

Investigating Integration and Exchange Rate Pass-Through in World Maize Markets Using Inferential LASSO Methods

Hongqiang Yan*, Barry K. Goodwin†, Mehmet Caner‡

October 10, 2023

Abstract

This paper investigates the extent of market integration and exchange rate pass-through but also those market factors that may be associated with deviations from perfect market integration and pass-through. To address the shortcomings of existing models on spatial market integration, we adopt an approach towards inference and model selection using the desparsified LASSO method for high-dimensional threshold regression. Our results support the integration of global corn markets, especially when the existence of thresholds is accounted for. We identify important relationships between several variables representing domestic and world economic conditions.

Keywords: Law of One Price, Threshold Regression Model, Exchange Rate

*North Carolina State University, Raleigh, NC 27695. Email: hyan6@ncsu.edu

†North Carolina State University, Raleigh, NC 27695. Email: bkgoodwi@ncsu.edu

‡North Carolina State University, Raleigh, NC 27695. Email: mehmet.caner@ncsu.edu

1 Introduction

Efficient markets are expected to eliminate any potential for riskless profits through arbitrage and trade, known as the "Law of One Price" (LOP). Economic arbitrage relies on the principle that prices of related goods should move together. The general implication here is that prices for homogeneous products at different geographic locations in otherwise freely functioning markets should differ by no more than transport and transactions costs. However, the existence of transactions costs can introduce a threshold effect, where deviations in prices above a certain threshold are necessary to trigger price movements. In recent years, studies analyzing this phenomenon have focused on developing nonlinear models that can better capture the effects of unobservable transaction costs in spatial price linkages. The motivation behind using such models is to better understand the dynamics of market integration and the role of transaction costs in the presence of regime changes. The use of nonlinear models has been largely driven by the application of threshold modeling techniques. These models are based on the idea that transaction costs and other barriers to spatial trade may lead to regime switching, with alternative regimes representing the trade and no-trade equilibria. This idea has been operationalized through various econometric techniques and model specifications.

Threshold autoregression (TAR) models have indeed had a significant impact on the analysis of asymmetric price transmission in agricultural economics. These models have been developed to capture the nonlinear dynamics of market integration and account for the effects of unobserved transaction costs that can affect spatial price linkages. A common approach to threshold modeling often involves an autoregressive model of the price differential. The study conducted by [Goodwin and Piggott \(2001\)](#) examined corn prices at local markets by combining a threshold structure with an error-correction model. [Goodwin et al. \(1990\)](#) noted that delivery lags that extend beyond a single time period may imply arbitrage conditions that involve noncontemporaneous price linkages. Based on this idea, [Lence et al. \(2018\)](#) examined the performance of the threshold cointegration approach, specifically Band-TVECM, in

analyzing price transmission in an explicit context where trade decisions are made based on the expectation of final prices because trade takes time. In addition to the threshold model, [Goodwin et al. \(2021\)](#) applied generalized additive models to empirical considerations of price transmission and spatial market integration.

Although exchange-rate pass-through, i.e. the degree to which exchange rate movements are reflected in prices has long been a question of interest in international economics, there is limited literature that examines exchange-rate pass-through in global agricultural commodity markets. One study by [Varangis and Duncan \(1993\)](#) uses an econometric model of the wheat, corn, and soybean markets to investigate the dynamic effects of exchange rate fluctuations on U.S. commodity markets. The study finds that exchange rate fluctuations have a significant real impact on agricultural markets, particularly on the volume of exports and the relative split between exports and domestic use of these commodities. The econometric model developed in the study shows that agricultural prices are sensitive to movements in the exchange rate, with short-run adjustments being more dramatic than longer-run adjustments. [Chambers and Just \(1981\)](#) found that the extent to which changes in exchange rates affect import prices. The paper presents an imperfect competition model to estimate the impact of changes in the yen/dollar exchange rate and other factors on US and Japanese steel prices. The results show that such exchange rate changes have a less than fully passed-through effect on steel prices, as indicated by the imperfect competition model used in the study.

LASSO (least absolute shrinkage and selection operator) is a regression technique that uses shrinkage methods for variable selection. LASSO employs L1 regularization and shrinkage techniques to penalize the model based on the absolute value of parameter values. It is a valid approach for identifying an optimal model specification by selecting the variables that contribute the most to explaining a regression-type relationship. Although LASSO models have been widely used in economics studies, the shrinkage bias introduced due to the penalization in the LASSO loss function can affect the properly scaled limiting distribution of the LASSO estimator. Therefore, to conduct statistical inference, we need to remove this bias. This paper uses the desparsified (debaised) LASSO (least absolute shrinkage and selection operator) method for high dimensional threshold regression, recently developed by [Yan and Caner \(2022\)](#) to model the nonlinearity in the spatial price integration models. The fact is that existing

literature on price transmission and exchange rate pass-through has developed from simple regression models to nonlinear specifications that allow differential impacts on price linkages. These differential effects are often identified using smooth or discrete threshold models.

The integration of world markets for grains and oilseeds has been of interest for many years. In recent years, the global maize market has been dominated by major exporters such as the United States, Argentina, and Ukraine, which have consistently ranked among the top maize producers and exporters worldwide. The US, the largest producer, and exporter of maize, alone accounts for over one-third of global maize exports. Argentina and Ukraine follow, collectively accounting for over one-fourth of global maize exports. The dominance of these countries in the global maize market is representative of the market and makes them candidates for studying price transmission and market integration. They play a crucial role in global maize prices and influencing maize markets worldwide. Likewise, the extent to which distortions arise due to incomplete pass-through of exchange rate shocks has been an important indicator of the overall functions of markets. Although trade in agricultural commodities is typically invoiced in US dollars, exchange rate shocks may still exhibit imperfect pass-through, which will distort international price linkages. Furthermore, market factors can be conceptually related to market linkages, such as aggregate economic indicators like industrial production, trade policies, and exogenous shocks, such as the recent pandemic, exchange rates, interest rates, and nominal inflation rates in each market. These factors may be associated with deviations from perfect market integration, as they can affect the costs of transportation, communication, and transaction between markets, as well as the demand and supply conditions in each market. Understanding the effects of these market factors on price linkages is essential for policymakers and market participants to make informed decisions about trade, investment, and risk management.

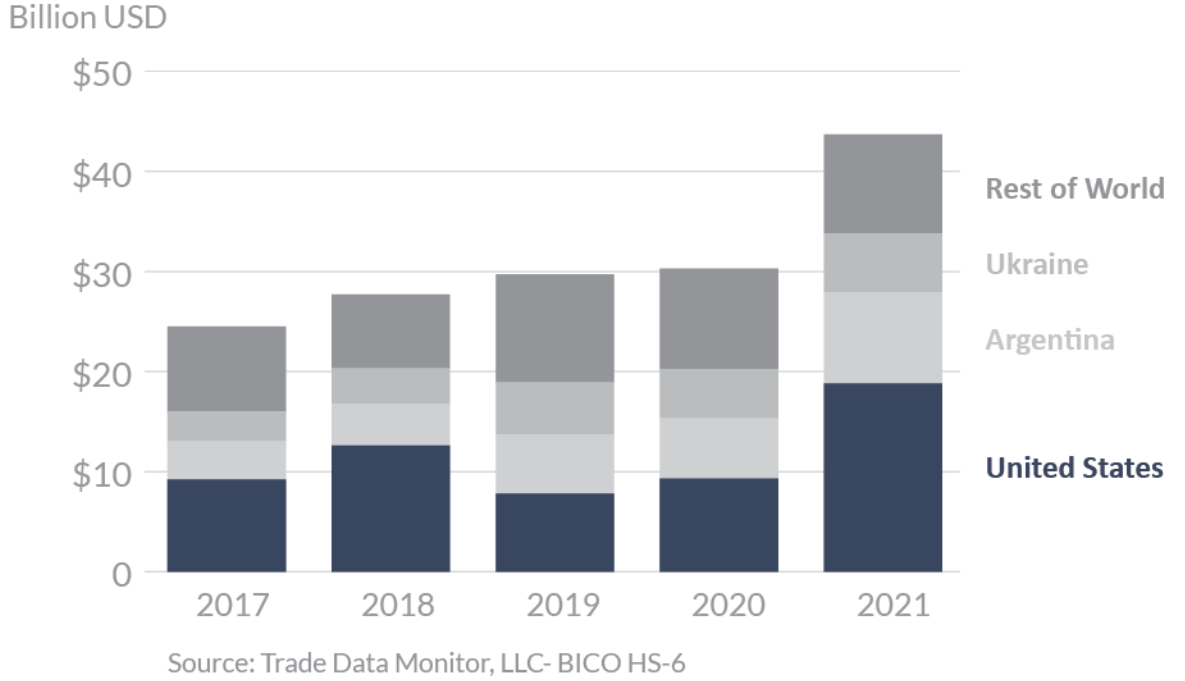


Figure 1: World Corn Exports by Country and Marketing Year, Source :[U.S. Department of Agriculture \(2022\)](#)

2 Econometrics Models of Spatial Market Integration

Spatial market integration in agricultural product markets has been extensively studied in the literature. Consider a homogeneous commodity traded in common currency in two regional or international markets represented by location indices i and j . The individual market prices are denoted by P^i and P^j , respectively. The arbitrage condition of perfect market integration reflects the equation $P_t^1/P_t^2 = 1$, abstracting from trade and transportation costs. This condition has been adjusted to account for the wedge between prices due to transaction or transportation costs, which may differ significantly in regional markets. The general representation for this adjusted arbitrage condition is $1/(1 - \kappa) \leq P_t^1/P_t^2 \leq 1 - \kappa$, where κ represents the proportional loss in commodity value due to transaction or transportation costs ($0 < \kappa < 1$). The

greater the distance between locations i and j , the closer κ is to one.

Many spatial economic models utilize the iceberg trade cost proposed by Samuelson (1954), which assumes that part of the produced output representing the material costs of transportation melts away during transportation. That is, after taking natural logarithms and denoting $p_t^i = \ln P_t^i$, the inequality is often presented as

$$(2.1) \quad |p_t^1 - p_t^2| \leq \ln(1 - \kappa).$$

The inequality (2.1) is generally considered to reflect two distinct states of the market. The first state corresponds to a condition where there is no profitable trading, with $|p_t^1 - p_t^2| \leq \ln(1 - \kappa)$. Under conditions of trade or profitable arbitrage opportunities, the condition holds as $|p_t^1 - p_t^2| > \ln(1 - \kappa)$. The speed at which the market adjusts to such deviations from the arbitrage equilibrium is often used as a measure of the degree of market integration. Typically, these discrete arbitrage and no-arbitrage conditions are represented using threshold models, where the threshold represents an empirical measure of the transaction cost, $\ln(1 - \kappa)$. Bidirectional trade models may allow for different thresholds depending on which market price is higher.

Over time, log price differentials within the band limits are expected to follow a unit root process. Conversely, log price differences outside the band are expected to be mean-reverting, which suggests the existence of a transactions cost band, as assumed in the literature.

A wide literature has examined spatial market integration in world markets for agricultural commodities. Likewise, a large related literature has examined how shocks to exchange rates affect domestic and export prices, a phenomenon known as ‘pass-through’. If a shock to exchange rates is fully reected in adjustments to prices, the shock is considered to have been fully passed through. Most empirical studies of market integration and exchange rate pass-through assume a linear relationship, as represented by

$$(2.2) \quad p_t^1 = \alpha_0 + \beta_1 p_t^2 + \gamma_1 \pi_t^{12} + \varepsilon_t,$$

where p_t^i is the price in market i in time period t and π_t^{12} is the exchange rate between currencies in markets i and j , all in logarithmic terms.

Perfect integration is implied if $\alpha_0 = 0$ and $\beta_1 = 1$. In cases where prices are

invoiced in different currencies, perfect integration also requires perfect exchange rate pass-through, which is implied if $\gamma_1 = 1$. If prices are invoiced in a common currency, as is often the case when trade is conducted in US dollar terms, the exchange rate is 1 and thus the logarithmic value of zero eliminates the exchange rate effect. However, it is possible that exchange rate distortions may still affect price linkages, which is implied if $\gamma_1 \neq 0$, even if prices are quoted in a common currency,

It is also essential to consider the market factors associated with deviations from perfect integration. To this end, we consider an alternative version of equation (2.2) that is expressed as:

$$(2.3) \quad p_t^1 - p_t^2 = \gamma_1 \pi_t^{12} + \gamma_2 Z_t^{12} + \varepsilon_t,$$

where Z_t^{12} is a set of factors that may be conceptually related to market linkages, γ_2 is a vector of parameters corresponding to Z_t^{12} . These factors include exogenous shocks such as exchange rates, interest rates, unemployment rates, and nominal inflation rates in each of the markets.

To further analyze spatial price linkages, we can evaluate the patterns of market price adjustments to isolated shocks that occur in distinct regional markets. In addition to the conventional specification of exchange rate pass-through, we propose an extension to this framework of spatial market integration that includes two regimes, where the regime switch depends on a forcing variable, usually a lagged price differential, that is expressed as:

$$(2.4) \quad \begin{aligned} \Delta(p_t^1 - p_t^2) = & \gamma_0 + \gamma_1 \Delta \pi_t^{12} + \gamma_2 \Delta Z_t^{12} \\ & + \mathbf{1}\{p_{t-1}^1 - p_{t-1}^2 \geq c\}(\delta_0 + \delta_1 \Delta \pi_t^{12} + \delta_2 \Delta Z_t^{12}) + \varepsilon_t, \\ & t = \{1, \dots, T\} \end{aligned}$$

where γ_0 is a time trend coefficient if we add a linear time trend to equation (2.3).

To assess the potential presence of changing transaction costs, we consider a multivariate threshold distributed lag model that includes price differential, exchange

rate, and exogenous shocks as well as their lagged (past period) values, as follows:

$$\begin{aligned}
(2.5) \quad \Delta(p_t^1 - p_t^2) = & \gamma_0 + \sum_{l=0}^L \gamma_{1l} \Delta \pi_{t-l}^{12} + \sum_{l=0}^L \gamma_{2l} \Delta z_{t-l}^{12} \\
& + \mathbf{1}\{Q_t \geq c\} \left[\delta_0 + \sum_{l=0}^L \delta_{1l} \Delta \pi_{t-l}^{12} + \sum_{l=0}^L \delta_{2l} \Delta z_{t-l}^{12} \right] + \varepsilon_t \\
& t = \{1, \dots, T\},
\end{aligned}$$

where L is the maximal possible lag, which may increase with the sample size (slowly grow to infinity), and Q_t is the lagged price differential used as the forcing variable to identify the thresholds, i.e., $Q_t \in \{p_{t-1}^1 - p_{t-1}^2, \dots, p_{t-L}^1 - p_{t-L}^2\}$. We assume that the maximal lag order L is known. This framework may provide a richer evaluation of price dynamics and patterns of adjustment.

Economic agents adjust their expectations of price differentials based on the level of transaction costs observed in previous periods. If the transaction costs (i.e., price differentials) exceed certain thresholds, agents anticipate larger effects when transaction costs are high. This implies that agents perceive an increase in transaction costs beyond the threshold to have a more prominent impact in the presence of high price differentials. The specified model offers the advantage of capturing simultaneous relationships between exchange rates and other variables. Linear modeling techniques may not accurately capture the nonlinearities present in exchange rate pass-through. Therefore, it is essential to investigate the impact of transaction costs on the market's response to an exchange rate shock. The existence of different levels of transaction costs can influence how price differentials respond to exchange rates or other shocks, as it determines the presence or absence of arbitrage opportunities. The proposed model recognizes that the movements in the exchange rate can adjust how markets respond to changes, leading to different regimes based on transaction costs. By considering the effects of transaction costs, we can gain a more comprehensive understanding of the dynamics of the exchange rate pass-through mechanism.

To obtain a specification that incorporates a broad range of variables in (2.5), we utilize a novel approach to inference and model selection: the desparsified LASSO (least absolute shrinkage and selection operator) method for high-dimensional threshold regression, which was recently developed by [Yan and Caner \(2022\)](#). This method

allows us to fit the threshold regression models using the threshold LASSO estimator of [Lee et al. \(2016\)](#) in conjunction with the work of [van de Geer et al. \(2014\)](#). Compared to other estimators, this approach can construct asymptotically valid confidence bands for a low-dimensional subset of a high-dimensional parameter vector. Understanding the significance of the estimators can provide insights into the changes in transaction costs and threshold effects over time. However, standard approaches to inference are not applicable to such models. To simplify, let

$$\alpha = (\gamma_0, \gamma_{10} \cdots, \gamma_{1L}, \gamma_{20} \cdots, \gamma_{2L}, \delta_0, \delta_{10} \cdots, \delta_{1L}, \delta_{20} \cdots, \delta_{2L})'$$

be slope parameter vector, The dimension of α is $2 + 2(1 + p)(L + 1)$, where p is number of other exogenous shocks. Let \mathbf{X} be a $T \times [1 + (1 + p)(L + 1)]$ matrix of all regressors. To provide a more precise description of our estimation procedures, we propose a three-step estimation approach for the model. The three-step procedure can be outlined as follows:

Step 1.

For each $c \in \mathbb{C}$, $\hat{\alpha}(c)$ is defined as

$$(2.6) \quad \hat{\alpha}(c) := \operatorname{argmin}_{\alpha} \left\{ T^{-1} \sum_{t=1}^T (\Delta(p_t^1 - p_t^2) - [X_t', X_t' \mathbf{1}\{Q_t \geq c\}])' \alpha)^2 + \lambda \|\mathbf{D}(c)\alpha\|_1 \right\},$$

where we can rewrite the ℓ_1 penalty as

$$\lambda \|\mathbf{D}(c)\alpha\|_1 = \lambda \sum_{j=1}^{1+(1+p)(L+1)} [\|X^{(j)}\|_n |\alpha^{(j)}| + \|X^{(j)}(\tau)\|_n |\alpha^{(1+(1+p)(L+1)+j)}|],$$

in order to adjust the penalty differently for each coefficient depending on scale normalizing factor.

Step 2.

Define \hat{c} as the estimate of c_0 such that:

(2.7)

$$\hat{c} := \operatorname{argmin}_{c \in \mathbb{C} \subset \mathbb{R}} \left\{ T^{-1} \sum_{t=1}^T (\Delta(p_t^1 - p_t^2) - [X_t', X_t' \mathbf{1}\{Q_t \geq c\}]\hat{\alpha}(c))^2 + \lambda \|\hat{\alpha}(c)\|_1 \right\}.$$

In accordance with [Yan and Caner \(2022\)](#), the first two steps involve LASSO estimates that can achieve threshold selection consistency under specific regularity conditions. Threshold selection consistency entails correctly identifying the estimates of differences between the two regimes, denoted as $(\delta_0, \delta_{10}, \dots, \delta_{1L}, \delta_{20}, \dots, \delta_{2L})$, as equal to zero if the model is linear. The consistency of the LASSO estimator implies that if the underlying true model is nonlinear, then the LASSO estimator will correctly estimate any of the non-zero parameters, including $(\delta_0, \delta_{10}, \dots, \delta_{1L}, \delta_{20}, \dots, \delta_{2L})$. In other words, if any of these parameters are non-zero, the LASSO estimator will consistently estimate them as non-zero, indicating the presence of a nonlinear relationship between the variables. This is in contrast to the conventional "self-exciting" threshold autoregressive (SETAR) model, where nonlinear tests such as Hansen's modification of standard Chow-type tests, [Tsay \(1989\)](#) linearity test, or neural network tests of linearity are utilized to detect nonlinearity. Therefore, if we misspecify a linear model and use the LASSO method for the threshold model described here, we may estimate all threshold effects as zero for a sufficiently large sample size. To put it another way, if our estimates of $(\delta_0, \delta_{11}, \dots, \delta_{1L}, \delta_{20}, \dots, \delta_{2L})$ after steps 1 and 2 have at least one non-zero, it indicates that the probability of the model being linear approaches 0.

As the shrinkage bias introduced due to the penalization in LASSO loss function will show up in the properly scaled limiting distribution of LASSO estimator. Therefore, to conduct statistical inference, we need to remove this bias. However, when modeling threshold regression with a rich set of variables, a challenge arises. Threshold models involve splitting the sample based on a continuously-distributed variable. With a rich set of regressors, there is a risk that the number of observations in any split sample may be less than the number of variables which causes the sample covariance matrix to be of reduced rank. However, standard approaches are invalid in such a situation. So in order to desparsify (debias) our LASSO estimator, we need an approximate inverse of a certain singular sample covariance matrix in the sense of [van de Geer et al. \(2014\)](#). We refer to [Yan and Caner \(2022\)](#) for details in the case

of the Lasso applied to the high-dimensional threshold regression model and do not pursue these extensions further here.

Step 3

Finally, we can obtain desparsified LASSO estimates for the threshold model, which is given by:

$$(2.8) \quad \hat{a}(\hat{c}) = \hat{\alpha}(\hat{c}) + \hat{\Theta}(\hat{c})\mathbf{X}'(\hat{c})(\Delta(p^1 - p^2) - \mathbf{X}(\hat{c})\hat{\alpha}(\hat{c}))/n,$$

where

$$(2.9) \quad \hat{\Theta}(\hat{c}) = \begin{bmatrix} \hat{\mathbf{B}}(\hat{c}) & -\hat{\mathbf{B}}(\hat{c}) \\ -\hat{\mathbf{B}}(\hat{c}) & \hat{\mathbf{A}}(\hat{c}) + \hat{\mathbf{B}}(\hat{c}) \end{bmatrix},$$

and $\hat{\mathbf{B}}(\hat{c})$ and $\hat{\mathbf{A}}(\hat{c})$ are the inverse or approximate (if the sample covariance matrix is singular) inverse of the split sample covariance matrices.

For model selection i.e. to determine the optimal lag structure on forcing variable Q_t , we use selection criteria such as the Akaike information criterion (AIC) or Bayesian information criterion (BIC) to select the optimal lag structure for the forcing variables. As the BIC applies a stronger penalty on the degree of freedom, it is more conservative in variable selection compared to AIC.

3 Empirical Application

The empirical analyses in our study focus on the international corn markets, specifically on three major exporting markets: the US, Argentina, and Ukraine. Additionally, we investigate the farthest two regional markets in the US as a comparison. The corn market is a highly significant commodity traded across large distances, making it a subject of great interest for economic research. Despite its widespread consumption and spatial dispersion, production is typically concentrated in specific regions. To gain a comprehensive understanding of its behavior, we focus our study on the corn markets in the US, Argentina, and Ukraine. These three markets collectively accounted for 66.2% of the global corn trade by value in 2021. Given the intricate spatial dynamics of the corn market, analyzing spatial linkages is crucial.

We collected monthly maize price data from multiple sources and are discussed

below. As mentioned above, the main dependent variable of interest in this study is the maize price data for international markets. we collected the yellow corn export price of the US, Ukraine, and Argentina. Price data for the main three export markets were obtained from the FAO Food Price Monitoring and Analysis (FPMA) Tool, reporting prices in US dollars per tonne. Our study also utilized the US Feed Grain Yearbook’s corn price dataset, which provides data on Yellow Corn No. 2 from nine regional markets across the United States, which are Gulf ports, Louisiana; St. Louis, Missouri; Omaha, Nebraska; Central Illinois; Chicago, Illinois; Kansas City, Missouri; Toledo, Ohio; Memphis, Tennessee; and Minneapolis, Minnesota.

According to the National Park Service, the agricultural products and agribusiness industry in the Mississippi basin are responsible for producing 92% of the nation’s agricultural exports. Moreover, they account for 78% of the world’s exports in feed grains and soybeans. The Mississippi River serves as a vital transportation route for this agricultural trade. Approximately 60% of all grain exported from the US is shipped through the Port of New Orleans and the Port of South Louisiana, both of which are situated along the river. In terms of corn exports, the Mississippi River connects various markets along its route. Gulf ports in Louisiana, such as the Port of New Orleans and the Port of South Louisiana, serve as the main locations for corn exports in the region. Additionally, other locations along the Mississippi River also play a role in corn export activities.

Our dataset spans from January 2000 to January 2023, comprising 277 monthly observations for each series. However, there were some missing values in the series, which we addressed by replacing them using spline interpolation during the selected period. Due to limitations in data availability, the time span for US market factors is limited to January 2000 to January 2023, resulting in a total of 277 observations. The available market factors data for Ukraine covers the period from March 2002 to January 2002, comprising 239 observations. The market factors data for Argentina spans from August 2003 to June 2020, encompassing 203 observations.¹.

In addition, we obtained the exchange rates for Ukraine (USD to Ukrainian Hryvnia) and Argentina (USD to Argentina Peso). To capture market factors related to the US market, we sourced data from the Federal Reserve Economic Data (FRED),

¹We employed cubic spline interpolation to address missing price data within selected continuous periods.

which included interest rates, nominal inflation rates, unemployment rates, industrial production monthly percent change, and US gas prices. For US corn stock data, we utilized quarterly data from the US Feed Grain Yearbook and converted it into monthly data for our analysis². Market factors for Argentina and Ukraine were sourced from the National Summary Data Pages (NSDPs). Furthermore, we collected the Baltic Exchange Dry Index, which measures the cost of shipping dry goods, such as maize, worldwide.

The basic unit of analysis used throughout the analysis is the natural logarithm of the price ratio, denoted as $p_t^i - p_t^j (= \ln(P_t^i/P_t^j))$, where i and j indicate locations (i.e., $i, j = 1, \dots, 11$), and t is a time index such that $i, j = 1, \dots, T$, where $T = 277$. The international price data and each pair of markets price are shown in logarithmic form in Figure 2, 3 4, 5 in appendix. The price data for Ukraine was collected and covers the period from January 2000 to April 2022, comprising a total of 267 monthly observations.

The data for the logarithmic price in all nine US markets were available from January 2000 to January 2023, resulting in 277 monthly observations, as shown in Figure 6. Specifically, Figure 7 illustrates the logarithmic prices in Kansas City, MO, and Gulf ports, LA. The spatial linkages of the corn market within the United States are particularly noteworthy. Gulf ports in LA play a crucial role as the main location for US corn exports, while Kansas City is traversed by the Missouri River, a tributary of the Mississippi River. Consequently, our objective is to examine and compare the spatial linkages in the corn market between the United States and Ukraine or Argentina, as well as distinct regions in the United States.

Figure 8 displays a graphical representation of logarithmic pairs of prices plotted against each other, providing insight into the relationship between price levels and price differentials, as indicated by deviations from the 45-degree line in each plot. The plots reveal distinct basis patterns where one price tends to be higher or lower than the other. These patterns likely reflect the presence of transaction costs associated with regionally distinct market trades. With the exception of the 4th panel, the plots show that the points are evenly distributed on both sides of the 45-degree line.

²To align the data frequencies for our econometric analysis, we employed cubic spline interpolation to convert the quarterly US corn stock data, Argentina unemployment rate, and Ukraine employment rate into the same frequency as all other monthly variables.

However, in the 4th panel representing Kansas City, MO, and Gulf ports, LA, all the points fall below the 45-degree line. This observation is consistent with reality, as the primary shipping route for most US corn exports involves transporting goods down the Mississippi River, leading to transportation occurring predominantly from Kansas City, MO, to Gulf ports, LA. Therefore, it is expected that the market price in Kansas City, MO would consistently be lower than that in Gulf ports, LA.

To analyze the properties of time series prices and determine the most suitable model for assessing spatial price linkages, we conducted augmented Dickey-Fuller tests for each pair of price differentials. In order to examine the characteristics of time series prices and identify the most appropriate model for evaluating spatial price linkages, we conducted augmented Dickey-Fuller tests for each pair of price differentials. The results of the augmented Dickey-Fuller tests for the stationarity of the price differentials are presented in Table 7 in the appendix, which indicates that the null hypothesis of nonstationarity of the price differentials is strongly rejected in every case. A finding of nonstationarity in the price differentials would suggest a lack of price parity in that individual market prices are allowed to wander arbitrarily far apart. Additionally, we performed ADF tests on the first difference of the logarithmic exchange rate and other exogenous shocks in Table 8 in the appendix and found that they were all significant in rejecting nonstationary series. Our augmented Dickey-Fuller test on the first difference of the logarithm of all variables strongly rejects the null hypothesis of nonstationarity. Thus, we can implement equation (2.5) for estimating the model with the available data.

As mentioned earlier, the LASSO for threshold regression offers the advantage of variable selection and selection consistency, eliminating the need for conventional nonlinear tests commonly used in threshold models. In our study, the covariates included in the analysis are the exchange rate, Baltic Exchange Dry Index, inflation, unemployment rate, and industrial production index for each market. Additionally, we included US interest rate, US Corn Stock, and US gas price as control variables. It is important to note that for the model focusing on Kansas City, MO and Gulf ports, LA, the exchange rate variable was not included in the model. A comprehensive list of the covariates used in each LASSO estimation for the four paired markets is provided in Table 1.

To determine the optimal lag structure for the forcing variable, we select the lag

Market	Variable
US/Argentina	Exchange rate(USD to Argentine Peso), Baltic Exchange Dry Index, US Unemployment Rate, US Monthly Inflation, US Interest Rate, US Industrial Production Index, US Gas Price, US Corn Stock, Argentina Unemployment Rate, Argentina Monthly Inflation, Argentina Industrial Production Index
US/Ukraine	Exchange rate(USD to Ukrainian hryvnia), Baltic Exchange Dry Index, US Unemployment Rate, US Monthly Inflation, US Interest Rate, US Industrial Production Index, US Gas Price, US Corn Stock, Argentina Unemployment Rate, Argentina Monthly Inflation, Argentina Industrial Production Index
Argentina/Ukraine	Exchange rate(Argentine Peso to Ukrainian hryvnia), Baltic Exchange Dry Index, Argentina Unemployment Rate, Argentina Monthly Inflation, Argentina Industrial Production Index Ukraine Unemployment Rate, Ukraine Monthly Inflation, Ukraine Industrial Production Index
Gulfs/MN	Baltic Exchange Dry Index, US Unemployment Rate, US Monthly Inflation, US Interest Rate, US Industrial Production Index, US Gas Price, US Corn Stock

Table 1: Covariates in Each pair of markets

order with the lowest AIC value for each model. Table 9 presents the AIC values for the threshold Lasso estimation, which is used to select the lag structure for the forcing variable Q_t . In this context, the lagged price differential $|p_{t-d}^1 - p_{t-d}^2|$ undergoes a transformation into $Q_t = \hat{F}(p_{t-d}^1 - p_{t-d}^2)$, where \hat{F} denotes the empirical distribution function of the data $\{p_1^1 - p_1^2, \dots, p_{T-d}^1 - p_{T-d}^2\}$. An assumption is imposed that all $|p_{t-d}^1 - p_{t-d}^2|$ values are distinct, a convenient condition ensuring that the transformation by \hat{F} is a one-to-one function without loss of generality. This assumption holds under the assumption of continuous distribution for $|p_{t-d}^1 - p_{t-d}^2|$. Consequently, the estimates of lagged price differential can be inverted using the function \hat{F}^{-1} with threshold estimates.

The standard threshold model assumes a fixed threshold, a potentially limiting assumption. It is reasonable to consider that relationships may evolve over time, signaling structural changes in the underlying economic dynamics. To investigate this possibility, we introduce partitions that reflect changes in market environments. The data is segmented into two periods corresponding to two significant economic shocks: the 2014 Crimean crisis and the global financial/economic crisis of 2008-09. Specifically, the breakpoints for these events are set in February 2014 and October 2008, respectively. The corresponding parameter estimates are detailed in Table 2³.

³Here, “break 2008” refers to the breakpoint of the 2008-2009 world financial/economic crisis,

The quantile estimates presented in Table 2 offer insights into whether, during the selected periods, the monthly observations are more frequently in the trade regime with lower quantile estimates. Additionally, larger estimates of price differentials in Table 2 suggest higher unobservable transaction costs, providing an indication of their magnitudes. For Argentina and Ukraine, the markets more frequently fall into profitable arbitrage opportunities over the entire period, as indicated in Table 2. However, upon introducing a break in the dataset corresponding to the 2014 Crimean crisis in February 2014, the markets exhibit a tendency to be more frequently in profitable arbitrage opportunities after February compared to the markets before the breakpoint. Furthermore, based on the estimates of price differentials, it is observed that unobserved transaction costs were lower after the 2014 Crimean crisis. In the US and Ukraine markets, the post-break period more frequently enters a trade regime and experiences lower unobserved transaction costs compared to the pre-break period, regardless of whether the break is associated with the 2014 Crimean crisis or the global financial/economic crisis of 2008-09. In the US and Argentina market pair, the post-break period less frequently enters a trade regime and experiences lower unobserved transaction costs than the pre-break period. For the markets within the US, specifically Gulf ports and Kansas City, the post-break period more frequently enters a trade regime and experiences higher unobserved transaction costs compared to the pre-break period.

When examining the magnitude of the price differential estimates, it becomes apparent that, for the Argentina/Ukraine markets, the price differential estimate for the entire period and that for the period before the 2014 Crimean crisis are remarkably close. However, if we restrict the model to use only the data starting from the breakpoint (2014), both the quantile estimates and the parameter estimates decrease. This indicates a notable change or shift in market dynamics following the breakpoint. In the case of the US and Ukraine markets, the price differential estimates for the periods before the 2008 or 2014 breaks are closely aligned, as are the estimates for the post-break periods, whether it's the 2008 or 2014 break. Notably, these estimates diverge significantly from the price differential estimates for the entire period. Regarding the US and Argentina markets, we find that the price differential estimates for the entire period and the period after the 2008-09 world financial/economic crisis

while “break 2014” represents the breakpoint of the 2014 Crimean crisis.

are quite close. Within the US markets, our results show that the price differential estimates for the entire period and the pre-break period are quite close.

However, Table 2 provides evidence suggesting that unobservable transaction costs are higher for US domestic markets compared to the US and international markets. This result can be attributed to the fact that all three export prices are free-on-board prices, whereas the domestic prices are not. As a result, the price differentials between gulfs and Kansas City tend to be larger compared to the price differentials among any two export markets.

Table 10, 11, 12, and 13 in the appendix present the AIC values for the threshold Lasso estimation, considering various forcing variables. These tables provide a comprehensive overview of the AIC values, allowing for comparisons of different estimation scenarios and their respective goodness-of-fit.

	forcing variable	threshold estimates quantile	threshold estimates price differentials
Argentina/Ukraine	$ p_{t-5}^1 - p_{t-5}^2 $	0.64	0.09584621
Argentina/Ukraine_pre_break_2014	$ p_{t-4}^1 - p_{t-4}^2 $	0.70	0.09097013
Argentina/Ukraine_post_break_2014	$ p_{t-1}^1 - p_{t-1}^2 $	0.52	0.04730247
US/Ukraine	$ p_{t-3}^1 - p_{t-3}^2 $	0.55	0.08861166
US/Ukraine_pre_break_2014	$ p_{t-4}^1 - p_{t-4}^2 $	0.67	0.1219093
US/Ukraine_post_break_2014	$ p_{t-1}^1 - p_{t-1}^2 $	0.38	0.05842136
US/Ukraine_pre_break_2008	$ p_{t-1}^1 - p_{t-1}^2 $	0.58	0.1112816
US/Ukraine_post_break_2008	$ p_{t-6}^1 - p_{t-6}^2 $	0.28	0.0461198
US_Argentina	$ p_{t-5}^1 - p_{t-5}^2 $	0.71	0.07225907
US/Argentina_pre_break_2008	$ p_{t-1}^1 - p_{t-1}^2 $	0.36	0.04512331
US/Argentina_post_break_2008	$ p_{t-1}^1 - p_{t-1}^2 $	0.62	0.06196773
Gulfs/KCMO	$ p_{t-3}^1 - p_{t-3}^2 $	0.77	0.1711215
Gulfs/KCMO_pre_break_2008	$ p_{t-4}^1 - p_{t-4}^2 $	0.61	0.1656999
Gulfs/KCMO_post_break_2008	$ p_{t-3}^1 - p_{t-3}^2 $	0.54	0.1286671

Table 2: Lasso Estimation of threshold parameter

Next, we remove the shrinkage bias introduced due to the penalization in Equation (2.6) using Equation (2.8) before conducting statistical inference.

Our estimation setup considers a richer examination of price linkage among global maize markets. The fundamental framework of the threshold model illustrates that if any of the estimates of the slope coefficients (exchange rate pass-through or exogenous shock) are regime-specific, the effects of certain lagged exchange rate or exogenous shock on price differentials (which could be lagged variables) between two distinct markets differs depending on the magnitude of a certain forcing variable representing unobserved transaction costs. Estimates of non-zero differences between the two regimes imply nonlinear relationships. The slope coefficient directly corresponds to elasticity, measuring the responsiveness of the dependent variable (the price linkages in time t) to changes in the explanatory factors (lagged exchange rate between the two markets or any market factor). A straightforward way to illustrate the effects of exchange rates, market factors, or exogenous shocks on potential deviations from perfect market integration is by analyzing the coefficient estimates obtained from our estimations. All lagged variables are allowed to have a dynamic linear effect or a dynamic nonlinear effect depending on the existence of a regime switch (threshold). The ranges of estimates vary from market-pair to market-pair in our results.⁴ Tables 3, 4, 5, and 6 present the signs of statistically significant estimates at the 5% significance level, consistent with the models in Table 2. Notably, the desparsified LASSO estimates are statistically insignificant when the slope coefficient estimates by Equations (2.6) and (2.7) are zero. Therefore, we only present non-zero estimates by the LASSO method.

⁴Details of the desparsified LASSO estimates for all models are not presented here in the interest of space but are presented in the “Appendix”.

Model	Argentina/Ukraine	pre break 2014	post break 2014
lag_5_FD_Argentina Monthly Inflation		-	
trade_lag_3_FD_Argentina Unemployment Rate		-	
trade_lag_4_FD_Ukraine Unemployment Rate		+	
lag_4_FD_Argentina Monthly I.P.I % Change			-
lag_4_FD_Ukraine Monthly Inflation			-
lag_4_Peso_UAH % Change			-
FD_Ukraine Unemployment Rate			-
lag_1_FD_Ukraine Monthly I.P.I % Change			-
trade_lag_2_Baltic_Freight % Change			-
trade_lag_2_FD_Ukraine Monthly Inflation			-
trade_FD_Argentina Unemployment Rate			-
trade_lag_1_FD_Argentina Monthly Inflation			+
lag_6_FD_Argentina Unemployment Rate			+
cos			+

Table 3: Argentina Ukraine Signs of Significant Estimates

Model	US/Ukraine	pre break 2014	post break 2014	pre break 2008	post break 2008
Baltic.Freight Percent Change	-		+		
lag_1.Baltic.Freight Percent Change	-				
lag_5.Baltic.Freight Percent Change	-				
trade_lag_3.FD.US Monthly Industrial Production Index	-				
trade_lag_4.FD.US Monthly Industrial Production Index	+				
lag_3.FD.US Monthly Inflation	+				
lag_4.FD.LN.US Corn Stock	+				
trade_lag_1.FD.US Unemployment Rate	+				-
lag_1.FD.Ukraine Monthly Inflation		-			
lag_2.FD.US Unemployment Rate		-			
lag_6.FD.US Unemployment Rate		-			
trade_lag_5.FD.US Unemployment Rate		-			
trade_lag_4.FD.Ukraine Unemployment Rate		+			
trade_lag_6.FD.Ukraine Unemployment Rate		-			
lag_6.Baltic.Freight Percent Change		-			
trade_lag_4.Baltic.Freight Percent Change		+			
lag_1.FD.US Monthly Inflation		+			
lag_3.FD.US Monthly Inflation		+			
lag_3.FD.LN.US Corn Stock		+			
lag_5.FD.LN.US Corn Stock		+			
lag_6.FD.LN.US Corn Stock		-			
FD.US Monthly Industrial Production Index		-			
trade_lag_1.FD.US Monthly Industrial Production Index		+			
lag_3.FD.Ukraine Monthly Industrial Production Index		+			
trade_lag_1.FD.Ukraine Monthly Industrial Production Index		+			
trade_lag_6.FD.US Interest Rate		+			
lag_6.FD.Ukraine Monthly Inflation			+		
trade_lag_6.US Monthly Gas Price Percent Change			+		
UAH.USDollar Percent Percent Change			+		
FD.US Interest Rate			+		
FD.US Monthly Inflation			+		
trade_lag_6.FD.US Monthly Inflation			+		
trade_lag_1.Baltic.Freight Percent Change			+		
FD.LN.US Corn Stock			+		
lag_3.FD.LN.US Corn Stock			+		
trade_lag_2.FD.LN.US Corn Stock			+		
trade_lag_5.FD.LN.US Corn Stock			-		
lag_4.US Monthly Gas Price Percent Change			-		
lag_5.FD.Ukraine Monthly Industrial Production Index			-		
lag_6.FD.Ukraine Monthly Industrial Production Index			-		
lag_6.FD.US Monthly Industrial Production Index			-		
trade_lag_3.FD.US Monthly Inflation				+	
trade_lag_6.FD.Ukraine Monthly Industrial Production Index				+	
trade_lag_4.US Monthly Gas Price Percent Change					+
lag_3.US Monthly Gas Price Percent Change					+
trade_lag_5.FD.US Interest Rate					+
lag_1.FD.US Interest Rate					-
lag_6.FD.US Interest Rate					-
lag_5.FD.Ukraine Monthly Inflation					-
lag_6.FD.Ukraine Monthly Inflation					-
FD.US Unemployment Rate					-
lag_5.Baltic.Freight Percent Change					-
lag_3.FD.Ukraine Unemployment Rate					-
trade_lag_3.UAH.USDollar Percent Change					-

Table 4: US Ukraine Signs of Significant Estimates

Model	US/Argentina	pre break 2008	post break 2008
lag_2_Baltic_Freight % Change		+	
lag_4_FD_Argentina Monthly I.P.I % Change		+	
lag_5_FD_US Interest Rate		+	
trade_lag_2_FD_US Monthly Inflation		+	
lag_2_FD_Argentina Monthly Inflation		-	
lag_2_Peso_USDollar % Change		-	
lag_4_Baltic_Freight % Change		-	
lag_5_FD_LN_US Corn Stock		-	+
lag_6_FD_LN_US Corn Stock		-	
lag_3_FD_LN_US Corn Stock			+
lag_3_FD_US Unemployment Rate			+
lag_6_FD_US Unemployment Rate			+
lag_6_Peso_USDollar % Change			+
trade_lag_2_Peso_USDollar % Change			+
trade_lag_6_FD_Argentina Monthly Inflation			+
lag_1_Baltic_Freight % Change			-
lag_5_Baltic_Freight % Change			-
lag_6_Baltic_Freight % Change			-
lag_3_FD_Argentina Monthly I.P.I % Change			-
trade_cos			-
trade_lag_1_FD_Argentina Monthly Inflation			-
trade_lag_5_FD_Argentina Unemployment Rate			-

Table 5: US/Argentina Signs of Significant Estimates

If we set aside the consideration of structural breaks and focus solely on estimating the entire period’s data, the findings reveal no significant estimates among the market pairs of Argentina/Ukraine, US/Argentina, and Gulf/KCMO—except for the US/Ukraine pair. The United States, holding a prominent global position in maize production and exportation, assumes a pivotal role. Meanwhile, Ukraine contends with a challenging and unstable economic and market environment. Consequently, the sensitivity of price linkages between the two markets is more clearly estimated, with several significant impact factors. Interestingly, we do not observe a significantly imperfect exchange rate pass-through effect in either US/Argentina, US/Ukraine, or Argentina/Ukraine.

Next, we examine the estimation results using the desparsified LASSO method for each case under the structural breaks specification we imposed.

In Table 3, it is evident that the 5-month lag in Argentina’s inflation rate consistently exhibits significant effects in both the no-trade and trade regimes. More-

Model	Gulfs/KCMO	pre break 2008	post break 2008
lag_5_FD_US Unemployment Rate		-	
FD_LN_US Corn Stock		-	
Baltic_Freight % Change		+	
lag_6_Baltic_Freight % Change		-	
FD_US Monthly I.P.I % Change		+	
lag_6_FD_US Monthly I.P.I % Change		+	
lag_2_FD_US Monthly I.P.I % Change		-	
lag_1_FD_US Monthly Inflation		-	
lag_3_FD_US Monthly Inflation		-	
lag_3_US Monthly Gas Price % Change		+	
lag_4_US Monthly Gas Price % Change		-	
lag_5_US Monthly Gas Price % Change		-	

Table 6: GulfsLA/KCMO Signs of Significant Estimates

over, notable additional significant factors emerge in the trade regime, including the 3-month lag in Argentina’s unemployment rate and the 4-month lag in Ukraine’s unemployment rate. These findings suggest nonlinearity in the Argentina/Ukraine case before the 2014 Crimean crisis. After the break, several factors achieve statistical significance. The Baltic index change at the second lag, Ukraine’s inflation at the second lag, Argentina’s inflation at the first lag, and Argentina’s unemployment rate show statistical significance only in the trade regime. Argentina’s unemployment at the sixth lag is positive and statistically significant in both trade and no-trade regimes. Consequently, the overall effects of Argentina’s unemployment rate remain uncertain in the trade regime. Additionally, the current month’s Argentina unemployment has a positive effect, particularly in the trade regime. The exchange rate pass-through is negative and statistically significant in both trade and no-trade regimes at the fourth lag. Generally, we identify more significant factors in the trade regime and more after the break.

The analysis of Table 4 reveals several significant factors during the partition periods in the case of the US/Ukraine, except for the period preceding the 2008/09 financial crisis break. When considering the structural break during the 2014 Crimea crisis in the pre-break situation, it is evident that the US inflation rate dynamically affects both the trade and no-trade regimes. The US unemployment rate at several lags, the Baltic Freight Index, the US Industrial Production Index, and the Ukraine Industrial Production Index exhibit significant effects on the price differentials, dis-

playing nonlinearity. Notably, certain estimates of the threshold effect (the difference between the two regimes) are significant. The consistent sign of estimates for different lagged periods in both the structural and threshold effect estimates implies a larger magnitude and a prominent effect of these factors in the trade regime. Regarding the US corn stock, the long-run propensity effects are significant and observed in both the trade and no-trade regimes, but the direction of its cumulative effect is uncertain. For Ukraine’s employment, the cumulative effect is only significant in the trade regime, with an uncertain direction. In the post-break scenario, accounting for the structural break during the 2014 Crimea crisis, we observe positive and nonlinear cumulative effects of the Baltic Freight Index and US inflation on price differentials. The US corn stock exhibits cumulative effects, though the overall impact in the trade regime is uncertain. Meanwhile, the Ukraine Industrial Production Index shows negative cumulative effects but follows a linear pattern. In the estimation corresponding to the selected data period before the 2008/09 financial crisis, only the US Monthly Inflation at the third lag and Ukraine’s Monthly Industrial Production Index at the sixth lag exhibit effects in the trade regime. It’s worth noting that no significant factors are found in the no-trade regime for this sub-period. However, for the selected data period after the 2008/09 financial crisis, we find that the cumulative effect of US gas prices is positive and nonlinear. Additionally, the cumulative effect of the US Unemployment Rate is negative and nonlinear. The effect of Ukraine inflation is cumulatively negative in both trade and no-trade regimes. Furthermore, the effect of US interest rates is nonlinear, with US interest rates at the fifth lag being only significant in the trade regime.

Turning to Table 5, we observe that the US corn stock demonstrates a negative cumulative effect pre-break but a positive cumulative effect post-break in both the trade and no-trade regimes. Moreover, there is a positive cumulative effect of the US unemployment rate and a negative cumulative effect of the Baltic Freight Index in both the trade and no-trade regimes after the break. Additionally, we note a nonlinear cumulative effect of the exchange rate of the US Dollar to the Argentine Peso, with the magnitude of the cumulative exchange rate pass-through effect being larger in the trade regime.

As a further illustration, we attempted to apply the method developed for the three international markets to the US domestic market. However, the results vary signif-

icantly compared to the previous three export market pairs. Despite the threshold estimates selected through the scaled LASSO method in Table 2, it’s worth noting the absence of significant factor estimates that differ between trade and no-trade regimes. Consequently, there are no significant factors indicating nonlinear relationships in either of the selected periods. Given that maize transportation within the US heavily relies on the Mississippi River system, and the movements of corn are one-directional, barge freight costs emerge as the most pertinent factor influencing the price linkages of the US domestic corn market. While we didn’t discover any significant factors in the entire period or post-2008 break, in the model of the pre-2008 financial crisis, we observed several significant factors. Notably, only US inflation rates at several lags have a negative overall effect on the pre-break markets. However, for the Baltic Freight Index, the US Industrial Production Index, and US gas prices, the cumulative effects don’t have patterns, displaying uncertainty with varied (positive or negative) effects across different lagged periods.

In the four cases, we observe that the results of partition periods reveal more significant factors influencing price linkages, considering that the threshold is not fixed throughout the entire period. Additionally, trade regimes appear to be influenced by a greater number of market factors, and the magnitudes of these factors affecting price linkages tend to be larger compared to the no-trade regime. In essence, market factors have a more lasting and prominent impact on price linkages within the trade regime.

4 Summary and Concluding Remarks

We develop a model of price linkages in spatially distinct international export markets for maize under perfect integration to investigate exchange rate pass-through and other market factor effects. The models are developed within the framework of high-dimensional threshold models. We consider such nonlinear models as natural extensions to an extensive literature that has developed an increasingly rich set of factors in models of spatial market integration. The desparsified LASSO estimation procedures are used to specify the models.

In summary, our results are consistent with the presence of imperfect pass-through, which distorts international price linkages. The markets appear to be strongly linked

in most cases, and nonlinear adjustments are confirmed in most cases. Consistent with existing research, the results indicate that distortions from market equilibrium caused by exchange rate or market factors are generally larger in response to large price differences, which reflect more substantial disequilibrium conditions and therefore larger arbitrage opportunities.

References

- Banerjee, A., J. J. Dolado, J. W. Galbraith, and D. Hendry (1993, 05). *Co-integration, Error Correction, and the Econometric Analysis of Non-Stationary Data*. Oxford University Press.
- Chambers, R. G. and R. E. Just (1981). Effects of exchange rate changes on u.s. agriculture: A dynamic analysis. *American Journal of Agricultural Economics* 63(1), 32–46.
- Goodwin, B. K., T. Grennes, and M. K. Wohlgenant (1990). Testing the law of one price when trade takes time. *Journal of International Money and Finance* 9(1), 21–40.
- Goodwin, B. K., M. T. Holt, and J. P. Prestemon (2021). Semi-parametric models of spatial market integration. *Empirical Economics* 61, 2335–2361.
- Goodwin, B. K. and N. E. Piggott (2001). Spatial market integration in the presence of threshold effects. *American Journal of Agricultural Economics* 83(2), 302–317.
- Lee, S., M. H. Seo, and Y. Shin (2016). The lasso for high dimensional regression with a possible change point. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)* 78(1), 193–210.
- Lence, S. H., G. Moschini, and F. G. Santeramo (2018). Threshold cointegration and spatial price transmission when expectations matter. *Agricultural Economics* 49(1), 25–39.
- Samuelson, P. A. (1954, 06). The Transfer Problem and Transport Costs, II: Analysis of Effects of Trade Impediments. *The Economic Journal* 64(254), 264–289.
- Tsay, R. S. (1989). Testing and modeling threshold autoregressive processes. *Journal of the American Statistical Association* 84(405), 231–240.
- U.S. Department of Agriculture (2022). 2021 agricultural export yearbook. Technical report, U.S. Department of Agriculture’s (USDA) Foreign Agricultural Service (FAS).

- van de Geer, S., P. Bühlmann, Y. Ritov, and R. Dezeure (2014). On asymptotically optimal confidence regions and tests for high-dimensional models. *The Annals of Statistics* 42(3), 1166 – 1202.
- Varangis, P. N. and R. C. Duncan (1993). Exchange rate pass through: An application to us and japanese steel prices. *Resources Policy* 19(1), 30–39.
- Yan, H. and M. Caner (2022). Uniform inference in high dimensional threshold regression models. https://hongqiangyan.github.io/files/Uniform_Inference_in_High_Dimensional_Threshold_Regression_Models.pdf.

5 Appendix

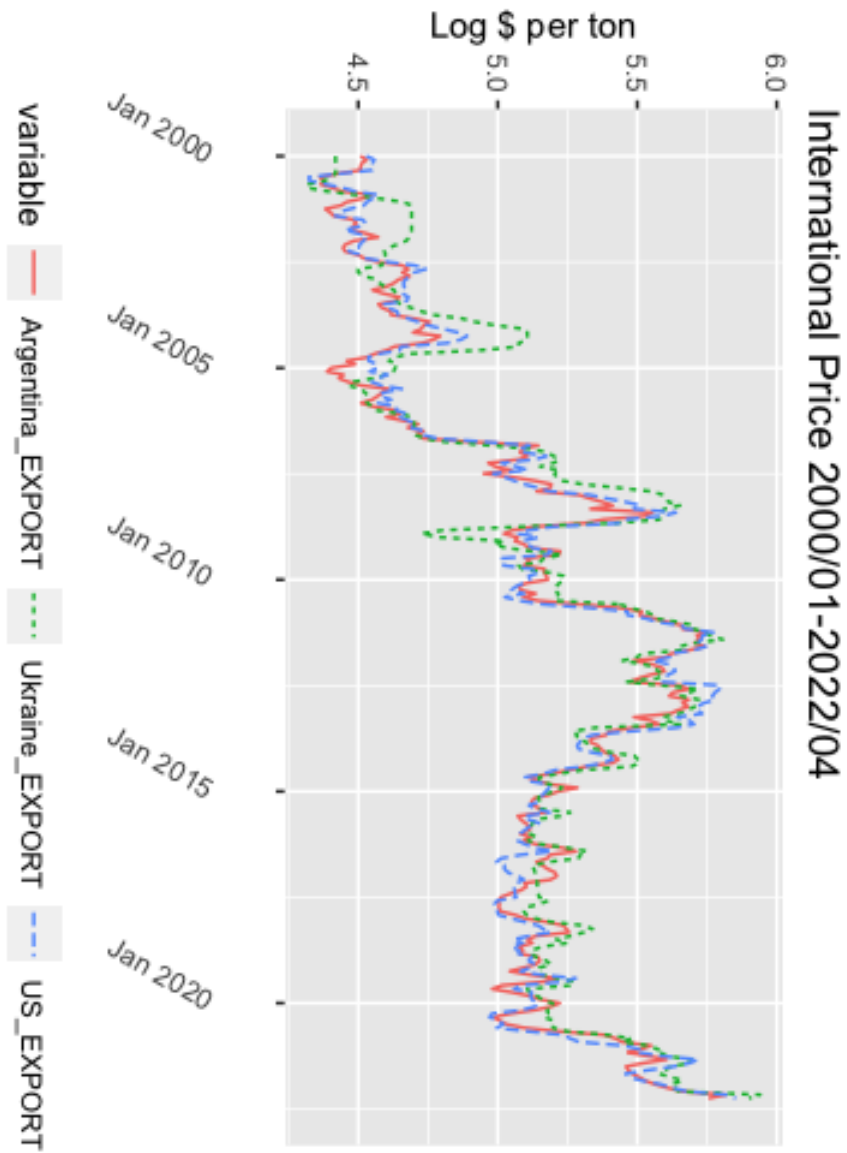


Figure 2: World Corn Export price by Country

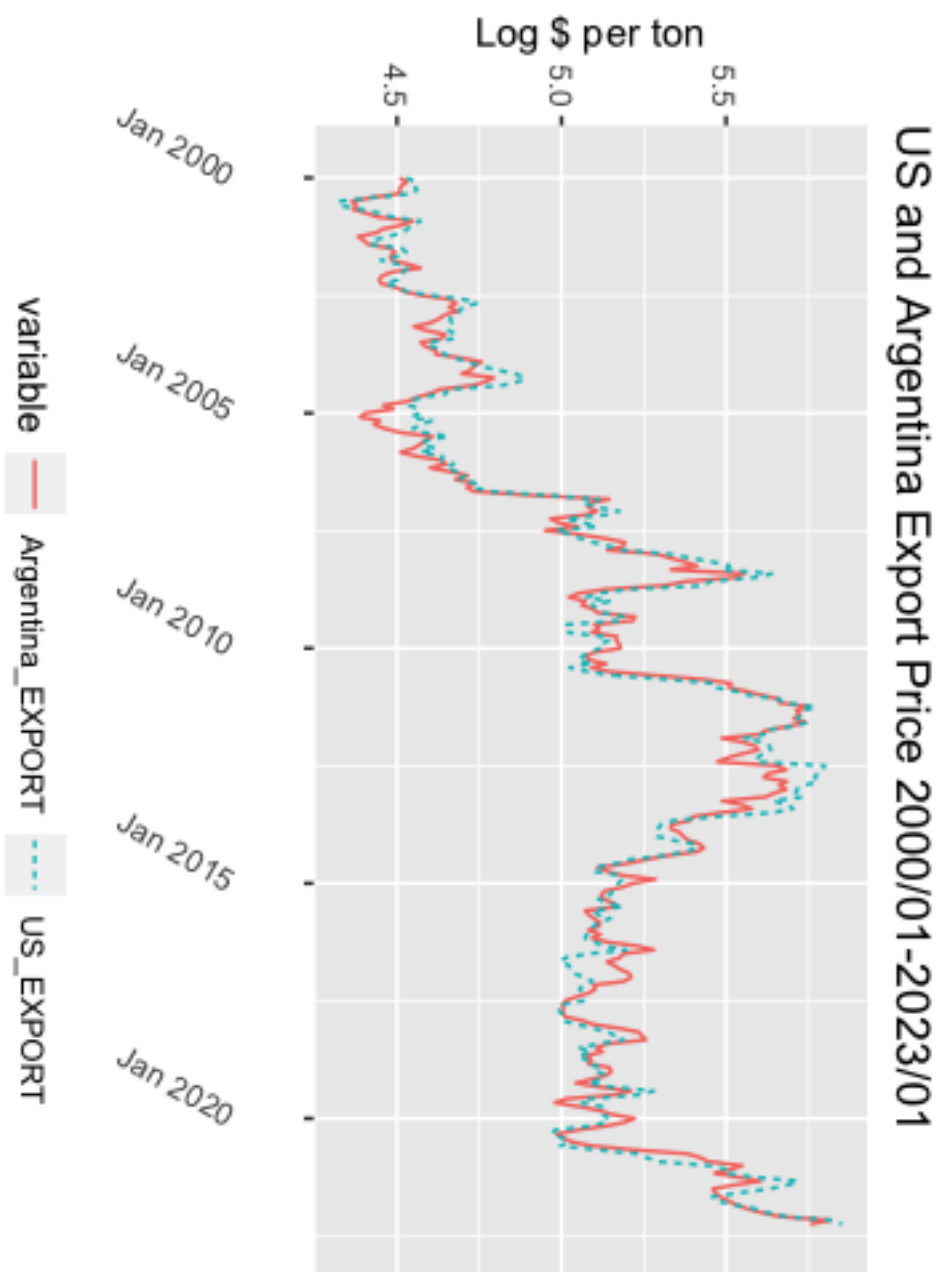


Figure 3: the U.S. and Argentina Corn Market Price

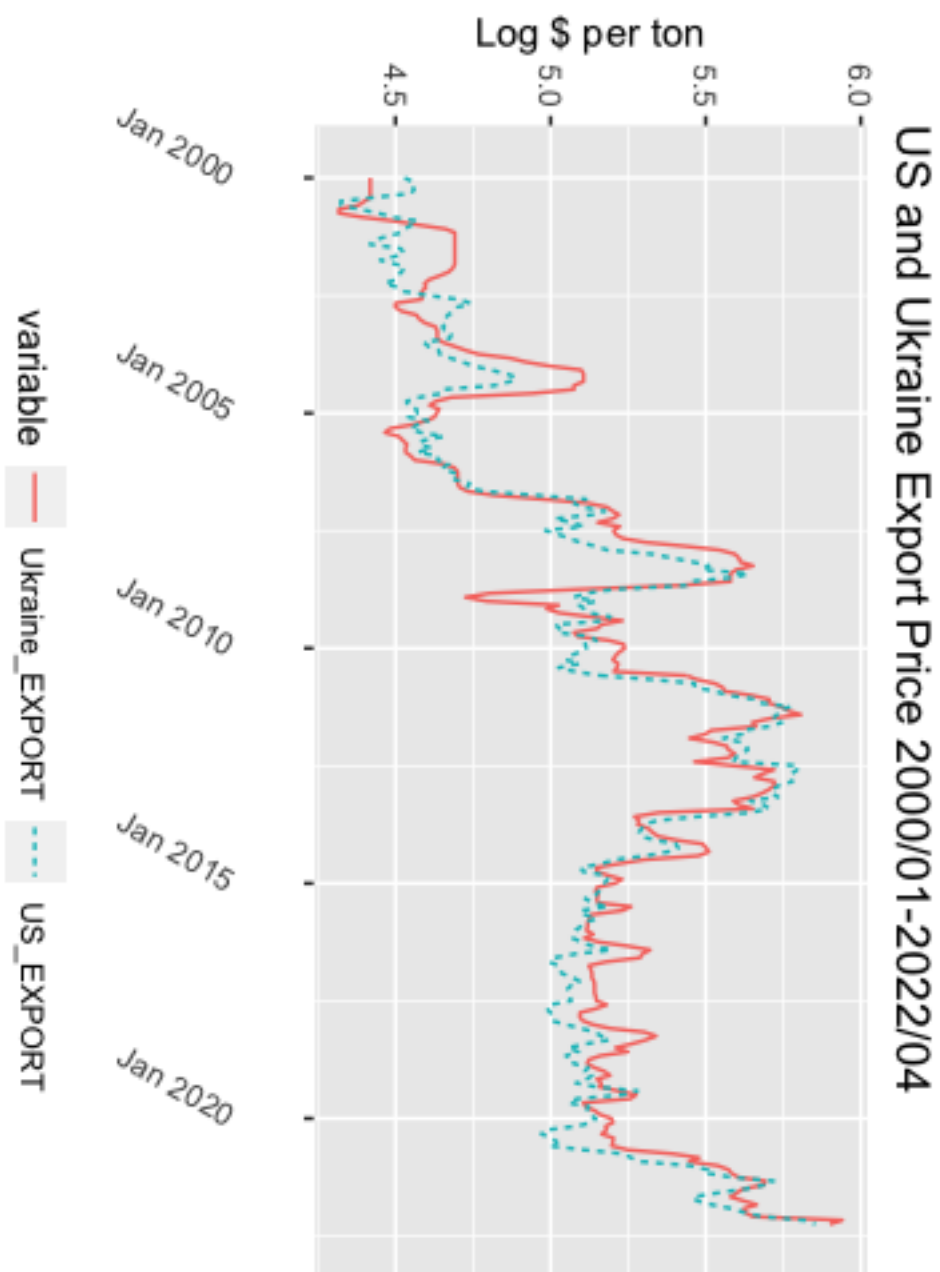


Figure 4: the U.S. and Ukraine Corn Market Price

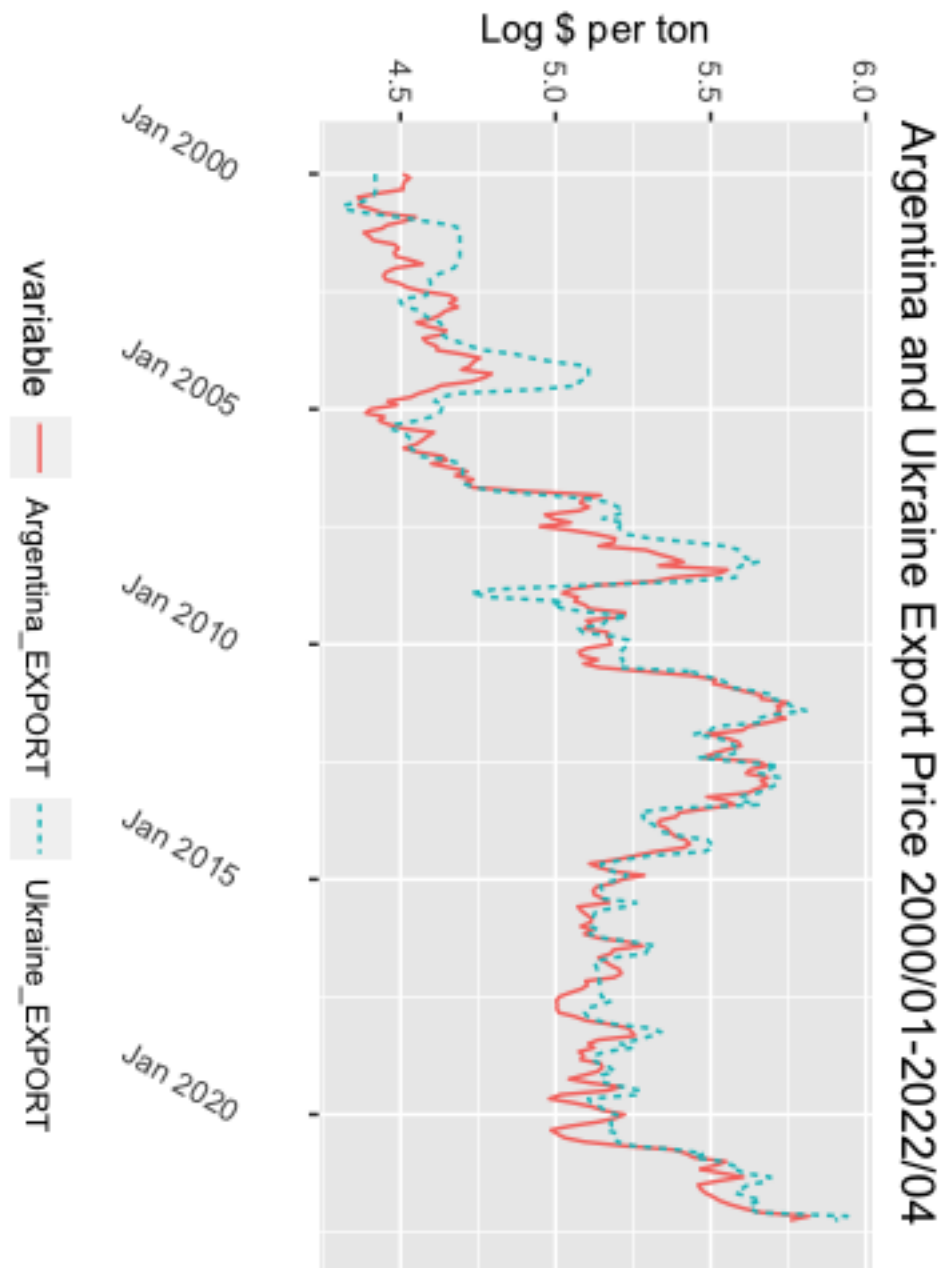


Figure 5: Argentina and Ukraine Corn Market Price

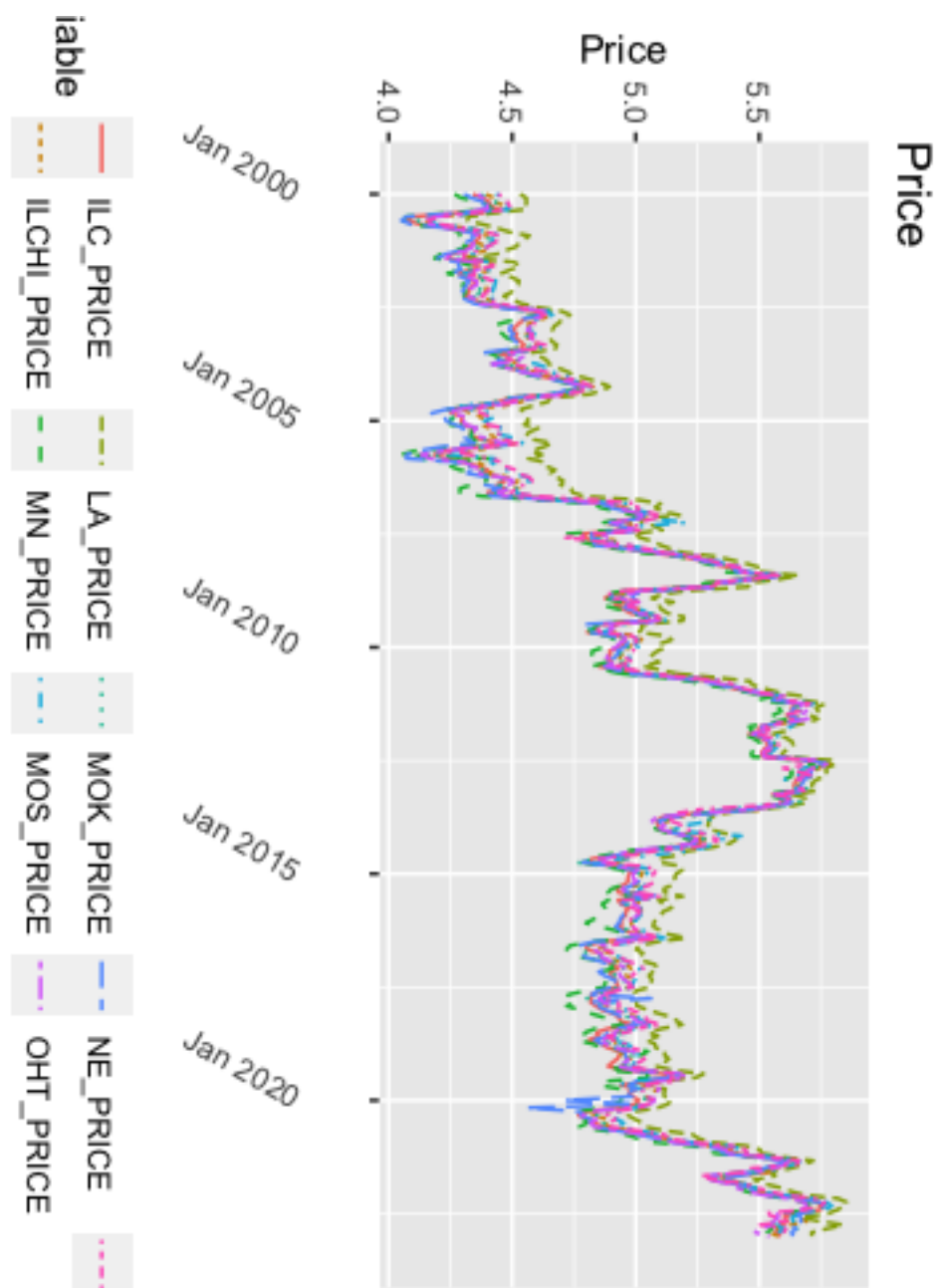


Figure 6: the U.S. Corn Market Price by Location

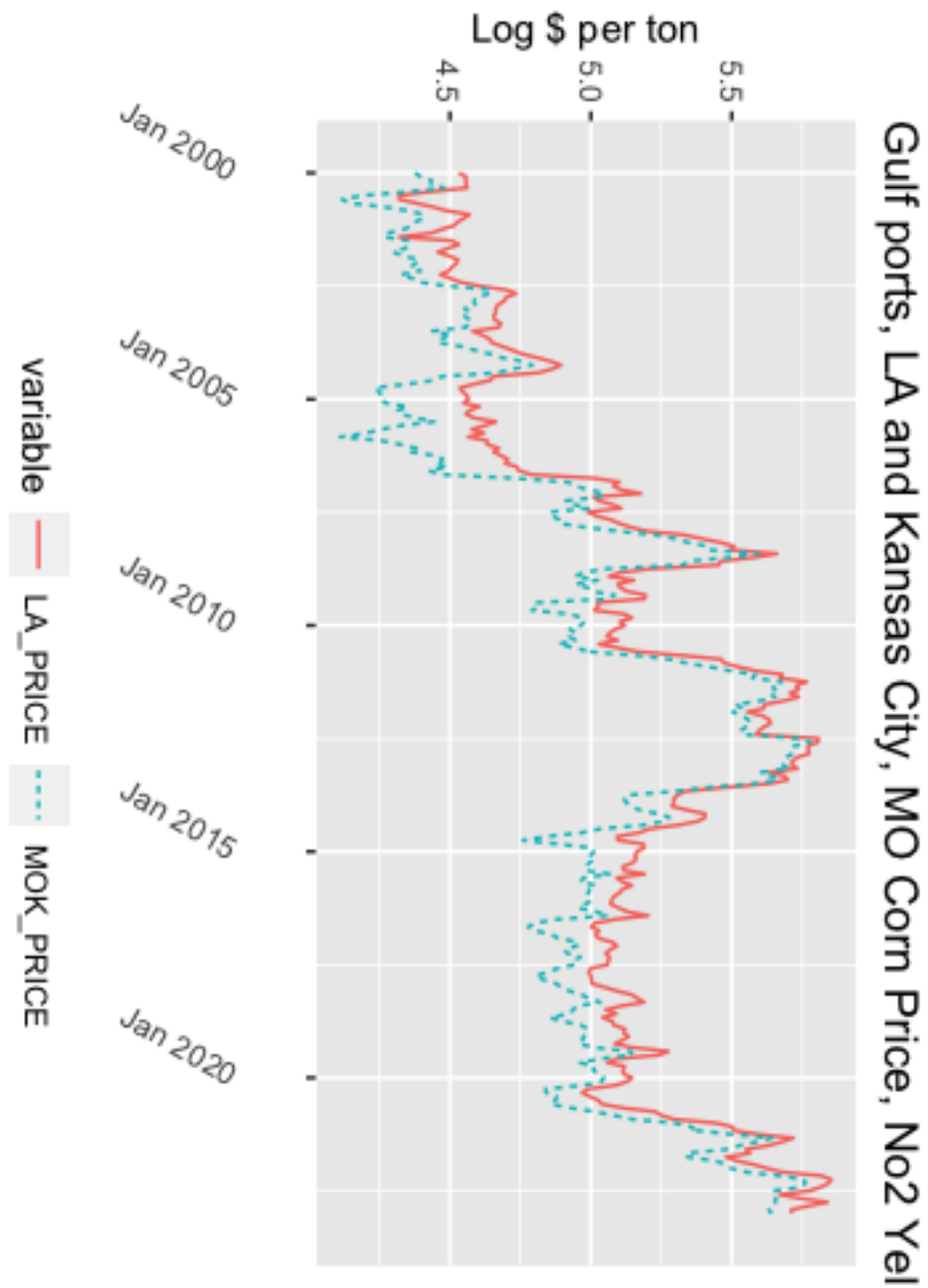


Figure 7: the U.S. Corn Market Price-Kansas City, MO&Gulf ports, LA

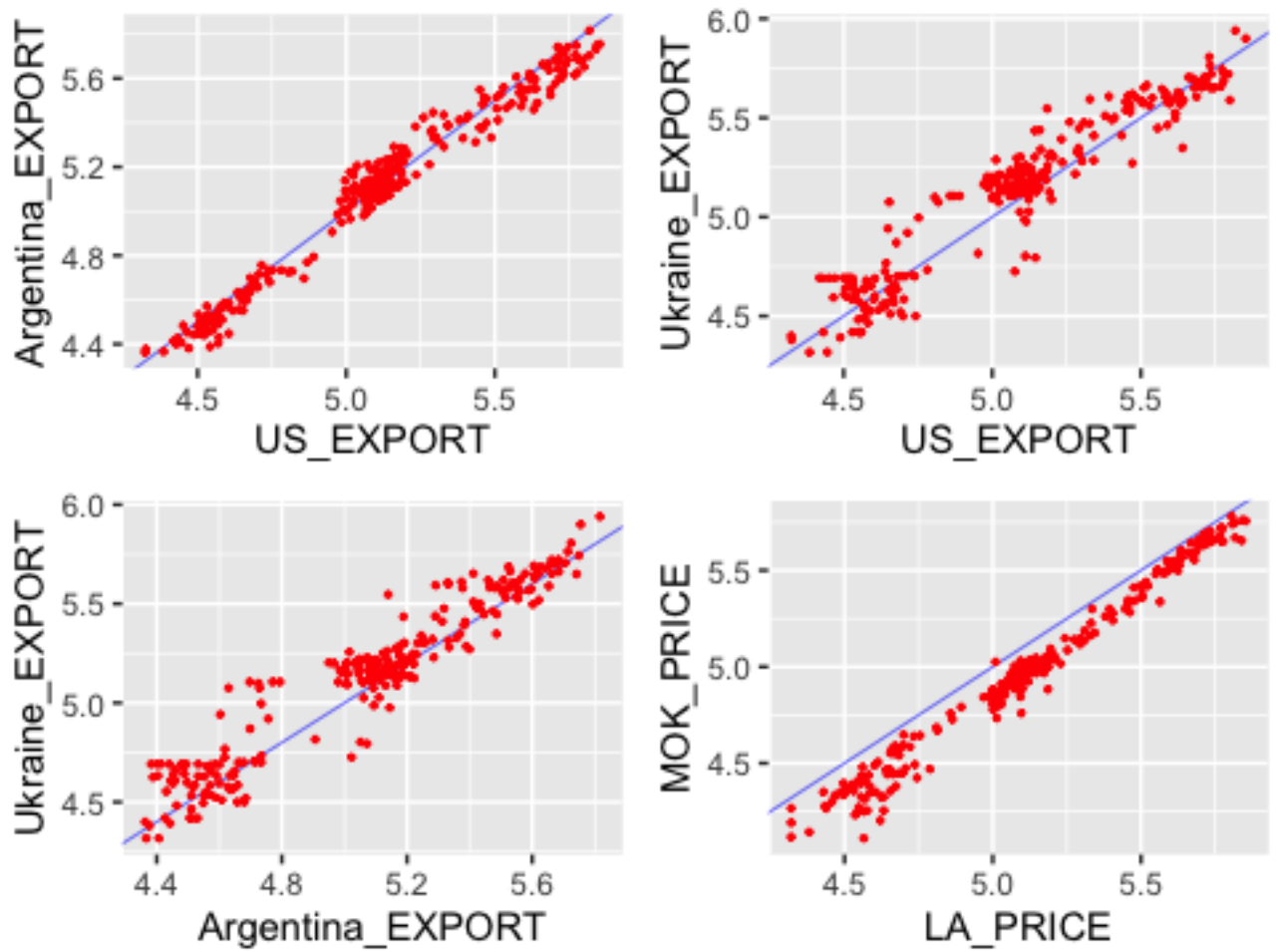


Figure 8: Corn Market Logarithmic Prices pairs

Augmented Dickey-Fuller test Results	
Variable	ADF
Unit Root	
price_diff_US_Argentina	-4.473
price_diff_US_Ukraine	-4.7348
price_diff_Argentina_Ukraine	-4.6487
price_diff_Gulf_KCMO	-3.1602
Alternative hypothesis: stationary	Lag order = 6
Significant level	Critical value
1%	-3.96
5%	-3.41
10%	-3.12

*The critical values are interpolated from Table 4.2 of [Banerjee et al. \(1993\)](#).

Table 7: Augmented Dickey-Fuller Test Results of Price Differentials

Augmented Dickey-Fuller Test	
Variable (1st diff)	Dickey-Fuller
price_diff_US_Argentina	-9.068
price_diff_US_Ukraine	-5.9761
price_diff_Argentina_Ukraine	-6.7176
price_diff_Gulf_KCMO	-8.7288
UAH_USDollar	-5.652
Peso_USDollar	-5.7734
Peso_UAH	-5.5003
Baltic_Freight	-7.8916
US Unemployment Rate	-7.4513
US Industrial Production Index	-9.9739
US Monthly Inflation	-9.3708
US Interest Rate	-3.2288
US Monthly Gas Price	-7.6682
US Corn Stock	-11.708
Argentina Unemployment Rate	-4.5384
Argentina Monthly Industrial Production Index	-12.332
Argentina Monthly Inflation	-7.2783
Ukraine Unemployment Rate	-6.3418
Ukraine Monthly Industrial Production Index	-9.3515
Ukraine Monthly Inflation	-8.6679
Alternative hypothesis: stationary	Lag order = 6
Significant level	Critical value
1%	-3.96
5%	-3.41
10%	-3.12

*The critical values are interpolated from Table 4.2 of [Banerjee et al. \(1993\)](#).

Table 8: Augmented Dickey-Fuller Test Results of First Difference of Time Series

		$p_{t-1}^1 - p_{t-1}^2$	$p_{t-2}^1 - p_{t-2}^2$	$p_{t-3}^1 - p_{t-3}^2$	$p_{t-4}^1 - p_{t-4}^2$	$p_{t-5}^1 - p_{t-5}^2$	$p_{t-6}^1 - p_{t-6}^2$
US/Argentina	AIC	-1.553418	-1.737098	-1.569497	-2.900425	-2.956548	-1.653093
	λ_T	5.111050e-07	2.210048e-06	1.152693e-06	2.536086e-04	3.149909e-04	2.442470e-06
	\hat{c}	0.49	0.56	0.57	0.42	0.71	0.59
US/Ukraine	AIC	-0.5051949	-1.1103581	-1.1205013	-0.7260766	-0.4189850	-0.9699245
	λ_T	1.133271e-06	1.019725e-04	6.635313e-05	1.449089e-05	1.542151e-06	4.878110e-05
	\hat{c}	0.61	0.75	0.55	0.60	0.39	0.50
Argentina/Ukraine	AIC	-1.3375471	-1.3777247	-1.2114806	-1.2856019	-1.4808931	-0.8535025
	λ_T	2.153163e-04	2.795255e-04	1.250354e-04	2.249827e-04	4.341559e-04	4.663529e-05
	\hat{c}	0.70	0.72	0.67	0.61	0.64	0.68
Gulfs/KCMO	AIC	-2.515462	-2.824062	-2.859255	-2.812807	-2.762981	-2.776374
	λ_T	2.960595e-05	1.780808e-04	2.515030e-04	2.099041e-04	1.972637e-04	1.900545e-04
	\hat{c}	0.76	0.84	0.77	0.76	0.69	0.73

Table 9: Lasso Estimation

		$p_{t-1}^1 - p_{t-1}^2$	$p_{t-2}^1 - p_{t-2}^2$	$p_{t-3}^1 - p_{t-3}^2$	$p_{t-4}^1 - p_{t-4}^2$	$p_{t-5}^1 - p_{t-5}^2$	$p_{t-6}^1 - p_{t-6}^2$
US/Ukraine	AIC	-0.5051949	-1.1103581	-1.1205013	-0.7260766	-0.4189850	-0.9699245
	λ_T	1.133271e-06	1.019725e-04	6.635313e-05	1.449089e-05	1.542151e-06	4.878110e-05
	\hat{c}	0.61	0.75	0.55	0.60	0.39	0.50
US/Ukraine_pre_break_2014	AIC	0.2719879	0.2384729	0.2584657	0.1553439	0.3059618	0.1965868
	λ_T	2.404328e-05	2.328192e-05	1.912262e-05	1.892201e-05	2.046114e-05	2.671763e-05
	\hat{c}	0.58	0.45	0.56	0.67	0.36	0.58
US/Ukraine_post_break_2014	AIC	-0.7497784	-0.5824867	-0.5695269	-0.7033671	-0.5125117	-0.6625862
	λ_T	1.133271e-06	1.019725e-04	6.635313e-05	1.449089e-05	1.542151e-06	4.878110e-05
	\hat{c}	0.38	0.42	0.35	0.43	0.46	0.35
US_Ukraine_pre_break_2008	AIC	-0.03886665	0.26819724	0.12303875	0.02702780	0.21128141	0.34608808
	λ_T	2.044458e-05	1.996483e-05	1.859907e-05	2.376336e-05	1.966192e-05	1.978563e-05
	\hat{c}	0.58	0.46	0.64	0.47	0.53	0.50
US_Ukraine_post_break_2008	AIC	-0.4001896	-0.2095196	-0.3998089	-0.3242917	-0.5911825	-0.8037958
	λ_T	1.720884e-06	5.482831e-07	1.416099e-06	1.641082e-06	1.769928e-06	1.058156e-05
	\hat{c}	0.48	0.52	0.52	0.46	0.39	0.28

Table 10: Lasso Estimation

		$p_{t-1}^1 - p_{t-1}^2$	$p_{t-2}^1 - p_{t-2}^2$	$p_{t-3}^1 - p_{t-3}^2$	$p_{t-4}^1 - p_{t-4}^2$	$p_{t-5}^1 - p_{t-5}^2$	$p_{t-6}^1 - p_{t-6}^2$
Argentina/Ukraine	AIC	-1.3375471	-1.3777247	-1.2114806	-1.2856019	-1.4808931	-0.8535025
	λ_T	2.153163e-04	2.795255e-04	1.250354e-04	2.249827e-04	4.341559e-04	4.663529e-05
	\hat{c}	0.70	0.72	0.67	0.61	0.64	0.68
Argentina/Ukraine_pre_break_2014	AIC	-0.122555394	-0.007617291	-0.219495484	-0.793025568	0.061087460	-0.359462421
	λ_T	6.612904e-07	1.282999e-06	1.541017e-06	5.816458e-05	4.822867e-07	1.483879e-05
	\hat{c}	0.69	0.56	0.65	0.70	0.54	0.67
Argentina/Ukraine_post_break_2014	AIC	-0.8867073	-0.7710295	-0.7334242	-0.7761687	-0.6126150	-0.7970872
	λ_T	1.477595e-05	1.592034e-05	1.441506e-05	1.381054e-05	1.552746e-05	1.409800e-05
	\hat{c}	0.52	0.52	0.54	0.69	0.34	0.59

Table 11: Lasso Estimation

		$p_{t-1}^1 - p_{t-1}^2$	$p_{t-2}^1 - p_{t-2}^2$	$p_{t-3}^1 - p_{t-3}^2$	$p_{t-4}^1 - p_{t-4}^2$	$p_{t-5}^1 - p_{t-5}^2$	$p_{t-6}^1 - p_{t-6}^2$
US/Argentina	AIC	-1.553418	-1.737098	-1.569497	-2.900425	-2.956548	-1.653093
	λ_T	5.111050e-07	2.210048e-06	1.152693e-06	2.536086e-04	3.149909e-04	2.442470e-06
	\hat{c}	0.49	0.56	0.57	0.42	0.71	0.59
US_Argentina_pre_break_2008	AIC	-1.2518930	-1.0846773	-0.9888356	-1.0262127	-0.8711668	-0.8109077
	λ_T	1.612861e-05	1.382888e-05	1.355596e-05	1.443525e-05	1.347417e-05	1.424458e-05
	\hat{c}	0.36	0.52	0.56	0.38	0.56	0.45
US_Argentina_post_break_2008	AIC	-1.498117	-1.320319	-1.311259	-1.458662	-1.345537	-1.381769
	λ_T	8.515443e-06	8.506276e-06	8.842351e-06	9.359523e-06	8.284913e-06	8.514304e-06
	\hat{c}	0.62	0.62	0.46 0	.33	0.62	0.57

Table 12: Lasso Estimation

		$p_{t-1}^1 - p_{t-1}^2$	$p_{t-2}^1 - p_{t-2}^2$	$p_{t-3}^1 - p_{t-3}^2$	$p_{t-4}^1 - p_{t-4}^2$	$p_{t-5}^1 - p_{t-5}^2$	$p_{t-6}^1 - p_{t-6}^2$
Gulfs/KCMO	AIC	-2.515462	-2.824062	-2.859255	-2.812807	-2.762981	-2.776374
	λ_T	2.960595e-05	1.780808e-04	2.515030e-04	2.099041e-04	1.972637e-04	1.900545e-04
	\hat{c}	0.76	0.84	0.77	0.76	0.69	0.73
Gulfs/KCMO_pre_break_2008	AIC	-1.441488	-1.490309	-1.481012 -	1.747033	-1.496295	-1.437110
	λ_T	1.776039e-05	1.461754e-05	1.813944e-05	2.550446e-05	1.562376e-05	1.357873e-05
	\hat{c}	0.55	0.72	0.64	0.61	0.61	0.57
Gulfs/KCMO_post_break_2008	AIC	-2.253965	-2.535333	-3.114062	-2.411973	-3.023359	-3.052794
	λ_T	9.445343e-06	2.851834e-05	4.483806e-04	2.117865e-05	3.439096e-04	3.438341e-04
	\hat{c}	0.66	0.47	0.54	0.45	0.43	0.39

Table 13: Lasso Estimation

Var Name	Scaled Lasso	Debiased Lasso	t-statistic
Peso_UAH Percent Change	-0.064	-0.033 (0.030)	-1.102
Baltic_Freight Percent Change	-0.020	-0.073 (0.053)	-1.375
lag_2_Peso_UAH Percent Change	0.032	0.255 (0.223)	1.144
lag_1_Baltic_Freight Percent Change	-0.018	-0.059 (0.040)	-1.460
lag_1_FD_Argentina Unemployment Rate	-2.876	20.124 (23.000)	0.875
lag_2_FD_Argentina Monthly Industrial Production Index Percent Change	0.015	-0.281 (0.296)	-0.949
lag_5_FD_Ukraine Monthly Industrial Production Index Percent Change	-0.006	-0.197 (0.191)	-1.030
trade_Baltic_Freight Percent Change	-0.032	0.036 (0.068)	0.529
trade_lag_1_FD_Argentina Unemployment Rate	-0.680	-13.140 (12.460)	-1.055
trade_lag_5_FD_Argentina Unemployment Rate	0.932	-32.657 (33.588)	-0.972
trade_lag_6_FD_Argentina Monthly Inflation	0.102	-1.609 (1.711)	-0.940
trade_lag_1_FD_Ukraine Monthly Inflation	0.122	-0.813 (0.935)	-0.870
trade_lag_3_FD_Ukraine Monthly Industrial Production Index Percent Change	0.080	0.961 (0.880)	1.091
trade_lag_5_FD_Ukraine Monthly Industrial Production Index Percent Change	-0.024	0.112 (0.136)	0.824

Table 14: Argentina Ukraine Regression Results

Var Name	Scaled Lasso	Debiased Lasso	t-statistic
lag_3.FD_LN_US Corn Stock	0.006	0.056 (0.051)	1.111
lag_6.FD_LN_US Corn Stock	-0.001	-0.111 (0.110)	-1.009
lag_4.FD_US Unemployment Rate	-0.384	-3.905 (3.521)	-1.109
lag_2.FD_US Monthly Inflation	0.540	3.490 (2.950)	1.183
lag_4.FD_US Monthly Inflation	-0.193	-9.803 (9.610)	-1.020
lag_6.FD_US Monthly Industrial Production Index Percent Change	0.109	2.928 (2.818)	1.039
trade.FD_Argentina Unemployment Rate	0.392	-18.560 (18.952)	-0.979
trade_lag_4.Baltic.Freight Percent Change	0.023	-0.086 (0.109)	-0.792
trade_lag_4.FD_LN_US Corn Stock	0.007	-0.124 (0.130)	-0.947
trade_lag_2.FD_Argentina Monthly Inflation	-0.158	-0.720 (0.562)	-1.281

Table 15: US/Argentina Regression Results

Var Name	Scaled Lasso	Debiased Lasso	t-statistic
FD_LN_US Corn Stock	-0.004	-0.011 (0.007)	-1.587
lag_2.Baltic.Freight Percent Change	-0.002	0.004 (0.005)	0.664
lag_1.FD_LN_US Corn Stock	-0.019	-0.040*** (0.021)	-1.904
lag_5.FD_LN_US Corn Stock	-0.008	0.031 (0.039)	0.793
lag_6.FD_US Unemployment Rate	0.019	-0.042 (0.061)	-0.682
trade.FD_US Monthly Industrial Production Index Percent Change	0.257	0.150 (0.107)	1.407
trade_lag_4.Baltic.Freight Percent Change	-0.033	0.042 (0.075)	0.563
trade_lag_2_US Monthly Gas Price Percent Change	0.109	-0.617 (0.727)	-0.850
trade_lag_2.FD_US Monthly Industrial Production Index Percent Change	-0.236	2.922 (3.159)	0.925

Table 16: GulfsLA/KCMO Regression Results