent.

There are many sources of energy conversion in the world but most of the energy is converted by the synchronous generator.

### **Principle of Operation:**

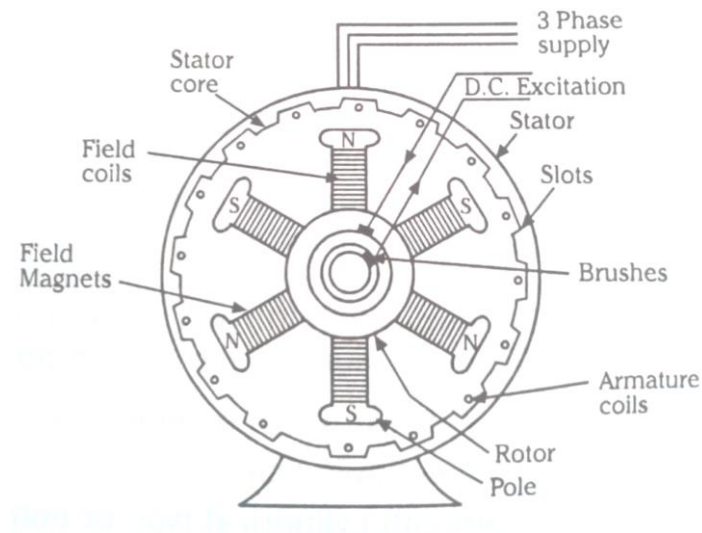
- Alternator (A.C generator) operates on the basic principle of electromagnetic induction i.e., when a conductor moves across a magnetic field or vice versa, an emf is induced in the conductor (Dynamically induced emf).
- The magnetic poles are excited by D.C. supply with a source of 125 V or 250 V.
- The exciting current is obtained from small DC Generator which is mounted on the shaft of the synchronous machine.
- When the rotor is rotated by means of any prime mover the stator conductors are cut by magnetic field, hence an emf is induced in the stator conductor.
- The frequency of the induced emf is given by  $f = \frac{PN}{120}$  Hz where P is the number of poles and N is the speed in rpm.

### **Advantages of Stationary Armature:**

1. It is simpler to insulate a stationary armature winding.
2. It is easier to brace armature winding against any deformation.
3. Only two slip rings are required for D.C supply for the rotor circuit.
4. Higher speed of the rotating field is possible.
5. It is easy to take power out from the stationary armature.
6. Problem of sparking at the slip ring can be avoided.
7. The High Voltage ac winding and its insulation not subjected to centrifugal forces.(11kV - 33 kV) (BETTER INSULATION)

## Construction of Alternator

The alternator consists of two parts: Stator and Rotor. Most of the alternators has stator as armature and rotor as field.



Stator:

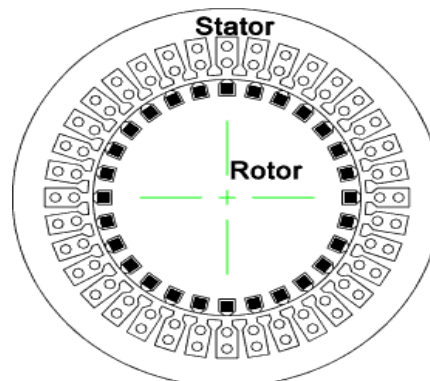


Fig: 4.6. Stator of alternator

It is stationary part of an alternator and it is built up of sheet steel of thin laminations having slots on its inner periphery (shown in Fig 4.6). A three-phase star connected winding is placed in the slots. The neutral of the winding is grounded. Steel is chosen to reduce hysteresis loss and laminated to reduce eddy current loss.

**Rotor:** There are two types rotors namely: Salient pole rotor and. Smooth cylindrical rotor

Salient pole rotor:

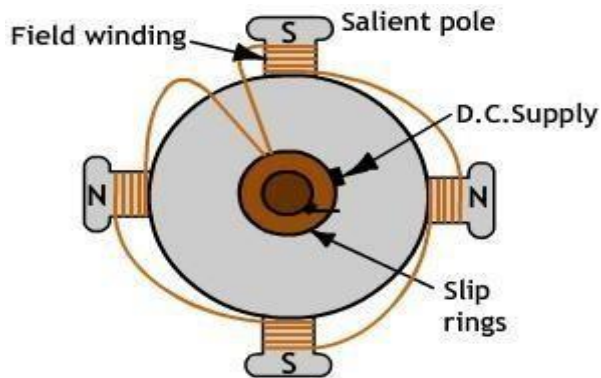


Fig:4.6(a) Salient pole Rotor

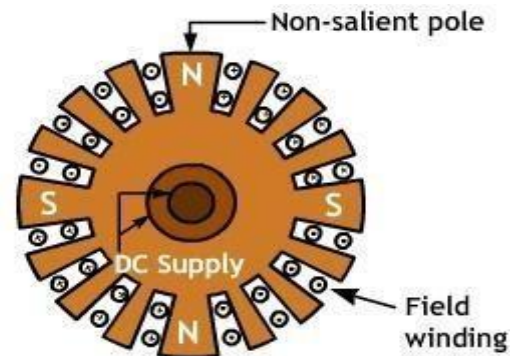
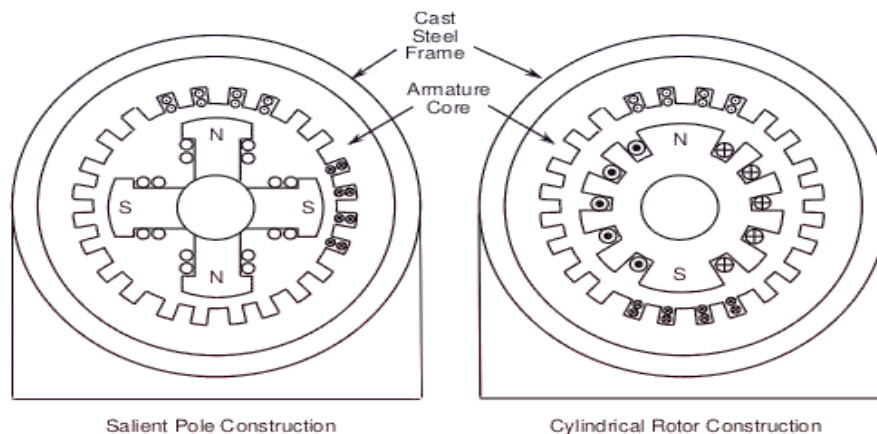


Fig:4.6(b) Smooth cylindrical Rotor



### Salient pole Rotor:

This is known as projected pole type as all the poles are projected out from the surface of the surface. Poles are made of thick steel laminations and bolted to rotor. These rotors have large diameter and small axial lengths. Mechanical strength is less, preferred for low speed alternators (125rpm-500rpm)

### Smooth cylindrical rotor:

This is known as non-salient type of rotor. The un slotted portions are the poles and surface is smooth which maintains uniform air gap b/w stator and rotor. These have small diameters and large axial lengths. Mechanically strong and can be used for high speed alternators (1500rpm-3000rpm)



Difference between Salient and Cylindrical Rotor:

**Difference Between Salient and Cylindrical Type of Rotor**

Salient Pole Type	Smooth Cylindrical Type
1 Poles are projecting out from the surface.	1. Unslotted portion of the cylinder acts as poles hence poles are non projecting.
2 Air gap is non uniform.	2. Air gap is uniform due to smooth cylindrical periphery.
3 Diameter is high and axial length is small.	3. Small diameter and large axial length is the feature.
4. Mechanically weak.	4. Mechanically robust.
5. Preferred for low speed alternators.	5. Preferred for high speed alternators i.e. for turboalternators.
6. Prime mover used are water turbines, I.C. engines.	6. Prime movers used are steam turbines, electric motors.
7. For same size, the rating is smaller than cylindrical type.	7. For same size, rating is higher than salient pole type.
8. Separate damper winding is provided.	8. Separate damper winding is not necessary.

Frequency of generated EMF:

If a conductor passes through a pair of poles, a complete cycle of emf will be induced. Let  $f$  = frequency of generated emf,  $P$  = no of poles,  $N$  =rpm speed .

Therefore, in one revolution,  $(P/2)$  pair of poles sweep past every armature conductor hence  $(P/2)$  emf cycles in one revolution. In one second there are  $N/60$  revolutions of rotor. Therefore, number of cycles of the induced emf /sec = number of cycles/revolution x No. of revolutions/sec.

$$(P/2) \times (N/60) = PN/120$$

$$\text{i.e., } f = PN/120 \text{ Hz.}$$

EMF Equation of Synchronous Generator:

# EMF EQUATION OF ALTERNATOR

Let  $Z$  = No. of conductors or coil sides in series per phase  
 $\phi$  = Flux per pole in webers  
 $P$  = Number of rotor poles  
 $N$  = Rotor speed in r.p.m.

In one revolution (i.e.,  $60/N$  second), each stator conductor is cut by  $P\phi$  webers  
 i.e.,

$$d\phi = P\phi; \quad dt = 60/N$$

$\therefore$  Average e.m.f. induced in one stator conductor

$$= \frac{d\phi}{dt} = \frac{P\phi}{60/N} = \frac{P\phi N}{60} \text{ volts}$$

Since there are  $Z$  conductors in series per phase,

$$\begin{aligned} \therefore \text{Average e.m.f./phase} &= \frac{P\phi N}{60} \times Z \\ &= \frac{P\phi Z}{60} \times \frac{120 f}{P} \quad \left( \because N = \frac{120 f}{P} \right) \\ &= 2f\phi Z \text{ volts} \end{aligned}$$

R.M.S. value of e.m.f./phase = Average value/phase  $\times$  form factor  
 $= 2f\phi Z \times 1.11 = 2.22 f\phi Z \text{ volts}$

$$\therefore E_{r.m.s.} / \text{phase} = 2.22 f\phi Z \text{ volts} \quad (i)$$

$$\frac{P\phi N}{60} \times Z_{ph} = \frac{P\phi N}{60} \times 2T_{ph} \text{ and}$$

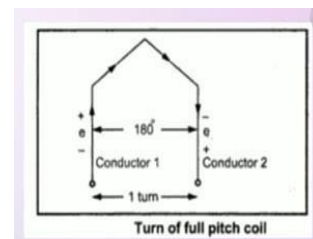
$$T_{ph} = \frac{Z_{ph}}{2}$$

$$\text{Average EMF} = 4 \times \phi \times T_{ph} \times \frac{PN}{120} = 4\phi f T_{ph}$$

**Form Factor = RMS Value / Average Value**

= RMS value = Form factor  $\times$  Average Value,

$$= 1.11 \times 4f\phi T = 4.44f\phi T \text{ Volts.}$$



And the actual available voltage per phase

$$= 4 K_c K_d f \phi T = 4 K_f K_c K_d f \phi T \text{ Volts.}$$

where  $T_{ph}$  = Number of turns per phase

$$\therefore T_{ph} = \frac{Z_{ph}}{2} \quad \dots \text{as 2 conductors constitute 1 turn}$$

**Winding Factor:**

The armature winding (conductor) of an alternator is distributed over the entire armature. Generally, we use short pitched, distributed windings, due to which voltage induced in the armature will reduce. Short pitched windings are used to get better waveform and to reduce unwanted harmonics.

$$K_w = K_p \cdot K_d \approx 0.95$$

**Pitch Factor:**

**Pitch factor ( $K_p$ )** = (vector sum of emf / arithmetic sum of emf)  $K_p = \cos(\alpha/2)$ ,

$K_p = 1$  for full pitched winding.

**Distribution factor**

$K_d$  = emf with distributed winding / emf with concentrated winding

$$K_d = \sin(m\beta/2) / (m \sin \beta/2)$$

$K_d = 1$  for concentrated winding.

$$\beta = 180^\circ / \text{no. of slots per pole.}$$

**Problems:**

1. The stator of an ac machine is wound for six poles, three phase. If the supply frequency is 25 Hz, what is the value of the synchronous speed?

$$\text{Solution: } N_s = 120f/P = 500 \text{ rpm}$$

2. Calculate the phase emf induced in a 4 pole, 3 phase, 50 Hz, star connected alternator with 36 slots and 30 conductors per slot. The flux per pole is 0.05 Webers. Assume factor of 0.95.

**Solution:**

Total number of slots = 36, Frequency  $f = NP / 120 = 375 \times 16 / 120 = 50 \text{ Hz}$

No. of slots per phase =  $36 / 3 = 12$

No. of conductors per slot = 30

No. of conductors per phase =  $12 \times 30 = 360$

No. of turns per phase =  $T = 360 / 2 = 180$

Assuming full pitch winding, pitch factor  $K_c = 1$

Phase emf =  $E_{ph} = 4K_f K_c K_d f T$  volts

$E_{ph} = 4 \times 1.11 \times 1 \times 0.95 \times 50 \times 0.05 \times 180 = 1898 \text{ V}$

3. A 3-phase, 16 pole alternator has a star connected winding having 144 slots and 10 conductors per slot. The flux per pole is 0.03 Webers and speed is 375 rpm. Find the frequency and phase and line voltage. Winding Factor  $K_d = 0.96$ , Pitch factor  $K_c = 1$ .

**Solution:**

Flux per pole,  $\phi = 0.03$  Webers

Frequency  $f = NP / 120 = 375 \times 16 / 120 = 50 \text{ Hz}$

No. of slots per phase =  $144 / 3 = 48$

No. of conductors per slot = 10

No. of conductors per phase =  $48 \times 10 = 480$

Turns per phase  $T = \text{conductors per phase} / 2 = 480 / 2 = 240$

Form factor =  $K_f = 1.11$

E.M.F generated per phase =  $E_{ph} = 4K_f K_c K_d f T$  volts

$$= 4 \times 1.11 \times 1 \times 0.96 \times 50 \times 0.03 \times 240$$

$$= 1534 \text{ volts.}$$

Line emf =  $\sqrt{3} \times 1534 = \mathbf{2657 \text{ volts}}$

4. A 3-phase star connected alternator with 12 poles generates 1100 volts on open circuit at a speed of 500 rpm. Assuming 180 turns per phase, a distribution factor of 0.96 and full pitched coils, find the useful flux per pole.

**Solution:**

Given line emf = 1100 volts

E.M.F EMF per phase  $E_{ph} = 1100 / \sqrt{3} = 635 \text{ volts}$

$f = NP / 120 = 500 \times 12 / 120 = 50 \text{ Hz}$

$$E_{ph} = 4K_f K_c K_d \Phi f \quad T \text{ volts}$$

$$K_f = 1.11$$

For full-pitched winding

$$\text{Pitch Factor} = K_c = 1$$

Distribution

$$\text{factor} = K_d = 0.96$$

$$T = \text{No. of turns per phase} = 180$$

Substituting in (1)

$$E_{ph} = 4K_f K_c K_d f \Phi T$$

volts

$$635 = 4 \times 1.11 \times 1 \times 0.96 \times 50 \times \quad \times 180$$

$$\text{Flux per pole} = \Phi = 635 / 4.44 \times 0.96 \times 50 \times 180 = \mathbf{0.0165 \text{ Webers}}$$

### Exercise Problems

1. A 12 pole 500 rpm star connected alternator has 48 slots with 15 conductors per slots. The flux per pole is 0.02wb. The winding factor is 0.97 and pitch factor is 0.98. Calculate the phase emf and line emf.
2. A 4 pole 1500 rpm star connected alternator has 9 slots per pole and 8 conductors per slot. Determine the flux per pole to give a terminal voltage of 3300V. Take winding factor and pitch factor as unity
3. A 2 pole, 3 phase alternator running at 3000rpm has armature slot with two conductors in each slot. Calculate flux per pole required to generate a line voltage of 2300V. Distribution factor is 0.952 and pitch factor is 0.956?
4. A 3 phase, star connected synchronous generator driven at 900 r/min is require to generate a line voltage of 460 V at 60 Hz on open circuit. This stator has two slots per pole per phase, and 4 conductors/slot. Calculate i) Number of poles  
ii) the useful flux per pole.