Task 2

Task 2: Develop a Newton-Raphson algorithm to estimate your model.

The target function f given in task 1:

$$f(\beta; \mathbf{y}, \mathbf{X}) = \sum_{i=1}^{n} \left[Y_i \mathbf{x}_i^{\mathsf{T}} \beta - \log \left(1 + e^{\mathbf{x}_i^{\mathsf{T}} \beta} \right) \right]. \tag{1}$$

We develop a modified Newton-Raphson algorithm including a step-halving step. (we probably don't need to ensure that the direction of the step is an ascent direction, since in this example Hessian is always negative-definite. but Hessian could be computationally singular when the starting points are bad)

Algorithm 1 Newton-Raphson algorithm including a step-halving step

```
Require: f(\beta) - target function as given in (1); \beta_0 - starting value
Ensure: \widehat{\boldsymbol{\beta}} such that \widehat{\boldsymbol{\beta}} \approx \arg \max_{\boldsymbol{\beta}} f(\boldsymbol{\beta})
  1: i \leftarrow 0, where i is the current number of iterations
 2: f(\boldsymbol{\beta}_{-1}) \leftarrow -\infty
  3: while convergence criterion is not met do
             i \leftarrow i + 1
              \mathbf{d}_i \leftarrow -[\nabla^2 f(\boldsymbol{\beta}_{i-1})]^{-1} \nabla f(\boldsymbol{\beta}_{i-1}), where \mathbf{d}_i is the direction in the i-th iteration
             \lambda_i \leftarrow 1, where \lambda_i is the multiplier in the i-th iteration
             \beta_i \leftarrow \beta_{i-1} + \lambda_i \mathbf{d}_i
  7:
             while f(\beta_i) \leq f(\beta_{i-1}) do
  8:
                    \lambda_i \leftarrow \lambda_i/2
 9:
                    \boldsymbol{\beta}_i \leftarrow \boldsymbol{\beta}_{i-1} + \lambda_i \mathbf{d}_i
10:
              end while
12: end while
13: \hat{\boldsymbol{\beta}} \leftarrow \boldsymbol{\beta}_i
```

We write an R-function NewtonRaphson to implement the algorithm.

```
NewtonRaphson <- function(dat, func, start, tol = 1e-8, maxiter = 200) {
   i <- 0
   cur <- start
   stuff <- func(dat, cur)
   res <- c(0, stuff$f, cur)
   prevf <- -Inf
   X <- cbind(rep(1, nrow(dat)), as.matrix(dat[, -1]))
   y <- dat[, 1]
   warned <- 0
   while (abs(stuff$f - prevf) > tol && i < maxiter) {
      i <- i + 1
      prevf <- stuff$f
      prev <- cur
      d <- -solve(stuff$Hess) %*% stuff$grad
      cur <- prev + d</pre>
```

```
lambda <- 1
 maxhalv <- 0
  while (func(dat, cur)$f < prevf && maxhalv < 50) {
    maxhalv <- maxhalv + 1</pre>
    lambda <- lambda / 2
    cur <- prev + lambda * d
 stuff <- func(dat, cur)</pre>
 res <- rbind(res, c(i, stuff$f, cur))
 y_hat <- ifelse(X %*% cur > 0, 1, 0)
 if (warned == 0 && sum(y - y_hat) == 0) {
    warning("Complete separation occurs. Algorithm does not converge.")
    warned <- 1
 }
}
colnames(res) <- c("iter", "target_function", "(Intercept)", names(dat)[-1])</pre>
return(res)
```

Data preprocessing and data partition.

##

smoothness_se

```
bc_df <- read.csv("breast-cancer.csv")[-c(1, 33)] %% # remove variable ID and an NA column
  mutate(diagnosis = ifelse(diagnosis == "M", 1, 0)) # code malignant cases as 1
bc_df[, -1] <- scale(bc_df[, -1]) # predictors are standardized for the logistic-LASSO model in task 3
set.seed(1)
indexTrain <- createDataPartition(y = bc_df$diagnosis, p = 0.8, list = FALSE)
Training <- bc_df[indexTrain, ]</pre>
Test <- bc_df[-indexTrain, ]</pre>
glm(diagnosis ~ ., family = binomial(link = "logit"), data = Training)
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
##
## Call: glm(formula = diagnosis ~ ., family = binomial(link = "logit"),
##
       data = Training)
##
## Coefficients:
##
               (Intercept)
                                        radius_mean
                                                                 texture_mean
##
                   90.9690
                                          -2560.3939
                                                                       0.8812
##
            perimeter_mean
                                                              smoothness_mean
                                           area_mean
##
                  789.2724
                                          1539.8346
                                                                     128.8762
##
          compactness_mean
                                     concavity_mean
                                                          concave.points_mean
##
                 -346.6692
                                              9.0810
                                                                      215.4808
##
             symmetry_mean fractal_dimension_mean
                                                                    radius se
                                                                     617.5687
##
                   10.4773
                                            -28.6917
##
                texture se
                                       perimeter_se
                                                                      area se
##
                  -79.9789
                                           -917.3917
                                                                     628.6222
```

compactness_se

concavity_se

```
fractal_dimension_se
##
         concave.points_se
                                         symmetry_se
##
                  374.7611
                                            -108.6212
                                                                      -339.1646
##
              radius_worst
                                                                perimeter_worst
                                       texture_worst
##
                   197.9315
                                             155.0787
                                                                      1068.1069
##
                area worst
                                    smoothness worst
                                                              compactness worst
##
                  -606.1658
                                             -26.4759
                                                                      -346.4052
##
           concavity_worst
                                concave.points_worst
                                                                 symmetry_worst
##
                  373.2089
                                            -161.6177
                                                                        71.9489
## fractal_dimension_worst
##
                  282.8254
##
## Degrees of Freedom: 455 Total (i.e. Null); 425 Residual
## Null Deviance:
                         601.3
## Residual Deviance: 1.311e-06
                                     AIC: 62
logisticstuff <- function(dat, betavec) {</pre>
 dat <- as.matrix(dat)</pre>
 n <- nrow(dat)</pre>
  p \leftarrow ncol(dat) - 1
  X <- cbind(rep(1, n), dat[, -1]) # design matrix</pre>
  y <- dat[, 1] # response vector
  u <- X %*% betavec # x_i^T beta, i=1,\ldots,n
  f \leftarrow sum(y * u - log1pexp(u)) # function `log1pexp` to compute log(1 + exp(x)))
  p_{vec} \leftarrow sigmoid(u) \# function \ sigmoid \ to \ compute \ exp(x)/(1 + exp(x))
  grad <- t(X) %*% (y - p_vec)
  Hess <- -t(X) %*% diag(c(p_vec * (1 - p_vec))) %*% X
  return(list(f = f, grad = grad, Hess = Hess))
}
We fit a logistic regression model on the training data using our NewtonRaphson function.
res <- NewtonRaphson(dat = Training, func = logisticstuff, start = rep(0, ncol(Training)))
## Warning in NewtonRaphson(dat = Training, func = logisticstuff, start = rep(0, :
## Complete separation occurs. Algorithm does not converge.
tail(res)
    iter target_function (Intercept) radius_mean texture_mean perimeter_mean
##
##
      26
           -3.235158e-07
                             89.24826
                                         -2822.544
                                                      -1.373617
                                                                       960.4715
##
      27
                                         -2977.405
           -1.190284e-07
                             94.06615
                                                      -1.518686
                                                                      1010.5839
##
      28
           -4.379281e-08
                            98.80114
                                         -3134.863
                                                      -1.704236
                                                                      1063.1357
##
      29
           -1.611204e-08 103.40055
                                         -3296.525
                                                      -1.956417
                                                                      1119.6337
##
      30
           -5.927773e-09
                            107.76671
                                         -3465.377
                                                      -2.323911
                                                                      1182.8800
           -2.180833e-09
##
      31
                            111.72302
                                         -3646.824
                                                      -2.894920
                                                                      1257.9481
##
    area_mean smoothness_mean compactness_mean concavity_mean concave.points_mean
##
     1628.129
                     140.0014
                                      -368.0153
                                                      2.2563839
                                                                            224.3770
##
     1719.801
                                                      2.1569756
                     147.7362
                                       -388.2773
                                                                             236.9795
##
     1811.729
                     155.5634
                                       -408.6480
                                                      1.9513295
                                                                             249.5825
##
                     163.5407
                                      -429.1918
     1904.079
                                                      1.5722084
                                                                            262.1834
##
     1997.154
                     171.7748
                                      -450.0285
                                                      0.8948694
                                                                             274.7774
```

344.3180

-323.8534

##

-63.7660

```
##
     2091.500
                      180.4591
                                       -471.3749
                                                      -0.3063034
                                                                              287.3555
##
    symmetry_mean fractal_dimension_mean radius_se texture_se perimeter_se
##
         8.431909
                                 -31.04890
                                             664.0699
                                                       -82.56232
                                                                     -964.1721
         9.125769
##
                                 -32.85952
                                             700.8645
                                                       -87.29044
                                                                    -1017.2613
##
         9.763178
                                 -34.69764
                                             737.9928
                                                       -92.00209
                                                                    -1070.4606
##
                                 -36.58090
                                             775.6589
                                                       -96.68750
                                                                    -1123.8325
        10.311347
##
        10.709177
                                 -38.54224
                                             814.2424 -101.32850
                                                                    -1177.4929
##
        10.845978
                                 -40.64135
                                             854.4291 -105.89208
                                                                    -1231.6515
##
     area_se smoothness_se compactness_se concavity_se concave.points_se
##
    627.0977
                  -65.29781
                                   368.1306
                                                -343.4408
                                                                    393.0646
##
    661.3045
                  -69.00116
                                   388.5425
                                                -362.5350
                                                                    414.9751
    695.0465
                  -72.68019
                                                -381.7210
##
                                   409.1130
                                                                    436.9259
##
    728.0267
                  -76.31976
                                   429.9373
                                                -401.0546
                                                                    458.9405
                                                -420.6395
##
    759.6946
                  -79.89169
                                   451.1922
                                                                    481.0630
##
    789.0550
                  -83.34497
                                                -440.6629
                                                                    503.3729
                                   473.1970
##
    symmetry_se fractal_dimension_se radius_worst texture_worst
                                                                    perimeter_worst
##
      -113.2103
                            -360.5082
                                            247.8024
                                                           164.0343
                                                                            1108.082
##
      -119.4203
                            -380.3806
                                            263.6037
                                                           173.3317
                                                                            1168.164
                            -400.3884
##
      -125.6423
                                            279.9778
                                                           182.6679
                                                                            1228.146
##
      -131.8815
                            -420.6120
                                            297.2940
                                                           192.0677
                                                                            1287.947
##
      -138.1475
                            -441.2006
                                            316.2365
                                                           201.5777
                                                                            1347.420
      -144.4581
                            -462.4243
                                            338.0409
                                                                            1406.298
##
                                                           211.2818
##
    area_worst smoothness_worst compactness_worst concavity_worst
##
     -659.5481
                       -32.14856
                                           -373.8623
                                                             401.9769
##
     -696.8089
                       -33.84766
                                           -394.4311
                                                             424.5118
##
     -734.3769
                       -35.62248
                                           -415.2146
                                                             447.2448
##
     -772.4418
                       -37.52094
                                                             470.2984
                                           -436.3424
##
     -811.3548
                       -39.63214
                                           -458.0558
                                                             493.8996
##
     -851.7493
                       -42.11738
                                           -480.7909
                                                             518.4595
    concave.points_worst symmetry_worst fractal_dimension_worst
##
##
                -169.3830
                                 77.46596
                                                           300.1686
##
                -178.8370
                                 81.34102
                                                           316.7304
##
                -188.3071
                                 85.28220
                                                           333.3894
##
                -197.8017
                                 89.32603
                                                           350.2048
##
                -207.3369
                                 93.54077
                                                           367.2864
                                 98.05014
##
                -216.9415
                                                           384.8331
```

Our function also does not converge, because a complete separation occurs. A complete separation in a logistic regression, sometimes also referred as perfect prediction, which occurs whenever there exists some vector of coefficients $\boldsymbol{\beta}$ such that $Y_i = 1$ whenever $\mathbf{x}_i^{\top} \boldsymbol{\beta} > 0$ and $Y_i = 0$ whenever $\mathbf{x}_i^{\top} \boldsymbol{\beta} \leq 0$. In other words, complete separation occurs whenever a linear function of predictors can generate perfect predictions of response.

```
X <- cbind(rep(1, nrow(Training)), model.matrix(diagnosis ~ ., Training)[, -1])
y <- Training$diagnosis
coef_newton <- res[nrow(res), -c(1, 2)]
y_hat <- ifelse(X %*% coef_newton > 0, 1, 0) # predictions
sum(y - y_hat) # prefect separation
```

[1] 0

We compare the results of using the glm function and our NewtonRaphson function. (meaningless, since both do not converge)

```
tibble(
  predictor = c("(Intercept)", names(Training)[-1]),
  ours = res[nrow(res), -c(1, 2)],
  glm = glm(diagnosis ~ ., family = binomial(link = "logit"), data = Training)$coefficients
) %>%
  knitr::kable()
```

predictor	ours	glm
(Intercept)	111.7230205	90.9690365
radius mean	-3646.8235396	-2560.3938902
texture_mean	-2.8949199	0.8812037
perimeter_mean	1257.9481182	789.2724398
area_mean	2091.5001211	1539.8345650
$smoothness_mean$	180.4591376	128.8762247
compactness_mean	-471.3749334	-346.6691873
concavity_mean	-0.3063034	9.0810082
concave.points_mean	287.3555092	215.4808031
symmetry_mean	10.8459784	10.4772590
fractal_dimension_mean	-40.6413497	-28.6916549
radius_se	854.4290934	617.5687358
texture_se	-105.8920782	-79.9788638
perimeter_se	-1231.6514585	-917.3916527
area_se	789.0550144	628.6222313
$smoothness_se$	-83.3449730	-63.7660367
$compactness_se$	473.1970464	344.3180183
concavity_se	-440.6629326	-323.8533730
concave.points_se	503.3728692	374.7610875
symmetry_se	-144.4580558	-108.6211792
$fractal_dimension_se$	-462.4242540	-339.1646360
radius_worst	338.0408767	197.9314738
texture_worst	211.2817780	155.0787339
perimeter_worst	1406.2984247	1068.1068808
area_worst	-851.7493135	-606.1657870
$smoothness_worst$	-42.1173805	-26.4759499
$compactness_worst$	-480.7909132	-346.4051824
concavity_worst	518.4595221	373.2089180
$concave.points_worst$	-216.9414972	-161.6177074
$symmetry_worst$	98.0501371	71.9488540
$fractal_dimension_worst$	384.8330525	282.8253512

Compute the test AUC. (should NOT be used for model comparison)

```
betavec.logit <- res[nrow(res), 3:ncol(res)]
# test data
X_test <- cbind(rep(1, nrow(Test)), model.matrix(diagnosis ~ ., Test)[, -1])
y_test <- Test$diagnosis
# AUC
u_test <- X_test %*% betavec.logit
phat_test <- sigmoid(u_test)[, 1]
roc.logit.test <- roc(response = y_test, predictor = phat_test)
auc.logit.test <- roc.logit.test$auc[1]</pre>
```

Resampling on training data: Does the following resampling method work?

```
?caret::resamples
```

Hothorn et al. The design and analysis of benchmark experiments. Journal of Computational and Graphical Statistics (2005) vol. 14 (3) pp. 675-699

https://ro.uow.edu.au/cgi/viewcontent.cgi?article=3494&context=commpapers

RW-OOB

```
B = 100 # number of bootstrap samples
set.seed(1)
auc.logit <- rep(NA, B)</pre>
for (i in 1:B) {
  index_bs <- sample(nrow(Training), replace = TRUE)</pre>
  sample <- Training[index_bs, ]</pre>
  out <- Training[-index_bs, ]</pre>
  res <- NewtonRaphson(dat = sample, func = logisticstuff, start = rep(0, ncol(sample)))
  betavec <- res[nrow(res), 3:ncol(res)]</pre>
  X <- cbind(rep(1, nrow(out)), model.matrix(diagnosis ~ ., out)[, -1])</pre>
 y <- out$diagnosis
  u <- X %*% betavec
  phat <- sigmoid(u)[, 1]</pre>
  roc <- roc(response = y, predictor = phat)</pre>
  auc <- roc$auc[1]</pre>
  auc.logit[i] <- auc</pre>
}
## Warning in NewtonRaphson(dat = sample, func = logisticstuff, start = rep(0, :
## Complete separation occurs. Algorithm does not converge.
## Warning in NewtonRaphson(dat = sample, func = logisticstuff, start = rep(0, :
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summary(auc.logit)

## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.9117 0.9518 0.9622 0.9611 0.9703 0.9933

boxplot(auc.logit)
```

