### Task 4

**Task 4:** Use 5-fold cross-validation to select the best  $\lambda$ . Compare the prediction performance between the "optimal" model and "full" model.

#### 5-fold CV

We write an R function cv.logit.lasso to conduct 5-fold cross-validation to select the best  $\lambda$ .

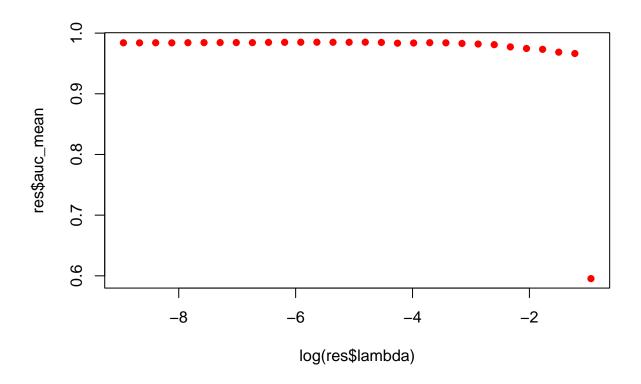
```
cv.logit.lasso <- function(x, y, nfolds = 5, lambda) {</pre>
  auc <- data.frame(matrix(ncol = 3, nrow = 0))</pre>
  colnames(auc) <- c("lambda", "fold", "auc")</pre>
  folds <- createFolds(y, k = nfolds)</pre>
  for (i in 1:nfolds) {
    valid_index <- folds[[i]]</pre>
    x_training <- x[-valid_index, ]</pre>
    y_training <- y[-valid_index]</pre>
    training_dat <- data.frame(cbind(y_training, x_training))</pre>
    x_valid <- cbind(rep(1, length(valid_index)), x[valid_index, ])</pre>
    y_valid <- y[valid_index]</pre>
    res <- LogisticLASSO(dat = training_dat, start = rep(0, ncol(training_dat)), lambda = lambda)
    for (k in 1:nrow(res)) {
      betavec <- res[k, 2:ncol(res)]</pre>
      u_valid <- x_valid %*% betavec
      phat_valid <- sigmoid(u_valid)[, 1]</pre>
      roc <- roc(response = y_valid, predictor = phat_valid)</pre>
      auc <- rbind(auc, c(lambda[k], i, roc$auc[1]))</pre>
  }
  colnames(auc) <- c("lambda", "fold", "auc")</pre>
  cv_res <- auc %>%
    group_by(lambda) %>%
    summarize(auc_mean = mean(auc)) %>%
    mutate(auc_ranking = min_rank(desc(auc_mean)))
  bestlambda <- min(cv_res$lambda[cv_res$auc_ranking == 1])
  return(cv_res)
}
```

Compare the results of cross-validation using glmnet and using our algorithm.

1. Our function cv.logit.lasso:

```
lambda_max <- max(t(x) %*% y) / length(y)
lambdas <- exp(seq(log(lambda_max), log(lambda_max) - 8, length = 30))
set.seed(1)
res = cv.logit.lasso(x, y, nfolds = 5, lambda = lambdas)
as.matrix(res %>% arrange(-lambda))
```

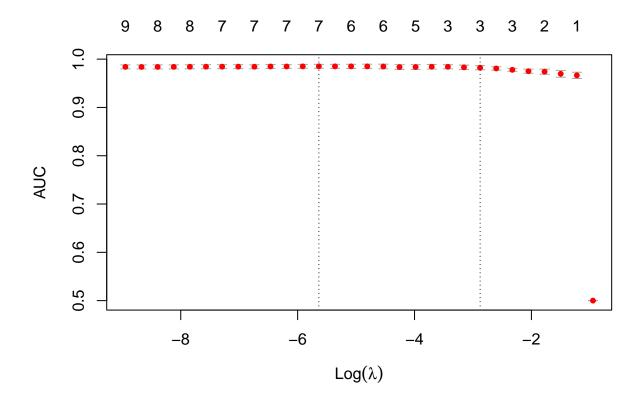
```
##
               lambda auc_mean auc_ranking
## [1,] 0.3880307793 0.5953964
                                         30
## [2,] 0.2944833885 0.9663792
                                         29
## [3,] 0.2234886270 0.9686033
                                         28
## [4,] 0.1696094528 0.9732774
                                         27
## [5,] 0.1287195992 0.9746754
                                         26
## [6,] 0.0976875695 0.9772606
                                         25
## [7,] 0.0741368160 0.9809819
                                         24
## [8,] 0.0562637346 0.9819983
                                         23
                                         22
## [9,] 0.0426995385 0.9829513
## [10,] 0.0324054314 0.9839803
                                         17
## [11,] 0.0245930523 0.9842396
                                         13
## [12,] 0.0186641003 0.9837128
                                         20
## [13,] 0.0141645142 0.9833856
                                         21
## [14,] 0.0107496992 0.9846370
                                          8
## [15,] 0.0081581359 0.9850634
                                          1
## [16,] 0.0061913529 0.9848939
                                          4
## [17,] 0.0046987267 0.9848928
                                          5
                                          3
## [18,] 0.0035659464 0.9849928
## [19,] 0.0027062595 0.9849937
                                          2
## [20,] 0.0020538280 0.9847940
                                          6
## [21,] 0.0015586862 0.9846939
                                          7
## [22,] 0.0011829144 0.9842929
                                         12
## [23,] 0.0008977346 0.9844208
                                          9
                                          9
## [24,] 0.0006813066 0.9844208
## [25,] 0.0005170555 0.9843215
                                         11
## [26,] 0.0003924025 0.9842212
                                         14
## [27,] 0.0002978012 0.9839216
                                         18
## [28,] 0.0002260066 0.9841236
                                         15
## [29,] 0.0001715204 0.9839214
                                         19
## [30,] 0.0001301698 0.9840223
                                         16
# best lambda
res$lambda[res$auc_ranking == 1]
## [1] 0.008158136
plot(log(res$lambda), res$auc_mean, pch = 16, col = "red")
```



#### 2. glmnet from ${\bf R}$ package caret

## [1] 0.003565946

```
plot(fit.logit.lasso)
```



The results are slightly different (mean AUC values).

```
tibble(
  lambda = lambdas,
  ours_AUC = res %>% arrange(-lambda) %>% .$auc_mean,
  cv.glmnet_AUC = fit.logit.lasso$cvm
) %>%
  knitr::kable()
```

lambda	ours_AUC	${\rm cv.glmnet\_AUC}$
0.3880308	0.5953964	0.5000000
0.2944834	0.9663792	0.9664002
0.2234886	0.9686033	0.9696155
0.1696095	0.9732774	0.9739870
0.1287196	0.9746754	0.9749820
0.0976876	0.9772606	0.9778663
0.0741368	0.9809819	0.9806886
0.0562637	0.9819983	0.9822062
0.0426995	0.9829513	0.9830639
0.0324054	0.9839803	0.9841889
0.0245931	0.9842396	0.9842478
0.0186641	0.9837128	0.9836220
0.0141645	0.9833856	0.9835959
0.0107497	0.9846370	0.9847465
0.0081581	0.9850634	0.9849718

lambda	ours_AUC	cv.glmnet_AUC
0.0061914	0.9848939	0.9850007
0.0046987	0.9848928	0.9849974
0.0035659	0.9849928	0.9850940
0.0027063	0.9849937	0.9849969
0.0020538	0.9847940	0.9847955
0.0015587	0.9846939	0.9847967
0.0011829	0.9842929	0.9842911
0.0008977	0.9844208	0.9844187
0.0006813	0.9844208	0.9844187
0.0005171	0.9843215	0.9843196
0.0003924	0.9842212	0.9842184
0.0002978	0.9839216	0.9840182
0.0002260	0.9841236	0.9839183
0.0001715	0.9839214	0.9838160
0.0001302	0.9840223	0.9840178

# ${\bf Prediction\ performance\ comparison}$

## NOT FINISHED!