

# A Machine Learning Approach to Equity Bubble Detection and Financial Crash Prediction

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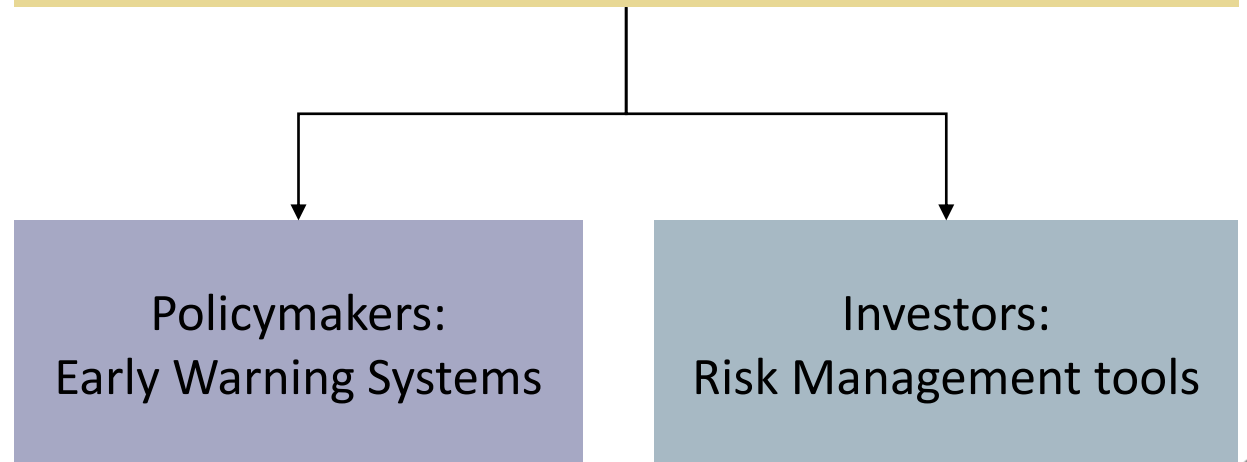
# Introduction: bubbles and market crashes cause losses, and predicting them can be valuable



*“In the summer of 1982, large American banks lost close to all their past earnings (cumulatively), about everything they ever made in the history of American banking—everything.”*

—Nassim N. Taleb

**Research purpose: predicting bubbles and financial crashes through machine learning**



# Literature: previous empirical studies are limited by their theoretical assumptions or feature selection

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## Too many theoretical assumptions

Rational, risk neutral agents  
Complete information  
Dividend as the fundamental value  
Stationary time series  
Brownian motion for asset prices  
...



## Critiques

Joint Hypothesis Problem  
No bubbles (Fama & French, 2014)  
Alternative explanations (Gürkaynak, 2008)  
Investors not rational (Daniel, 2005)  
Stationary tests inconclusive (Evans, 1991)  
Normal distributions unreliable (Taleb, 2009)



## Too few features included in ML studies

Only the price index (Moser, 2019)  
Price index, bond yield, exchange rate  
(Chatzis et al., 2018)



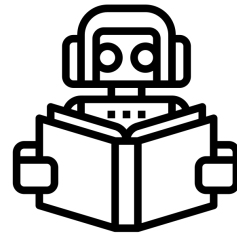
**Research methodology:**  
**model-free machine learning,**  
**features are selected based on**  
**theories but not rely on theories**



# Data: indicators of trading, macroeconomics, and market fundamentals; the definition of bubbles

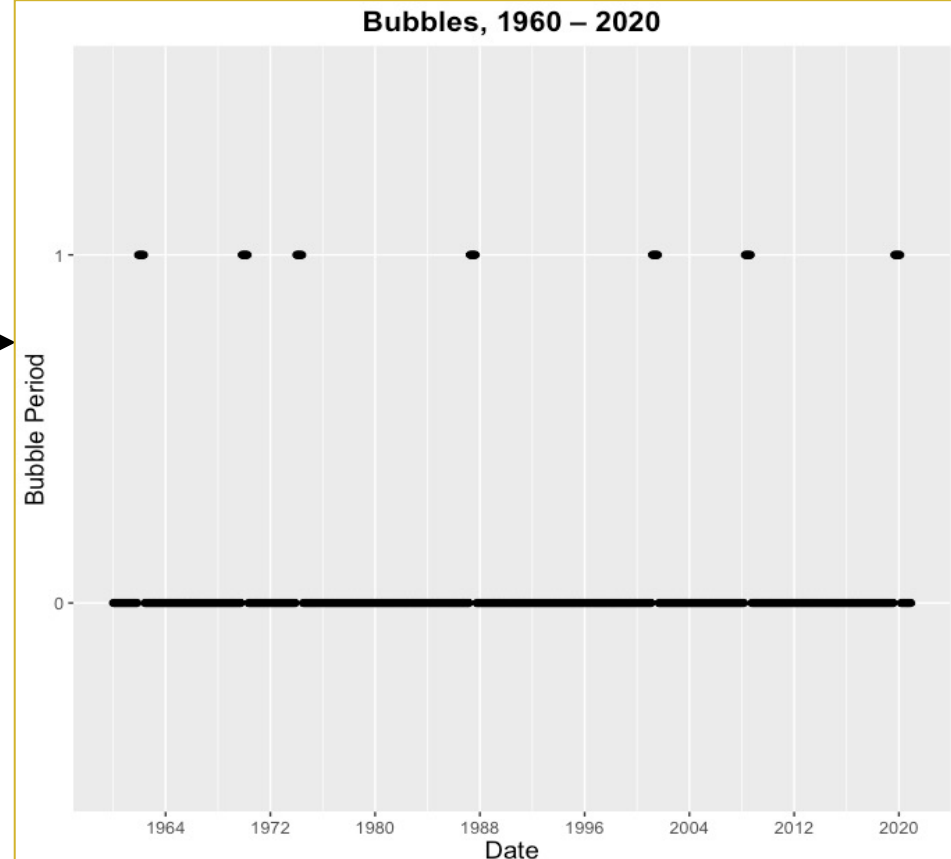
X

Shiller P/E ratio  
Market-cap-to-GDP  
Consumer confidence  
S&P 500 return  
(1, 3, 6, 12, 60  
months)  
T-bill yield  
Inflation  
GDP growth rate



machine  
learning

Y (Bubble): a market crash (1% quantile return) will happen in the next 6 months



# Models: three models are adopted based on the nature of the problem and previous studies

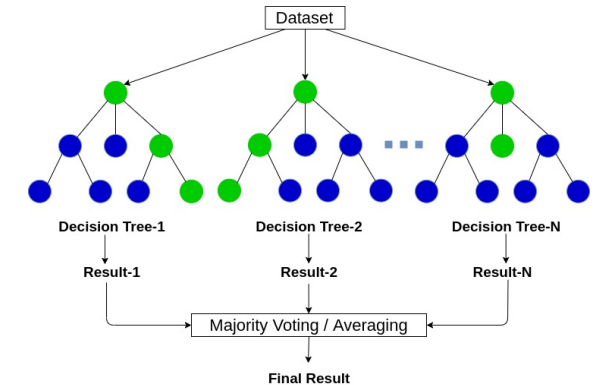
Logistic  
Regression

Predicting log-odds by linear models  
Baseline predictor for binary classification

$$\log \left( \frac{p(X)}{1 - p(X)} \right) = \beta_0 + \beta_1 X$$

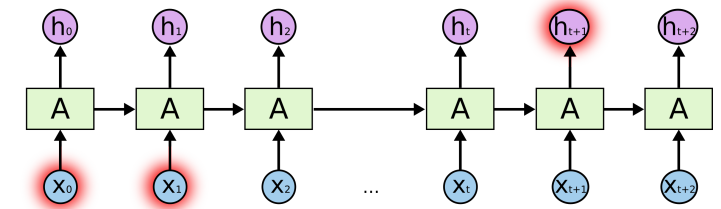
Random  
Forests

Detecting non-linear patterns with decision trees  
Ensemble methods are promising (Lin et al., 2012)



RNN +  
BiLSTM

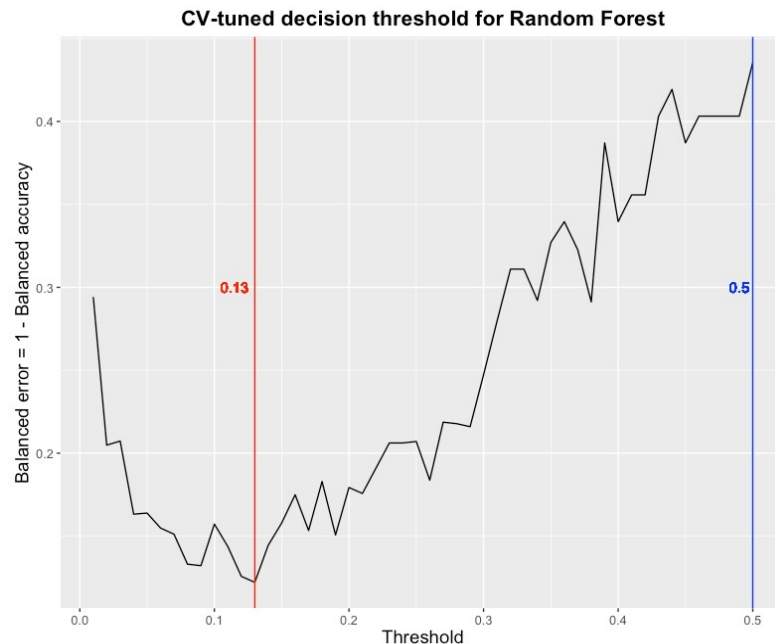
Good with financial time series (Namini et al., 2019)  
Similar studies (Bashchenko & Marchal, 2020)



# Models: the imbalanced nature of the dataset requires special consideration for classification

Problem: Even a naïve classifier  $f(x) = 0$  can achieve a (useless) high overall accuracy

Category	Non-bubble	bubble
Count	690	42



CV-tuned decision thresholds

Re-sampling for balancing weights

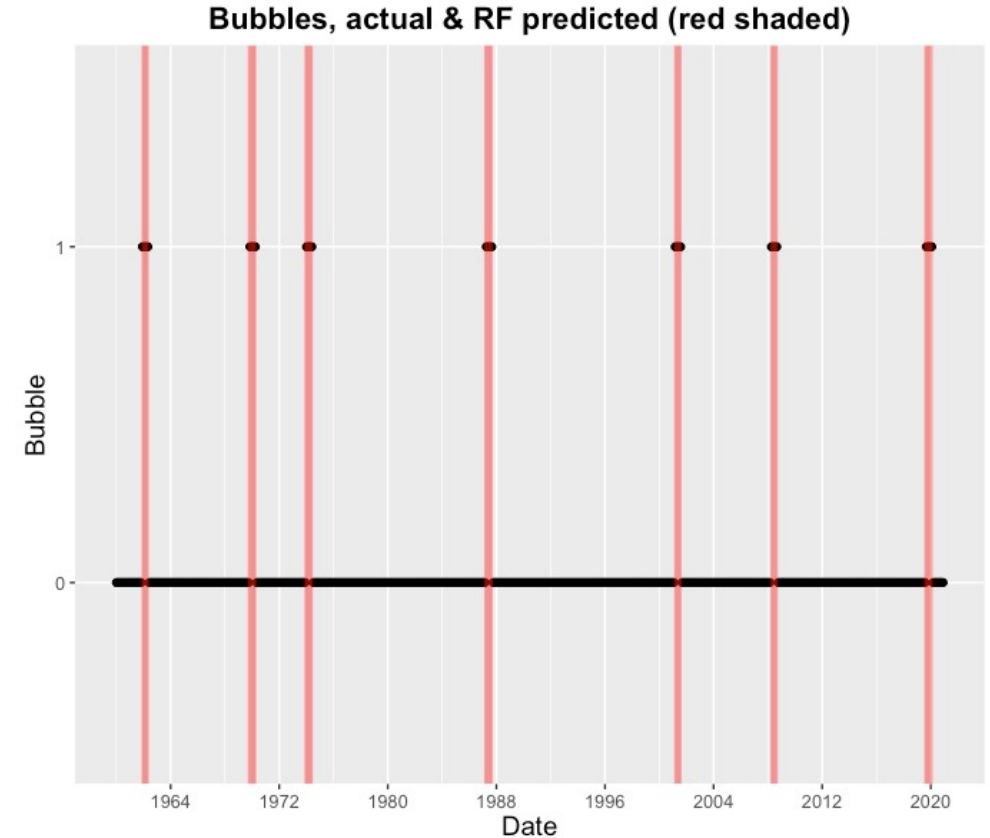
Asymmetric loss (Lin et al., 2018)

**Model Evaluation:**  
 $Balanced Accuracy = (Sensitivity + Specificity)/2$



# Result: the Random Forest model with a CV-tuned threshold has the highest balanced accuracy

Performance on test data	Sensitivity	Specificity	Balanced Accuracy
Logistic regression, threshold as prevalence	72.72%	72.06%	72.39%
Logistic regression, re-weighted data	72.72%	73.52%	73.12%
Random Forest, CV-tuned threshold	100%	94.85%	97.43%
Random Forest, re-weighted data	45.46%	100%	72.72%
RNN + BiLSTM, focal Loss	0%	100%	50%



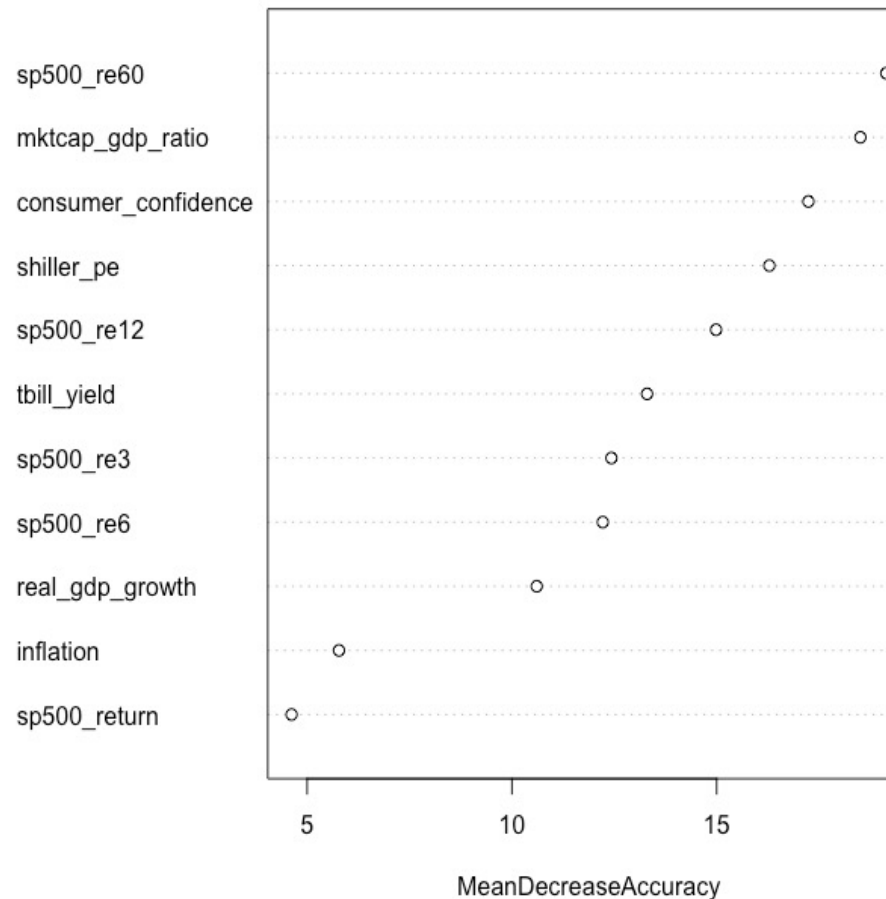
# Insights: the most important factors for prediction are fundamental indicators and long-term trends

Random Forest,  
CV-tuned threshold (left)

Logistic regression,  
re-weighted dataset (right)

Short-term index returns  
have low predictive power

Variable importance for Random Forest



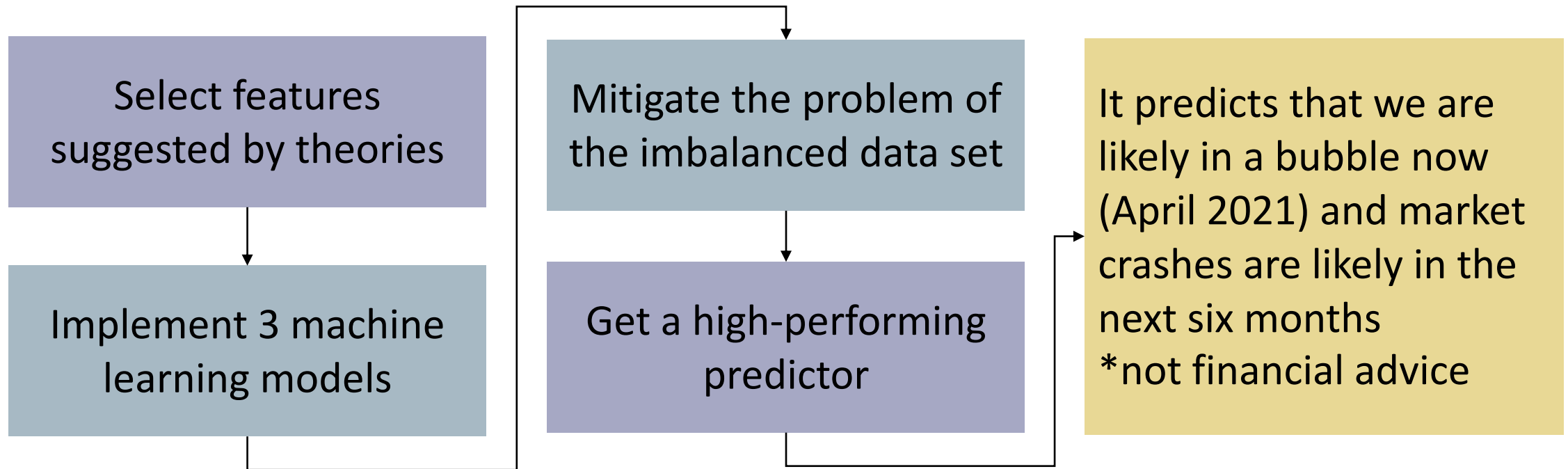
	Dependent variable:
	bubble
real_gdp_growth	-0.007 (0.035)
inflation	0.099*** (0.028)
tbill_yield	0.237*** (0.073)
shiller_pe	-0.658*** (0.058)
consumer_confidence	-1.182*** (0.147)
mktcap_gdp_ratio	216.592*** (18.361)
sp500_return	-0.105*** (0.033)
sp500_re3	0.018 (0.022)
sp500_re6	-0.021 (0.020)
sp500_re12	-0.143*** (0.016)
sp500_re60	0.075*** (0.006)
Constant	106.314*** (13.641)
Observations	1,112
Log Likelihood	-410.346
Akaike Inf. Crit.	844.693
Note:	* p<0.1; ** p<0.05; *** p<0.01





# Conclusion: a high-performing predictor is found, and it predicts that we are likely in a bubble now

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Research contributions: New methodology and strong performance  
100% sensitivity, 94.85% specificity vs. 59%, 90% (Chatzis et al., 2018)

