

## Task 4

**Task 2:** With the estimated model parameters and covariate values, you can calculate the predicted wind speed for each time point using the model equation. This way, you can track the hurricane and compare the predicted wind speeds with the actual wind speeds recorded during the hurricane. Please evaluate how well the estimated Bayesian model can track individual hurricanes.

### Prediction Functions

Import parameters from task 1 & 2.

```
# load parameters
beta_list = read.csv("./data/B_list_lastmean.csv")
gamma_list = read.csv("./data/gamma_list.csv")
```

Implement the prediction process of wind speed for each hurricane in R.

```
Speed_Prediction = function(beta, gamma, burn_bindex, burn_times){
  # final parameters to be used
  # the rows of beta_sample means the last 5000, 4000, 3000, 2000 and 1000
  # burn in the MC chains. change this based on the resulting plots
  # if burn-in is set to 8000, then we set burn_bindex as 4 to pick the 4th row of beta_sample
  # index is the useful samples (used for estimates & CIs)
  para_beta = beta[burn_bindex,]
  para_beta = as.matrix(para_beta)
  index = (burn_times + 1):10000
  gamma_sample = gamma[index, ]
  para_gamma = rbind(colMeans(gamma_sample))

  # prediction function
  Windspeed_Predict = function(index_hurricane, index_time){
    predict_speed =
      Z[[index_hurricane]][index_time,] %*% para_beta[((index_hurricane - 1) * 5 + 1):((index_hurricane - 1) * 5 + 5)] +
      (X %*% t(para_gamma))[index_hurricane, ]
    return(predict_speed)
  }

  # initialize prediction table
  Y_table = split(Training$Wind.kt, Training$ID) %>%
    lapply(function(x) x[-c(1:2)]) %>%
    lapply(as.data.frame) %>%
    lapply(function(df) {
      df$wind_obs = df$X[[1]]
      df$wind_predict = df$wind_obs
      df = as.matrix(df)
      subset(df, select = c("wind_obs", "wind_predict"))
    })

  # updating prediction table
  for (i in 1:length(names(Z))) {
```

```

    for (j in 1:nrow(Z[[i]])) {
      Y_table[[i]][, 2][j] = Windspeed_Predict(i, j)
    }
  }
  return(Y_table)
}

Y_table_set = Speed_Prediction(beta = beta_list, gamma = gamma_list, burn_bindex = 4, burn_times = 8000)

Visual_Table = function(Y_table_input){
  Y_table = Y_table_input
  hurri_res = data.frame(ID = "example",
                        RMSE = 0,
                        R_squared = 0)
  for (i in 1:length(names(Z))) {
    # calculate
    RMSE = sqrt(mean((Y_table[[i]][,1] - Y_table[[i]][,2])^2))
    # calculate R^2
    y = Y_table[[i]][,1]
    y_hat = Y_table[[i]][,2]
    mean_y = mean(y)
    SSR = sum((y_hat - y)^2)
    SST = sum((y - mean_y)^2)
    R_squared = 1 - SSR/SST
    new_row = c(names(Z)[i], RMSE, R_squared)
    hurri_res = rbind(hurri_res, new_row)
  }

  hurri_res = hurri_res[-1, ]
  hurri_res$RMSE = as.numeric(hurri_res$RMSE)
  hurricane_info = Training %>%
    group_by(ID) %>%
    slice(1) %>%
    dplyr::select(ID, Season, Month, Nature) %>%
    ungroup(ID) %>%
    mutate(
      Active = ifelse(Month %in% month.name[8:10], "Active", "Inactive"),
      Active = factor(Active, levels = c("Inactive", "Active")))

  hurricane_loc = Training %>%
    distinct(ID, .keep_all = TRUE) %>%
    dplyr::select(ID, Latitude, Longitude, Wind.kt) %>%
    mutate(Start_Lat = Latitude,
           Start_Lon = Longitude,
           Start_Speed = Wind.kt) %>%
    dplyr::select(ID, Start_Lat, Start_Lon, Start_Speed)

  hurricane_info = left_join(hurricane_info, hurricane_loc, by = "ID")

  hurri_res = left_join(hurri_res, hurricane_info, by = "ID")

  hurri_res$R_squared = as.numeric(hurri_res$R_squared)

  return(hurri_res)
}

```

```
}
```

## Visualization Analysis

### Summary Table

```
hurri_res = Visual_Table(Y_table_set)

hurri_res_brief = hurri_res %>%
  dplyr::select(c(1:3)) %>%
  head(15)

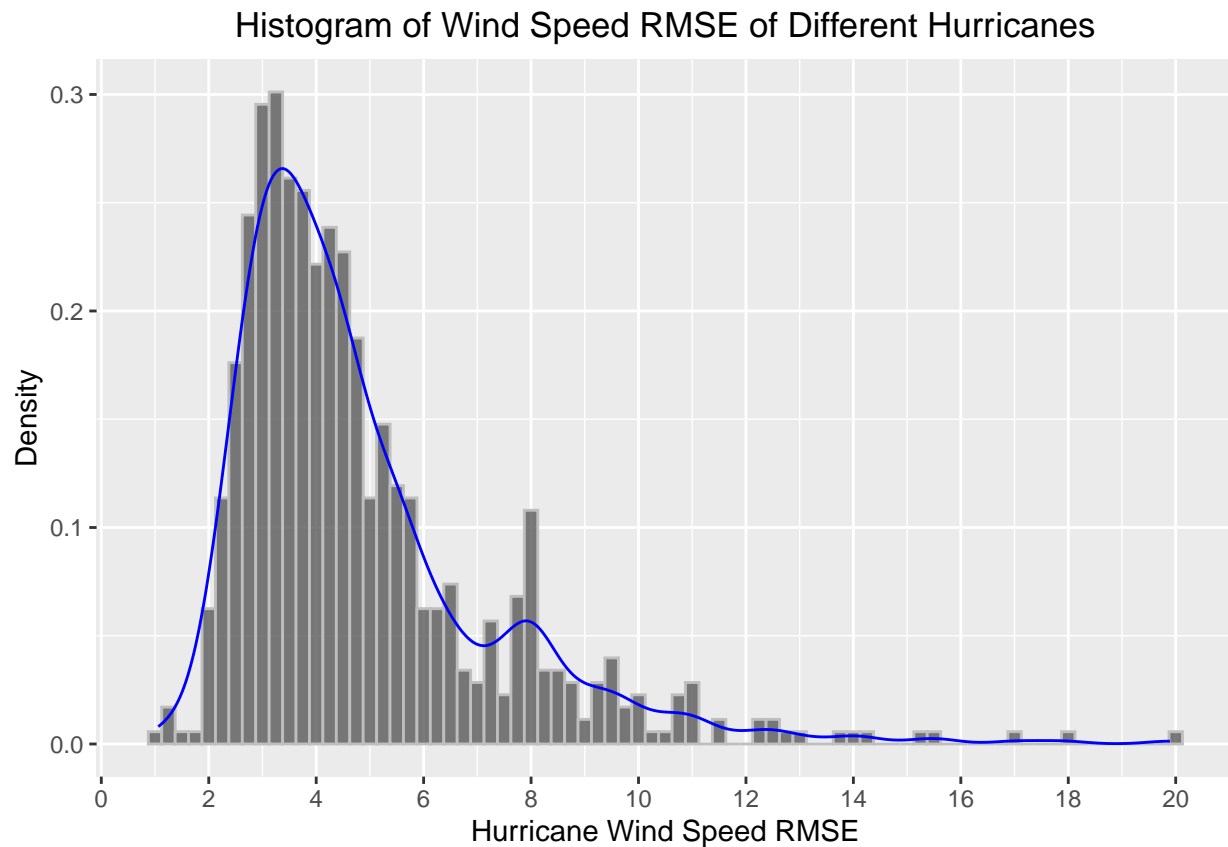
write.csv(hurri_res_brief, "data/prediction_brief.csv", row.names = FALSE)
write.csv(hurri_res, "data/prediction_all.csv", row.names = FALSE)

hurri_res_brief %>%
  knitr::kable(digits = 4)
```

ID	RMSE	R_squared
ABBY.1960	8.8618	0.7710
ABBY.1964	9.6232	0.3062
ABBY.1968	3.5170	0.9355
ABLE.1950	3.6853	0.9812
ABLE.1951	3.4945	0.9766
ABLE.1952	4.5528	0.9576
AGNES.1972	5.2515	0.8880
ALBERTO.1982	8.0544	0.7494
ALBERTO.1988	2.6070	0.7430
ALBERTO.1994	4.3865	0.8811
ALBERTO.2000	3.7848	0.9626
ALBERTO.2006	4.3741	0.7867
ALBERTO.2012	3.2393	0.8012
ALEX.1998	2.9373	0.7284
ALEX.2004	5.4494	0.9540

### Overall RMSE prediction performance.

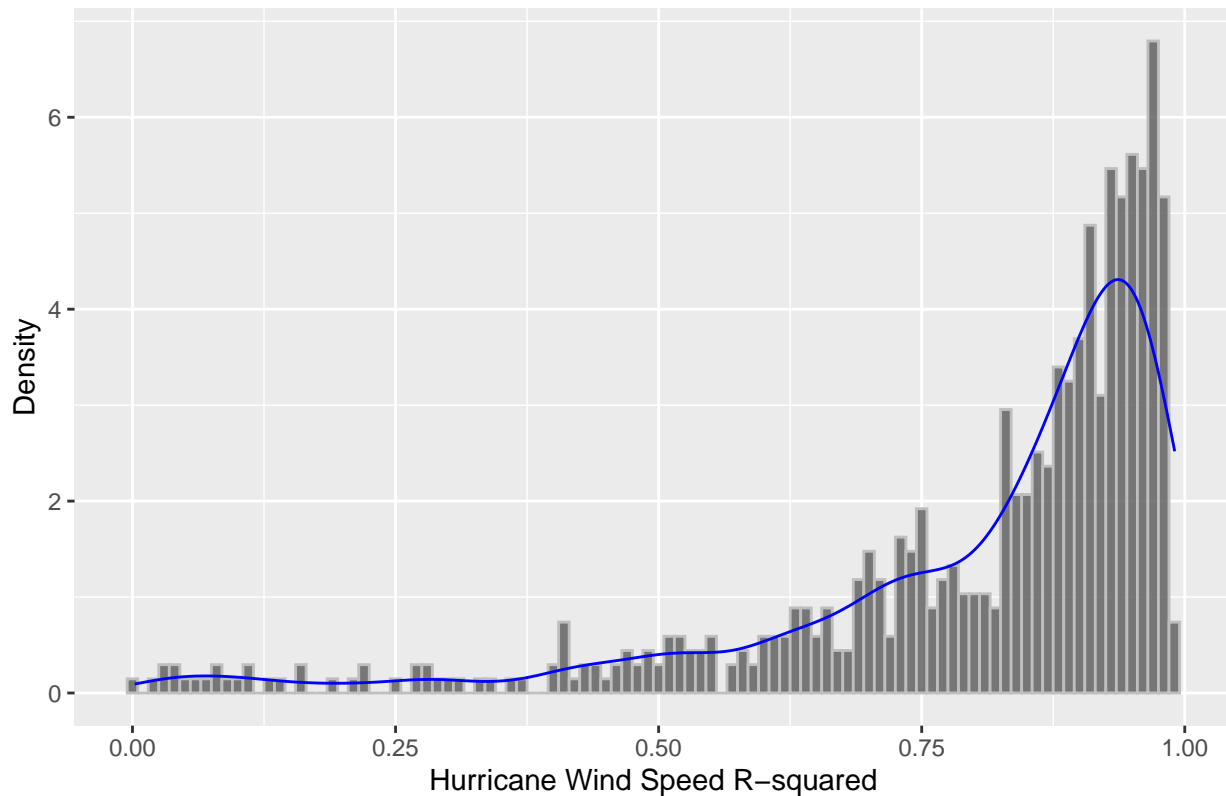
```
# overall density of RMSE
ggplot(hurri_res, aes(x = RMSE)) +
  geom_histogram(aes(y = after_stat(density)), binwidth = 0.25, alpha = 0.8, color = "grey") +
  geom_density(size = 0.5, color = "blue", lty = 1) +
  scale_x_continuous(breaks = seq(0, 20, by = 2)) +
  labs(title = "Histogram of Wind Speed RMSE of Different Hurricanes", x = "Hurricane Wind Speed RMSE",
  theme(plot.title = element_text(hjust = 0.5))
```



Overall R-squared performance.

```
# overall density of R-squared
ggplot(hurri_res %>% filter(0 <= R_squared & R_squared <= 1), aes(x = R_squared)) +
  geom_histogram(aes(y = after_stat(density)), binwidth = 0.01, alpha = 0.8, color = "grey") +
  geom_density(size = 0.5, color = "blue", lty = 1) +
  labs(title = "Histogram of Wind Speed R-squared of Different Hurricanes", x = "Hurricane Wind Speed R")
theme(plot.title = element_text(hjust = 0.5))
```

Histogram of Wind Speed R-squared of Different Hurricanes



Difference of overall RMSE using different numbers of burn-in.

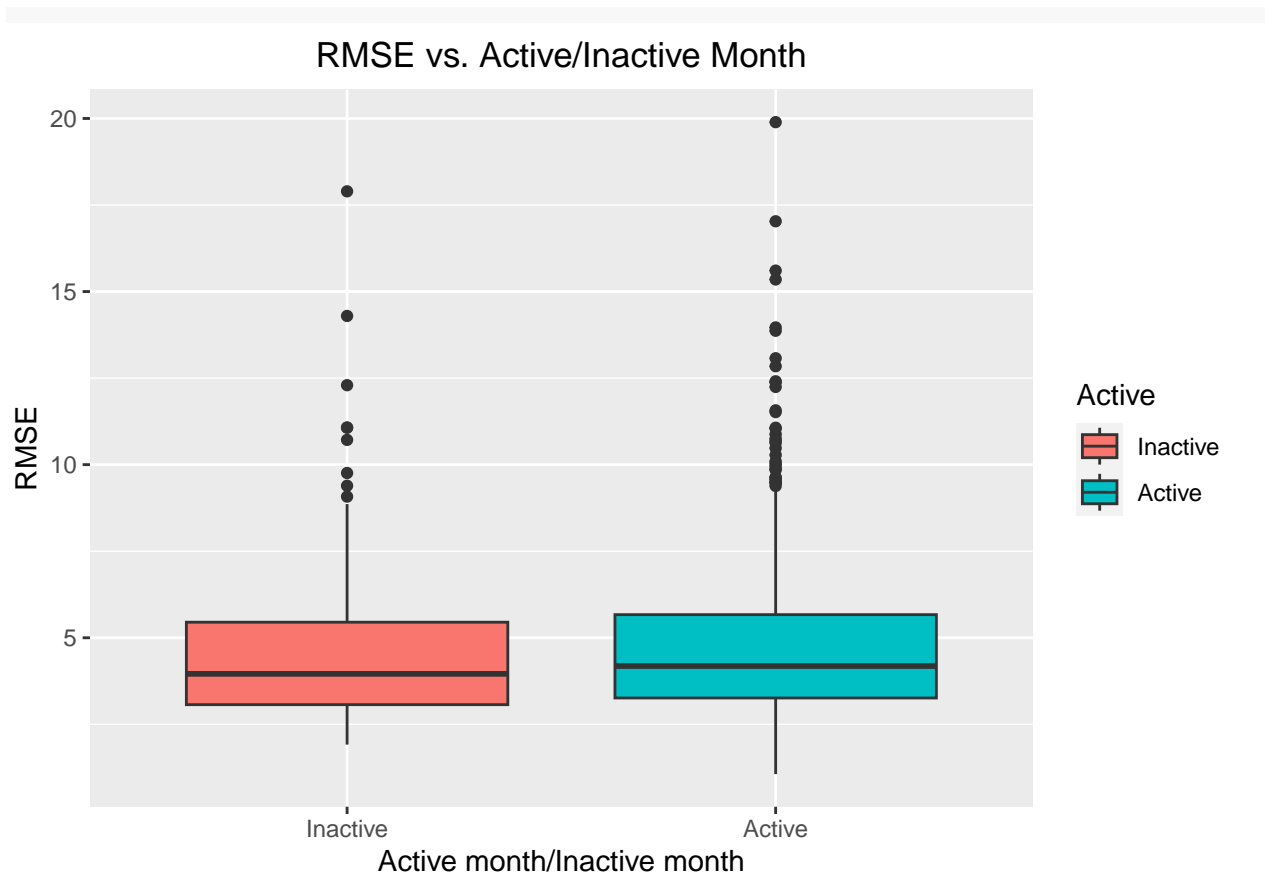
Result shows that there is not obvious difference here.

The difference of RMSE distribution of difference properties.

```
# distribution of RMSE on hurricane nature
nature1=ggplot(hurri_res, aes(x = Nature, y = RMSE, fill = Nature)) +
  geom_boxplot() +
  scale_color_manual(values = c("#E69F00", "#56B4E9", "#009E73", "#F0E442", "#0072B2")) +
  labs(title = "RMSE vs. Nature", x = "Nature", y = "RMSE") +
  theme(plot.title = element_text(hjust = 0.5))

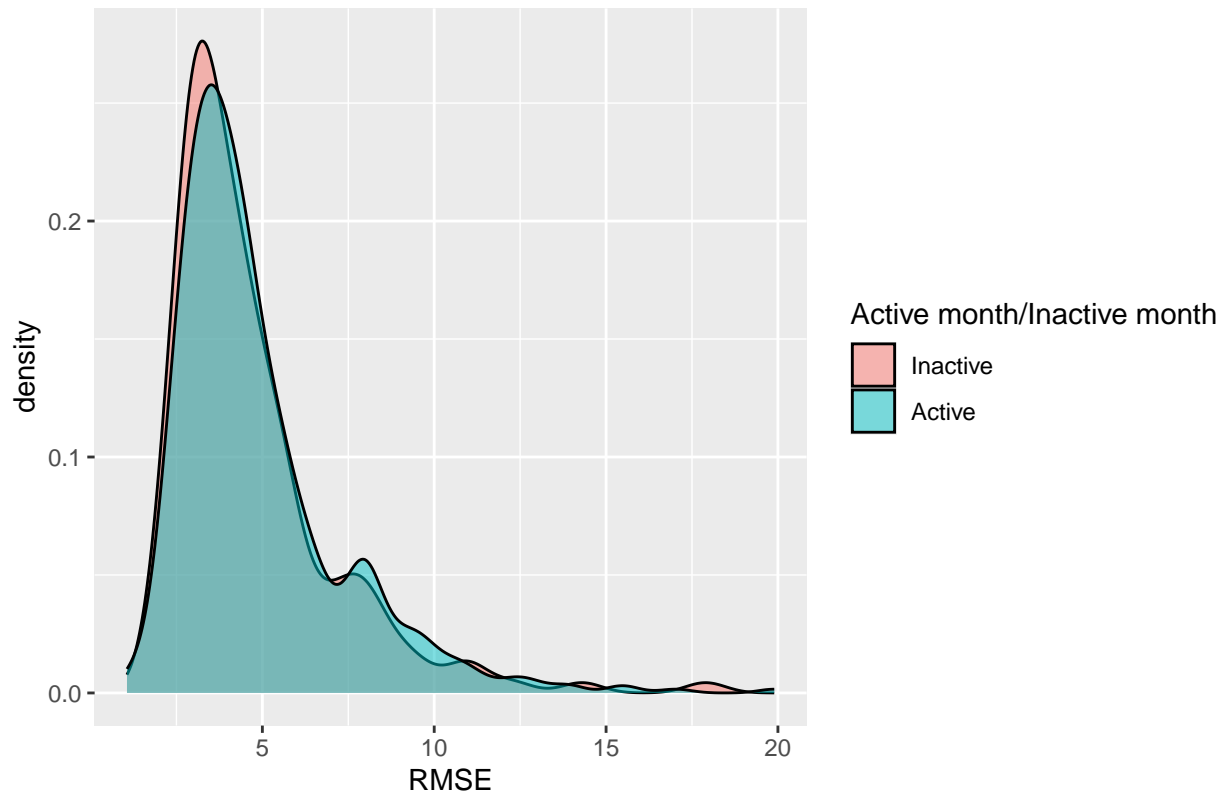
nature2=ggplot(hurri_res, aes(x = RMSE, fill = Nature)) +
  geom_density(alpha = 0.5) +
  labs(title = "RMSE vs. Nature", x = "RMSE", fill = "Nature") +
  theme(plot.title = element_text(hjust = 0.5))

# distribution of RMSE on hurricane active months
ggplot(hurri_res, aes(x = Active, y = RMSE, fill = Active)) +
  geom_boxplot() +
  labs(title = "RMSE vs. Active/Inactive Month", x = "Active month/Inactive month", y = "RMSE") +
  theme(plot.title = element_text(hjust = 0.5))
```

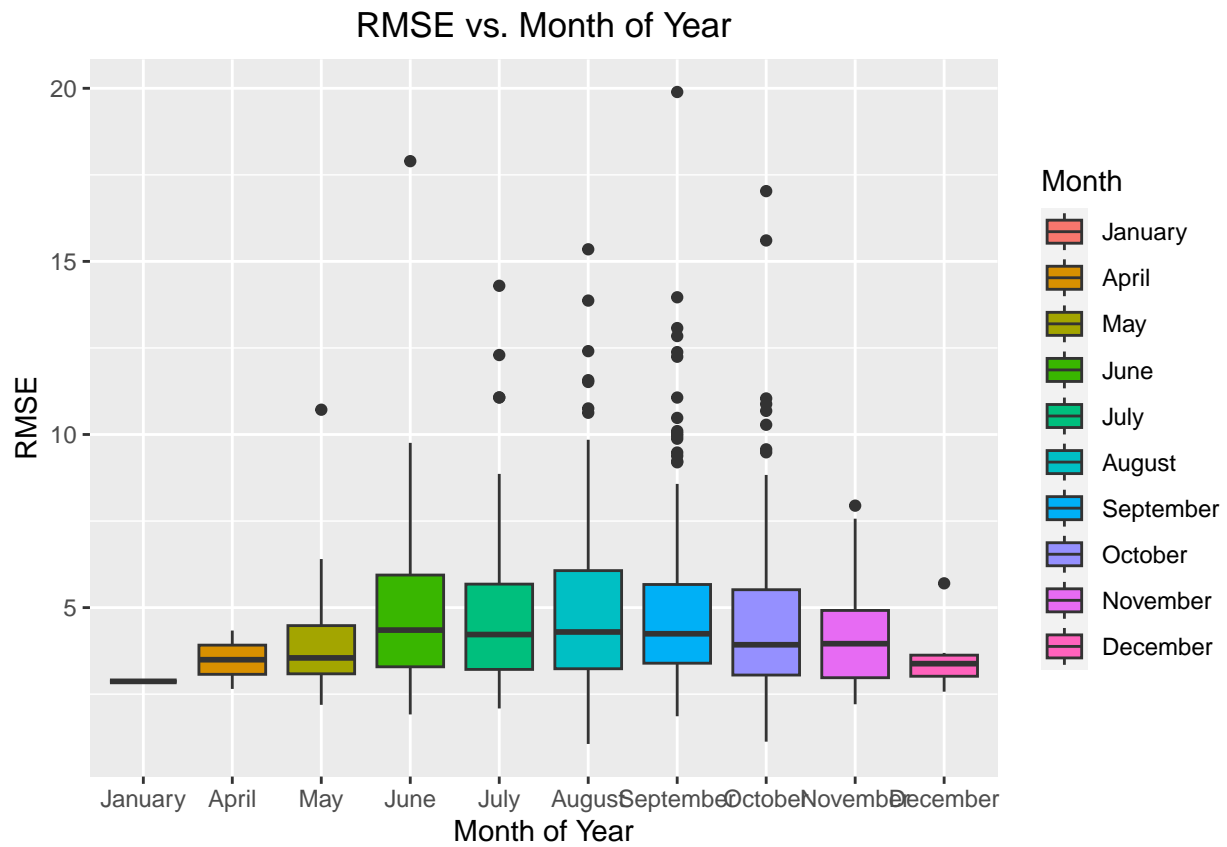


```
ggplot(hurri_res, aes(x = RMSE, fill = Active)) +
  geom_density(alpha = 0.5) +
  labs(title = "RMSE vs. Active/Inactive Month", x = "RMSE", fill = "Active month/Inactive month") +
  theme(plot.title = element_text(hjust = 0.5))
```

RMSE vs. Active/Inactive Month



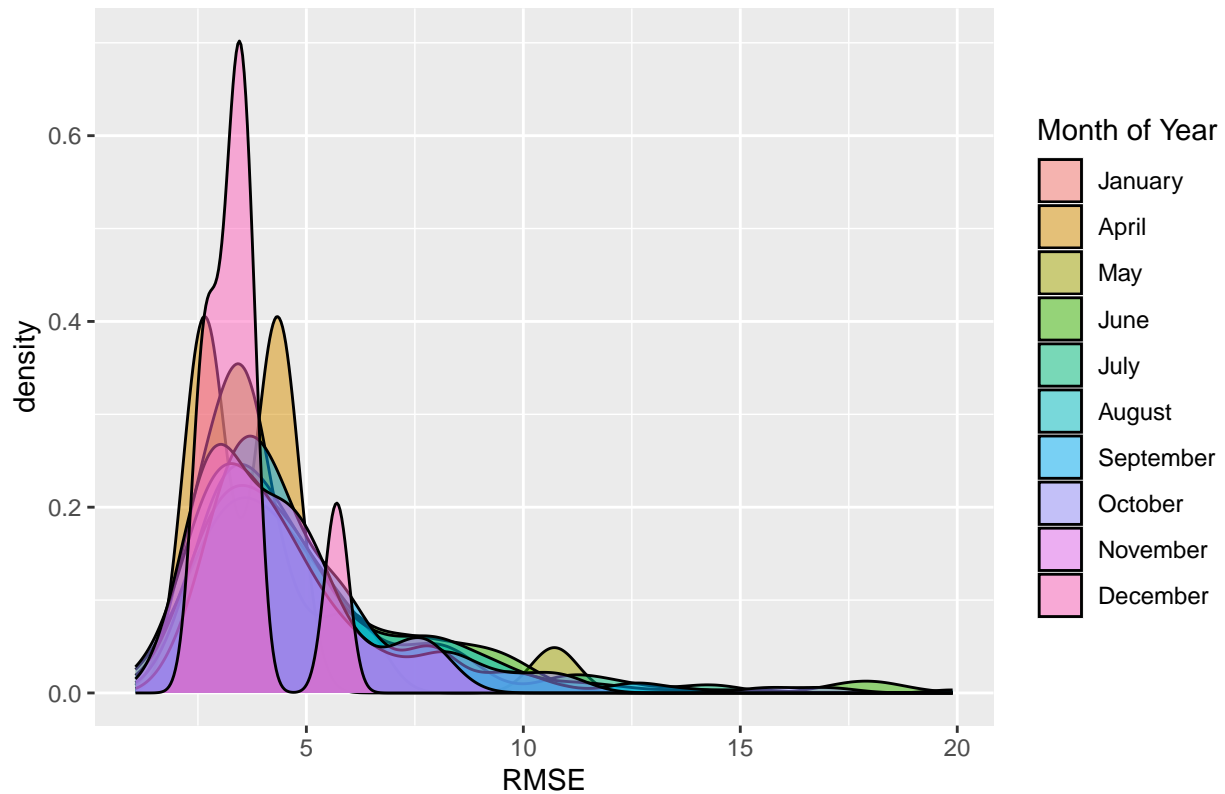
```
ggplot(hurri_res, aes(x = Month, y = RMSE, fill = Month)) +  
  geom_boxplot() +  
  labs(title = "RMSE vs. Month of Year", x = "Month of Year", y = "RMSE") +  
  theme(plot.title = element_text(hjust = 0.5))
```



```
ggplot(hurri_res, aes(x = RMSE, fill = Month)) +
  geom_density(alpha = 0.5) +
  labs(title = "RMSE vs. Month of Year", x = "RMSE", fill = "Month of Year") +
  theme(plot.title = element_text(hjust = 0.5))
```

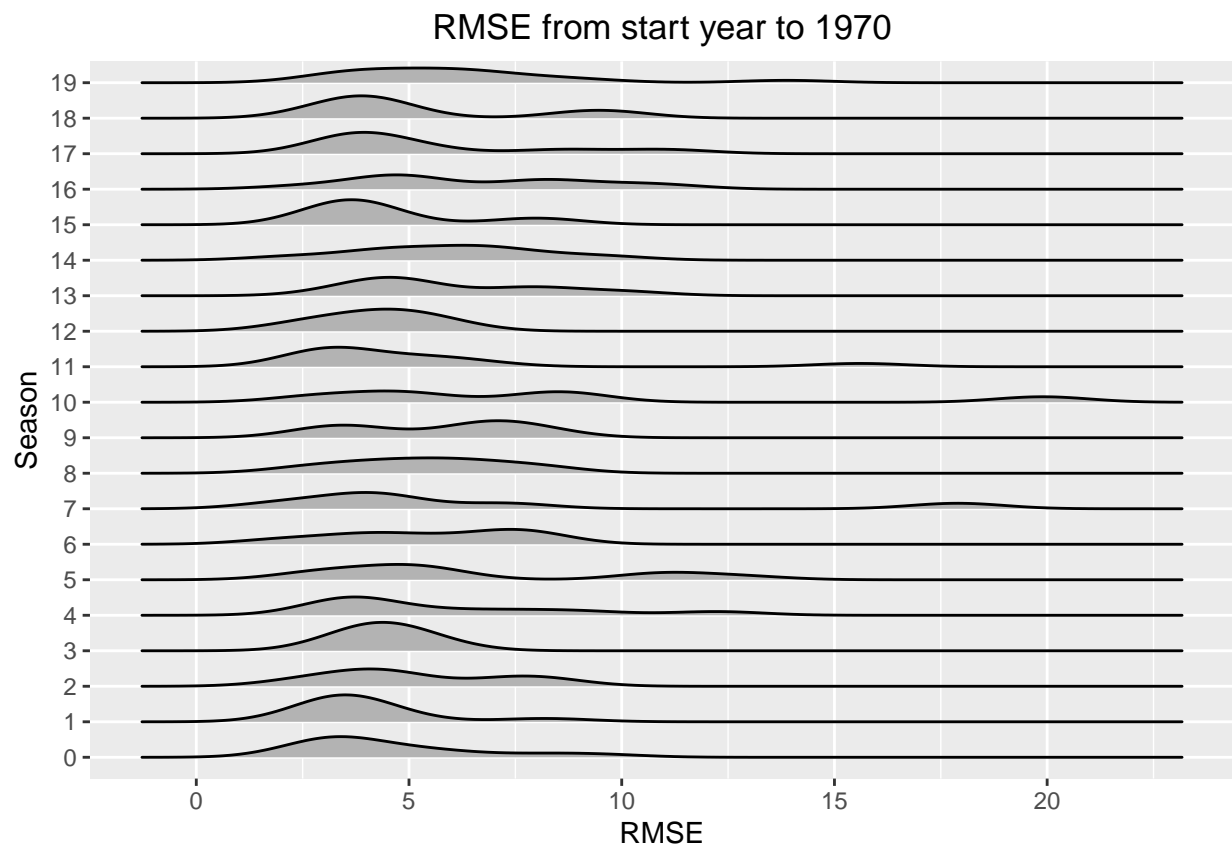


RMSE vs. Month of Year



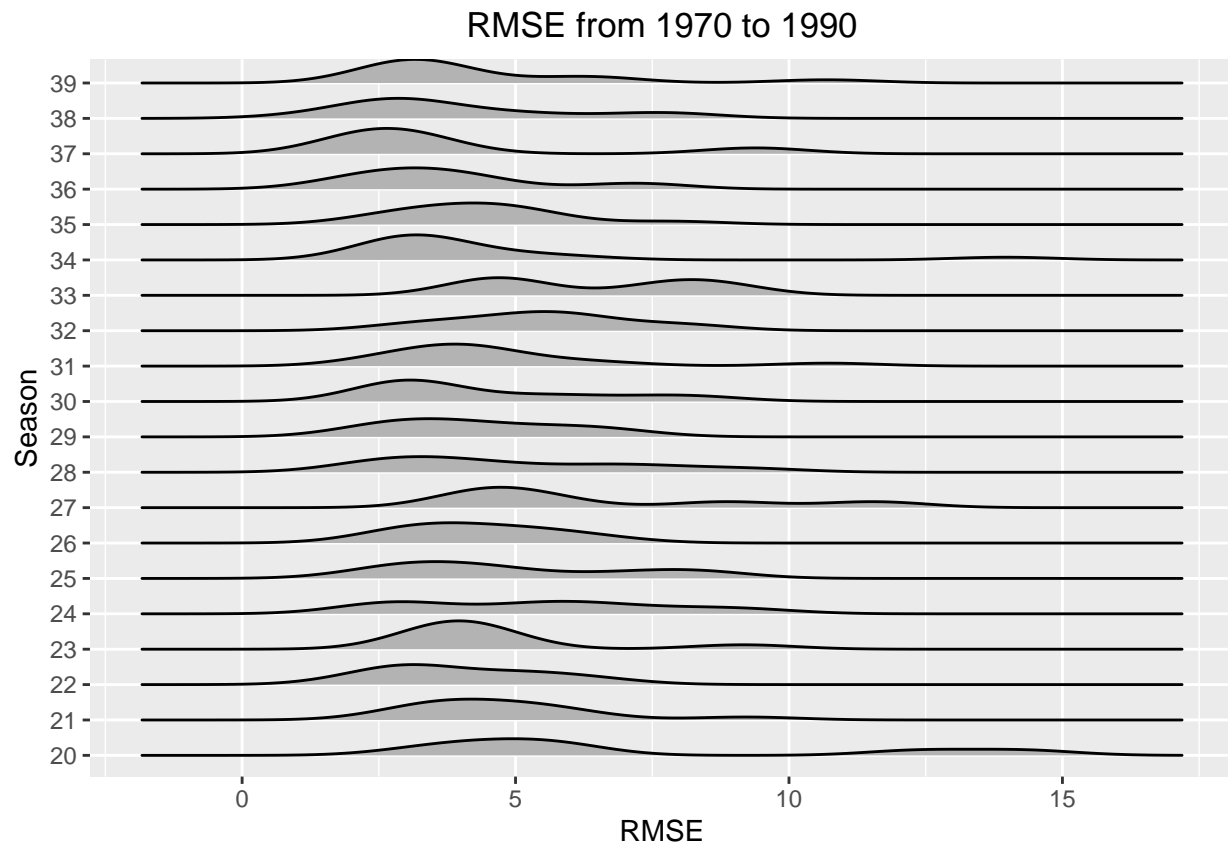
```
# distribution of RMSE on hurricane season
ggplot(hurri_res %>% filter(Season < 20) %>% mutate(Season = factor(Season)), aes(x = RMSE, y = Season)) +
  geom_density_ridges(scale = 0.8) +
  labs(title = "RMSE from start year to 1970", x = "RMSE", y = "Season") +
  theme(plot.title = element_text(hjust = 0.5))
```

```
## Picking joint bandwidth of 1.09
```



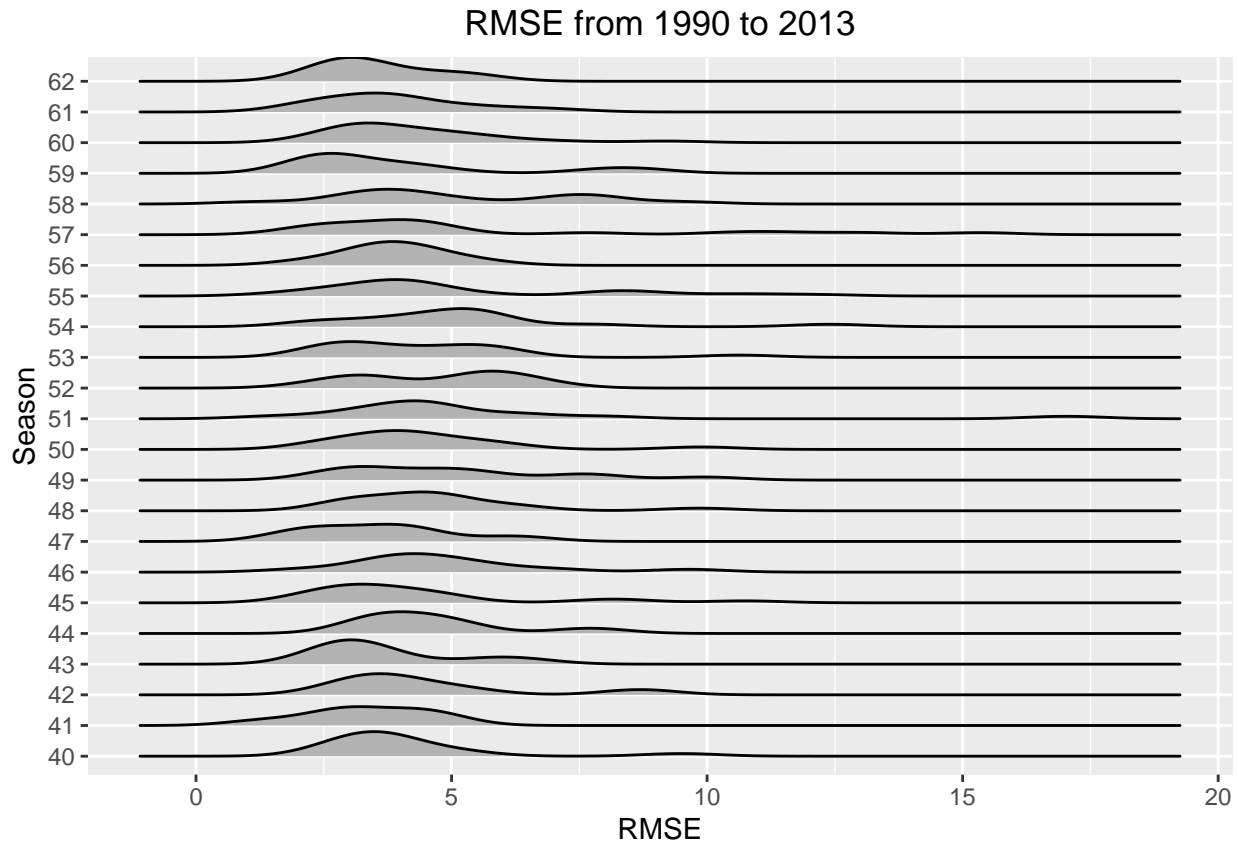
```
ggplot(hurri_res %>% filter(Season >= 20 & Season < 40) %>% mutate(Season = factor(Season)), aes(x = RMSE, y = Season)) +
  geom_density_ridges(scale = 0.8) +
  labs(title = "RMSE from 1970 to 1990", x = "RMSE", y = "Season") +
  theme(plot.title = element_text(hjust = 0.5))
```

```
## Picking joint bandwidth of 0.964
```



```
ggplot(hurri_res %>% filter(Season >= 40 & Season < 63) %>% mutate(Season = factor(Season)), aes(x = RMSE, y = Season)) +
  geom_density_ridges(scale = 0.8) +
  labs(title = "RMSE from 1990 to 2013", x = "RMSE", y = "Season") +
  theme(plot.title = element_text(hjust = 0.5))
```

```
## Picking joint bandwidth of 0.741
```



Relation between RMSE and the start location information.

(not finally included since there is not much useful information in there)

Prediction performance on some specific example hurricanes.

```
for (i in 1:5) {
  example_hurri = as.data.frame(Y_table_set[[i*5]])
  example_hurri$index = 1:nrow(example_hurri)

  # example visualization of example hurricanes
  graph_a = ggplot(example_hurri, aes(x = wind_predict, y = wind_obs)) +
    geom_point() +
    geom_smooth(method = "lm", se = FALSE) +
    labs(title = paste("Observation vs. Prediction of", "Example Hurricane", i), x = "Prediction", y = "Observation") +
    theme(plot.title = element_text(hjust = 0.5))

  graph_b = ggplot(example_hurri, aes(x = index)) +
    geom_point(aes(y = wind_obs, color = "Observed")) +
    geom_point(aes(y = wind_predict, color = "Predicted")) +
    geom_line(aes(y = wind_obs, color = "Observed")) +
    geom_line(aes(y = wind_predict, color = "Predicted")) +
    labs(title = paste("Fitting Performance", "Example Hurricane", i), x = "Time Index", y = "Wind Speed") +
    scale_color_manual(name = "Legend",
                       values = c("Observed" = "#1E90FF", "Predicted" = "orange"),
                       labels = c("Observation", "Prediction")) +
    theme(plot.title = element_text(hjust = 0.5))
}
```

```

ggsave(filename = paste0("predict_plots/", "plot_", i, "_a.png"), plot = graph_a, width = 6, height = 6)
ggsave(filename = paste0("predict_plots/", "plot_", i, "_b.png"), plot = graph_b, width = 6, height = 6)
}

## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'

ID_name=as.matrix(Training%>%
  group_by(ID) %>%
  slice(1) %>% dplyr::select(ID))

plot_list_a = list()
plot_list_b = list()

for (i in 1:5) {
  example_hurri = as.data.frame(Y_table_set[[i*5]])
  example_hurri$index = 1:nrow(example_hurri)

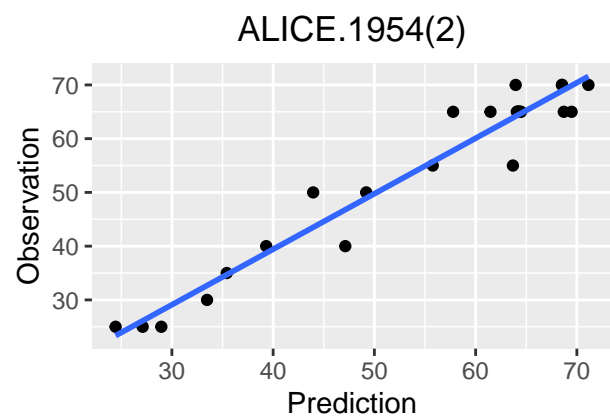
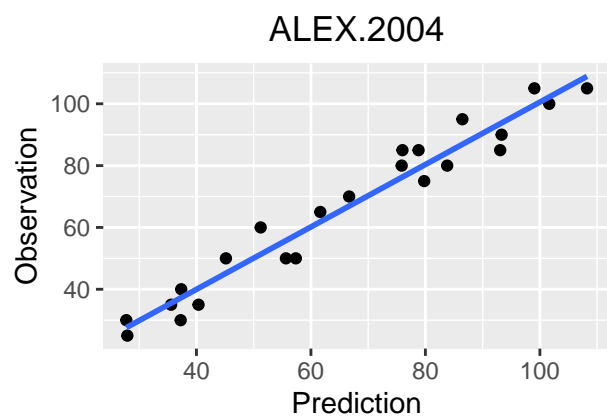
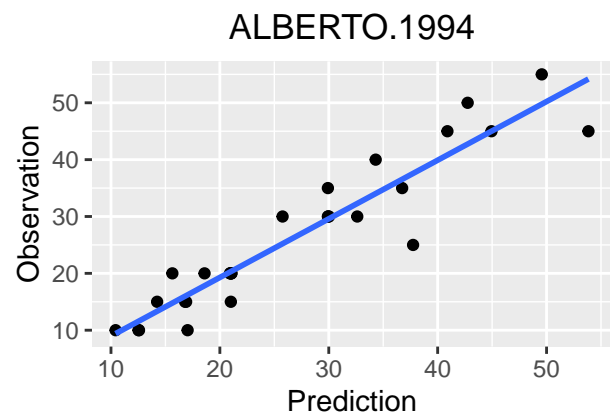
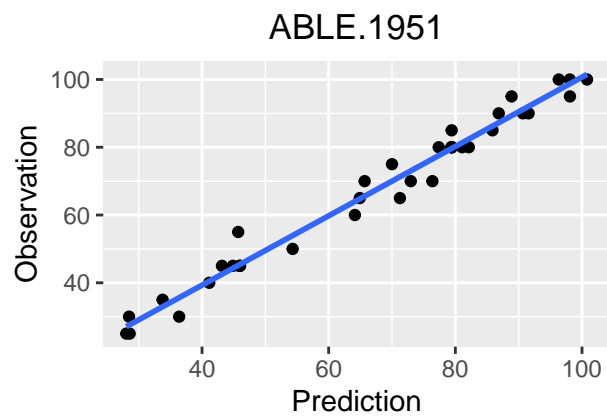
  # example visualization of example hurricanes
  graph_a = ggplot(example_hurri, aes(x = wind_predict, y = wind_obs)) +
    geom_point() +
    geom_smooth(method = "lm", se = FALSE) +
    labs(title = ID_name[i*5,], x = "Prediction", y = "Observation") +
    theme(plot.title = element_text(hjust = 0.5))

  graph_b = ggplot(example_hurri, aes(x = index)) +
    geom_point(aes(y = wind_obs, color = "Observed")) +
    geom_point(aes(y = wind_predict, color = "Predicted")) +
    geom_line(aes(y = wind_obs, color = "Observed")) +
    geom_line(aes(y = wind_predict, color = "Predicted")) +
    labs(title = ID_name[i*5,], x = "Time Index", y = "Wind Speed") +
    scale_color_manual(name = "Legend",
      values = c("Observed" = "#1E90FF", "Predicted" = "orange"),
      labels = c("Observation", "Prediction"))+
    theme(plot.title = element_text(hjust = 0.5))
  plot_list_a[[i]] = graph_a
  plot_list_b[[i]] = graph_b
}

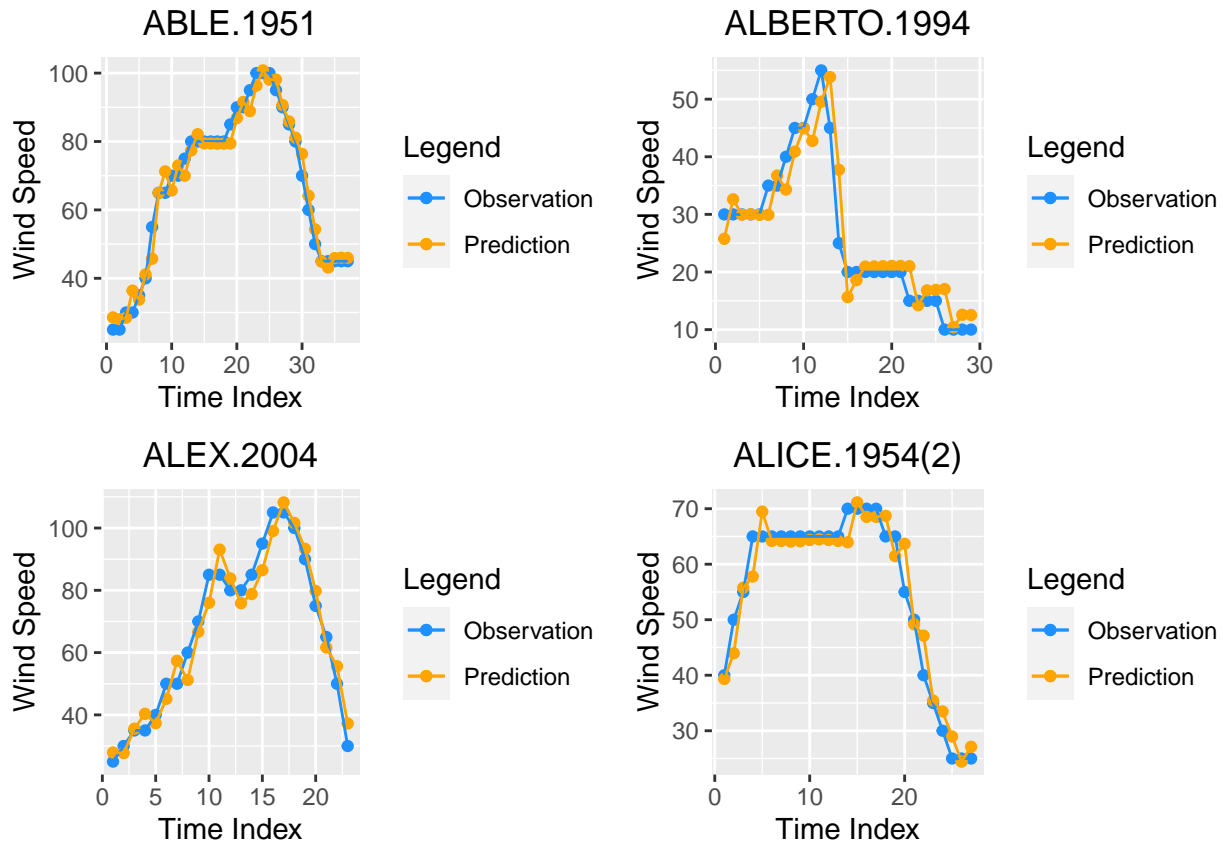
grid_a = grid.arrange(grobs = plot_list_a[c(1:4)], ncol = 2, nrow=2)

## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'
## `geom_smooth()` using formula = 'y ~ x'

```



```
grid_b = grid.arrange(grobs = plot_list_b[c(1:4)], ncol = 2, nrow=2)
```



```
ggsave(filename = "predic_plots/a_1_4.png",grid_a,width = 6, height = 4, dpi = 300)
ggsave(filename = "predic_plots/b_1_4.png",grid_b,width = 6, height = 4, dpi = 300)
```

```
library(cowplot)

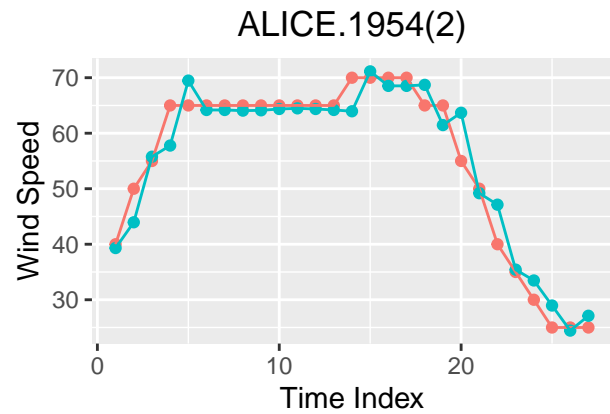
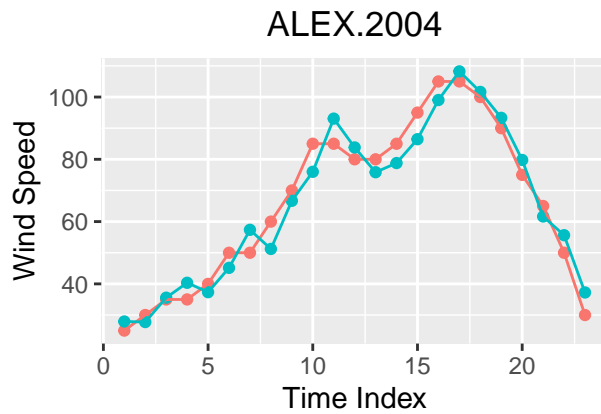
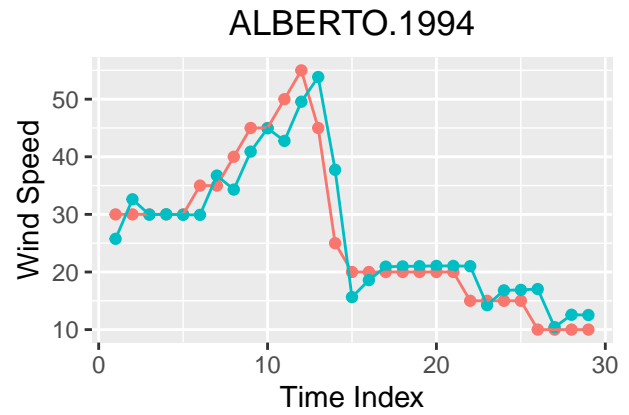
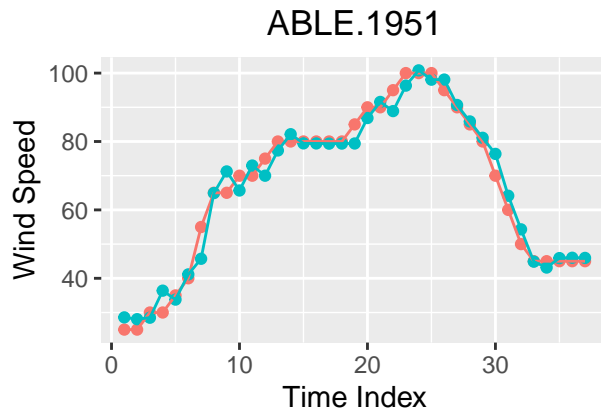
# create the plots
plot_list_c = list()

for (i in 1:5) {
  example_hurri = as.data.frame(Y_table_set[[i*5]])
  example_hurri$index = 1:nrow(example_hurri)

  graph_b = ggplot(example_hurri, aes(x = index)) +
    geom_point(aes(y = wind_obs, color = "Observed")) +
    geom_point(aes(y = wind_predict, color = "Predicted")) +
    geom_line(aes(y = wind_obs, color = "Observed")) +
    geom_line(aes(y = wind_predict, color = "Predicted")) +
    labs(title = ID_name[i*5,], x = "Time Index", y = "Wind Speed") +
    theme(legend.position = "none") +
    theme(plot.title = element_text(hjust = 0.5))

  plot_list_c[[i]] = graph_b
}

# arrange the plots using grid.arrange
grid_c = grid.arrange(grobs = plot_list_c[c(1:4)], ncol = 2, nrow=2)
```



```
# extract the legends from each plot
```

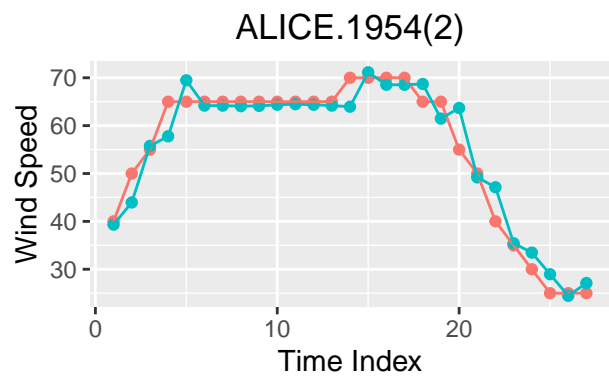
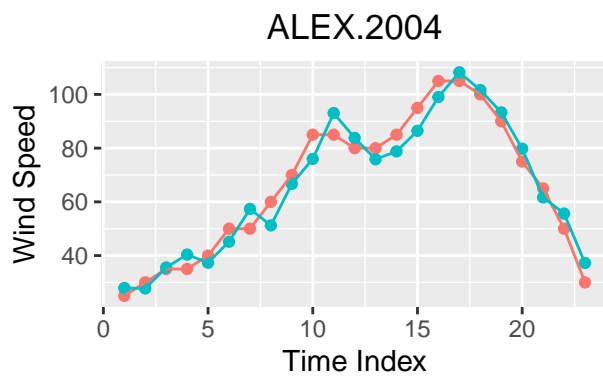
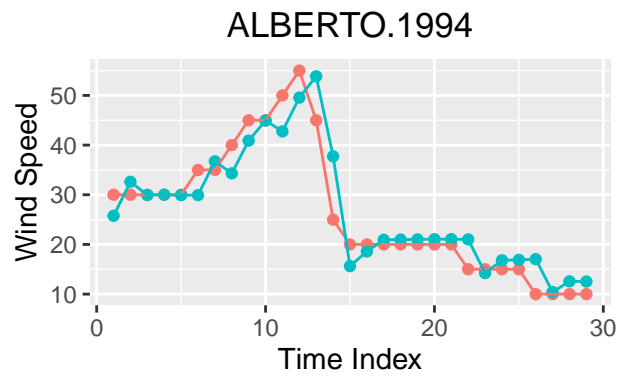
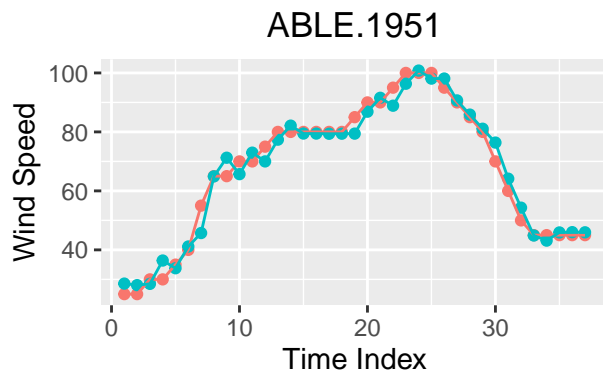
```
# merge the legends into one common legend
```

```
legend = cowplot::get_legend(plot_list_c[[1]]+theme(legend.position="bottom"))
```

```
# add the common legend to the grid of plots
```

```
plot_grid(grid_c, legend, ncol = 1, rel_heights = c(1, .1))
```





colour —●— Observed —●— Predicted